



# Cosmology in our backyard

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*Institute for Computational Cosmology,*  
*Durham*



cold dark matter



$\Lambda$ CDM: the standard model of  
cosmology



cosmological constant

Why is this the standard model?

New tests and possible problems

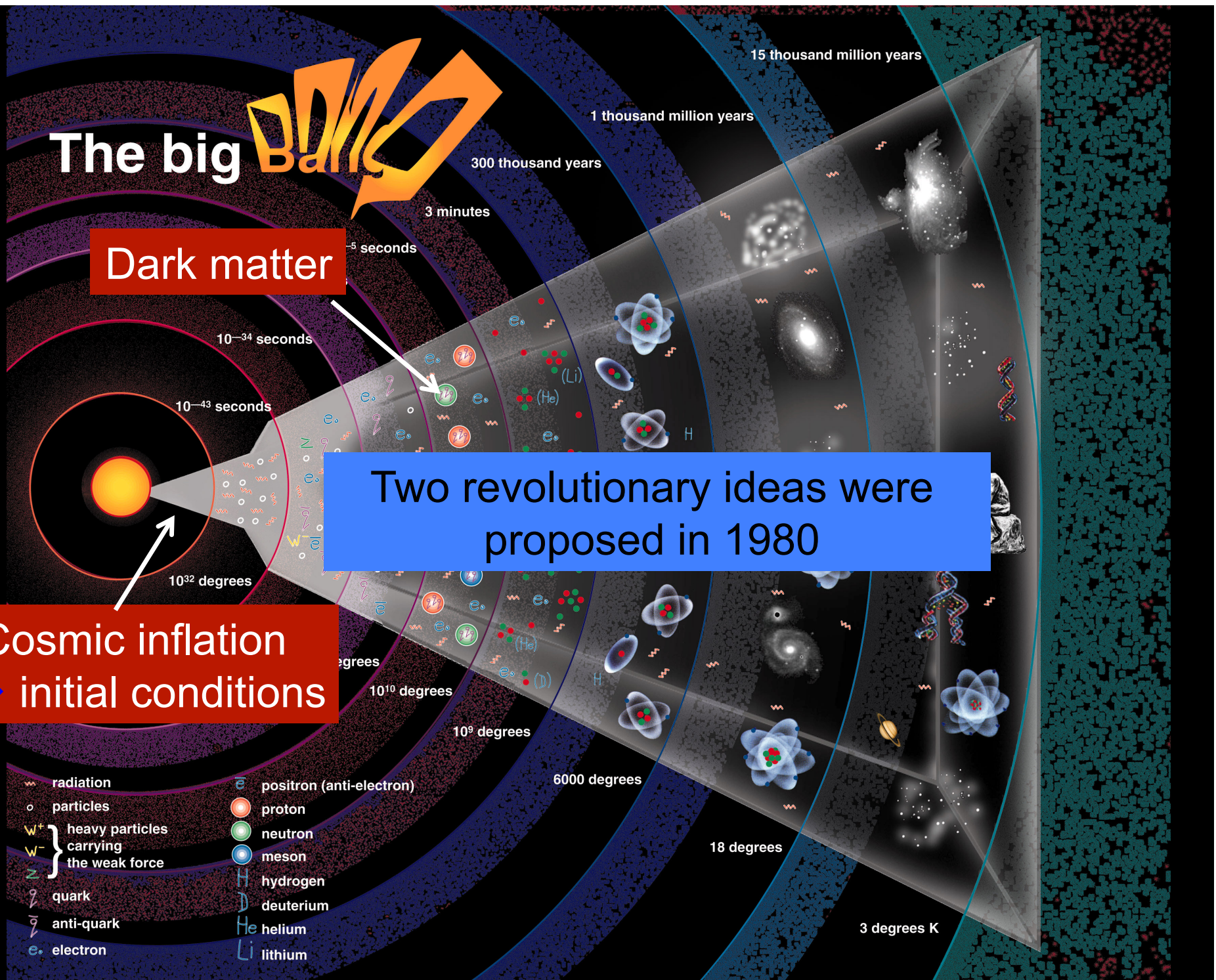


# The big Bang

Dark matter

Cosmic inflation  
→ initial conditions

Two revolutionary ideas were  
proposed in 1980



# Non-baryonic dark matter candidates

Type	example	mass
hot	neutrino	a few eV
warm	sterile $\nu$ majoron; KeV $\nu$	keV-MeV
cold	axion neutralino	$10^{-5}\text{eV}-$ $>100\text{ GeV}$

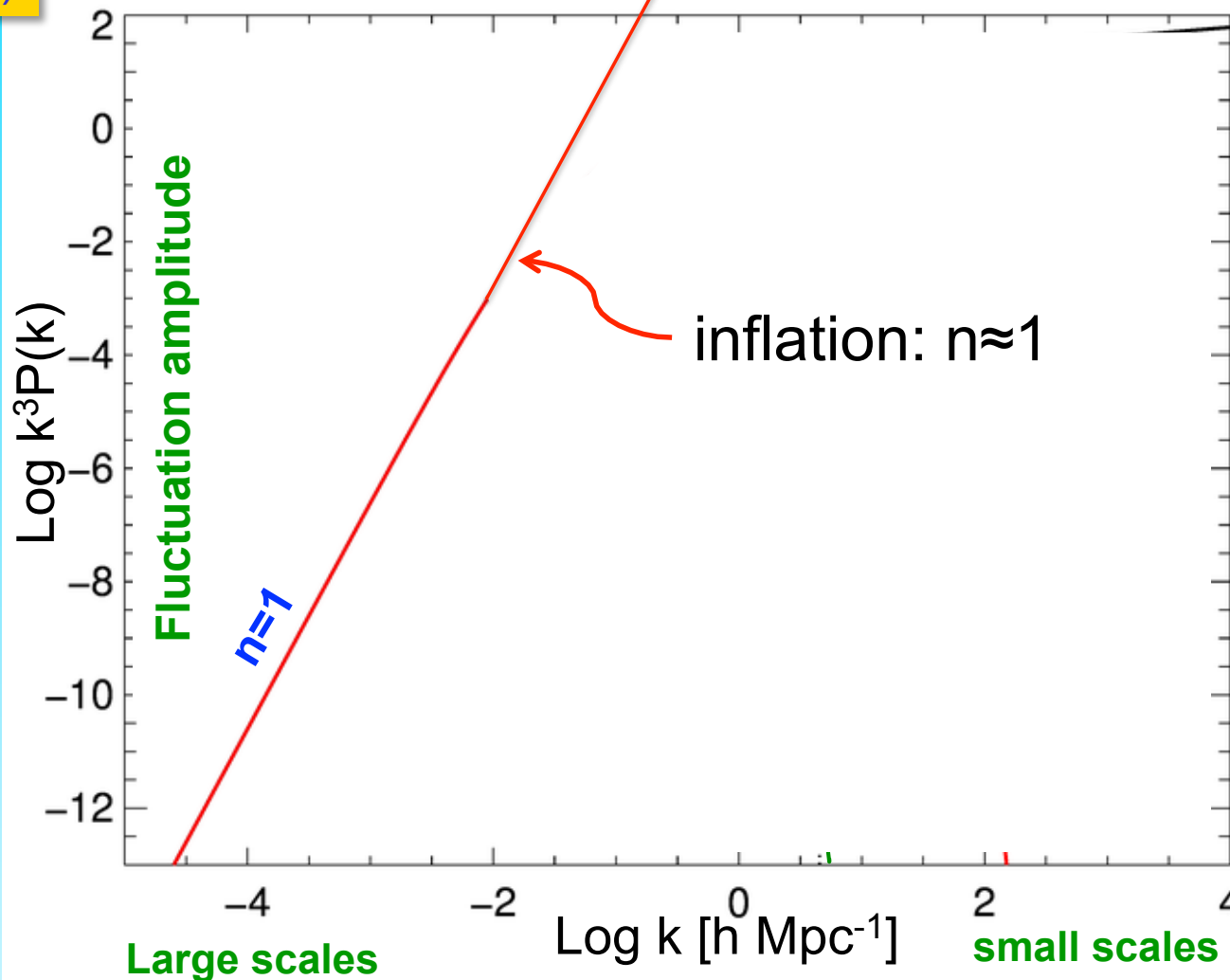


# The dark matter power spectrum

$k^3 P(k)$

The linear power spectrum (“power per octave”)

Prediction from  
inflation



# The dark matter power spectrum

$k^3 P(k)$

Free streaming →

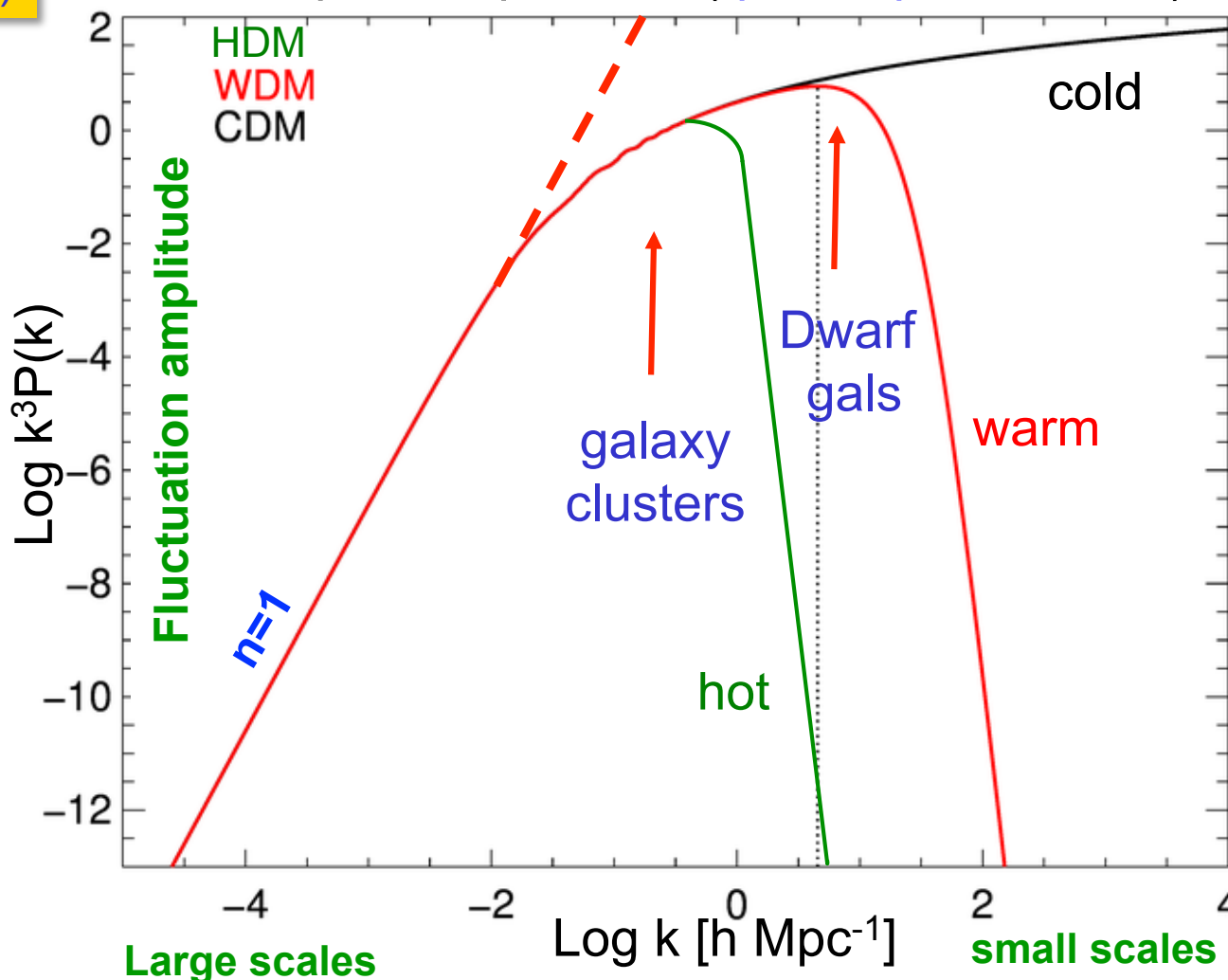
$\lambda_{\text{cut}} \propto m_x^{-1}$   
for thermal relic

$m_{\text{CDM}} \sim 100 \text{ GeV}$   
susy;  $M_{\text{cut}} \sim 10^{-6} M_{\odot}$

$m_{\text{WDM}} \sim \text{few keV}$   
sterile  $\nu$ ;  $M_{\text{cut}} \sim 10^9 M_{\odot}$

$m_{\text{HDM}} \sim \text{few eV}$   
light  $\nu$ ;  $M_{\text{cut}} \sim 10^{15} M_{\odot}$

The linear power spectrum (“power per octave”)

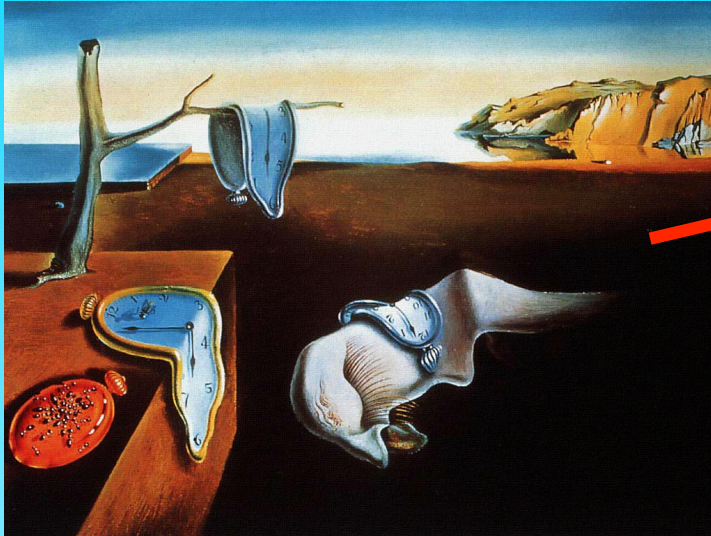




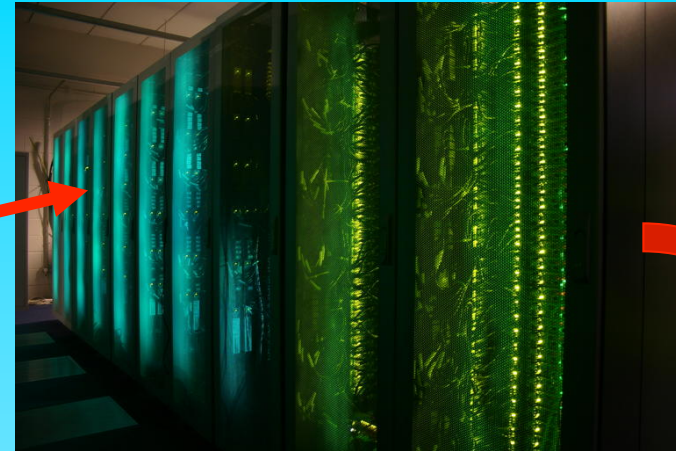
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# The formation of cosmic structure

$t=10^{-35}$  seconds



“Cosmology machine”



$t=380,000$  yrs

$\delta\rho/\rho \sim 10^{-5}$

Simulations

Supercomputer **simulations** are the best technique for calculating how small **primordial perturbations** grow into **galaxies** today



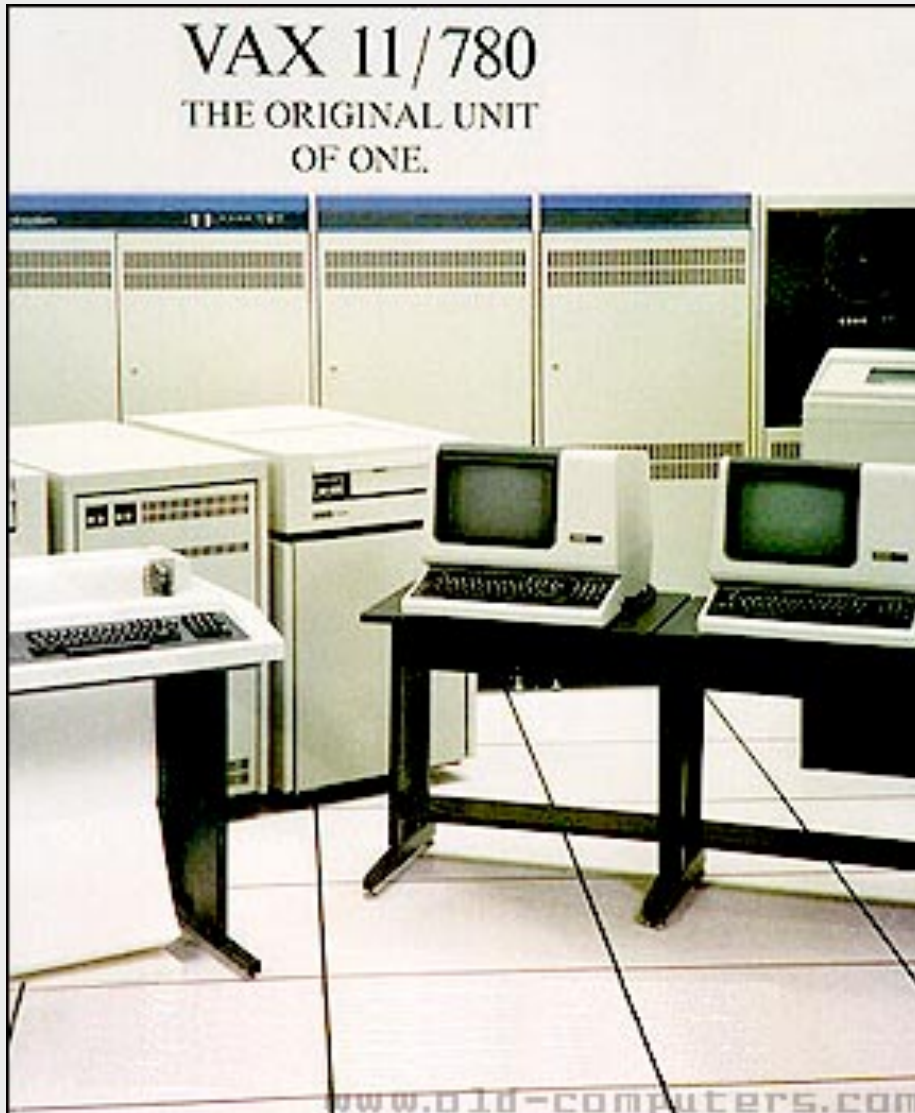
$t=13.8$  billion yrs

$\delta\rho/\rho \sim 1-10^6$

Institute for Computational Cosmology



# The universe in a computer



December 1981

Speed = 500,000 FLOPS

RAM = 4 Mbytes

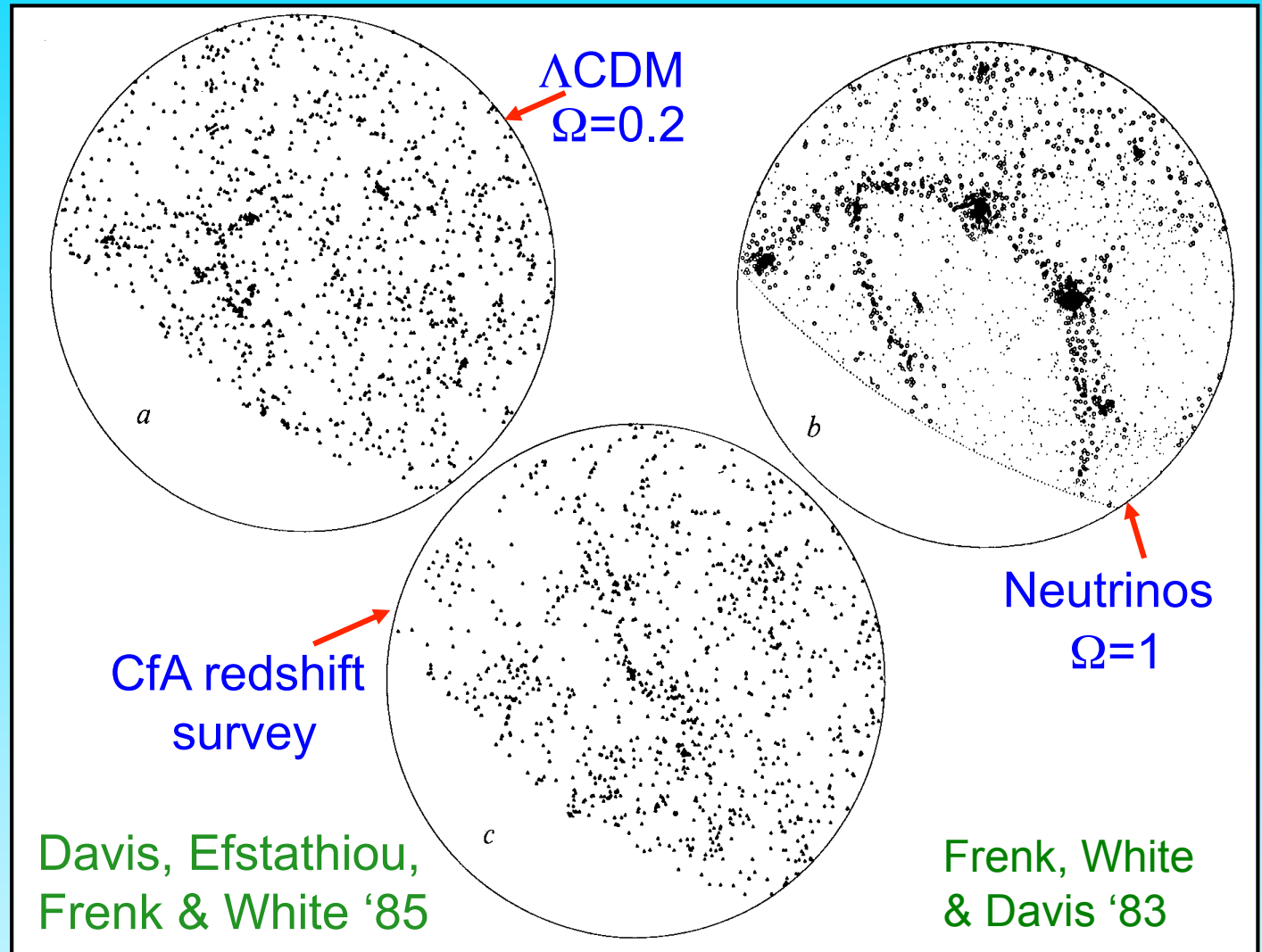
# Non-baryonic dark matter cosmologies

Neutrino DM →  
unrealistic clust'ing

Neutrinos cannot  
make appreciable  
contribution to  $\Omega$   
→  $m_\nu \ll 10$  eV

