



# Dark matter crisis on small scales?

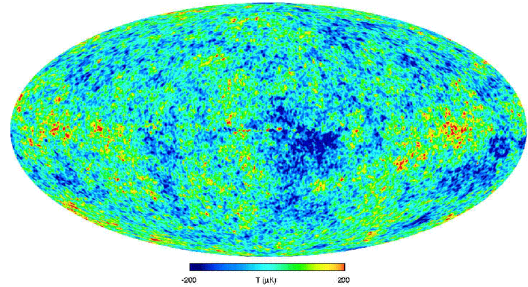
*Carlos S. Frenk*  
*Institute for Computational Cosmology,*  
*Durham*

# Four problems for CDM on small scales?

1. The “missing satellites” problem
2. The “too-big-to-fail” problem
3. The “core-cusp” problem
4. The “satellite disk” problem



# The cosmic power spectrum: from the CMB to the 2dFGRS

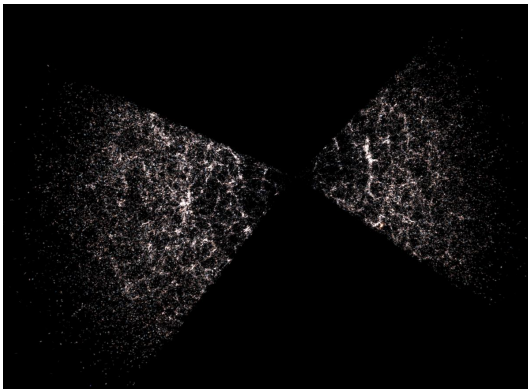


$z \sim 1000$

$\text{Log } k^3 P(k)$

wavelength  $k^{-1}$  (comoving  $h^{-1}$  Mpc)

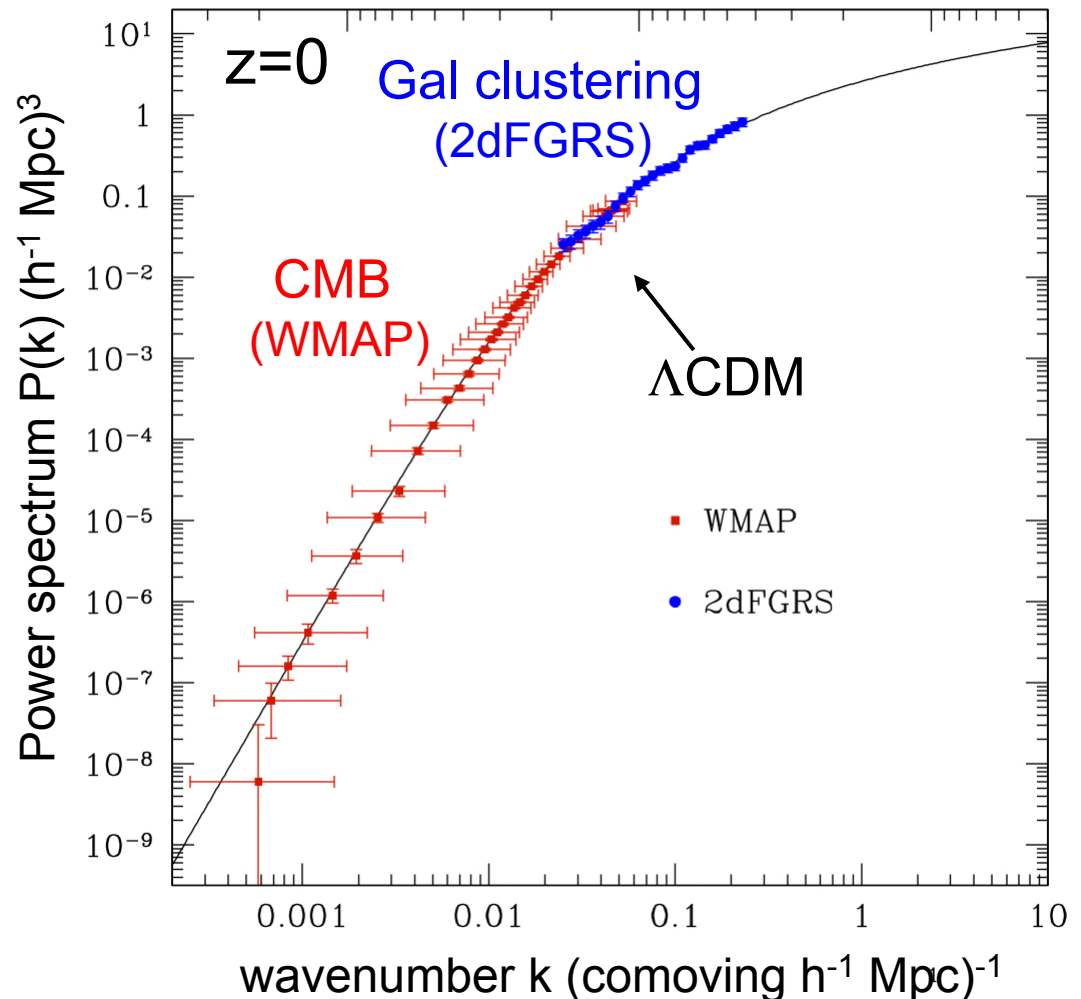
1 000 100 10



$z \sim 0$

$\Rightarrow \Lambda\text{CDM}$  provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06



