## ELEMENTS OF QUANTUM MECHANICS - EXAMPLES CLASS 2

Q1 The infinite potential well in 1 dimension has energy eigenfunctions  $\psi_n$  with energy  $E_n = n^2 E_1$ . An electron in this potential has a wavefunction  $\psi(x, t = 0) = A[\psi_1 + 3\psi_2 + \psi_3].$ 

- (a) Use the normalisation condition on  $\psi(x, t = 0)$  and the orthonormal properties of the energy eigenfunctions to show that  $A = 1/\sqrt{11}$ .
- (b) What is the probability (3 sig figs) that a measurement of energy gives  $E_1$ ?
- (c) If the system has been measured to have energy  $E_1$ , what is the probability that a subsequent measurement of energy will give  $E_2$ ?
- (d) Write down  $\langle E \rangle$  in terms of  $E_1$  and calculate it. can any single measurement of E give this value?

Q2. An electron in the infinite potential well has a wavefunction which is symmetric about L/2. What is the probability that the system is found in state  $\psi_2$ ? Hint: draw the n=1,2 and 3 wavefunctions of the infinite square well, and consider their symmetry properties.

Q3. Sketch (without calculation) the potential and its wavefunctions of the n=1,2 and 3 levels. For each potential, comment on whether the number of bound states is finite or infinite.

- (a) the finite square well potential where V = 0 for -L/2 < x < L/2 and  $V = V_0$  elsewhere
- (b) the asymmetric finite square well potential where V = 0 for -L/2 < x < L/2 and  $V = V_0$  for x > L/2 and  $V = 2V_0$  for x < L/2
- (c) the inverse gaussian potential  $V = V_0(1 e^{-x^2/2L^2})$  for  $-\infty < x < \infty$