Early CDM N-body  
simulations gave  
promising results

In CDM structure  
forms hierarchically



# Non-baryonic dark matter candidates

Type                      example                      mass

hot	neutrino	a few eV
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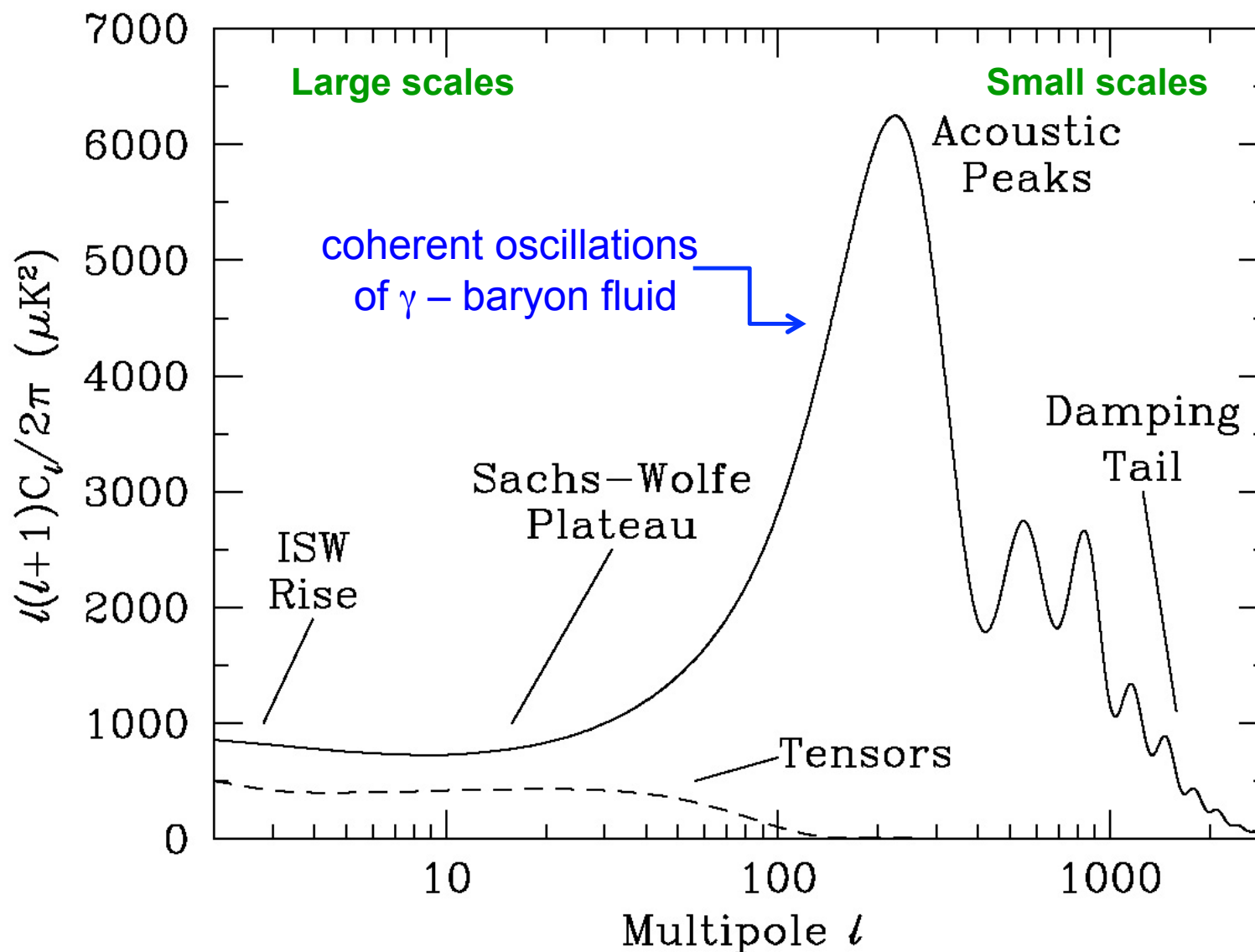
$\Lambda$ CDM model is an *a priori*  
implausible model!

... but makes definite predictions and is therefore testable

Main successes of the CDM cosmogony:

1. CMB temp. anisotropies: predicted in 1981, discovered in 1993
2. Spatial distribution of gals (1990- QDOT, APM, 2dFGRS, SDSS)
3. General features of galaxy luminosity function (1991 - )
4. Evolution of the galaxy population (2000 - )

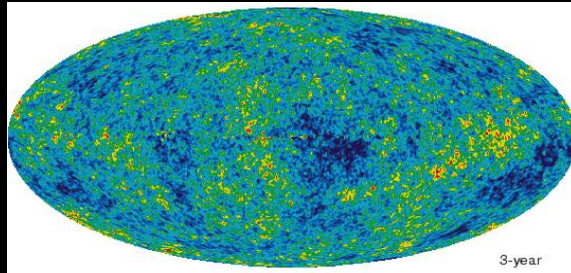
# Temperature anisotropies in CMB



After Peebles & Yu '70; Peebles '82



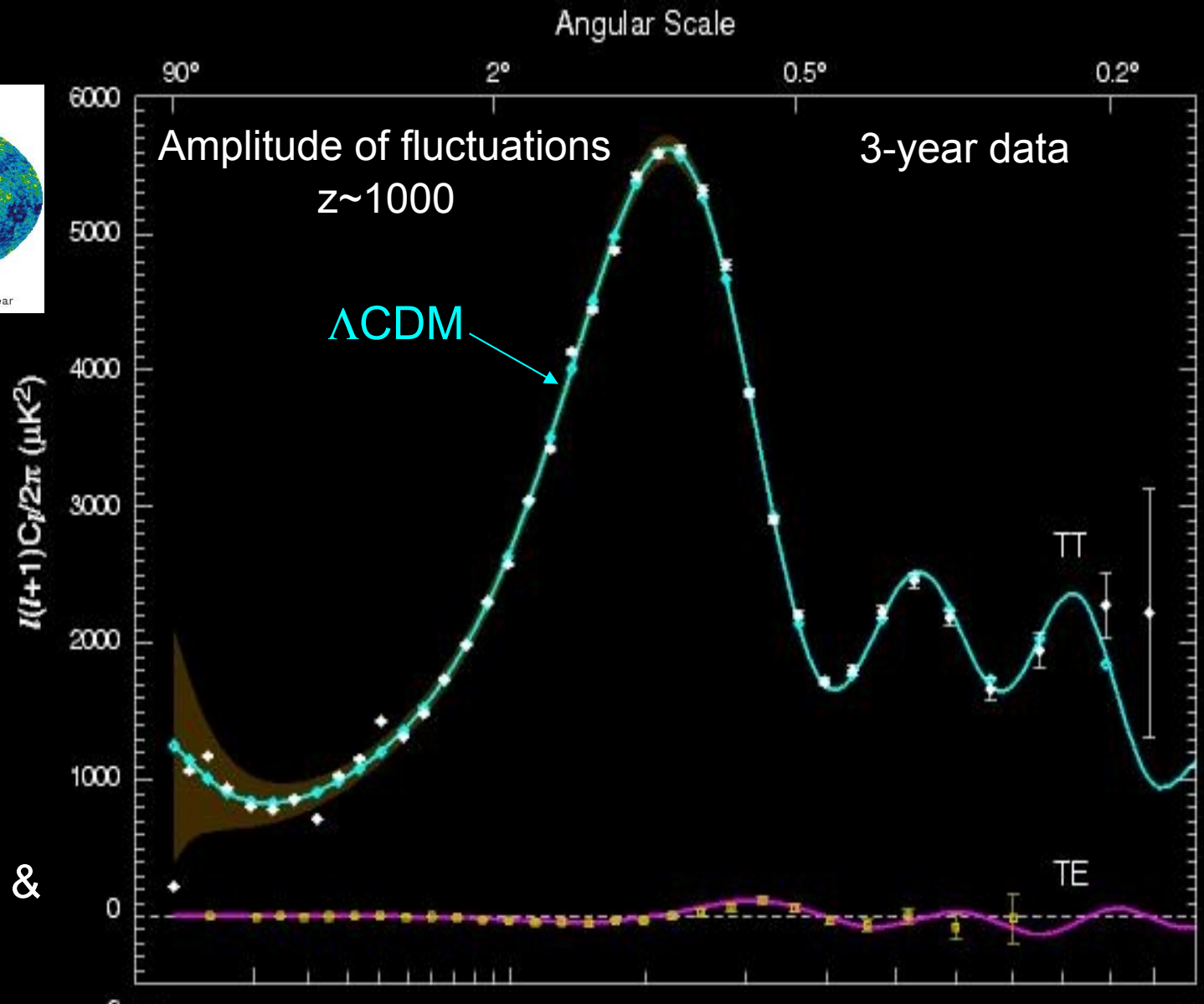
# WMAP temp anisotropies in CMB



The data confirm  
the theoretical  
predictions  
(linear theory)

Peebles '82; Bond &  
Efstathiou '80s

Hinshaw et al '06



# The cold dark matter cosmogony

Main successes of the CDM cosmogony:

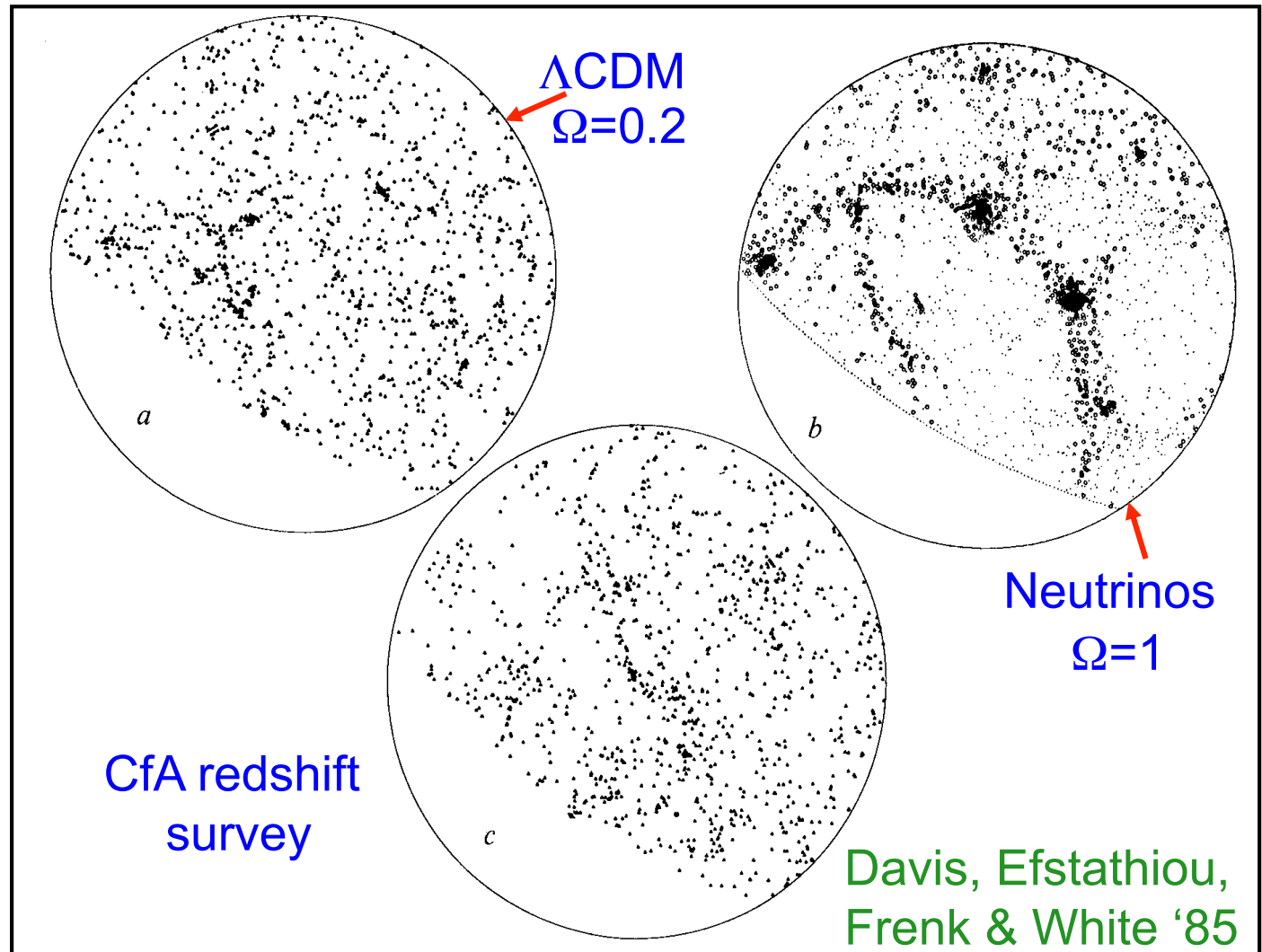
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# Non-baryonic dark matter cosmologies

Neutrino dark matter produces unrealistic clustering

Early CDM N-body simulations gave promising results

In CDM structure forms hierarchically



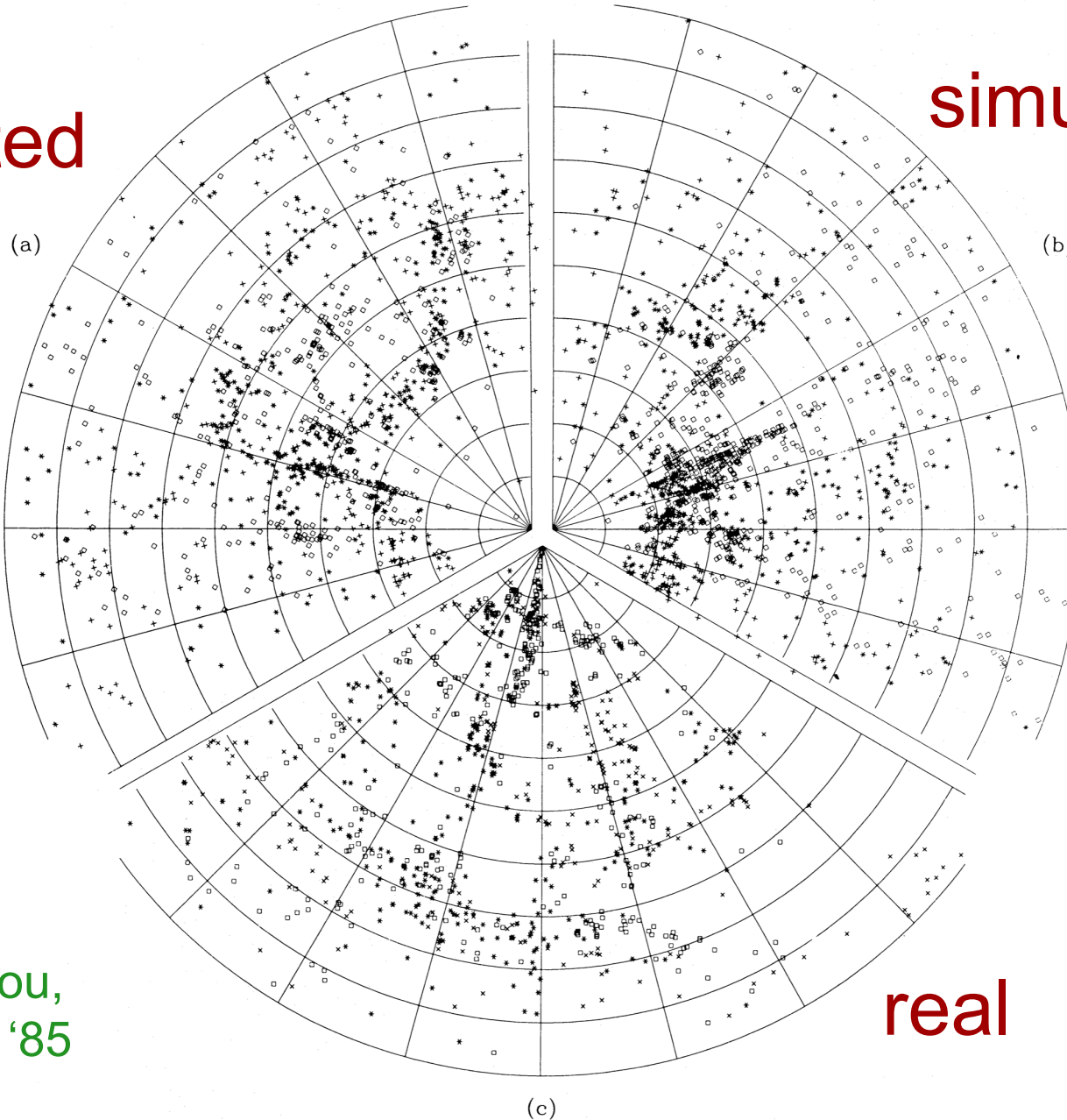




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# Early simulations of $\Lambda$ CDM