# The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming  $\rightarrow$

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

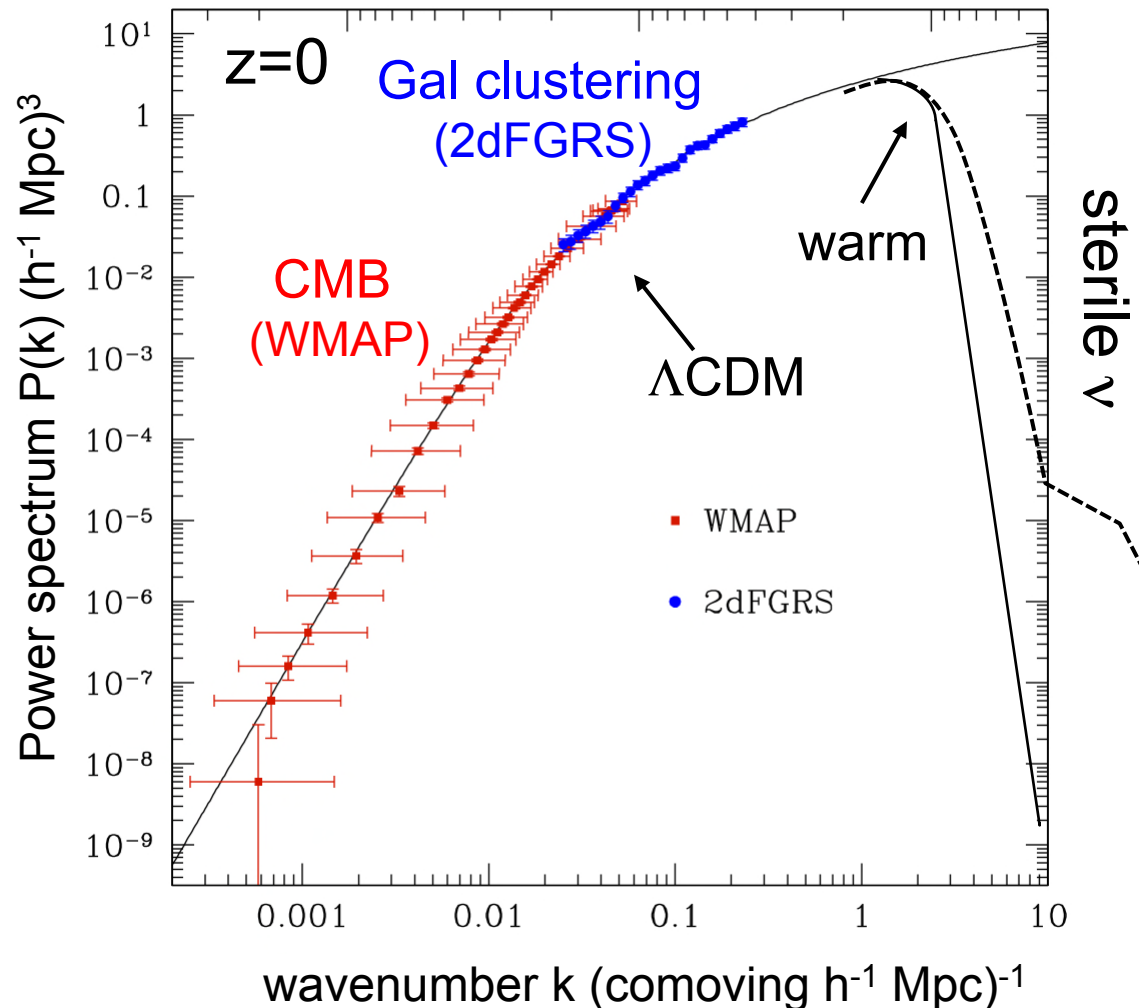
$$m_{\text{CDM}} \sim 100 \text{ GeV}$$

$$\text{susy}; M_{\text{cut}} \sim 10^{-6} M_{\odot}$$

$$m_{\text{WDM}} \sim \text{few keV}$$

$$\text{sterile } \nu; M_{\text{cut}} \sim 10^9 M_{\odot}$$

Log  $k^3 P(k)$  wavelength  $k^{-1}$  (comoving  $h^{-1}$  Mpc)



cold dark matter



warm dark matter



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
Boyarski & Ruchayskiy '12



# Four problems for CDM on small scales?

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These problems have all been identified in N-body simulations that follow only dark matter

Need to consider “baryon effects”

$z = 48.4$

$T = 0.05 \text{ Gyr}$

500 kpc



VIRGO

[icc.dur.ac.uk/Eagle](http://icc.dur.ac.uk/Eagle)

“Evolution and assembly of galaxies and  
their environment”

# THE EAGLE PROJECT

**Durham:** Richard Bower, Michelle Furlong, Carlos Frenk, Matthieu Schaller, James Trayford, Yelti Rosas-Guevara, Tom Theuns, Yan Qu, John Helly, Adrian Jenkins.

**Leiden:** Rob Crain, Joop Schaye.

**Other:** Claudio Dalla Vecchia, Ian McCarthy, Craig Booth...

+ Virgo Consortium

# The EAGLE simulations

EVOLUTION AND ASSEMBLY OF GALAXIES AND THEIR ENVIRONMENTS

A project of the Virgo consortium

$z = 19.9$

$L = 25.0 \text{ cMpc}$

Visible components:

CDM



# The Eagle Simulations

EVOLUTION AND ASSEMBLY OF GALAXIES AND THEIR ENVIRONMENTS

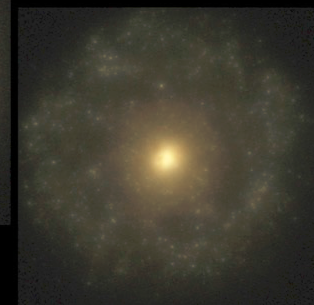
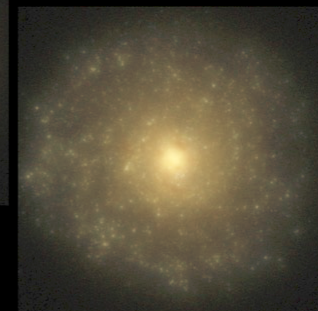
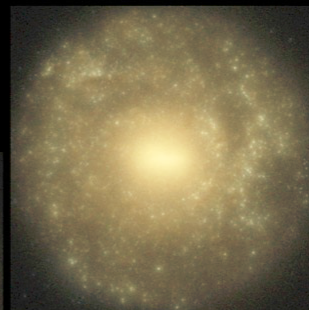
The Hubble Sequence realised in cosmological simulations

