THE BOLSHOI COSMOLOGICAL SIMULATIONS AND THEIR IMPLICATIONS

JOEL PRIMACK, UCSC

$\Lambda$CDM Cosmological Parameters for Bolshoi and BigBolshoi
Halo Mass Function is 10x Below Sheth-Tormen at $z=10$
Cluster Concentrations Agree with $\Lambda$CDM Predictions
Improved Halo Finding and Merger Trees
Predicted LMC/SMC Likelihood Agrees with Observations
HAM Galaxy Correlations Agree with Observations
HAM Galaxy Luminosity-Velocity Relations OK
Galaxy Velocity Function OK for $V_{\text{circ}} > 80$ km/s
The Millennium Run

- properties of halos (radial profile, concentration, shapes)
- evolution of the number density of halos, essential for normalization of Press-Schechter-type models
- evolution of the distribution and clustering of halos in real and redshift space, for comparison with observations
- accretion history of halos, assembly bias (variation of large-scale clustering with assembly history), and correlation with halo properties including angular momenta and shapes
- halo statistics including the mass and velocity functions, angular momentum and shapes, subhalo numbers and distribution, and correlation with environment

The Millennium Run was a landmark simulation, and it has been the basis for ~400 papers.

- void statistics, including sizes and shapes and their evolution, and the orientation of halo spins around voids
- quantitative descriptions of the evolving cosmic web, including applications to weak gravitational lensing
- preparation of mock catalogs, essential for analyzing SDSS and other survey data, and for preparing for new large surveys for dark energy etc.
- merger trees, essential for semi-analytic modeling of the evolving galaxy population, including models for the galaxy merger rate, the history of star formation and galaxy colors and morphology, the evolving AGN luminosity function, stellar and AGN feedback, recycling of gas and metals, etc.

Springel et al. 2005
WMAP-only Determination of $\sigma_8$ and $\Omega_M$
WMAP+SN+Clusters Determination of $\sigma_8$ and $\Omega_M$
WMAP+SN+Clusters Determination of $\sigma_8$ and $\Omega_M$

Millennium is now about 4σ away from observations.
Cosmological parameters are consistent with the latest observations.

Force and Mass Resolution are nearly an order of magnitude better than Millennium-I.

Force resolution is the same as Millennium-II, in a volume 16x larger.

Halo finding is complete to \( V_{\text{circ}} > 50 \) km/s, using both BDM and ROCKSTAR halo finders.

Bolshoi and MultiDark halo catalogs will be available by August 2011 at Astro Institut Potsdam.
1000 Mpc/h  BigBolshoi / MultiDark  8G particles

Same cosmology as Bolshoi: $h=0.70$, $\sigma_8=0.82$, $n=0.95$, $\Omega_m=0.27$

7 kpc/h resolution, complete to $V_{\text{circ}} > 170$ km/s

Monday, July 18, 2011
The Millennium Run (Springel+05) was a landmark simulation, and it has been the basis for ~400 papers. However, it and the new Millennium-II and XXL were run using WMAP1 (2003) parameters, and the Millennium-I resolution was inadequate to see many subhalos. The new Bolshoi simulation (Klypin, Trujillo & Primack 2011) used the WMAP5 parameters (consistent with WMAP7) and has nearly an order of magnitude better mass and force resolution than Millennium-I. We have now found halos in all 180 stored timesteps, and we have complete merger trees based on Bolshoi.


Halos and galaxies: results from the Bolshoi simulation

Cosmological Parameters

Velocity Function of Distinct Halos at z = 6.5, 5, 3, 2, 0

Subhalos follow the dark matter distribution

Power Spectrum

Clusters

BDM halo finder

Galaxies

Monday, July 18, 2011
The Sheth-Tormen approximation with the same WMAP5 parameters used for the Bolshoi simulation very accurately agrees with abundance of halos at low redshifts, but increasingly overpredicts bound spherical overdensity halo abundance at higher redshifts. ST agrees well with FOF halo abundances, but FOF halos have unrealistically large masses at high $z$. 

Each panel shows 1/2 of the dark matter particles in cubes of $1h^{-1}\text{Mpc}$ size. The center of each cube is the exact position of the center of mass of the corresponding FOF halo. The effective radius of each FOF halo in the plots is $150 - 200\ h^{-1}\text{kpc}$. Circles indicate virial radii of distinct halos and subhalos identified by the spherical overdensity algorithm BDM.

Halo mass–concentration relation of distinct halos at different redshifts in the Bolshoi (open symbols) and MultiDark (filled symbols) simulations is compared with an analytical approximation.