simulated



Davis, Efstathiou,  
Frenk & White '85

# The 2dF Galaxy Redshift Survey

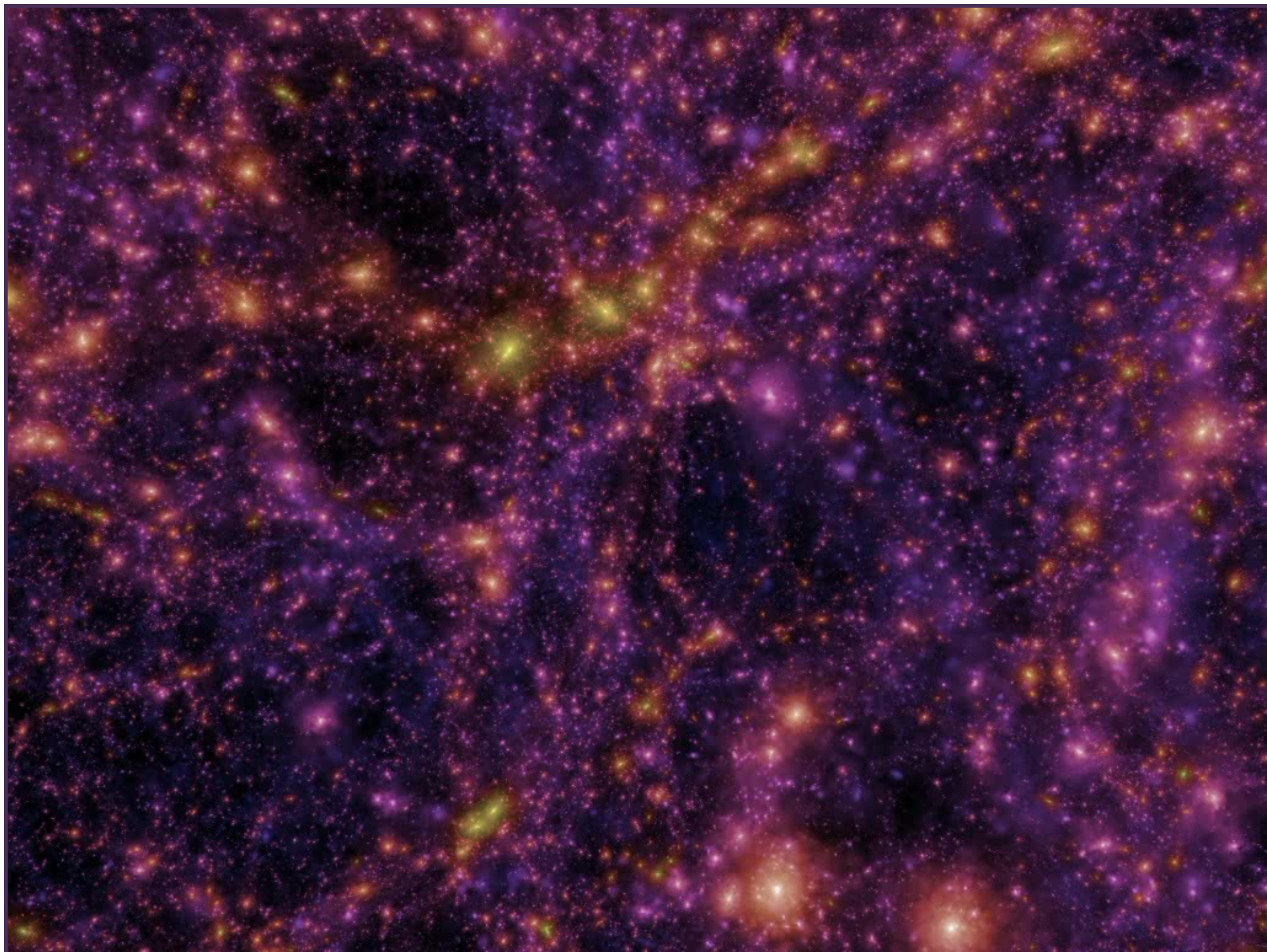
221,000 redshifts

$z \sim 0$

2005









$z = 0$  Dark Matter

125 Mpc/h

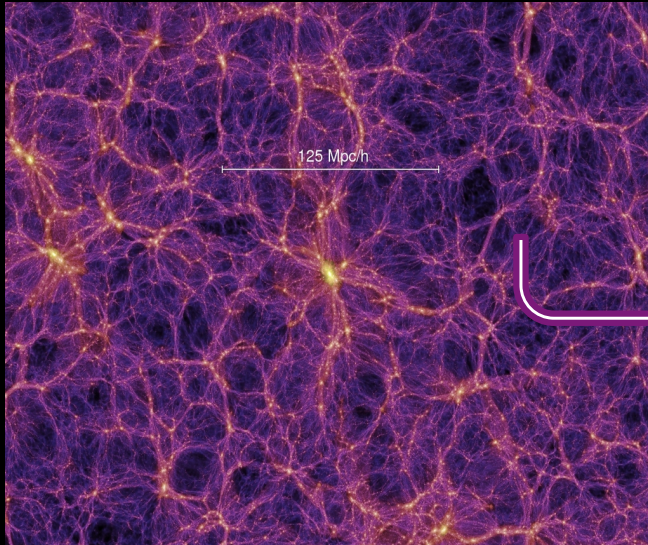


Springel et al 05

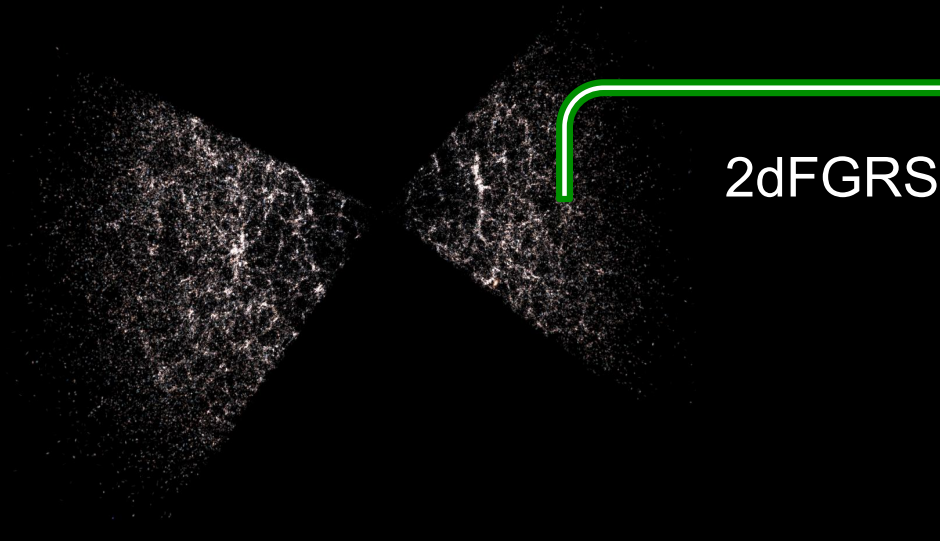
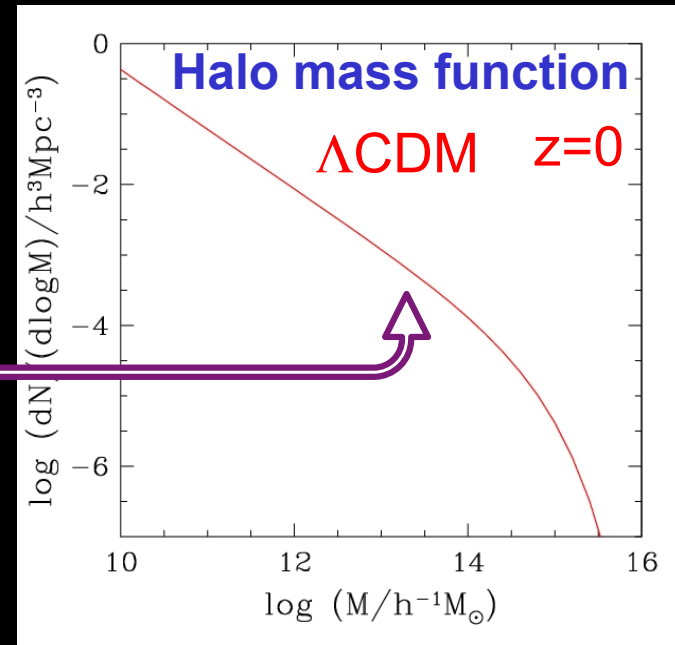




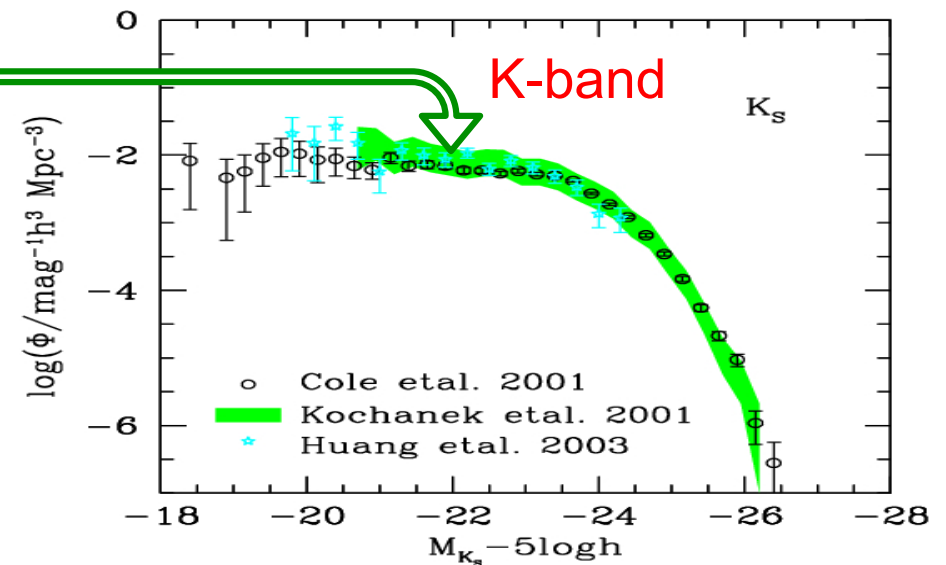
# Abundance of gals & dark halos



Millennium run



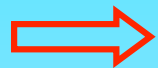
2dFGRS



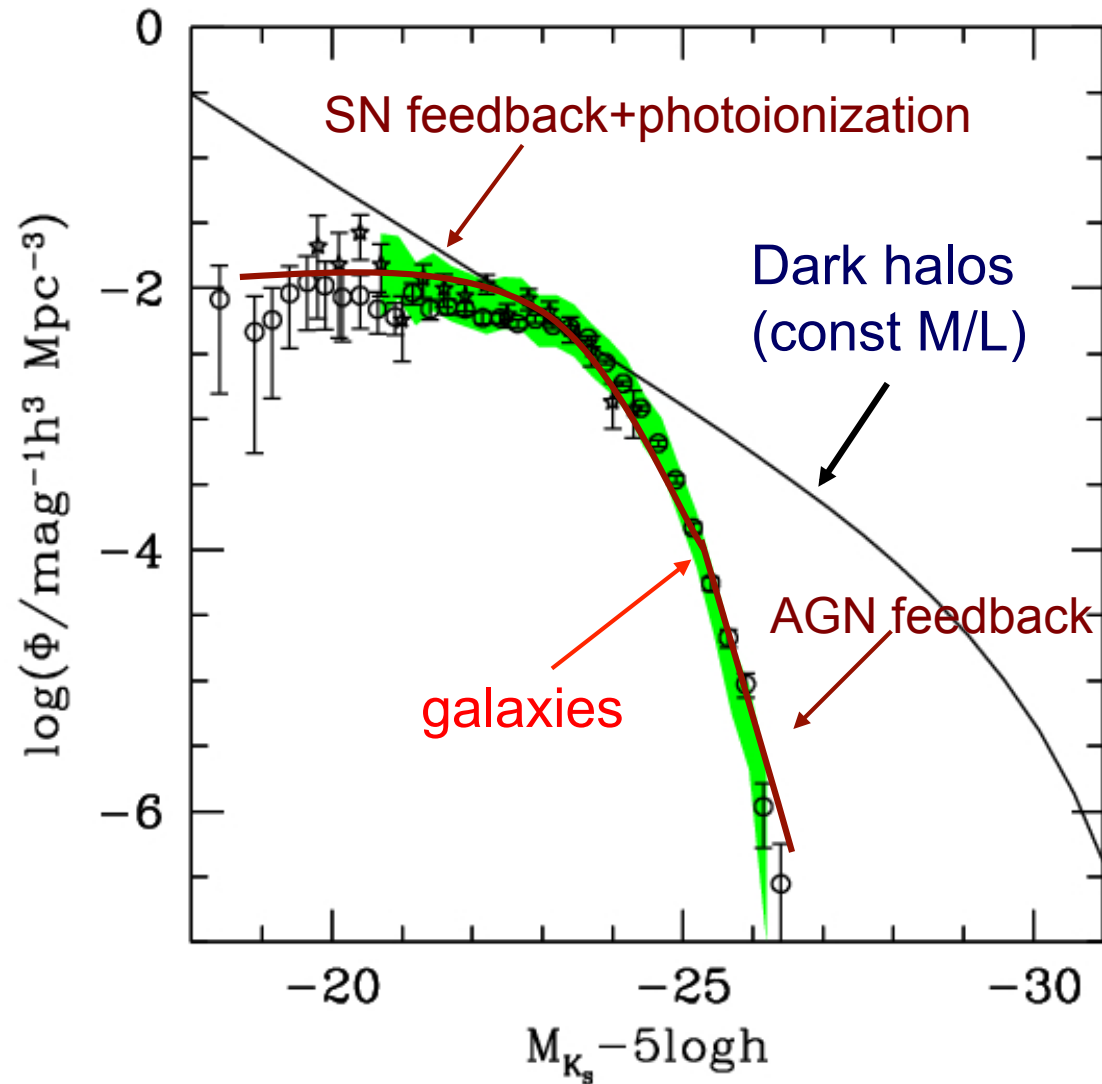


# The galaxy luminosity function

The halo mass function and the galaxy luminosity function have different shapes



Complicated variation of M/L with halo mass



White & Frenk '91; Kauffmann et al '93; Benson et al '03; Croton et al '05; Bower et al. '06

Main successes of the CDM cosmogony:

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$z = 0$  Dark Matter

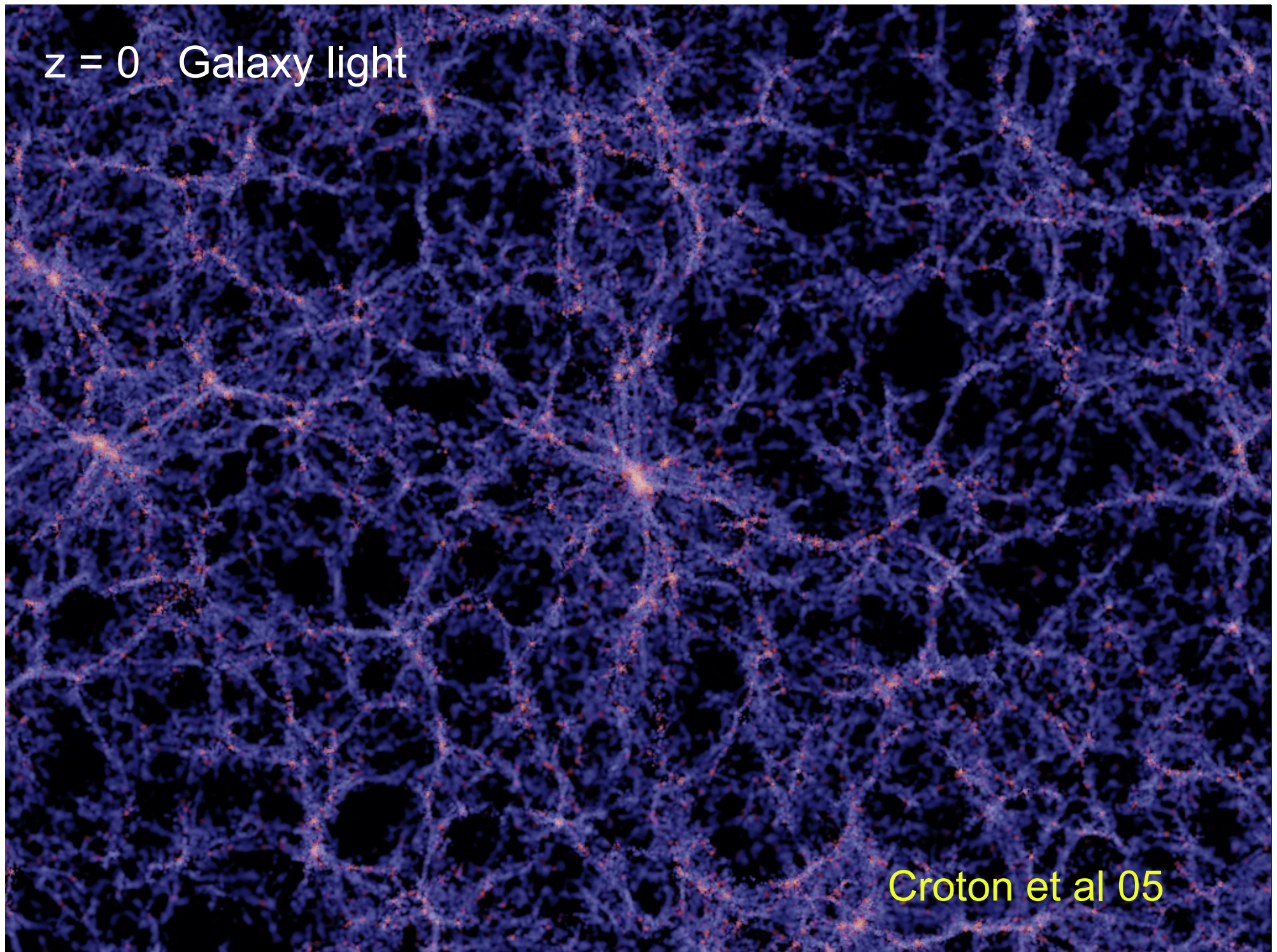
125 Mpc/h



Springel et al 05



$z = 0$  Galaxy light



Croton et al 05

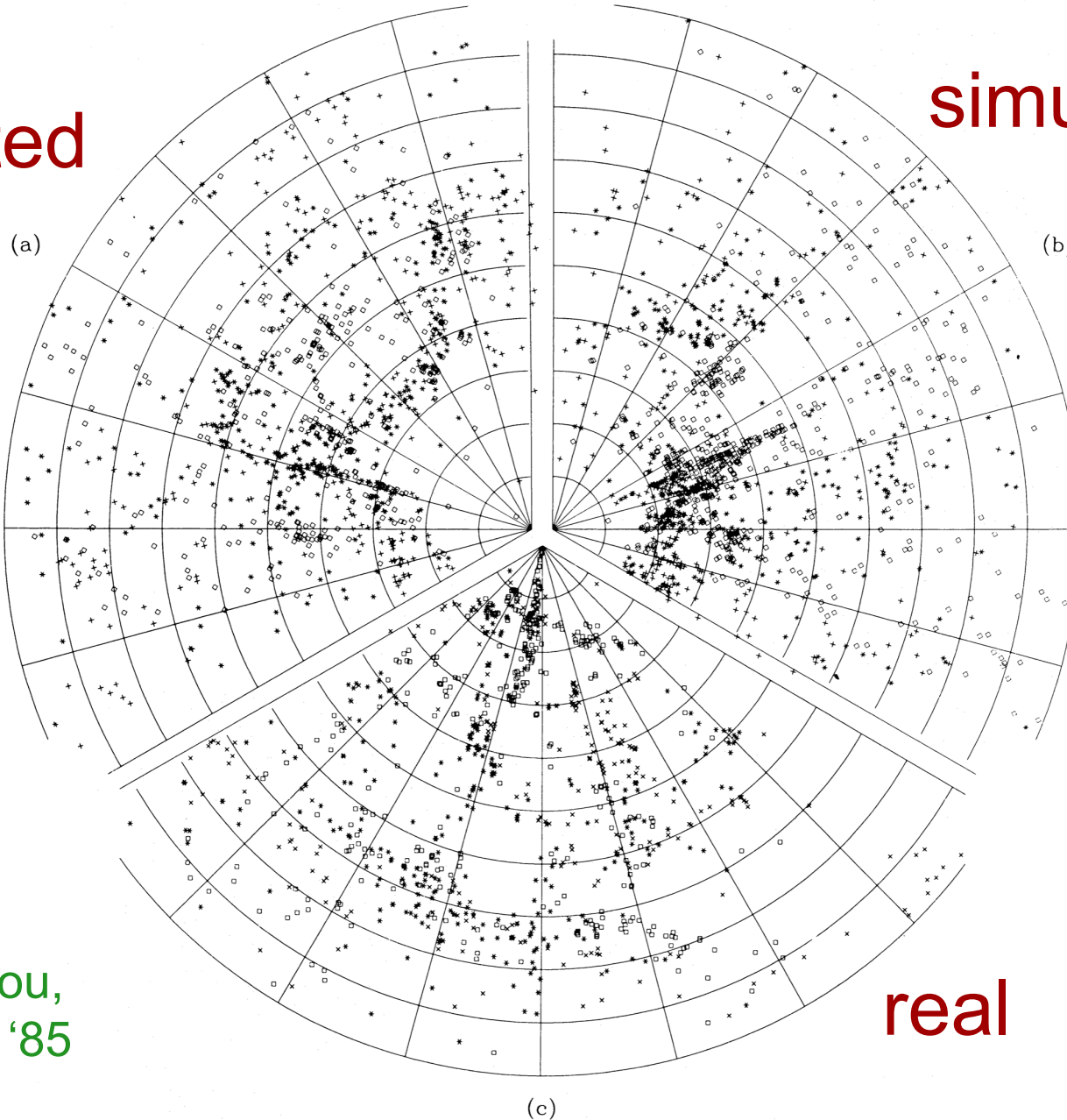




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# Early simulations of $\Lambda$ CDM

simulated



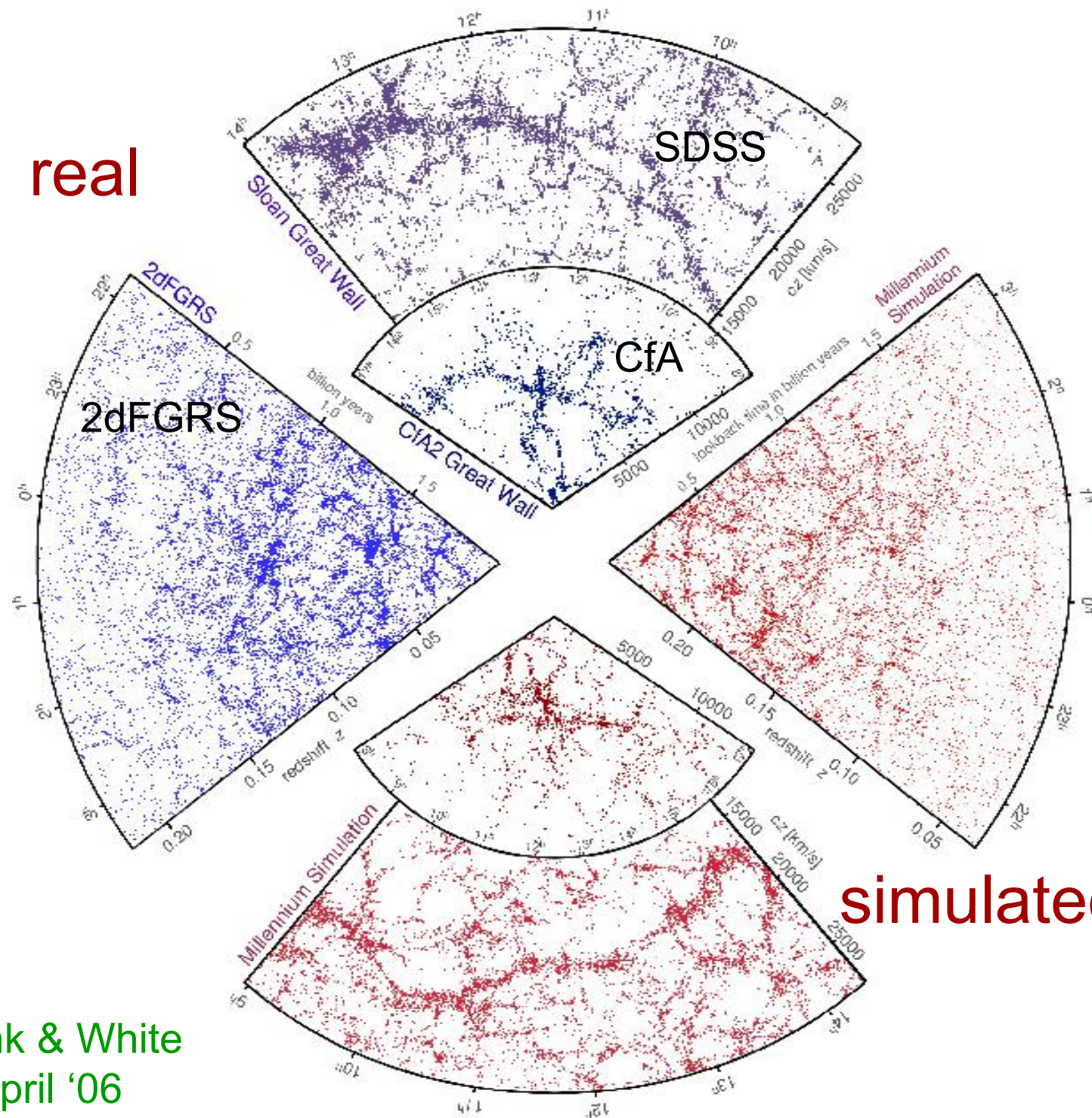
simulated

Davis, Efstathiou,  
Frenk & White '85

real



real

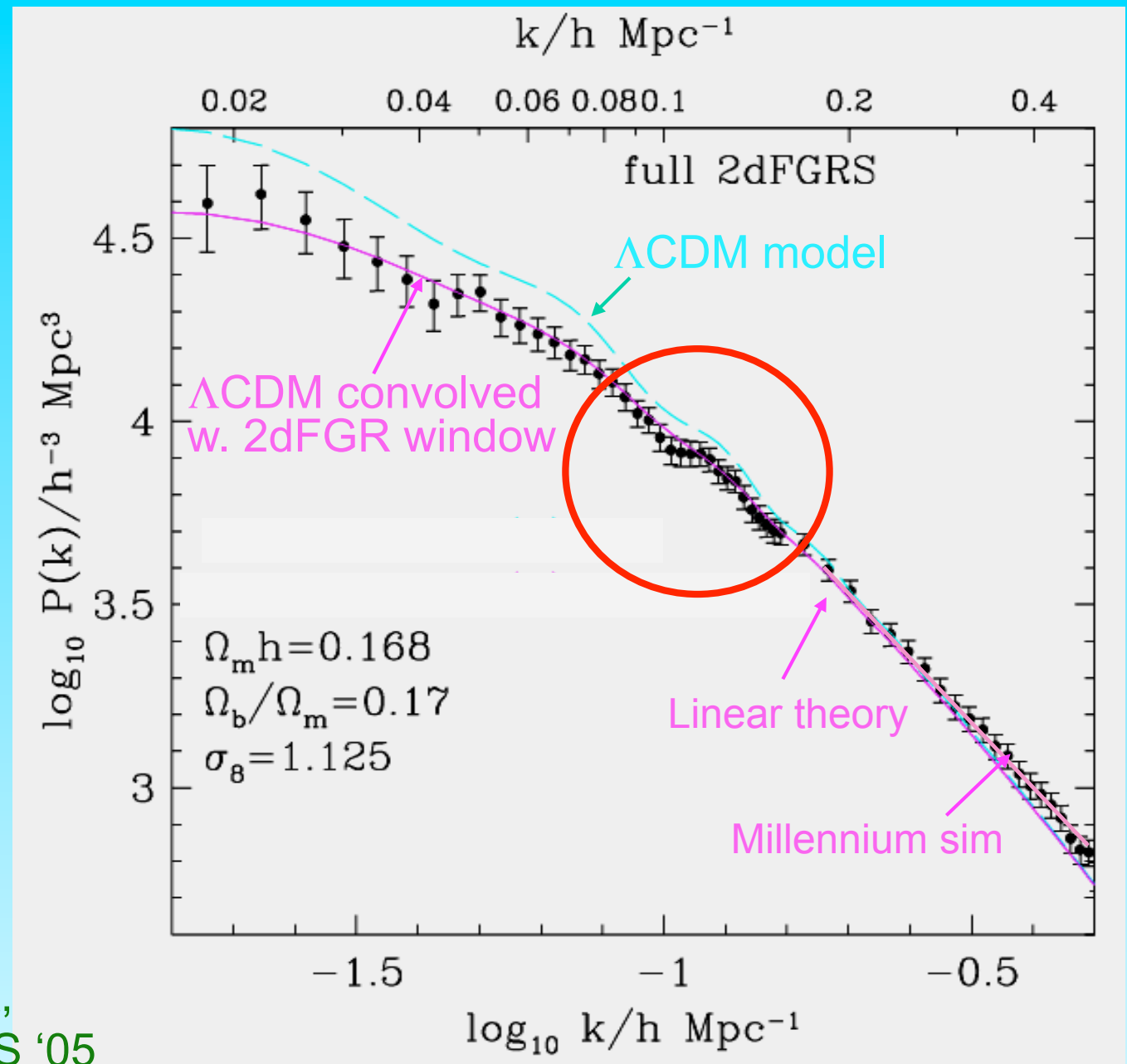


simulated

Springel, Frenk & White  
Nature, April '06

# The final 2dFGRS power spectrum

2dFGRS  $P(k)$   
well fit by  $\Lambda$ CDM  
model convolved  
with window  
function