SB

E0

E7

S0



S

Irr

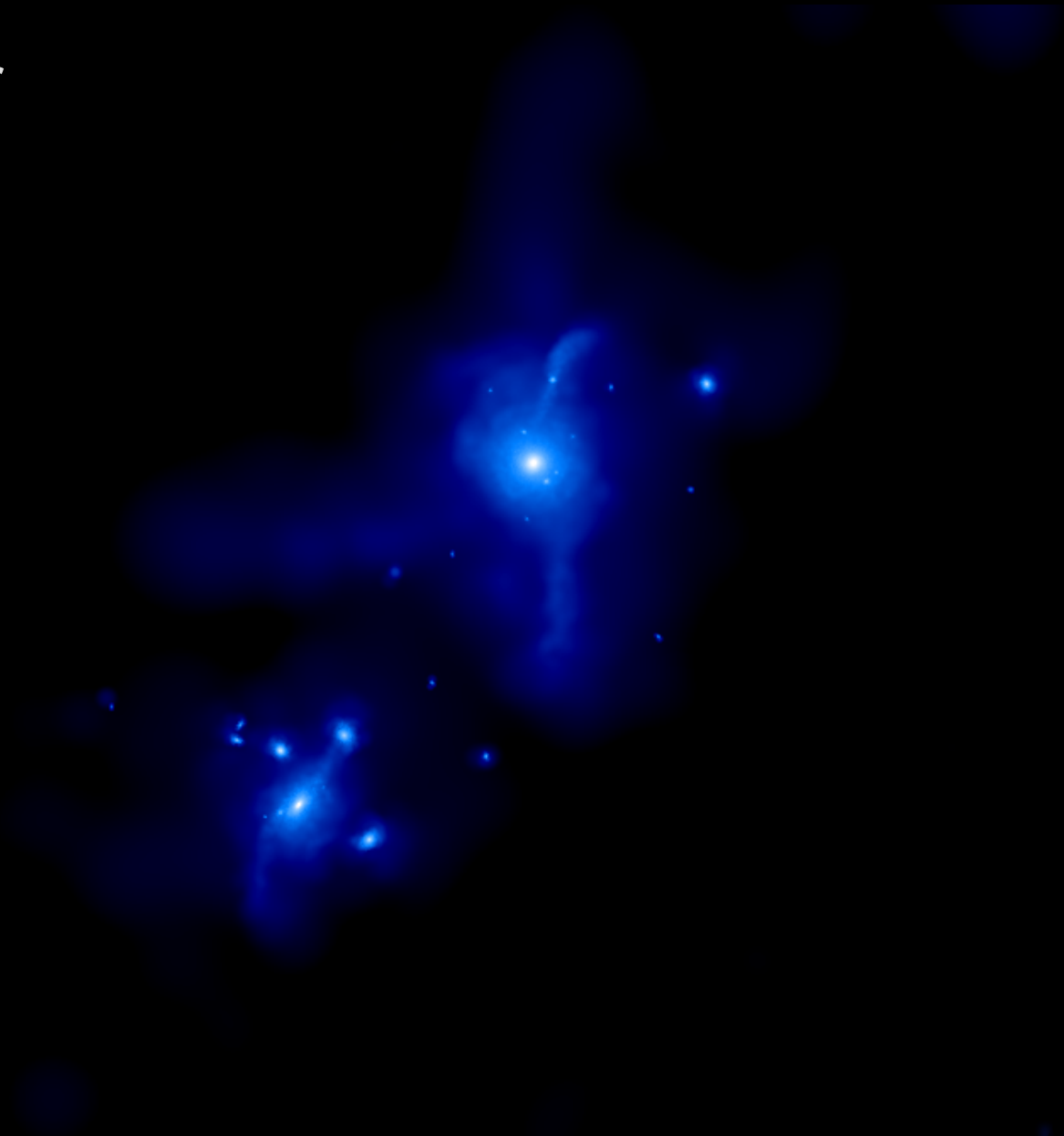
Trayford et al '14



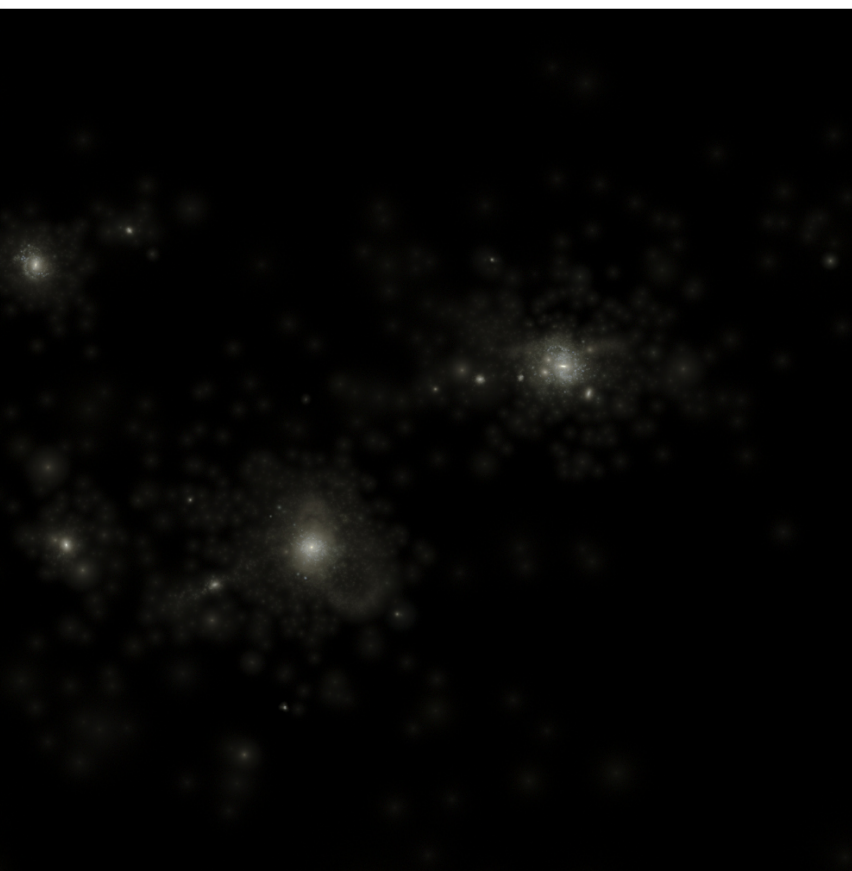
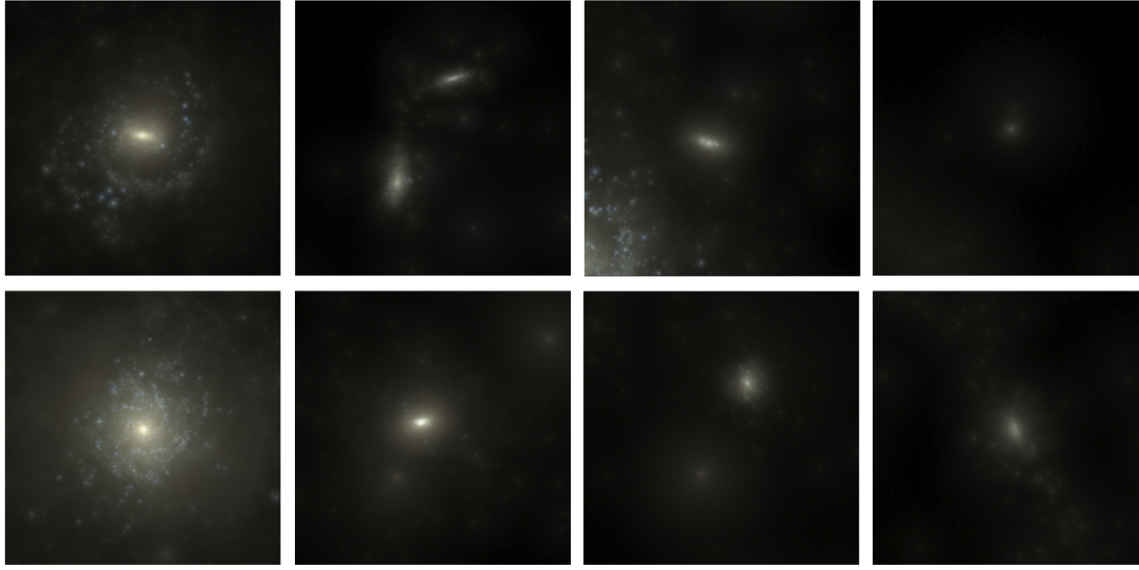
# EAGLE full hydro Local Group simulations

Dark Matter

Gas







# Four problems for CDM on small scales?

1. The “missing satellites” problem