Comparison of observed cluster concentrations (data points with error bars) with the prediction of our model for median halo concentration of cluster-size halos (full curve). Dotted lines show 10% and 90% percentiles. Open circles show results for X-ray luminous galaxy clusters observed with XMMNewton in the redshift range 0.1-0.3 (Ettori et al. 2010). The pentagon presents galaxy kinematic estimate for relaxed clusters by Wojtak & Lokas (2010). The dashed curve shows prediction by Macciò, Dutton, & van den Bosch (2008), which significantly underestimates the concentrations of clusters.
Halo concentrations in the standard CDM cosmology

Francisco Prada, Anatoly A. Klypin, Antonio J. Cuesta, Juan E. Betancort-Rijo, and Joel Primack

$v_{\text{max}}/v_{200}$ for Millennium-I, II and Bolshoi/MultiDark

**Figure 5.** The ratio $v_{\text{max}}/v_{200}$ of the maximum circular velocity to the virial velocity as a function of mass $M_{200}$ for distinct halos at different redshifts for MS-I (filled symbols) and MS-II (open symbols) simulations. Error bars are statistical uncertainties. The MS-I and MS-II simulations agree quite well at $z = 0$. At higher redshifts there are noticeable differences between MS-I and MS-II.

**Figure 6.** The same as Figure 5 but for Bolshoi (open symbols) and MultiDark (filled symbols) simulations. Both simulations show remarkable agreement at all masses and redshifts.
We present a new algorithm for generating merger trees and halo catalogs which explicitly ensures consistency of halo properties (mass, position, velocity, radius) across timesteps. Our algorithm has demonstrated the ability to increase both the completeness (through inserting otherwise missing halos) and purity (through removing spurious objects) of both merger trees and halo catalogs. In addition, our method is able to robustly measure the self-consistency of halo finders; it is the first to directly measure the uncertainties in halo positions, halo velocities, and the halo mass function for a given halo finder based on actual cosmological simulations. We use this algorithm to generate merger trees for two large simulations (Bolshoi and Consuelo) and evaluate two halo finders (BDM and ROCKSTAR). We find that the ROCKSTAR halo finder self-consistently recovers the halo mass function at the 1-2% uncertainty level, whereas BDM recovers it at the 5-10% uncertainty level. Our code is publicly available at http://code.google.com/p/consistent-trees; our trees and catalogs are available on request, and they will be posted on a public website once the referee process is complete.
HALO MERGER TREE ALGORITHM

1. Identify halo descendants using a traditional particle algorithm.

2. Gravitationally evolve the positions and velocities of all halos at the current timestep back in time to identify their most likely positions at the previous timestep.

3. Based on predicted progenitor halos in step (2), cut ties to spurious descendants.

4. Create links for halos with likely progenitors at the previous timestep for cases in which step (2) has identified a good match.

5. For halos in the current timestep without likely progenitors, create a new halo at the previous timestep with position and velocity given by the evolution in step (2). Remove any such halos generated from previous rounds if they have had no real progenitors for several timesteps.

6. For halos in the previous timesteps which have no descendants, assume that a merger occurred into the halo exerting the strongest tidal field across it at the previous timestep. If a halo with no descendant is too far removed from other halos to experience a significant tidal field, assume that it is a statistical fluctuation and remove it from the tree and catalogs.

Behroozi et al. in prep.
BOLSHOI
Merger Tree
Peter Behroozi, et al.
The Milky Way has two large satellite galaxies, the small and large Magellanic Clouds.

The Bolshoi simulation + halo abundance matching predicts the likelihood of this.
Apply the same absolute magnitude and isolation cuts to Bolshoi+SHAM galaxies as to SDSS:

- Identify all objects with absolute $0.1M_r = -20.73 \pm 0.2$ and observed $m_r < 17.6$
- Probe out to $z = 0.15$, a volume of roughly 500 (Mpc/h)$^3$
- Leaves us with 3,200 objects.

Comparison of Bolshoi with SDSS observations is in close agreement, well within observed statistical error bars.

Statistics of MW bright satellites: SDSS data vs. Bolshoi simulation

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Similarly good agreement with SDSS for brighter satellites with spectroscopic redshifts compared with Millennium-II using abundance matching -- Tolorud, Boylan-Kolchin, et al.
The correlation function of SDSS galaxies vs. Bolshoi galaxies using halo abundance matching, with scatter using our stochastic abundance matching method. This results in a better than 20% agreement with SDSS. *Top left*: correlation function in three magnitude bins, showing Poisson uncertainties as thin lines. *Remaining panels*: correlation function in each luminosity bin compared with SDSS galaxies (points with error bars: Zehavi et al. 2010).