Cole, Percival, Peacock,  
Baugh, Frenk + 2dFGRS '05

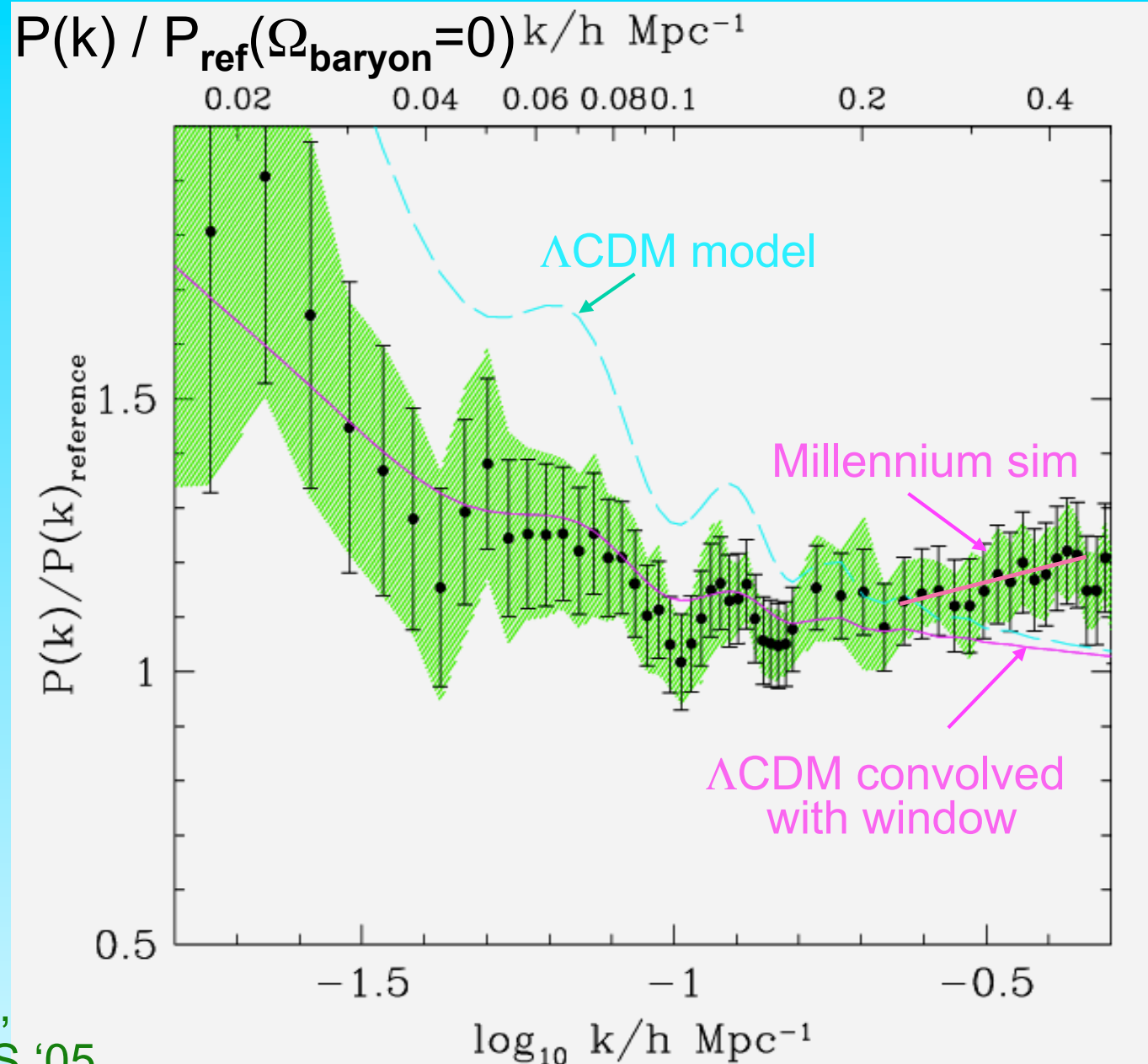
# The final 2dFGRS power spectrum

Baryon oscillations  
conclusively  
detected in  
2dFGRS!!!

Demonstrates that  
structure grew by  
gravitational  
instability in  $\Lambda$ CDM  
universe

Also detected in  
SDSS LRG sample  
(Eisenstein et al 05)

Cole, Percival, Peacock,  
Baugh, Frenk + 2dFGRS '05





# The cold dark matter cosmogony

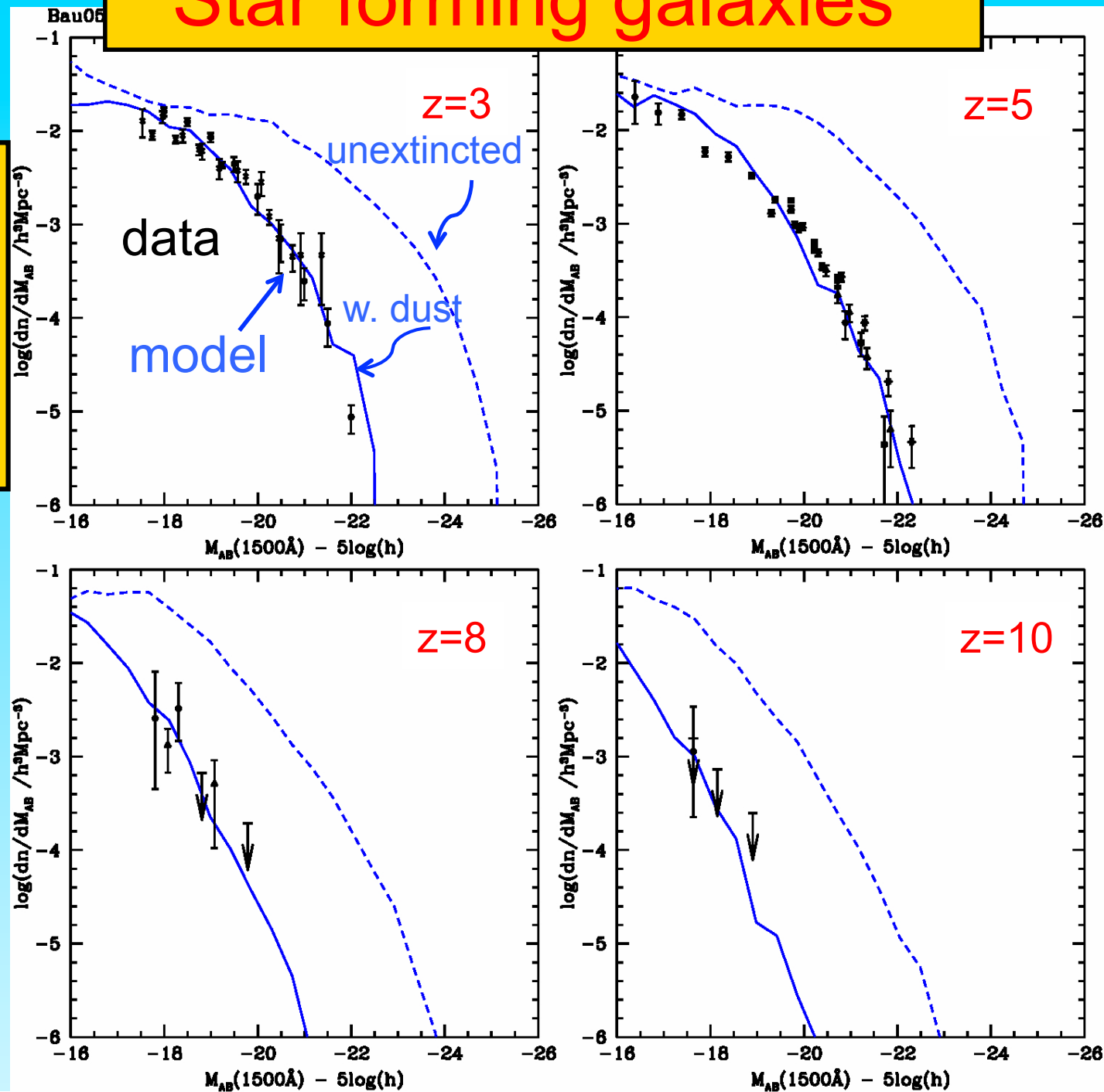
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# Star forming galaxies

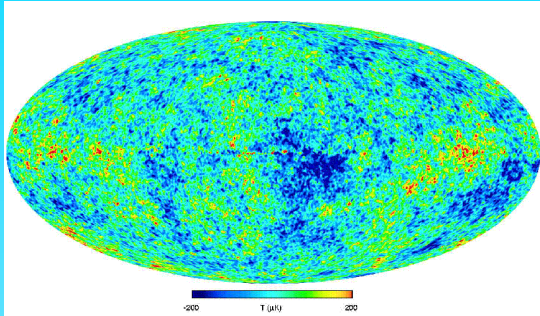
## Evolution of Lyman-break galaxy lum. function

Lacey, Baugh,  
Frenk, Benson '11

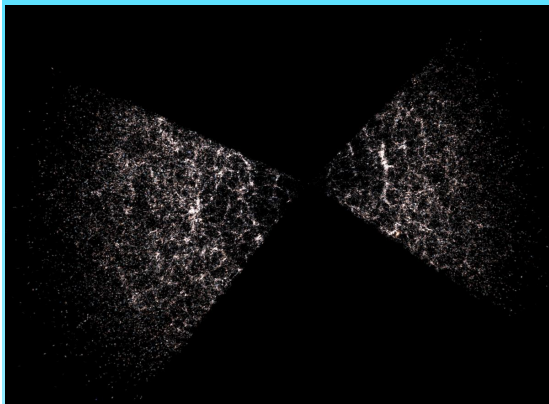




# The cosmic power spectrum: from the CMB to the 2dFGRS



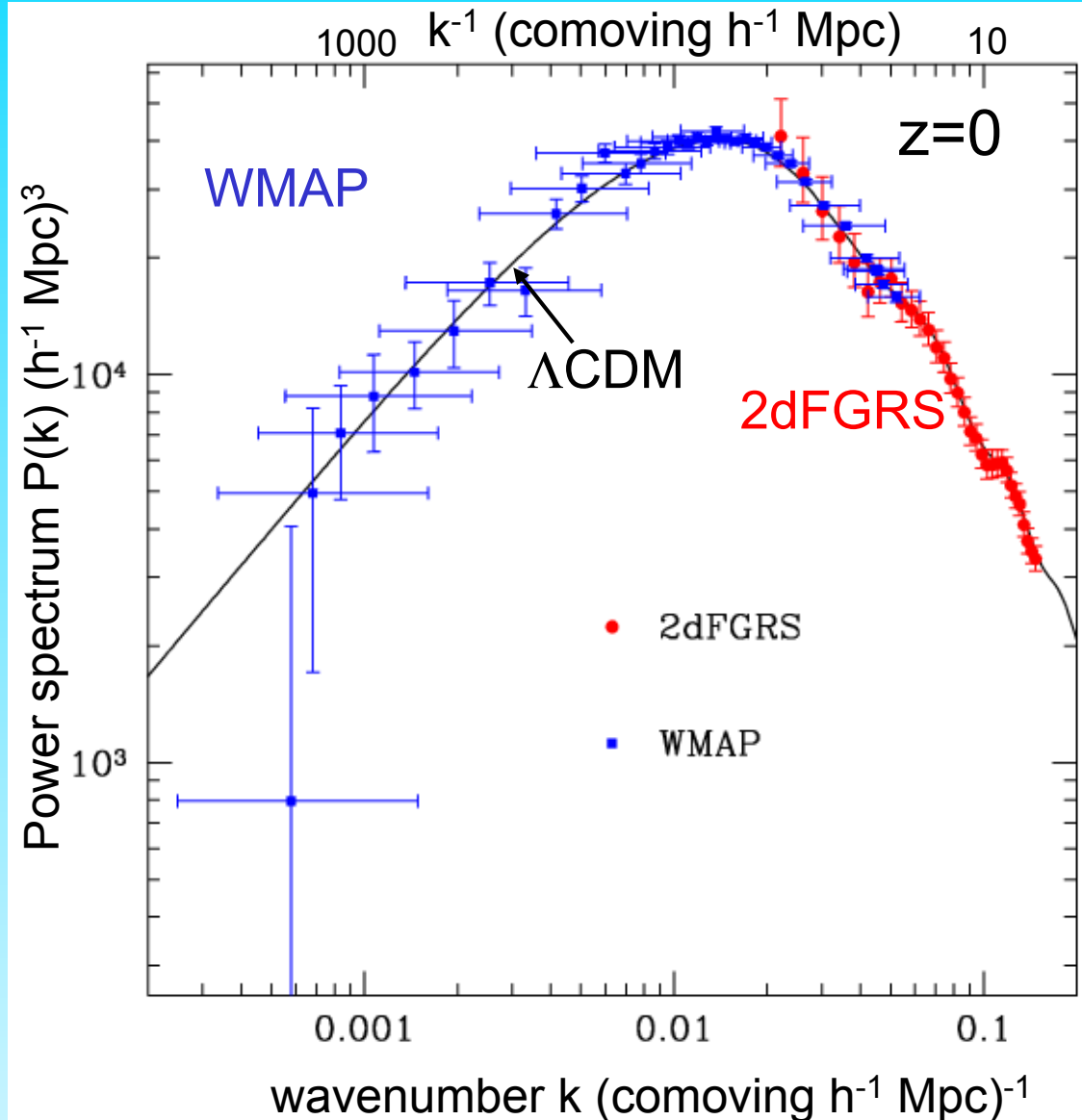
$z \sim 1000$



$z \sim 0$

⇒  $\Lambda$ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06



# The dark matter power spectrum

$k^3 P(k)$

Free streaming →

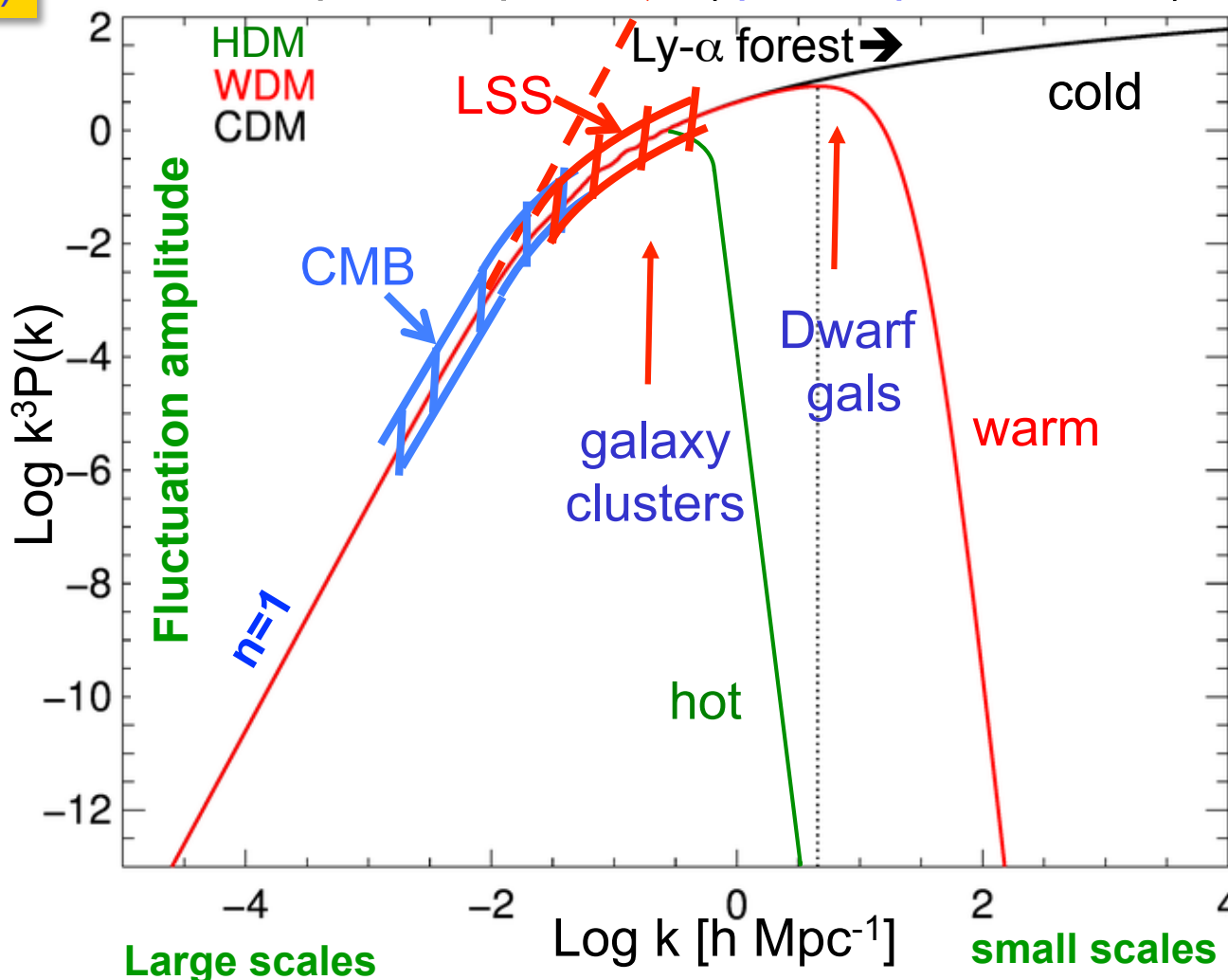
$\lambda_{\text{cut}} \propto m_x^{-1}$   
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The linear power spectrum (“power per octave”)





Cosmology on small – **strongly  
non-linear** – scales

→ key to the identity of the dark matter

$z = 48.4$

$T = 0.05 \text{ Gyr}$

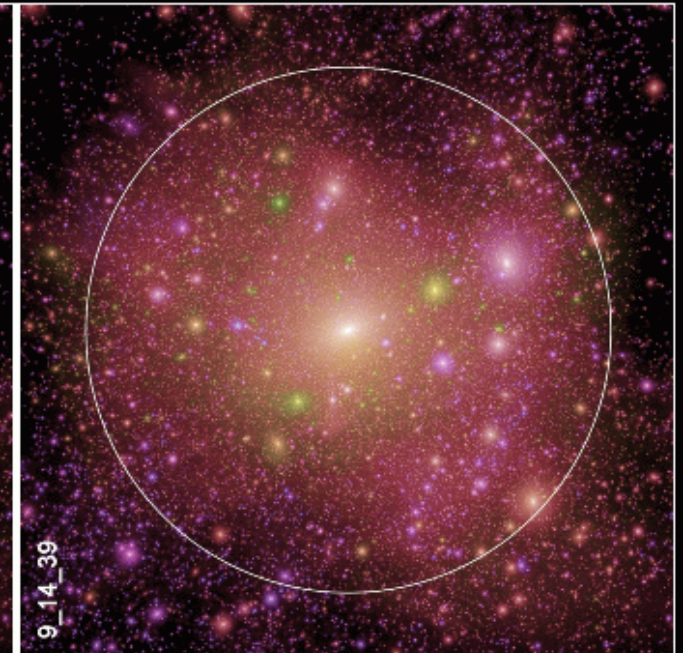
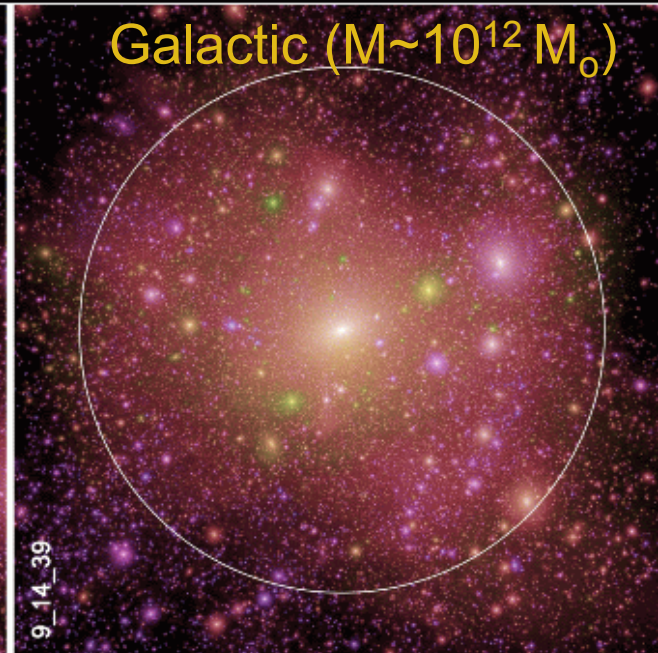
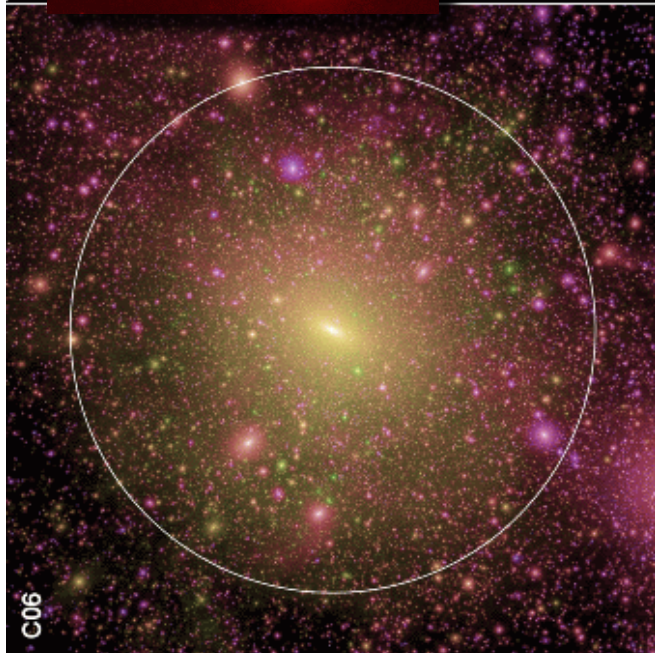
500 kpc

The image shows a dark, textured field of purple and black, representing a simulated galaxy at a very early stage. The texture is grainy and noisy, with some faint, irregular patterns of slightly lighter purple. In the top left corner, the text "z = 48.4" is displayed. In the top right corner, the text "T = 0.05 Gyr" is displayed. At the bottom center, there is a horizontal scale bar with vertical end caps, and the text "500 kpc" is written below it.