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3. The “core-cusp” problem
4. The “satellite disk” problem



# The “missing satellites” problem

The satellites of the MW



Dark matter subhalos in CDM

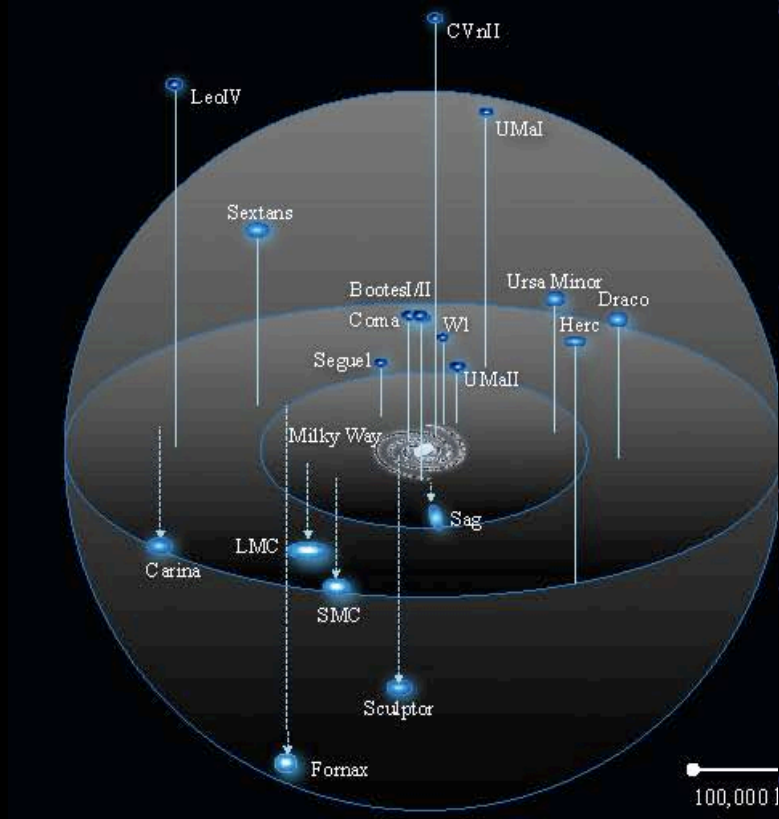
“Missing satellites” problem:

The Milky way has only about 25 satellites

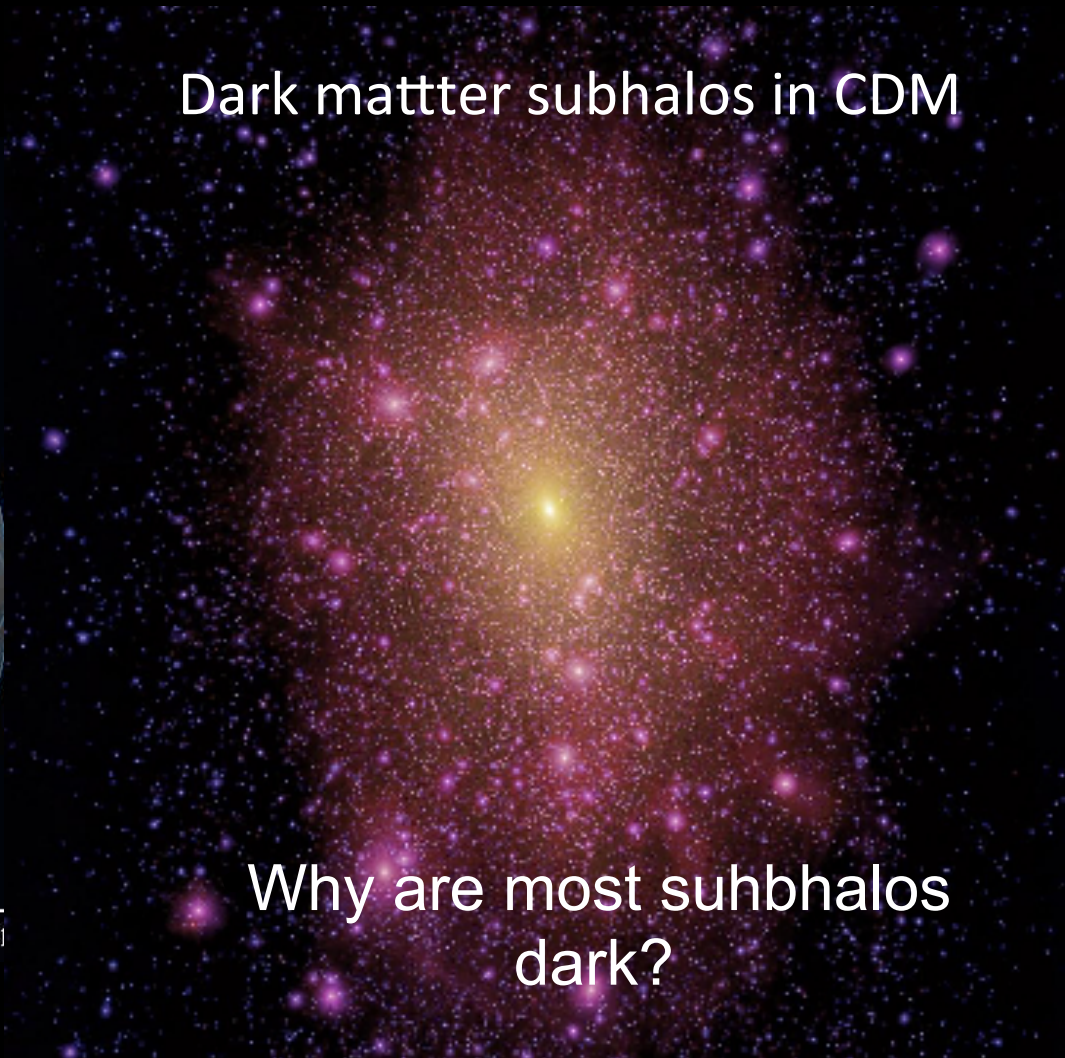
**BUT:** CDM halos have a huge number of subhalos