Projected correlation functions for galaxies in different stellar mass ranges, in SAM based on Millennium I and II. Black solid and blue dashed curves give results for preferred model applied to the MS and the MS-II, respectively. Symbols with error bars are results for SDSS/DR7 calculated using the same techniques as in Li et al. (2006). The two simulations give convergent results for $M_*> 6 \times 10^9 \, M_\odot$. At lower mass the MS underestimates the correlations on small scales. The model agrees quite well with the SDSS at all separations for $M_*> 6 \times 10^{10} \, M_\odot$. But at smaller masses the correlations are overestimated substantially, particularly at small separations. The authors attribute this to the too-high $\sigma_8 = 0.90$ used in MS-I & II.

Fig. 4.— Comparison of the observed Luminosity Velocity relation with the predictions of the ΛCDM model. The solid curve shows the median values of $0.1\sigma$-band luminosity vs. circular velocity for the model galaxy sample. The circular velocity for each model galaxy is based on the peak circular velocity of its host halo over its entire history, measured at a distance of 10 kpc from the center including the cold baryonic mass and the standard correction due to adiabatic halo contraction. The dashed curve show results for a steeper ($\alpha = -1.34$) slope of the LF. The dot-dashed curve shows predictions after adding the baryon mass but without adiabatic contraction. Points show representative observational samples.
Fig. 10.— Mass in cold baryons as a function of circular velocity. The solid curve shows the median values for the $\Lambda$CDM model using halo abundance matching. The cold baryonic mass includes stars and cold gas and the circular velocity is measured at 10 kpc from the center while including the effect of adiabatic contraction. For comparison we show the individual galaxies of several galaxy samples. Intermediate mass galaxies such as the Milky Way and M31 lie very close to our model results.
Fig. 11.— Comparison of theoretical (dot-dashed and thick solid curves) and observational (dashed curve) circular velocity functions. The dot-dashed line shows the effect of adding the baryons (stellar and cold gas components) to the central region of each DM halo and measuring the circular velocity at 10 kpc. The thick solid line is the distribution obtained when the adiabatic contraction of the DM halos is considered. Because of uncertainties in the AC models, realistic theoretical predictions should lie between the dot-dashed and solid curves. Both the theory and observations are highly uncertain for rare galaxies with \( V_{\text{circ}} > 400 \text{ km s}^{-1} \). Two vertical dotted lines divide the VF into three domains: \( V_{\text{circ}} > 400 \text{ km s}^{-1} \) with large observational and theoretical uncertainties; \( 80 \text{ km s}^{-1} < V_{\text{circ}} < 400 \text{ km s}^{-1} \) with a reasonable agreement, and \( V_{\text{circ}} < 80 \text{ km s}^{-1} \), where the theory significantly overpredicts the number of dwarfs.
First SAM galaxy results with Bolshoi - Rachel Somerville

Star Formation Efficiency

Galaxy Baryonic Mass Function

Metallicity Evolution

Gas Fraction vs. $M_{\text{star}}$

Preliminary

Monday, July 18, 2011
Stellar Mass Function

Cold Gas Mass Function

Black Hole Mass Function

Black Hole Mass vs. Bulge Mass

Theory & Observations Agree Pretty Well

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Bolshoi simulations - recent progress

• Anatoly Klypin has improved his BDM halofinder. It now finds the spin parameter, concentration, shape and orientation of all halos. It also produces catalogs for both “virial” and overdensity-200 halo definitions. Results on all 180 stored timesteps of the Bolshoi simulation will be available. Peter Behroozi new phase-space halo finder ROCKSTAR finds subhalos better in the central regions of larger halos.

• All catalogs are finished for BigBolshoi/MultiDark, which has the same cosmology as Bolshoi in a volume 64x larger. It has 7 kpc/h resolution, and is complete to $V_{\text{circ}} > 170$ km/s (so all MWy-size halos are found). BigBolshoi simulations can now be run and analyzed in one week; two more are planned to get statistics for BOSS. Merger trees are coming soon.

• A new miniBolshoi simulation is running now. It will have a force resolution of about 100 pc and a mass resolution of about $2 \times 10^6 M_{\odot}$ and it will be complete to 15 km/s or better. We will have complete merger histories and substructure for hundreds of MWy-size halos.

• Halo catalogs will be available by August 2011 at Astro Institut Potsdam: [http://www.multidark.org/MultiDark/](http://www.multidark.org/MultiDark/) (You have to get an account there.)

Next: Merger Trees. We hope to have them up soon also at other sites.
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