VIRG

# Aquarius and Phoenix halos (level-2)



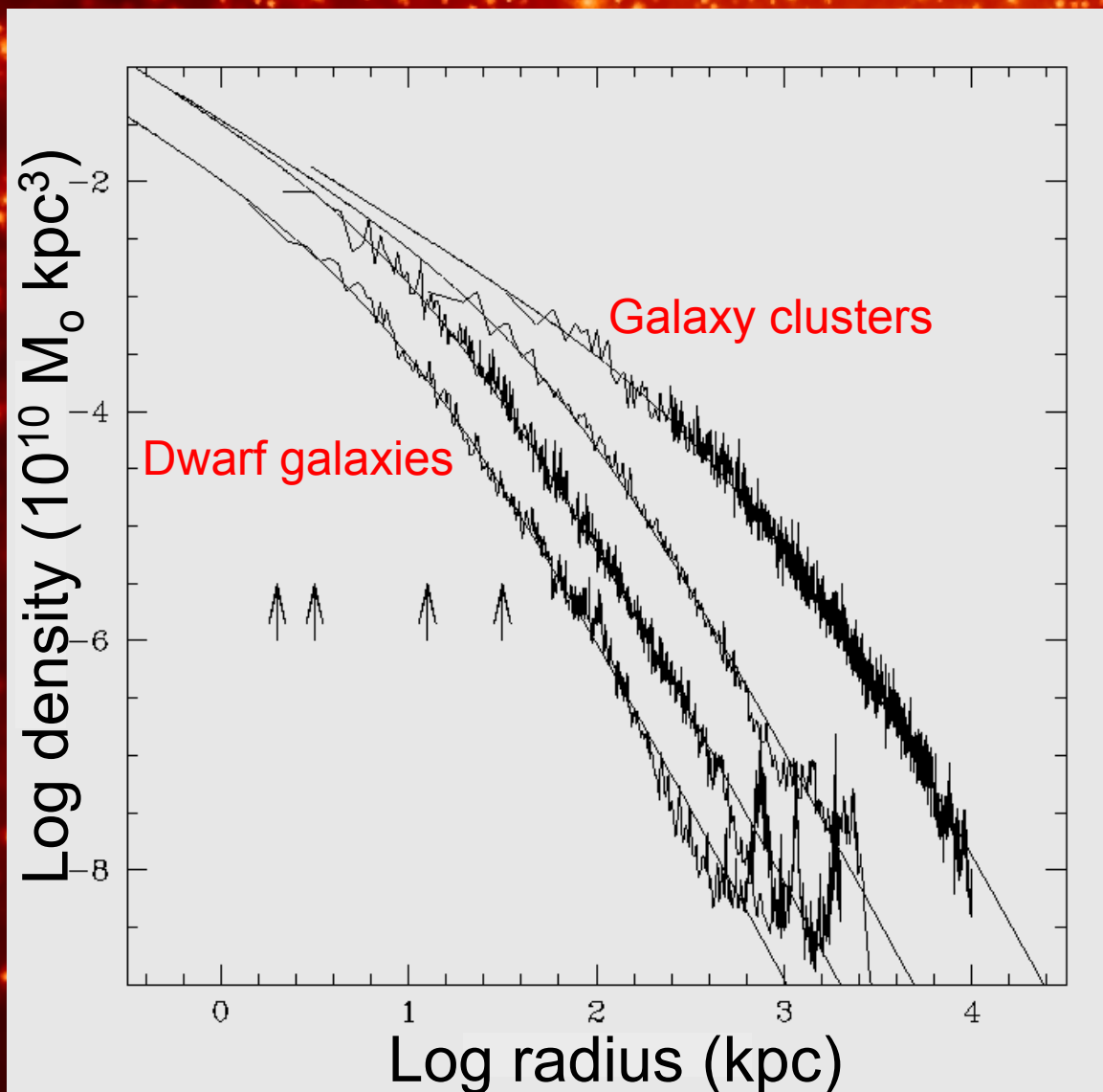


# A cold dark matter universe

CDM N-body simulations make two important predictions on non-linear (halo) scales:

- The main halo and its subhalos have “cuspy” density profiles
- Large number of self-bound substructures (**10% of mass**) survive

# The Density Profile of Cold Dark Matter Halos



Halo density profiles are independent of halo mass & cosmological parameters

There is no obvious density plateau or 'core' near the centre.

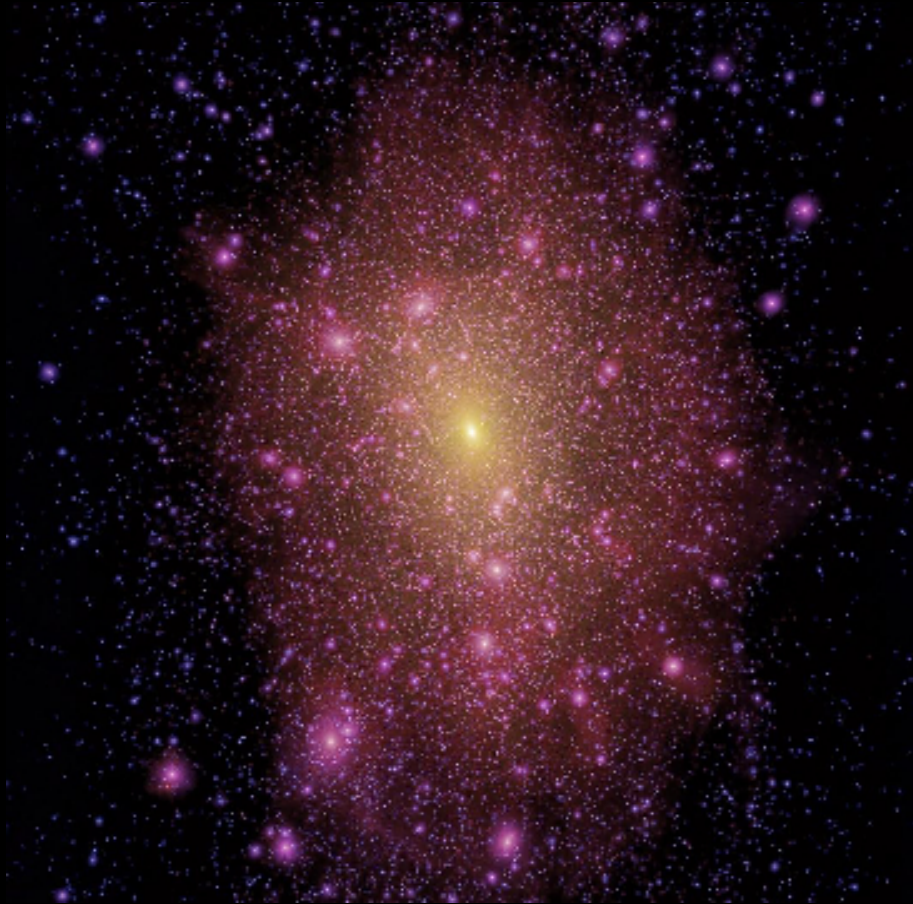
(Navarro, Frenk & White '97)

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

Halos that form earlier have higher densities (bigger  $\delta$ )



cold dark matter



warm dark matter



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
Boyerski & Ruchayskiy '12

Institute for Computational Cosmology

# A warm dark matter universe

For viable WDM particle masses, there is little difference between CDM and WDM on scales larger than galaxies.

## On subgalactic scales:

- Subhalos still “cuspy” but less concentrated than in CDM
- Far fewer self-bound substructures (**3% of mass**) survive

→ Can test for identity of the dark matter!





# The structure of dark matter halos

(Both CDM and WDM predict cuspy density profiles)

# A Cold dark matter universe

N-body simulations show that cold dark matter halos  
(from galaxies to clusters) have:

“Cuspy” density profiles

Does nature have them?

Look in galaxies and clusters



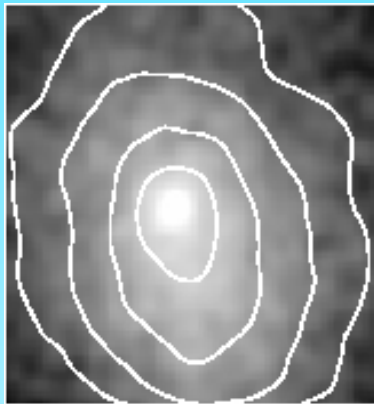
Galaxy halo structure strongly modified by baryons?

Cluster profiles can be probed with:

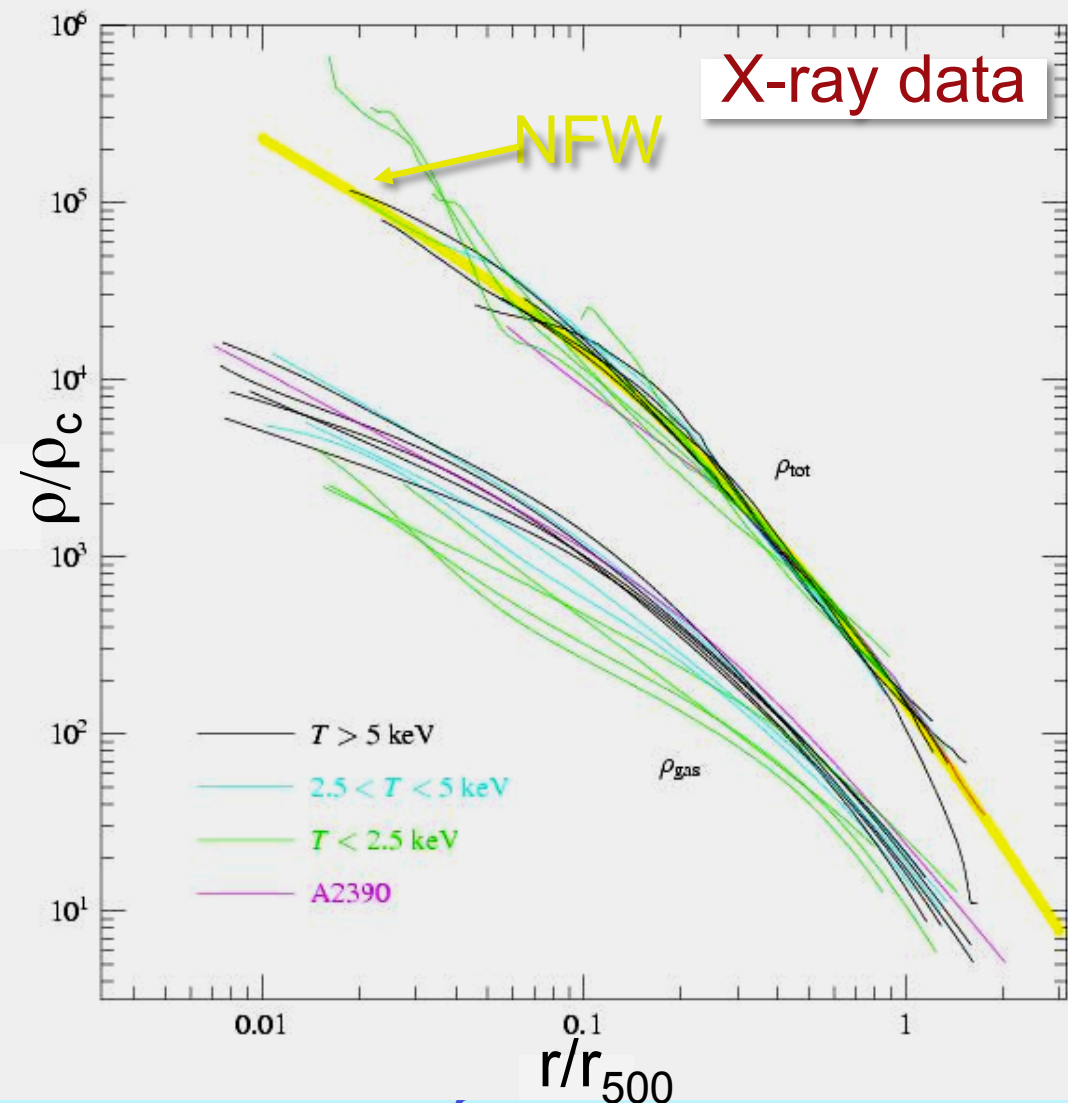
- X-ray emission
- Gravitational lensing

# The central density profile of galaxy cluster dark halos

Mass profile of galaxy clusters, from X-ray data & assumption of hydrostatic equilibrium



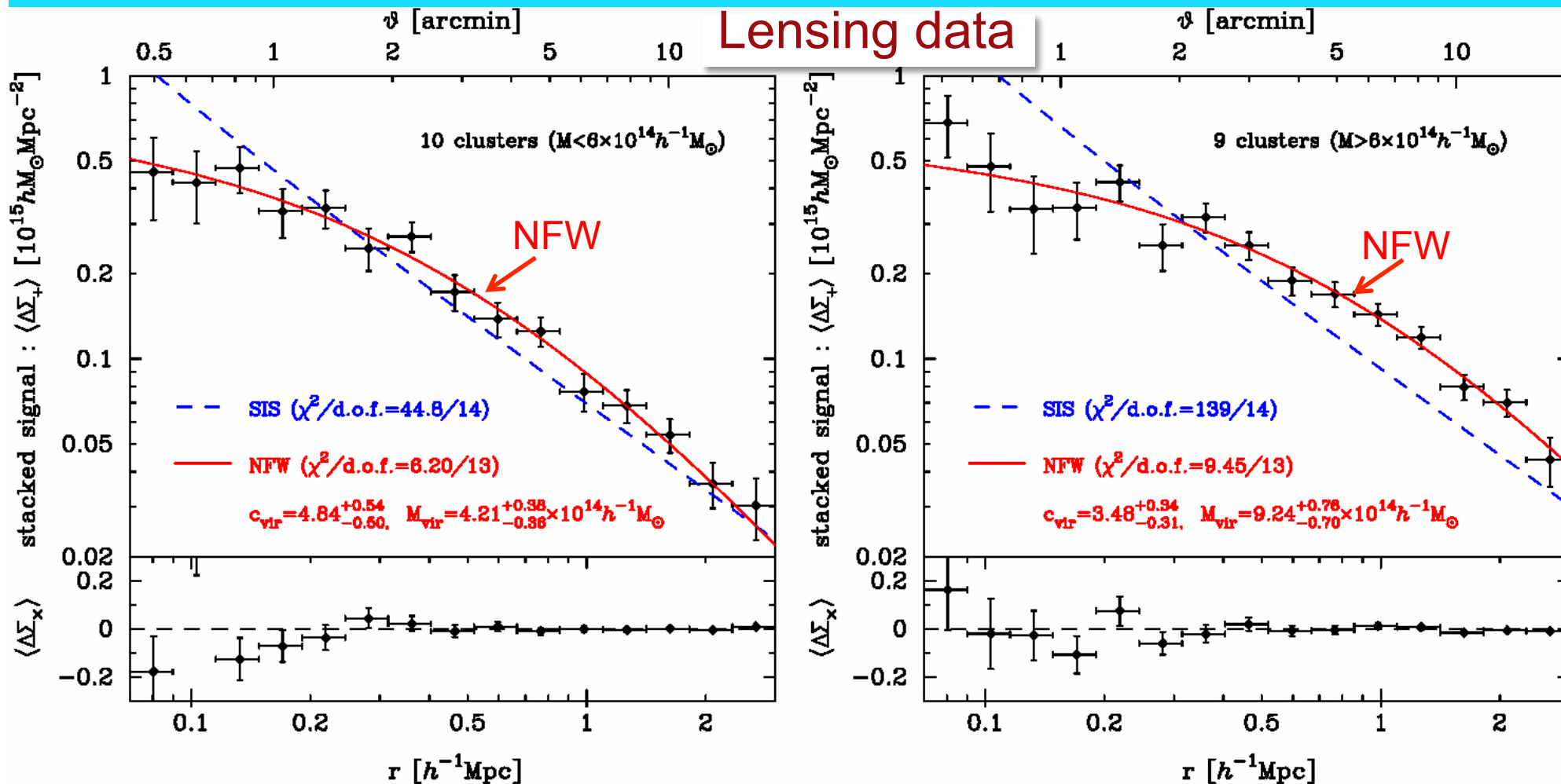
Excellent agreement with CDM halo predictions





# The density profile of galaxy cluster dark halos

## Lensing data



Okabe et al '10



$\Lambda$ CDM and WDM  $\rightarrow$  OK on scales  
of galaxy clusters and larger

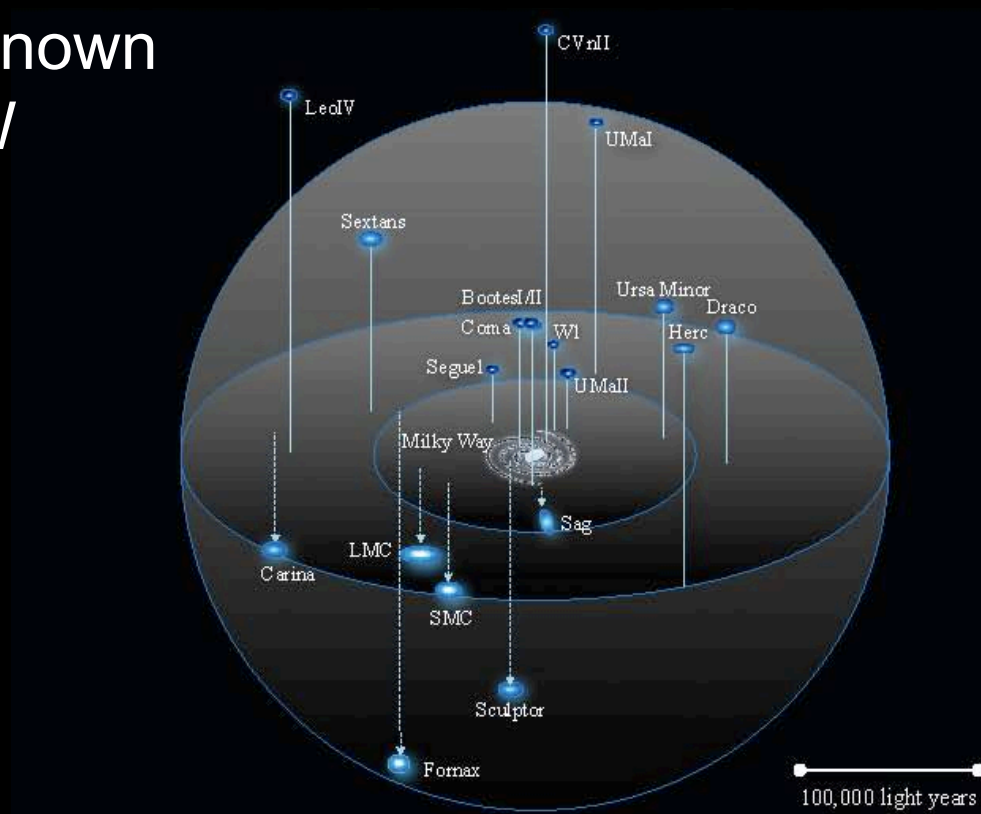
How about on smaller scales?