# The “missing satellites” problem

## The satellites of the MW



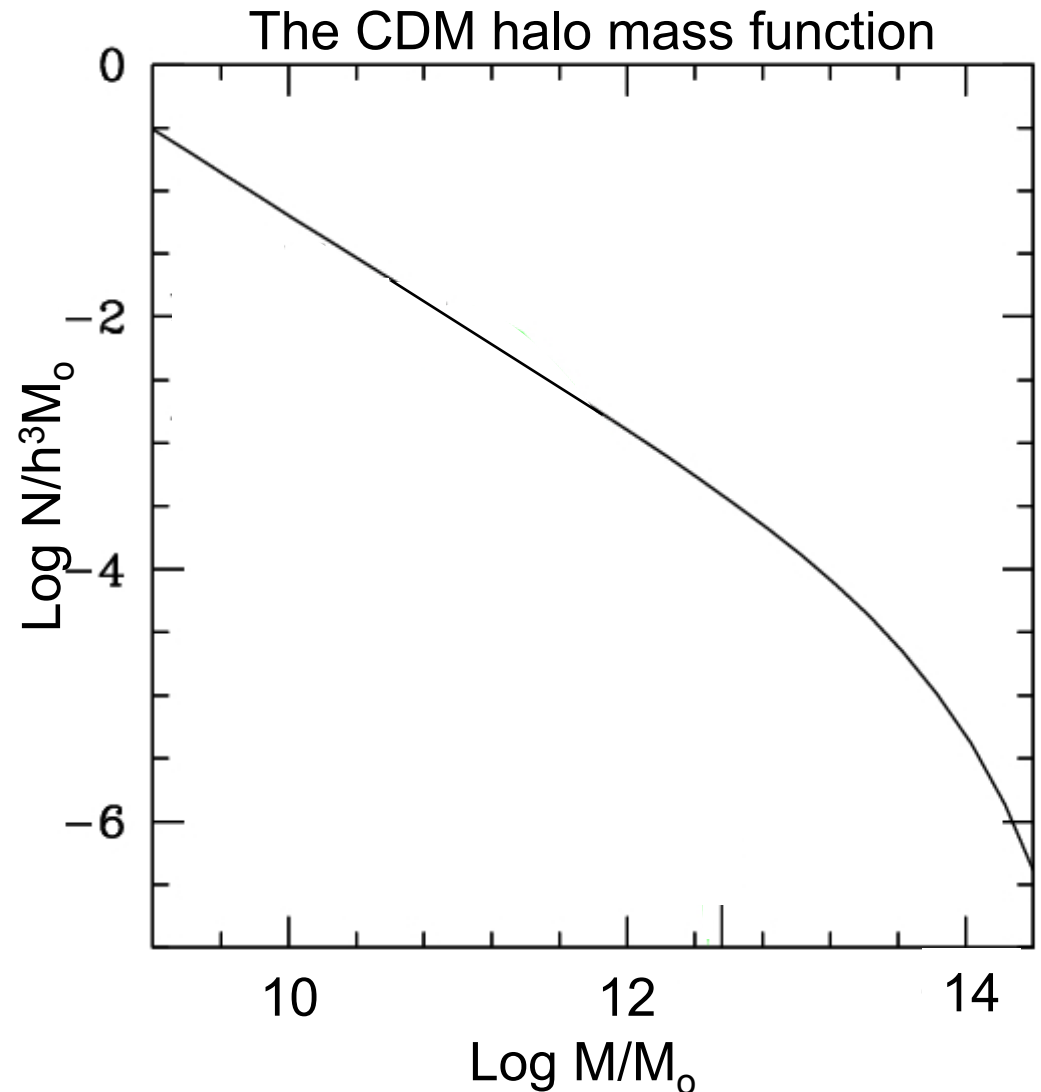
## Dark matter subhalos in CDM



Why are most subhalos dark?

# The CDM halo mass function

Jenkins et al. '01





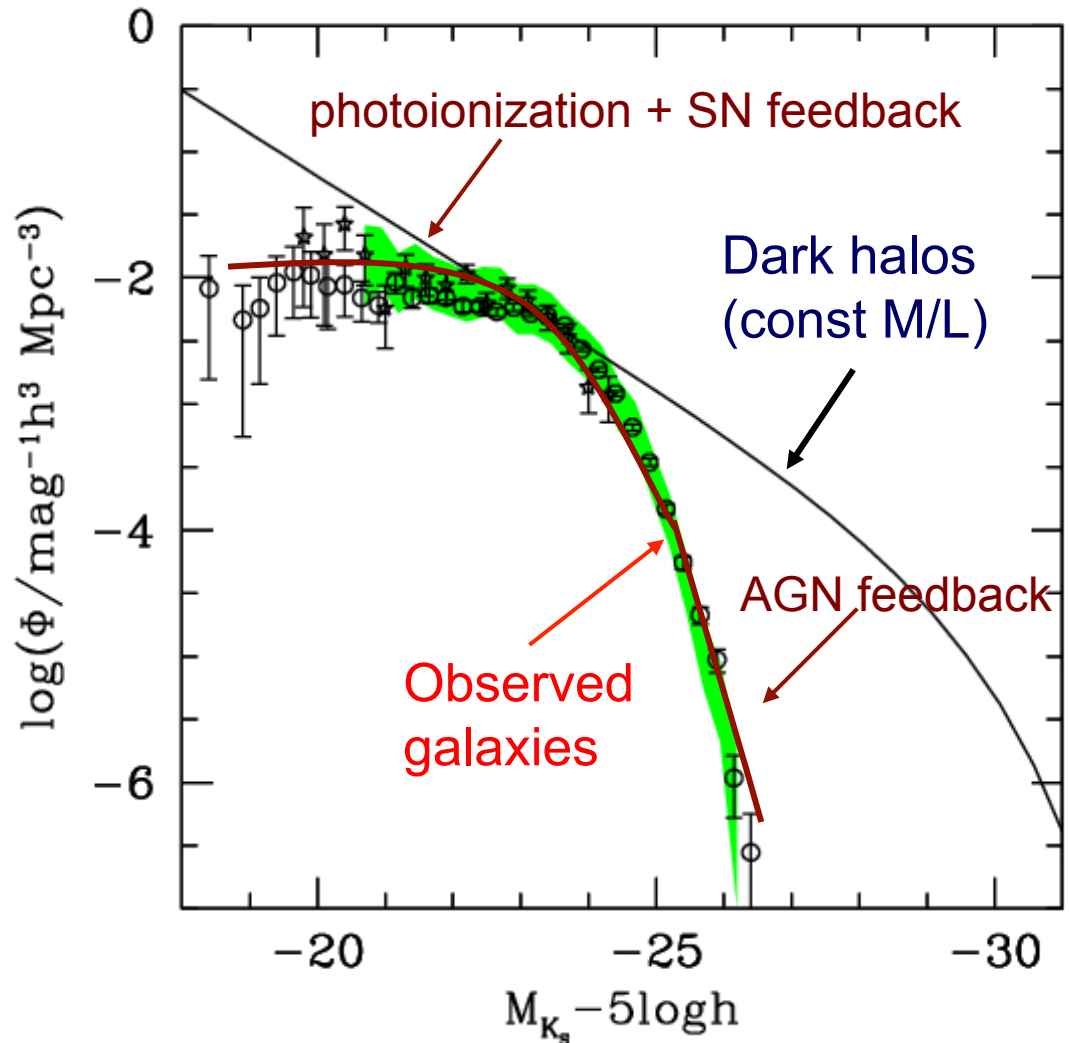
# The galaxy luminosity function

The halo mass function and the galaxy luminosity function have different shapes



Galaxy luminosity not just  $\propto$  halo mass

Complicated variation of M/L with halo mass



White & Frenk '91; Kauffmann et al '93; Benson et al '03; Croton et al '06; Bower et al. '06



