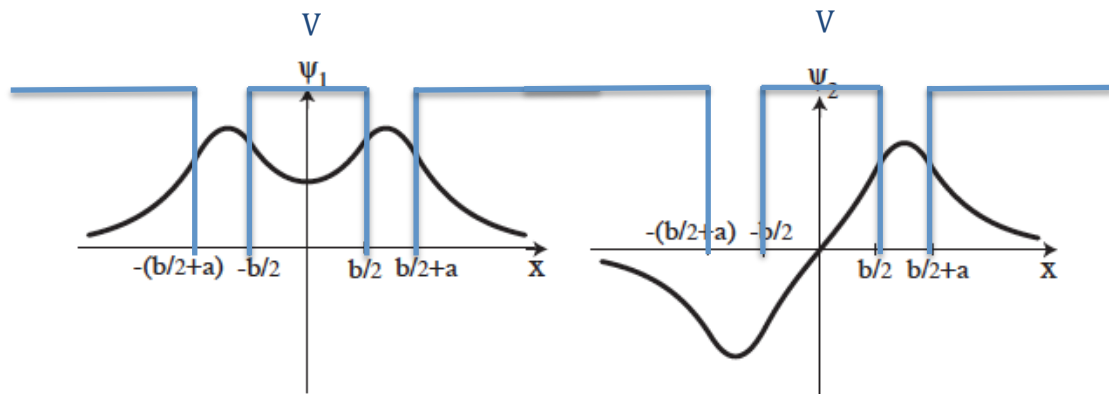


- (a) $p = -i\hbar d/dx$ [1 mark]
 $\langle p \rangle = \int \Psi^* p \Psi dx$ [1 mark]
 $= -A^2 i\hbar \int x(L-x) d/dx [x(L-x)] dx = -A^2 i\hbar \int x(L-x)(L-2x) dx =$
 $-A^2 i\hbar \int x(L^2 - 3Lx + 2x^2) dx = -A^2 i\hbar [L^2 x^2/2 - 3Lx^3/3 + 2x^4/4]_0^L = 0$
[1 mark]
its a standing wave [1 mark]
- (b) see sketch [3 marks]
the peak is shifted away from the midpoint towards the origin as there is more probability that it can be in the middle energy barrier than at the edges due to leakage from the other well [1 mark]
- (c) $E = \hbar\omega_x(n_x + 1/2) + \hbar\omega_x(n_y + 1/2) + 2\hbar\omega_x(n_z + 1/2)$
 $= \hbar\omega_x(n_x + n_y + 2n_z + 2)$ [1 mark]
ground. $n_x = n_y = n_z = 0$ so $E = 2\hbar\omega_x$ degeneracy 1 [1 mark]
first excited $n_x = 1, n_y = n_z = 0$
or $n_x = 0, n_y = 1, n_z = 0$ (not $n_x = 1$ as this is next level up) so
degeneracy is 2 and energy $E = 3\hbar\omega_x$ [1 mark]
maximize degeneracy if $\omega_x = \omega_y = \omega_z$. minimize if not comensurate
[1 mark]
- (d) prob is $\psi_{000}^* \psi_{000} dV = \psi_{000}^* \psi_{000} r^2 \sin\theta dr d\theta d\phi$ [1 mark]
prob within dr of r means integrate over angles so
 $= \int_0^\pi \int_0^{2\pi} (\pi a^3)^{-1} e^{-2r/a} r^2 \sin\theta dr d\theta d\phi$ [1 mark]
 $= 4\pi / (\pi a^3) e^{-2r/a} r^2 dr = (4/a^3) r^2 e^{-2r/a}$ [1 mark]
peaks when $dD(r)/dr = 0$ so $2re^{-2r/a} - 2/ar^2 e^{-2r/a} = 0$ and $r = a$.
[1 mark]



1 mark for potential
 1 mark for ground state
 1 mark for excited state