(again, expect cusps in both CDM and WDM)



# The satellites of the Milky Way

~25 satellites known  
in the MW

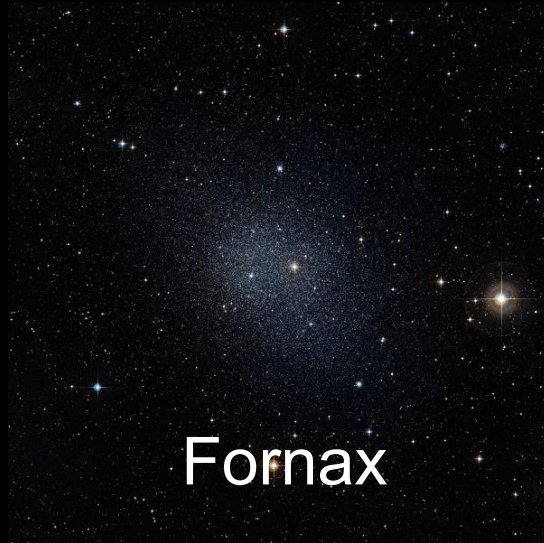


J. Bullock





# Dwarf galaxies around the Milky Way



Fornax



Sculptor



Leo I

© Anglo-Australian Observatory



Sextans



Carina



Sagittarius

# The structure of dark matter halos

Dwarf sphs: cores or cusps?

Jeans eqn:

$$\frac{GM(r)}{r} = -\sigma_r^2 \left[ \frac{d \ln \rho_*}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right]$$

stellar density profile

radial velocity dispersion

from Aquarius sim

vel. anisotropy

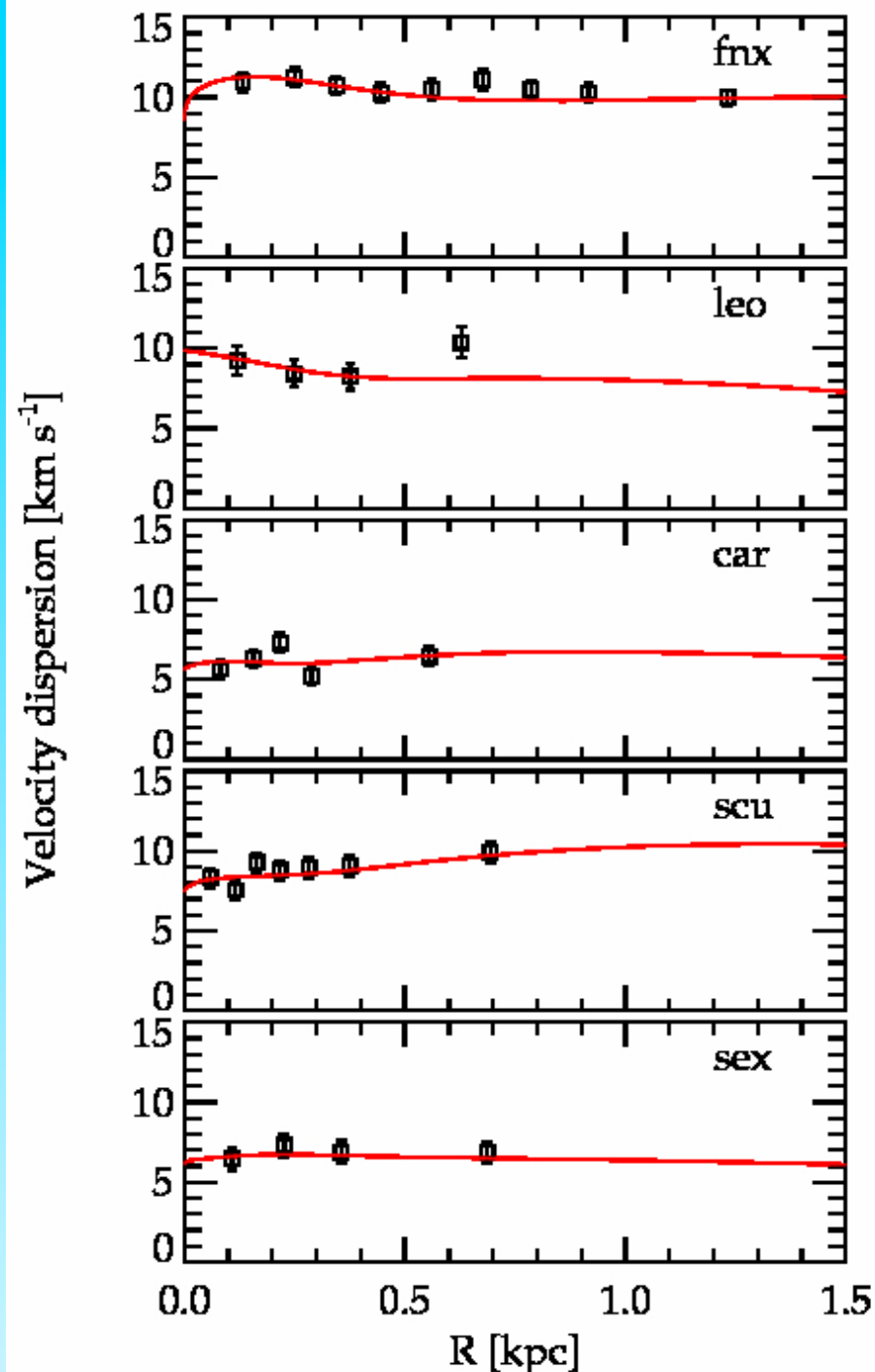
## Dwarf spherical galaxies: cores or cusps?

Jeans eqn:

$$\frac{GM(r)}{r} = -\sigma_r^2 \left[ \frac{d \ln \rho_*}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right]$$

from Aquarius sim
vel. anisotropy

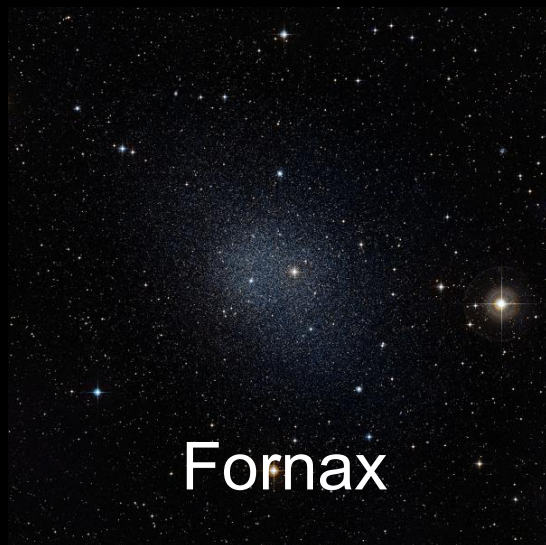
- Assume isotropic orbits
- Solve for  $\sigma_r(r)$
- Compare with observed  $\sigma_r(r)$
- Find “best fit” subhalo







# Dwarf galaxies around the Milky Way



Fornax



Sculptor



Leo I



Sextans



Carina



Sagittarius

Cuspy NFW profiles consistent with MW satellite kinematic data



Halo structure, from galaxy clusters  
to dwarf satellites seems **OK** in  
**both**  $\Lambda$ CDM and WDM

How can we distinguish between CDM & WDM ?

# Galactic halos

N-body simulations make two important predictions on non-linear (halo) scales:

## CDM:

- The main halo and its subhalos have “cuspy” density profiles
- Large number of self-bound substructures (**10% of mass**) survive

## WDM:

- The main halo and its subhalos have “cuspy” density profiles, but the subhalos are less concentrated
- Small number of self-bound substructures (**3% of mass**) survive





cold dark matter

warm dark matter



Spot the difference!

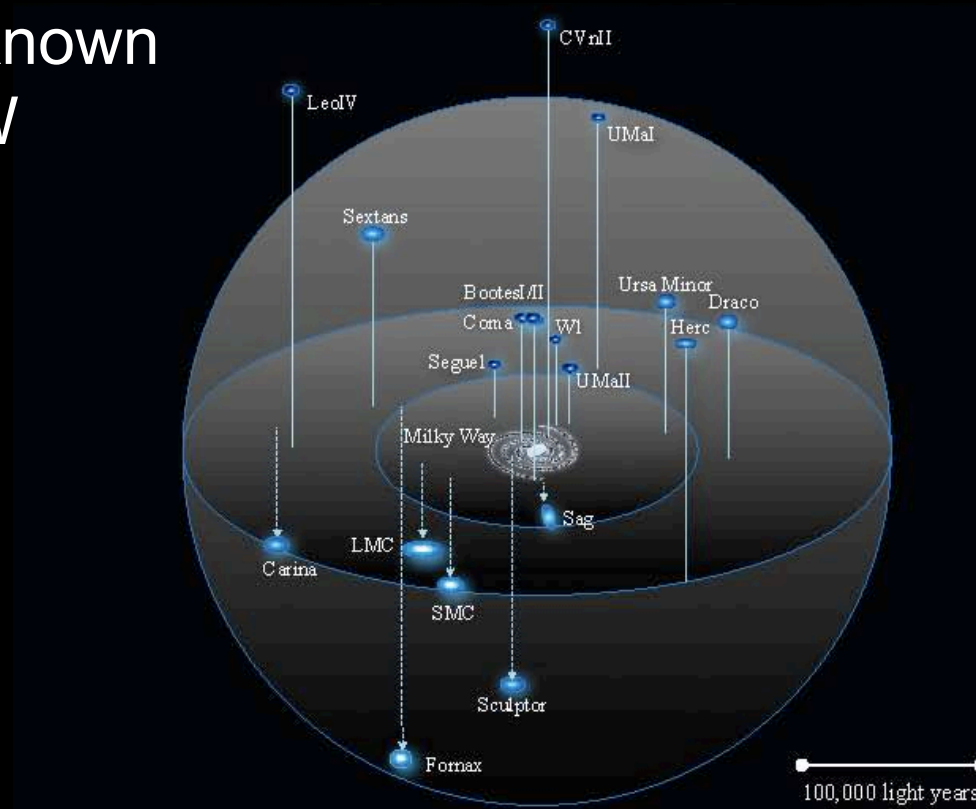


Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
Boyarski & Ruchayskiy '12

Institute for Computational Cosmology

# The satellites of the Milky Way

~25 satellites known  
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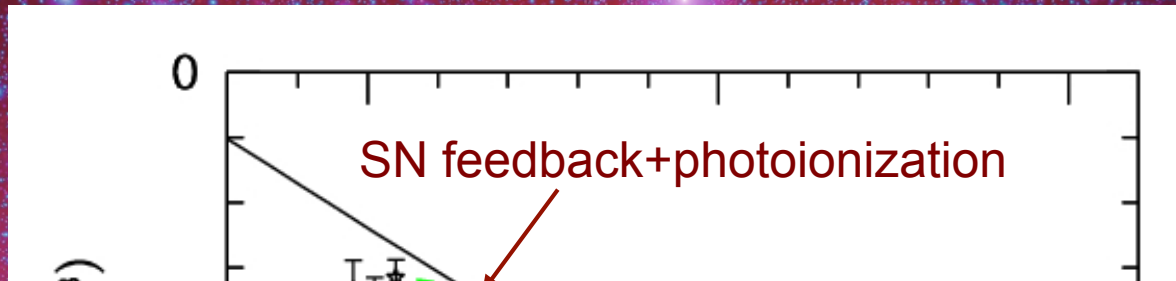


The background of the slide is a deep space image showing a vast field of stars and galaxies. A prominent, bright yellowish-white galaxy is located in the center, surrounded by a dense field of smaller, distant galaxies and stars. The colors range from deep reds and oranges near the center to dark blues and purples at the edges.

CDM simulations produce  $>10^5$  subhalos

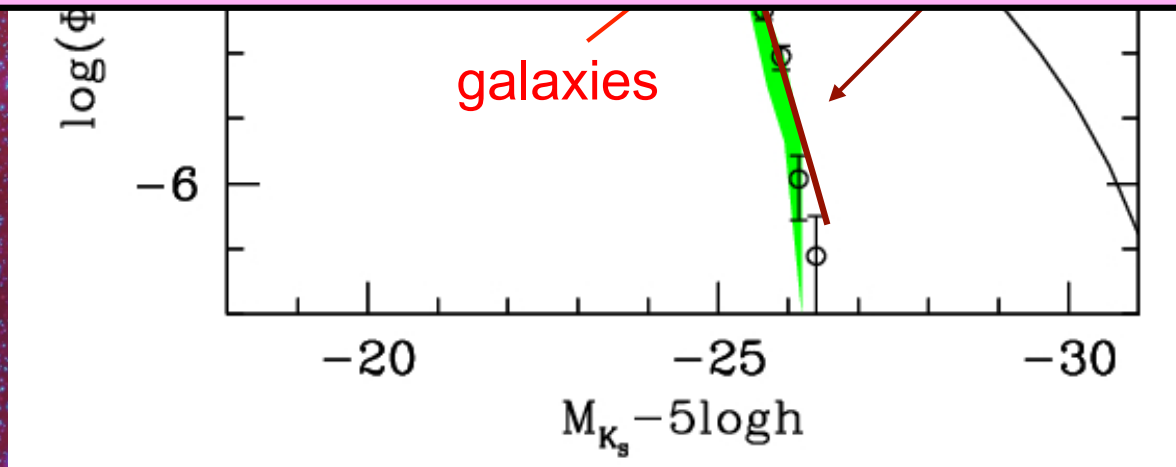
Most of these subhalos never manage  
to make a visible galaxy





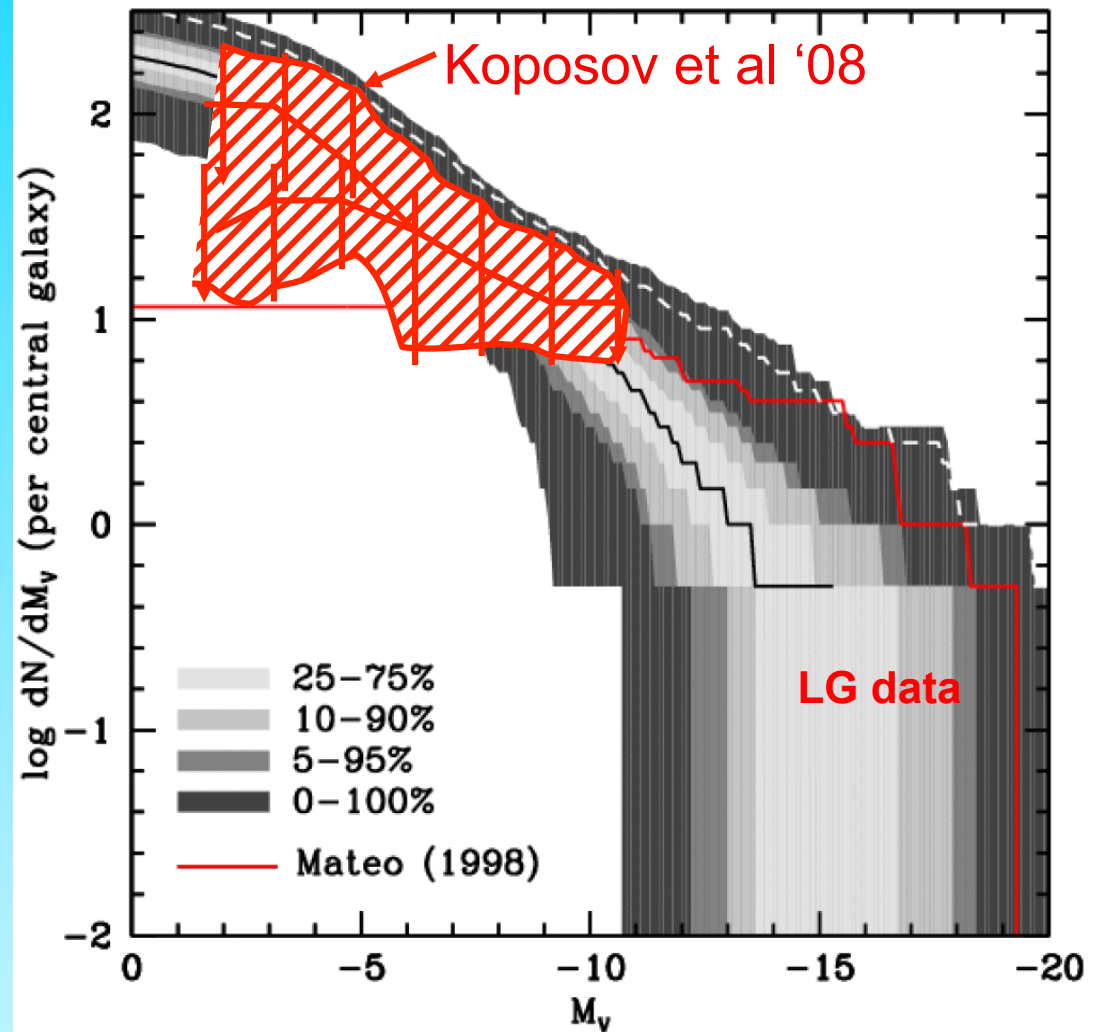
Making a galaxy in a small halo is hard because:

- Early reionization heats gas above  $T_{\text{vir}}$
- Supernovae feedback expels gas



# Luminosity Function of Local Group Satellites

- Median model → correct abund. of sats brighter than  $M_V = -9$  and  $V_{\text{cir}} > 12$  km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare (~2% of cases)







cold dark matter

warm dark matter

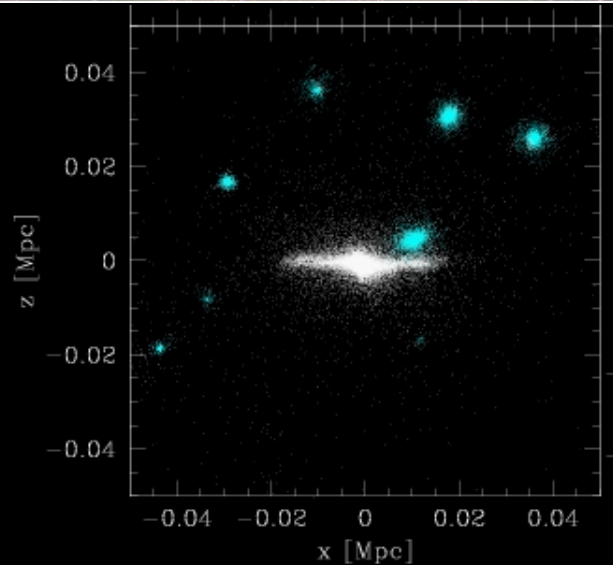
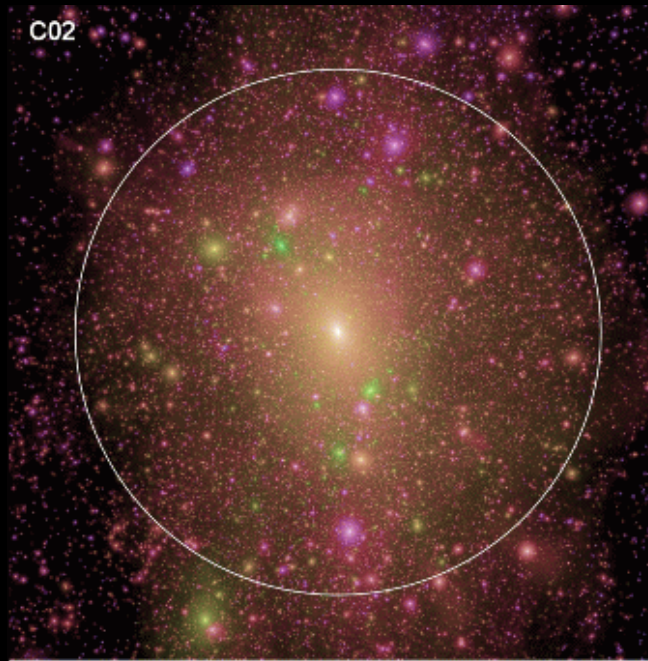
Counting satellites cannot distinguish CDM from WDM!