Making a galaxy in a small halo is hard because:

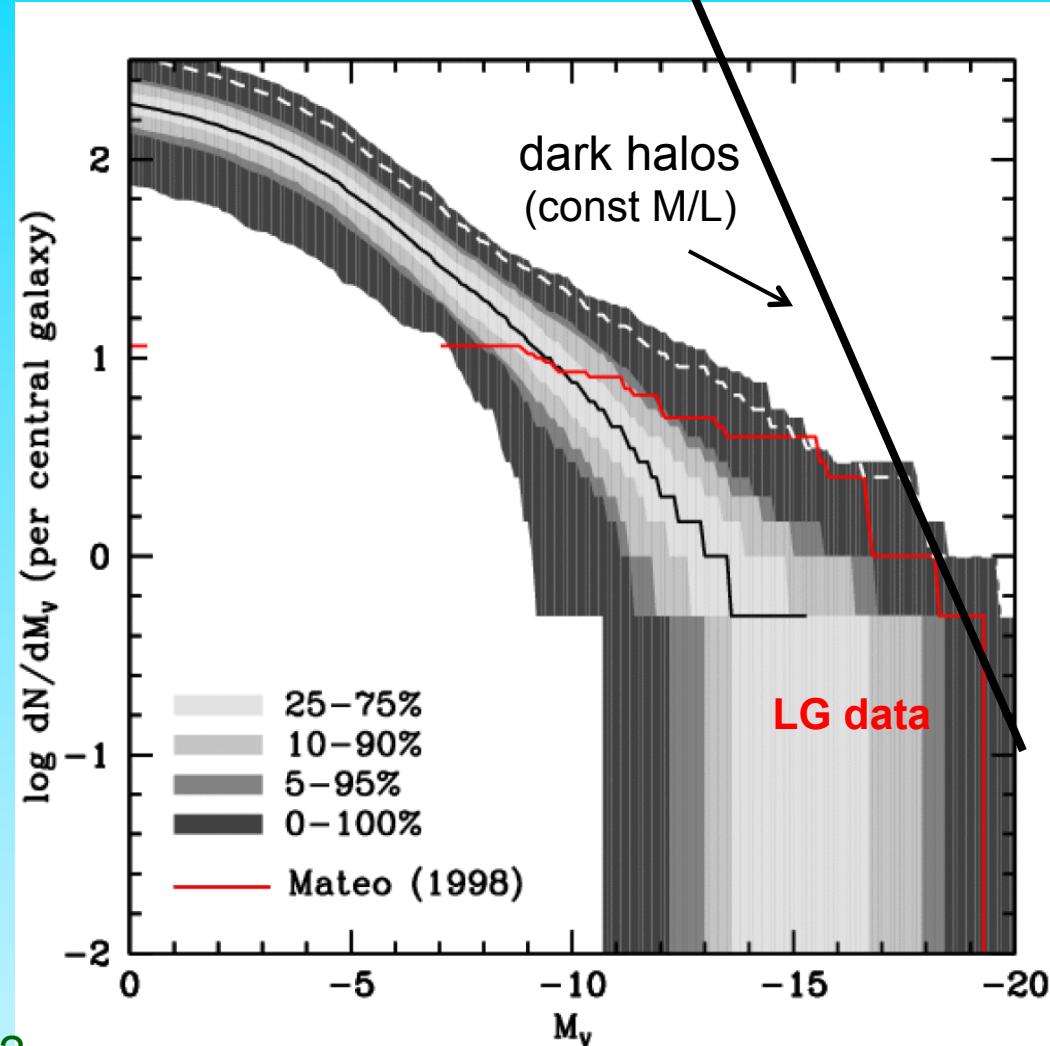
- Reionization heats gas above  $T_{\text{vir}}$ , preventing it from cooling and forming stars in small halos
- Supernovae feedback expels residual gas

Most subhalos never make a galaxy!