Need to look in more detail at the structure of small halos

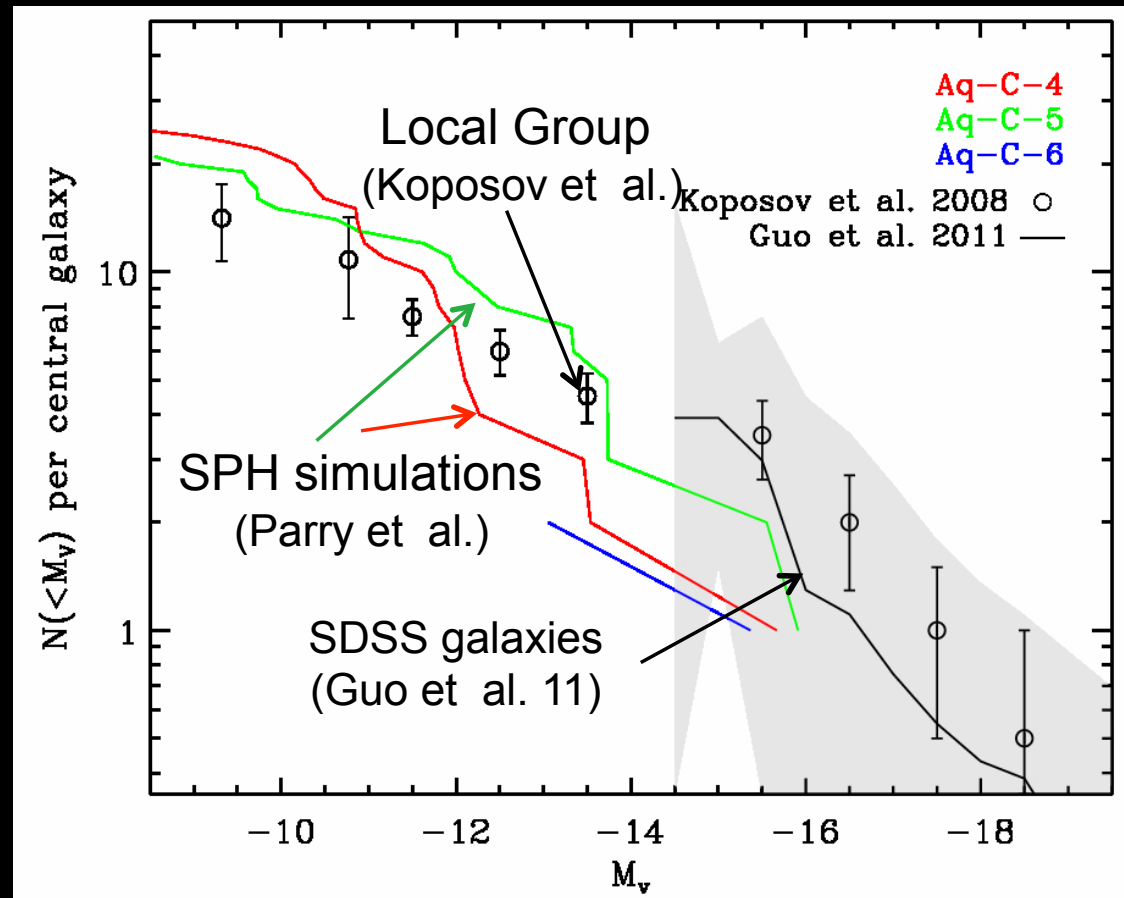
Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
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Institute for Computational Cosmology

# The satellites of the Milky Way



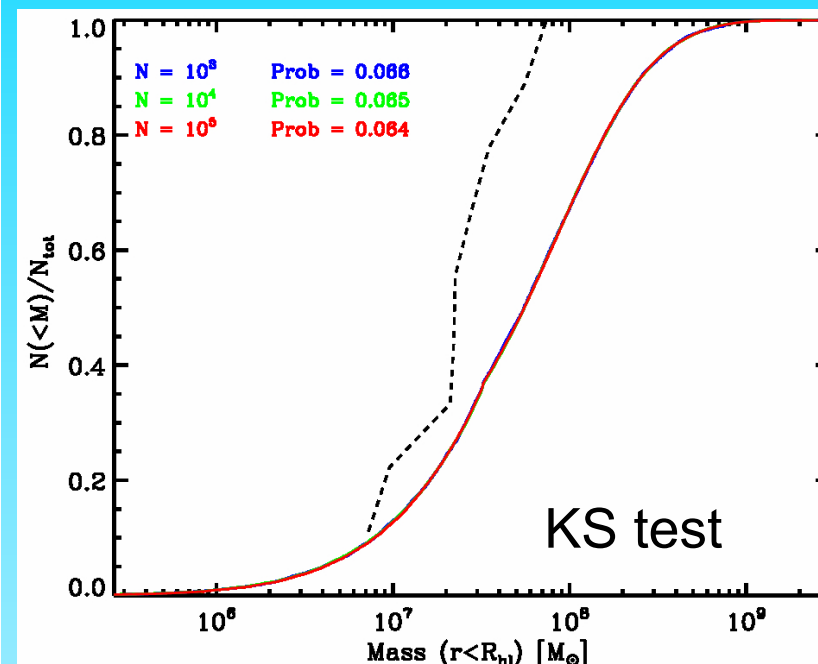
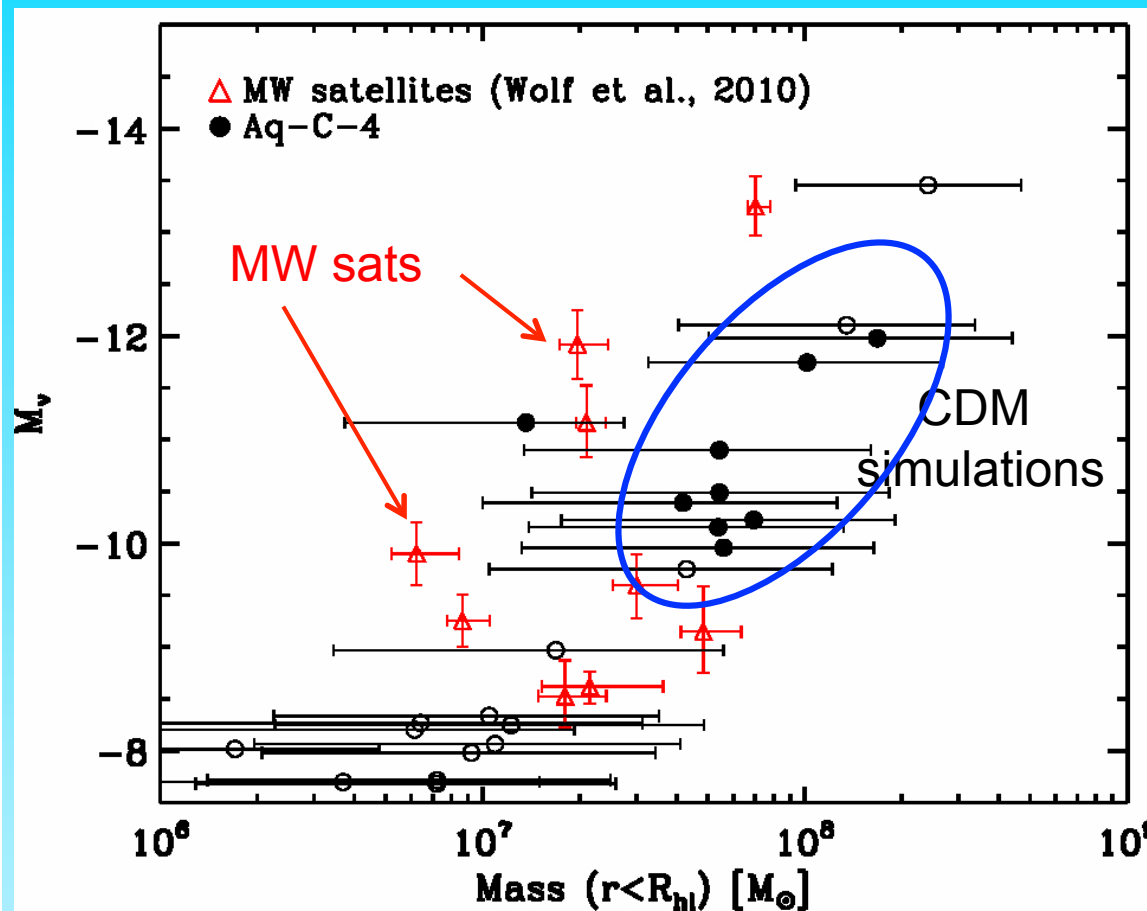
SPH simulations of galaxy formation  
in one of the Aquarius halos



Parry, Eke, Frenk & Okamoto '11

# The satellites of the Milky Way

Mass within half-light rad. (spectroscopy)



CDM puts the brightest sats in the biggest halos, but these are more massive than those indicated by the real data

CDM rejected at 93.6% confidence level

Parry, Eke & Frenk & Okamoto'11



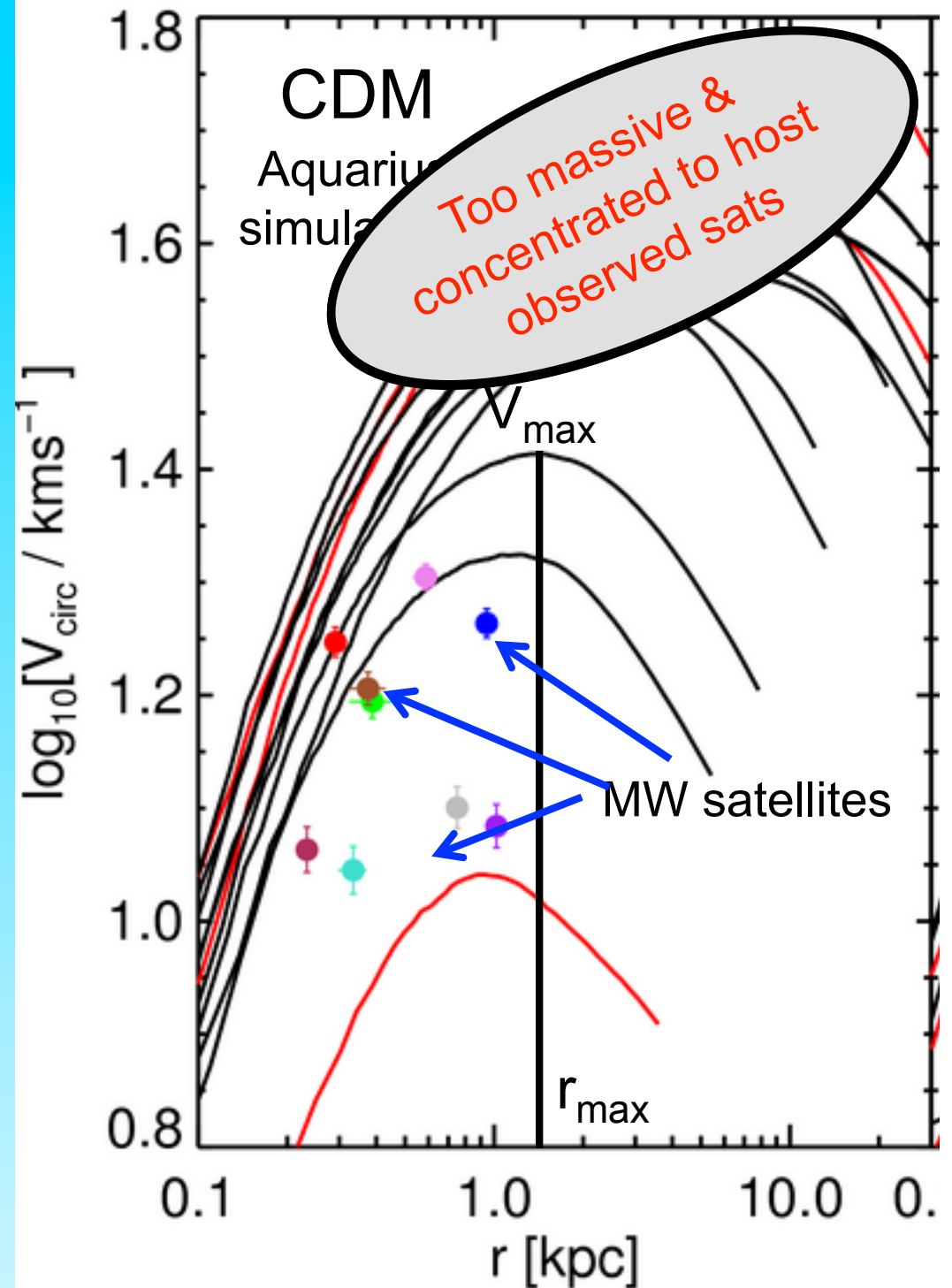
# Is CDM compatible w. luminosity & structure of observed satellites?

$$V_c = \sqrt{\frac{GM}{r}} \quad V_{\max} = \max V_c$$

Rotation curves of 12 subhalos with most massive progenitors

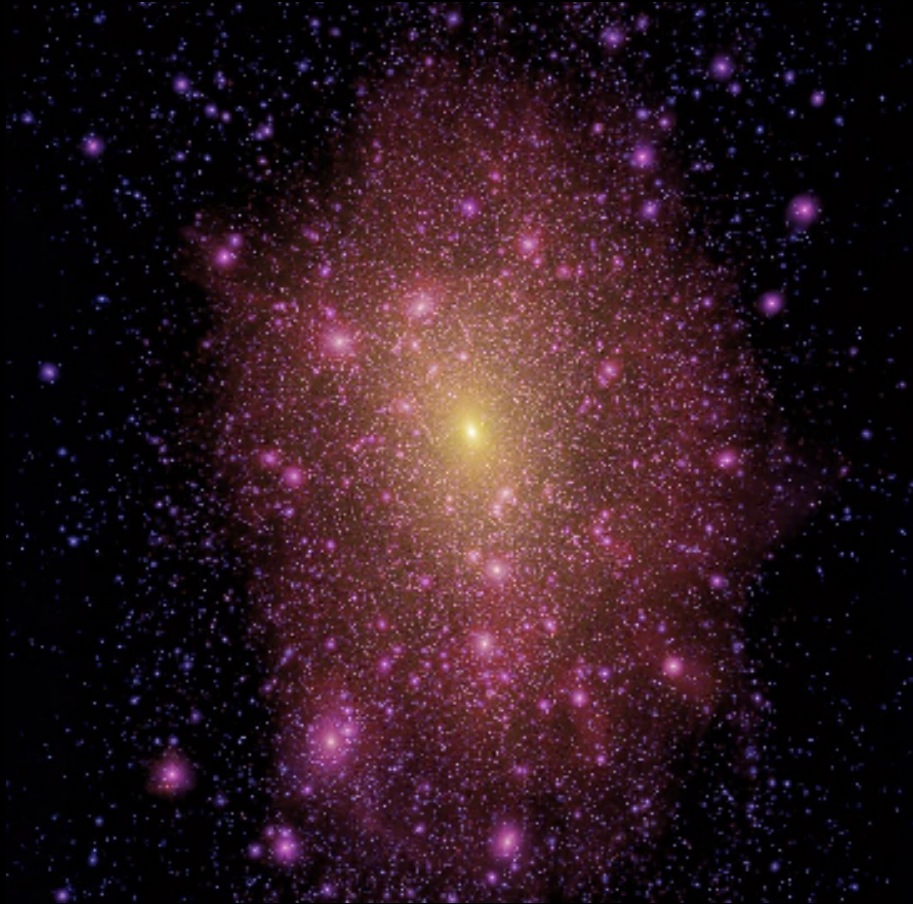
Red → 3 halos with most massive progenitors (LMC, SMC, Sagittarius?)

Lovell, Eke, Frenk, Gao et al '11;  
see also Boylan-Kolchin et al '11a,b





cold dark matter

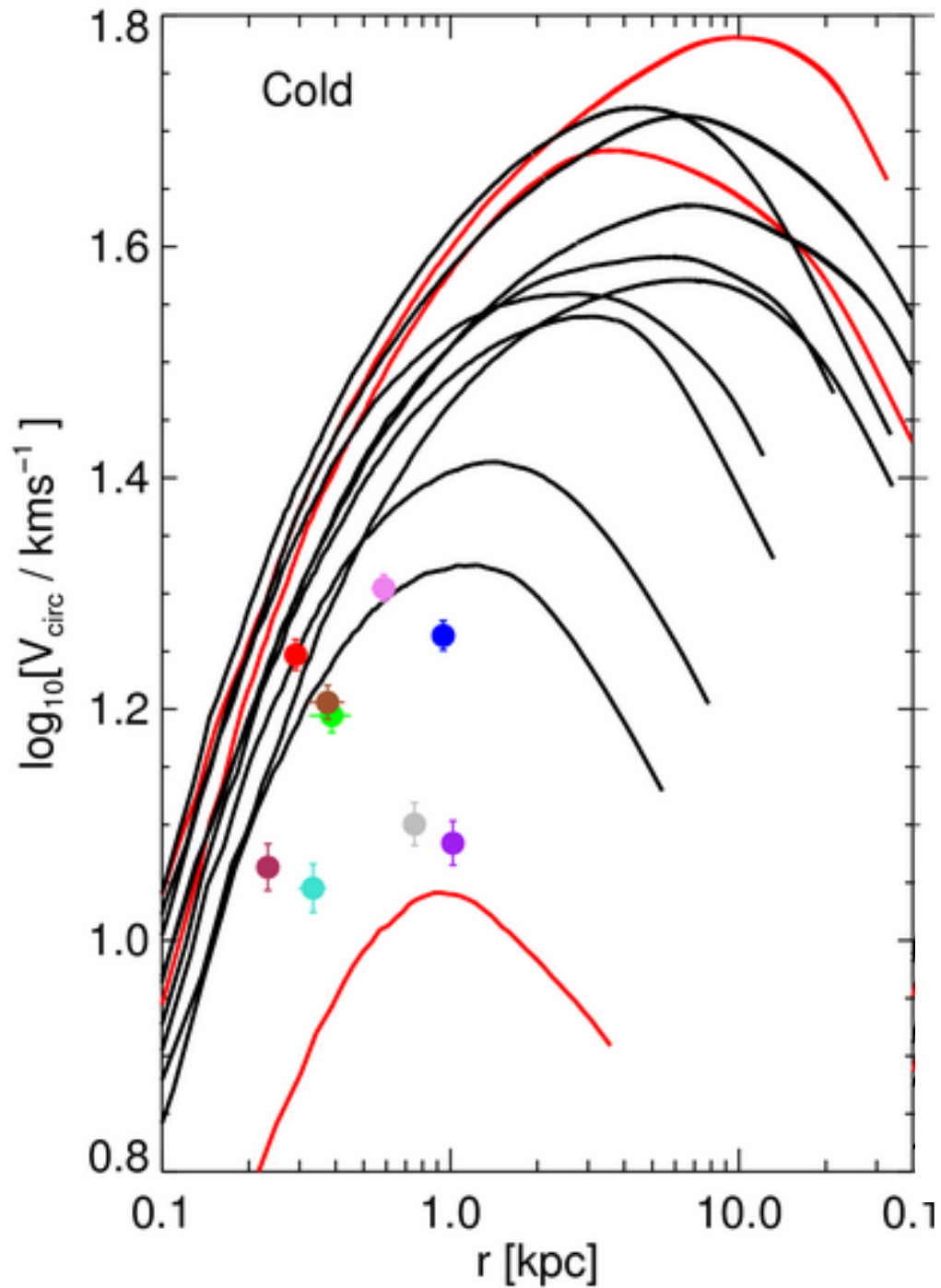


warm dark matter



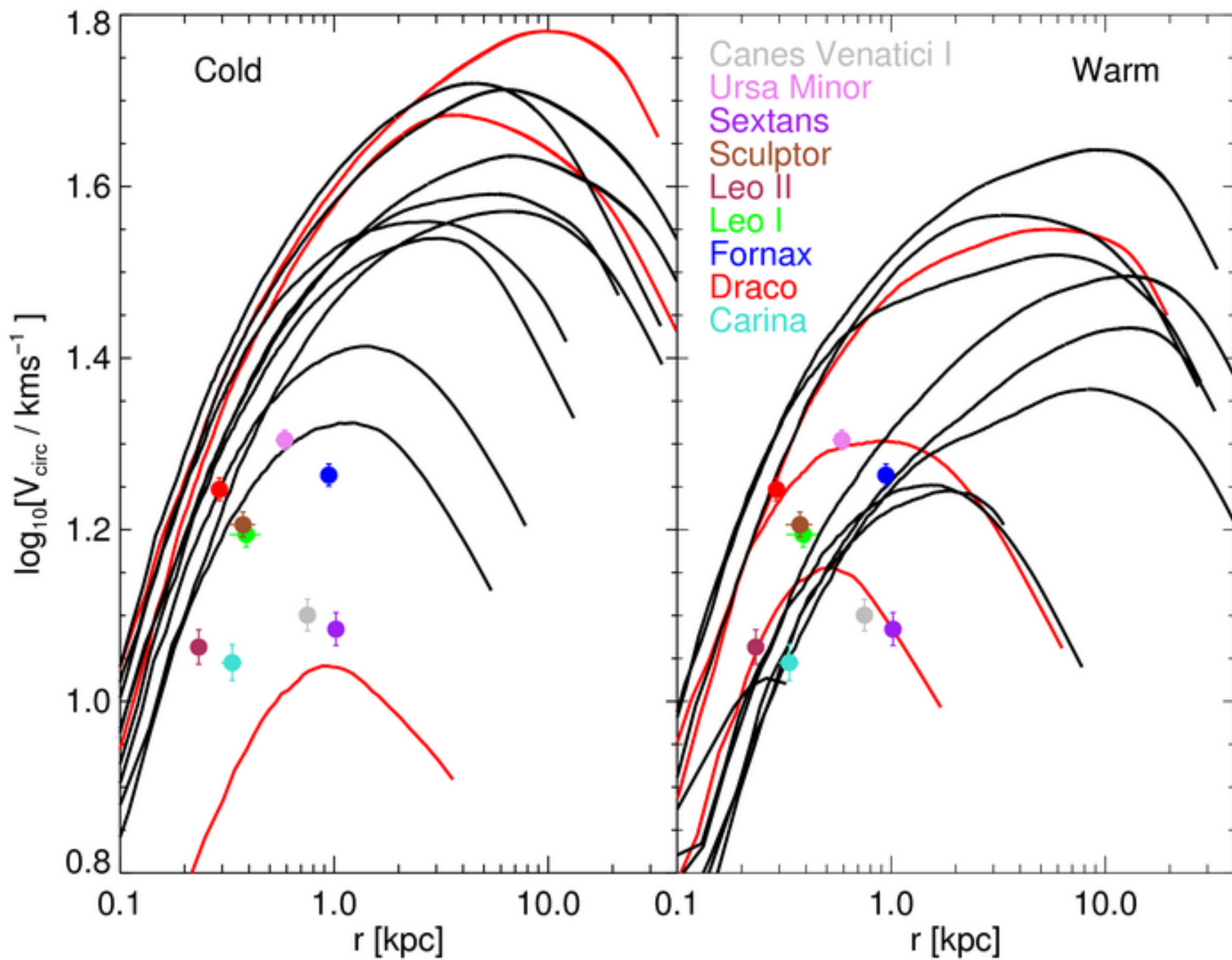
Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
Boyarski & Ruchayskiy '11

Institute for Computational Cosmology



Lovell, Eke, Frenk, Gao,  
Jenkins, Wang, White, Theuns,  
Boyarski & Ruchayskiy '11





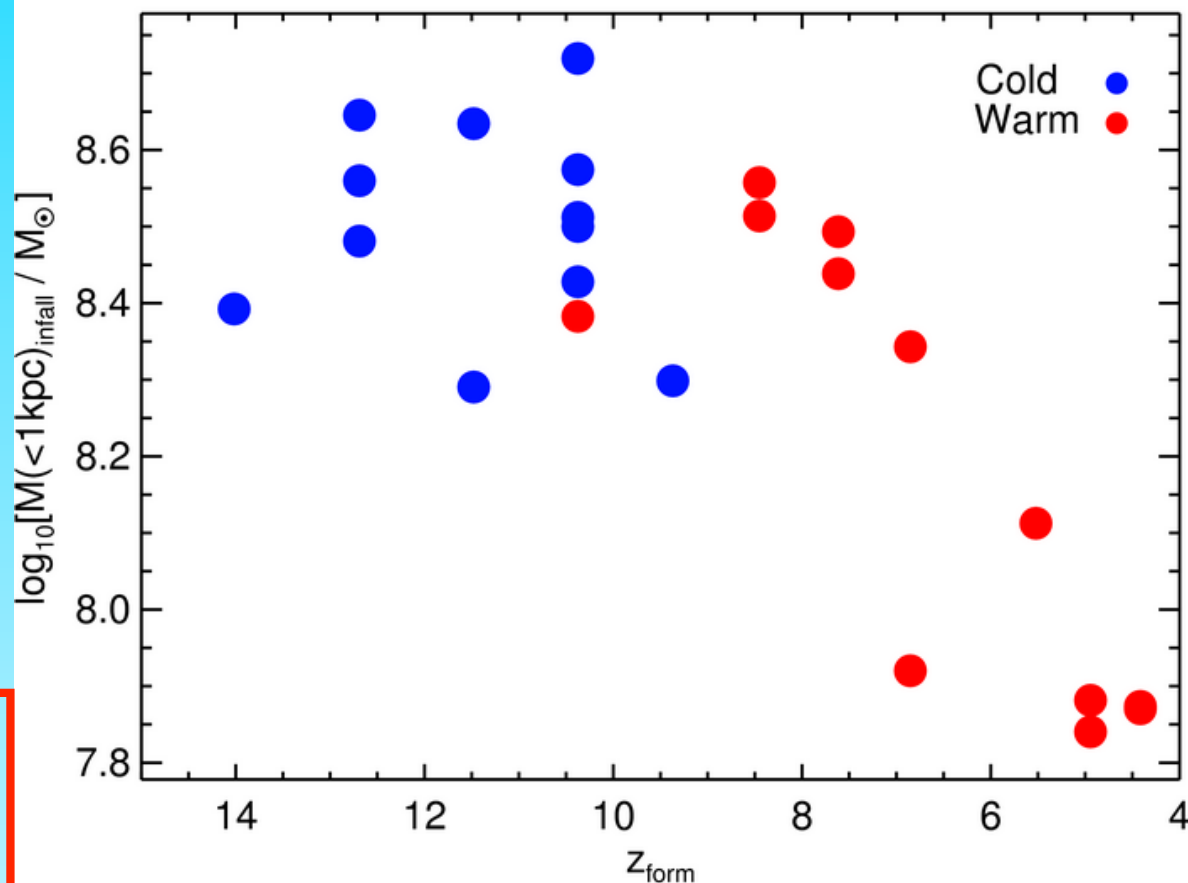
# Warm vs cold dark matter subhalos

“Formation redshift” →  
z at which  $M_{\text{halo}}$  first  
exceeded  $M_{\text{infall}}(<1\text{kpc})$

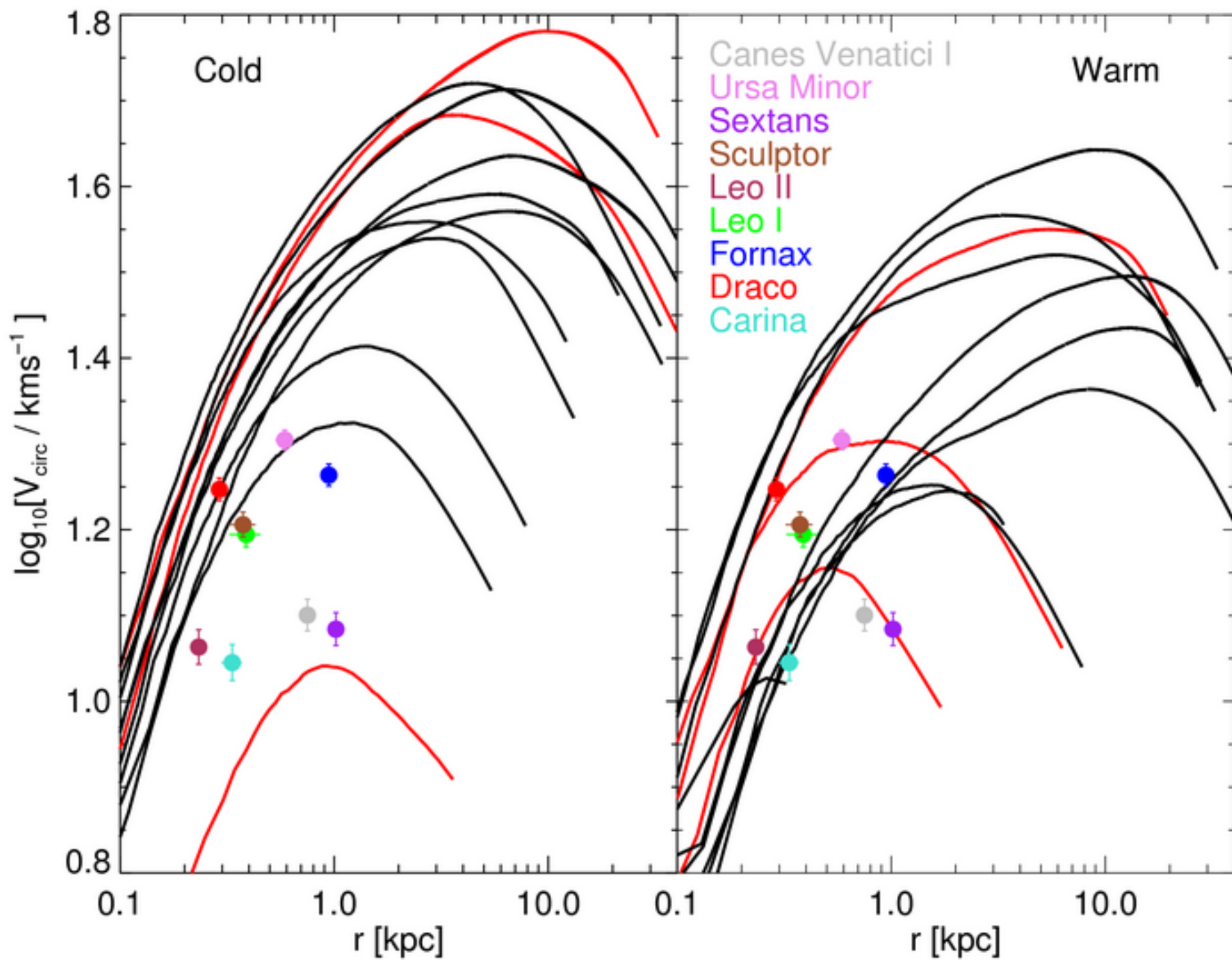
WDM halos form later  
& have lower central  
masses than their  
CDM counterparts!



WDM subhalos are still  
cuspy but are less  
concentrated than CDM  
subhalos



Lovell, Eke, Frenk, Gao, Jenkins et al '11







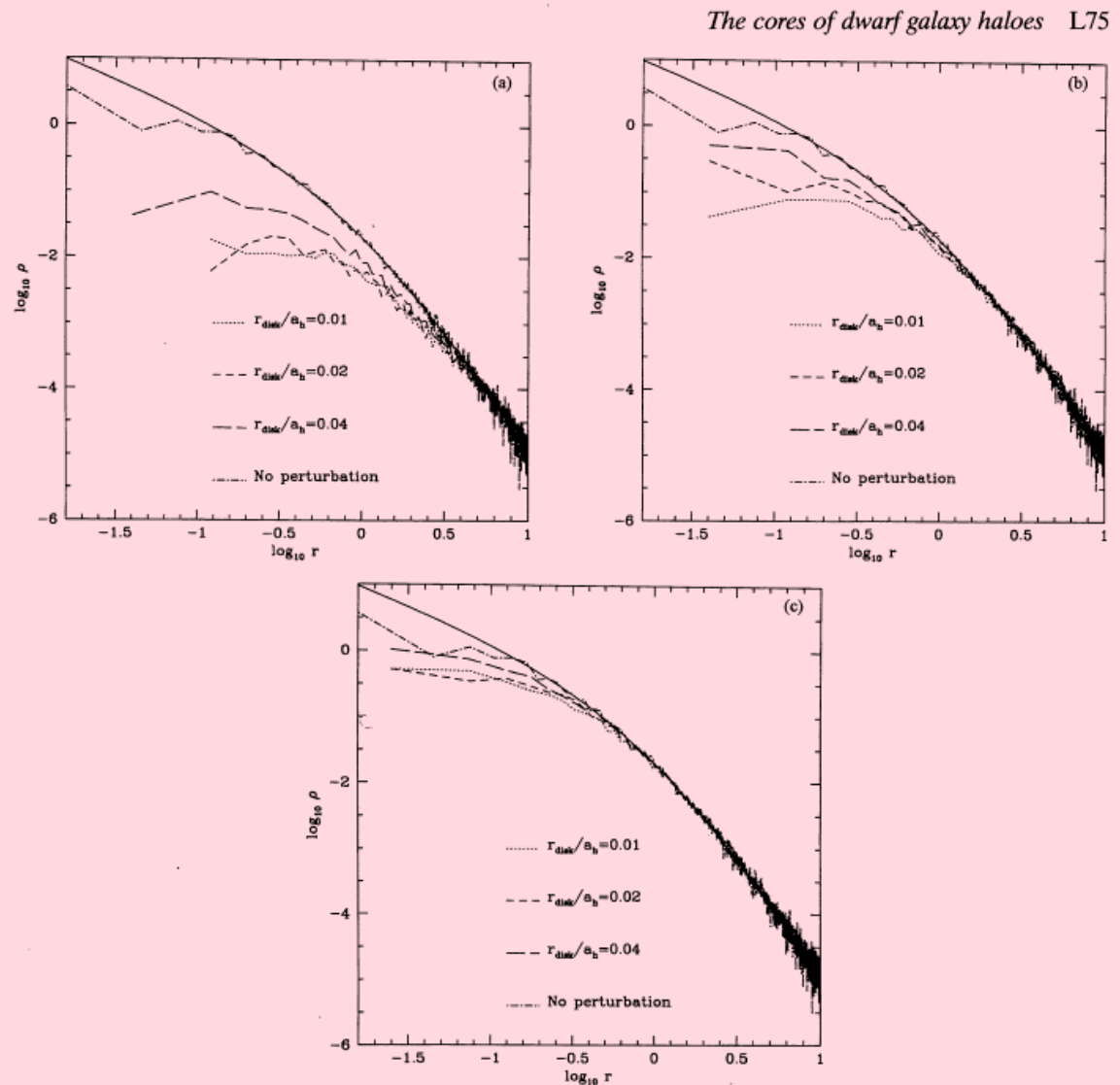
## Is this the end of CDM?

1. Baryon effects
2. The mass of the MW

Let baryons cool and condense to the galactic centre

Rapid ejection of large fraction of gas during starburst can lead to a core in the halo dark matter density profile

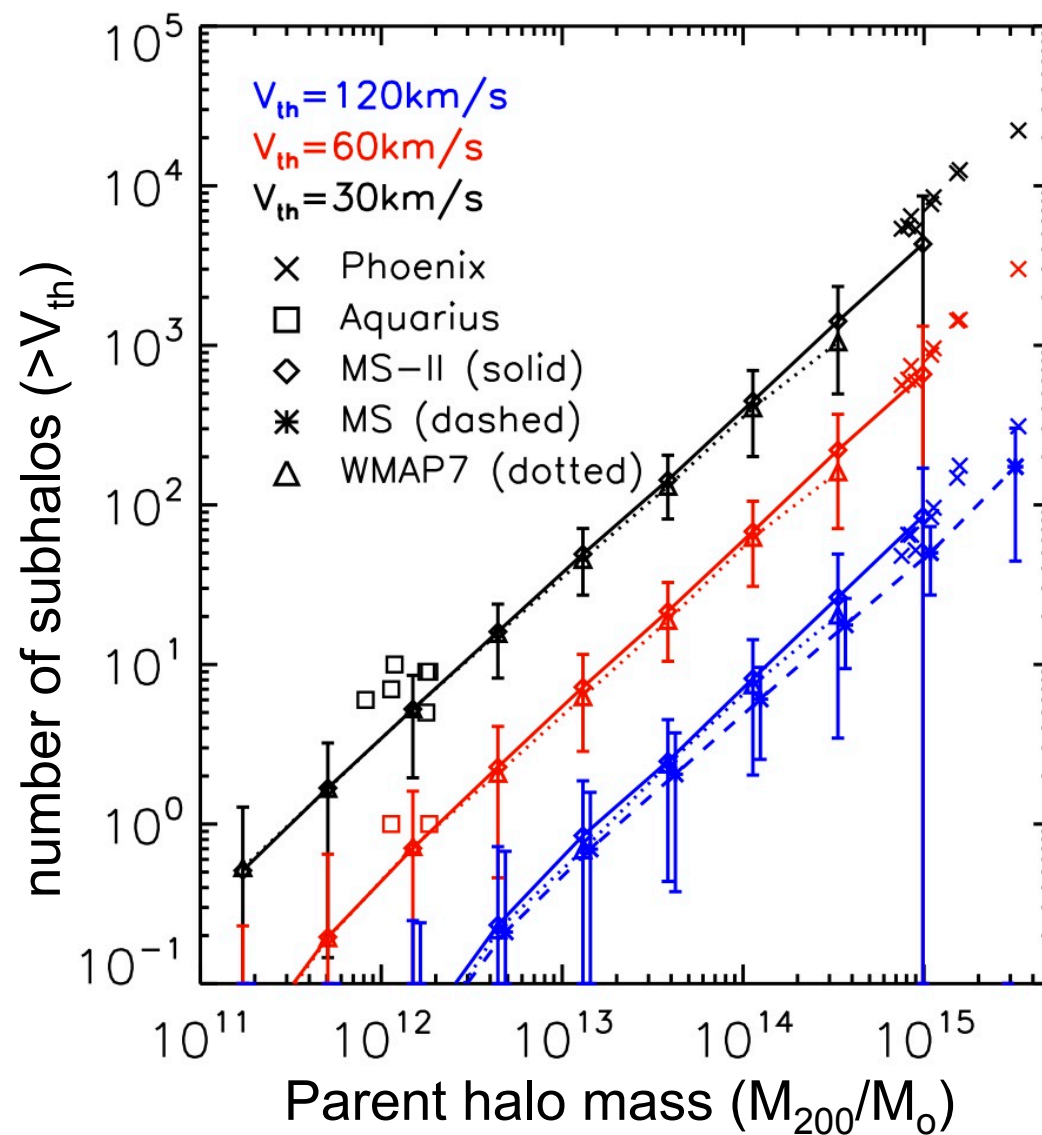
Navarro, Eke, Frenk '96



**Figure 3.** Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10 000-particle realization of the Hernquist model run in isolation at  $t=200$ . (a)  $M_{\text{disc}}=0.2$ . (b)  $M_{\text{disc}}=0.1$ . (c)  $M_{\text{disc}}=0.05$ .

# Number of massive subhalos

Number of subhalos increases rapidly with halo mass





# Probability of massive subhalos

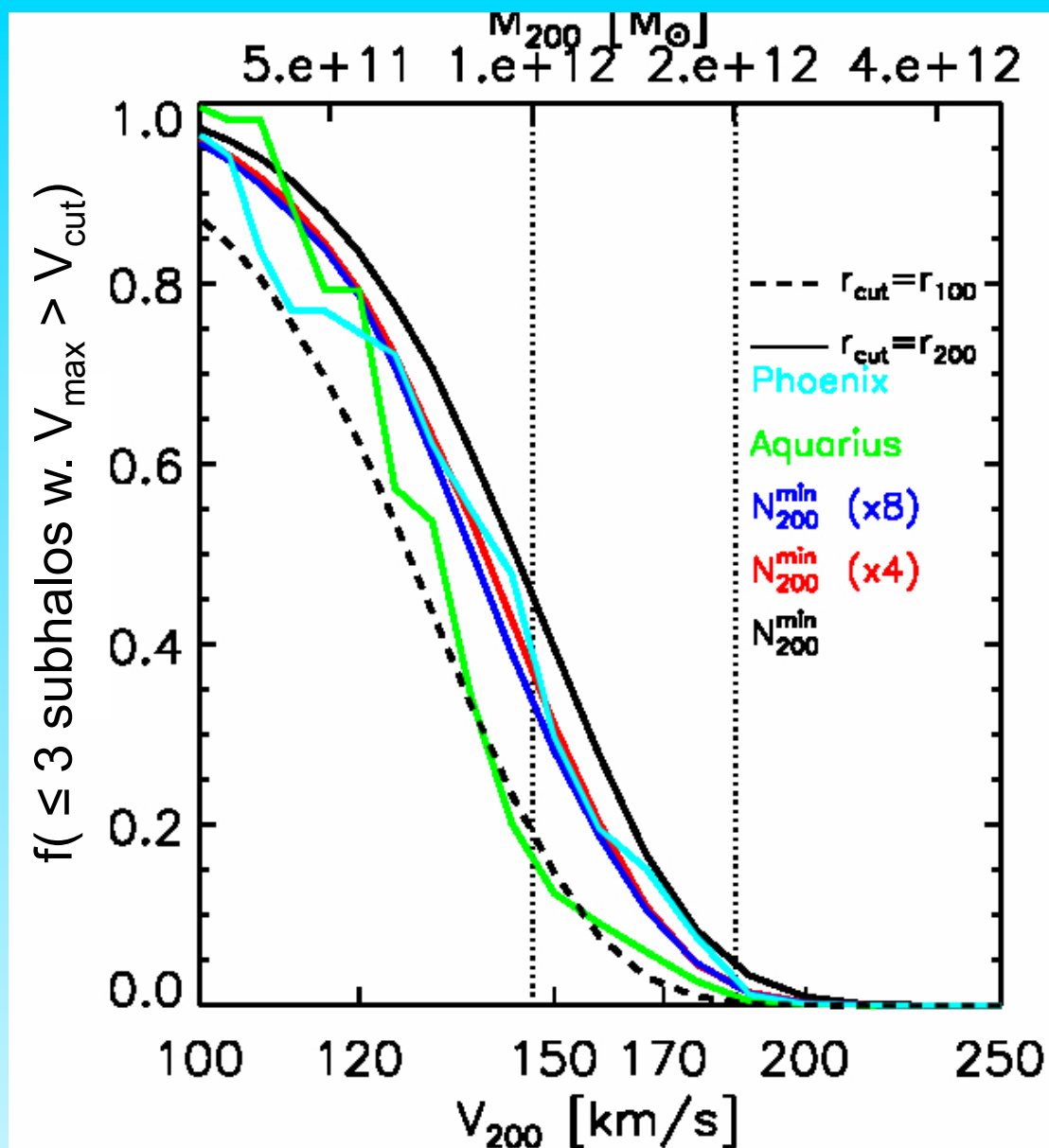
Probability of having no more than 3 subhalos with

$$V_{\max} > V_{\text{cut}}$$

Depends strongly on

$V_{\text{cut}}$  and  $M_{200}$

If mass of MW  $\sim 1 \times 10^{12} M_{\odot}$ ,  
CDM may be OK!



## $\Lambda$ CDM: problems/possible solutions

- $\Lambda$ CDM great **success** on scales  $> 1\text{Mpc}$ : CMB, LSS, gal evolution

A problem on subgalactic scales?

Two NO-problems:

1. The satellite **LF**  $\rightarrow$  can be explained by **galaxy formation**
2. Central **cores**  $\rightarrow$  data **consistent** with **cusps**

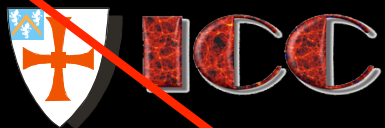
However:

- CDM models place **brightest sats** in most massive subhalos and these appear to be **too concentrated** to be **compatible** w. **kinematics**

Possible solutions:

- Warm dark matter
- Baryon effects that make large CDM subhalos less concentrated
- Sat. pop. in the MW is atypical or  $V_{\text{cut}} > 25 \text{ km/s}$  or  $M_{\text{halo}} \leq 10^{12} M_{\odot}$

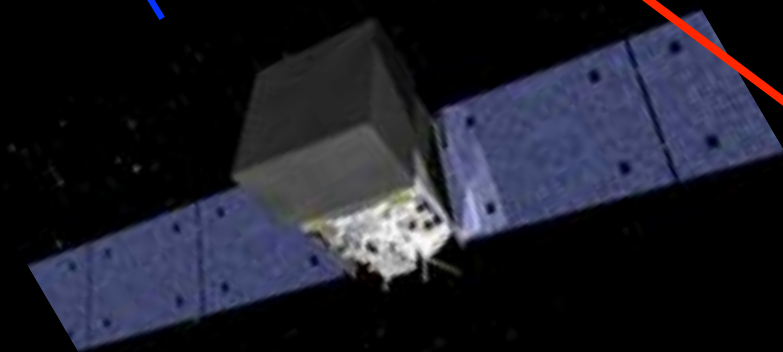




# Cold dark matter ?

Dark matter discovery possible in several ways

Fermi

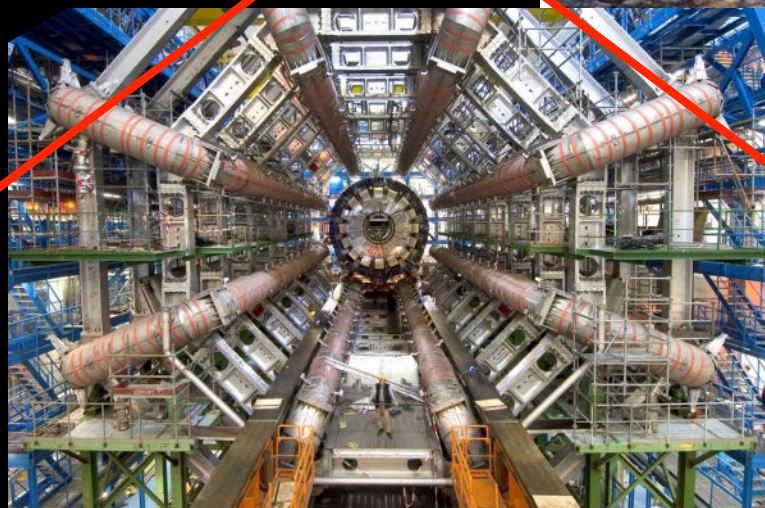


Annihilation radiation

Direct detection



UK DM search  
(Boulby mine)



Evidence for SUSY



# Warm dark matter ?

Sterile neutrino detection possible

Decay line in X-rays



Constellation X