# Luminosity Function of Local Group Satellites

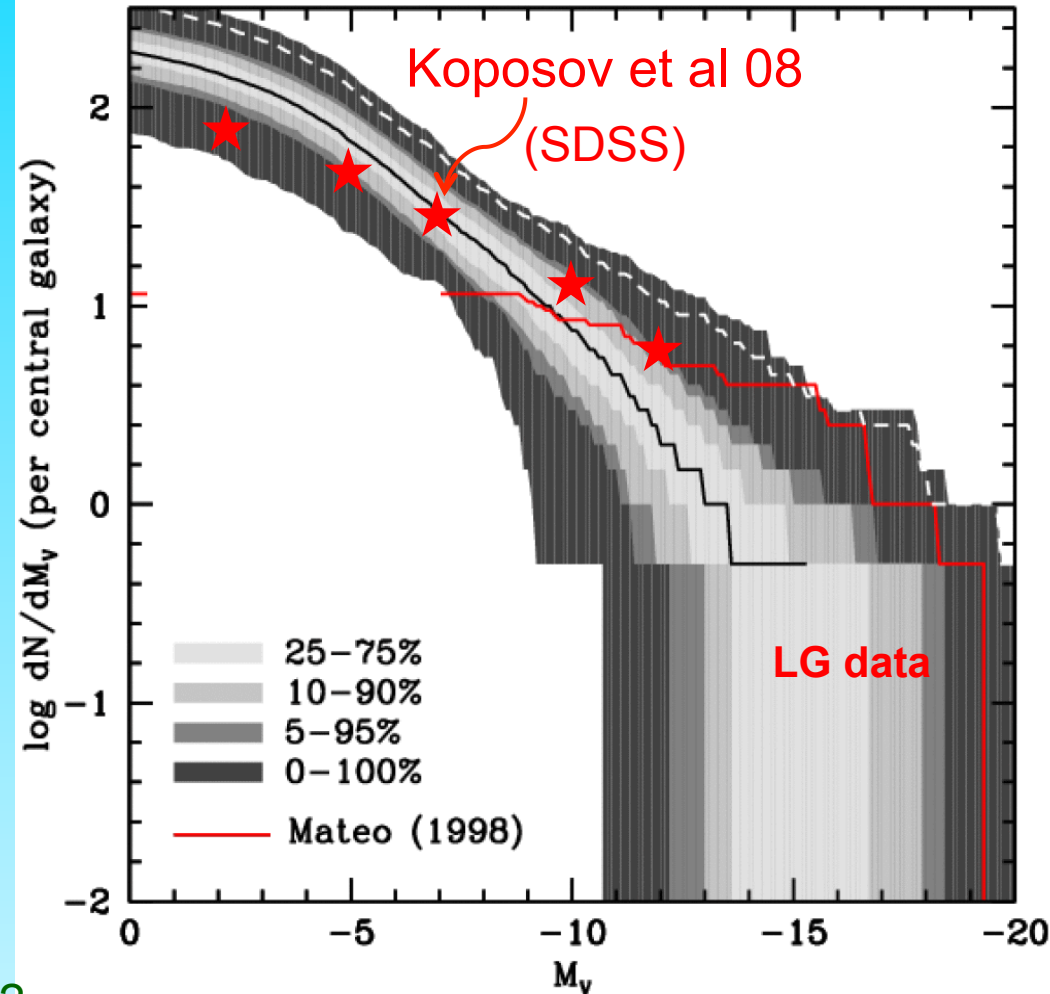
- Median model → correct abund. of sats brighter than  $M_V = -9$  and  $V_{\text{cir}} > 12$  km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare (~2% of cases)



Benson, Frenk, Lacey, Baugh & Cole '02  
(see also Kauffman et al '93, Bullock et al '01)

# Luminosity Function of Local Group Satellites

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VIRG

EAGLE full  
hydro  
simulations

Local Group

Sawala et al '14

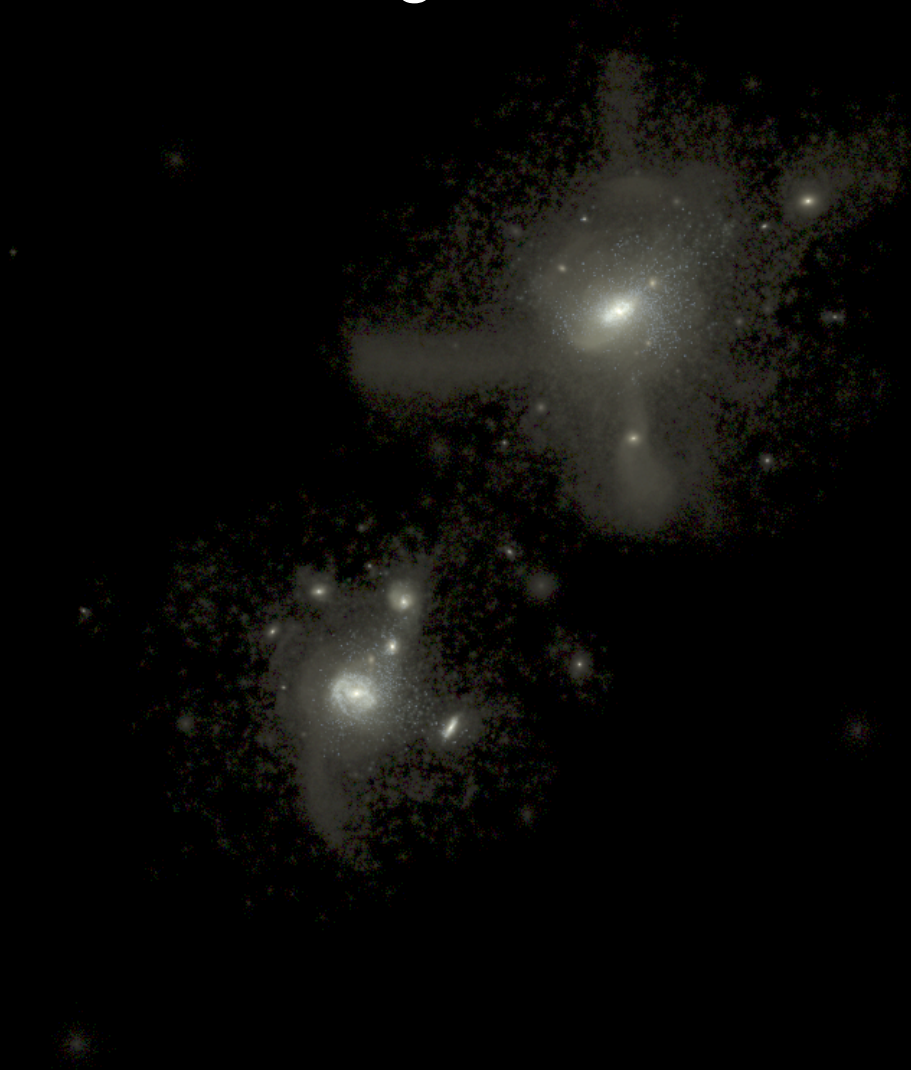


VIRG

Far fewer satellite galaxies than CDM halos

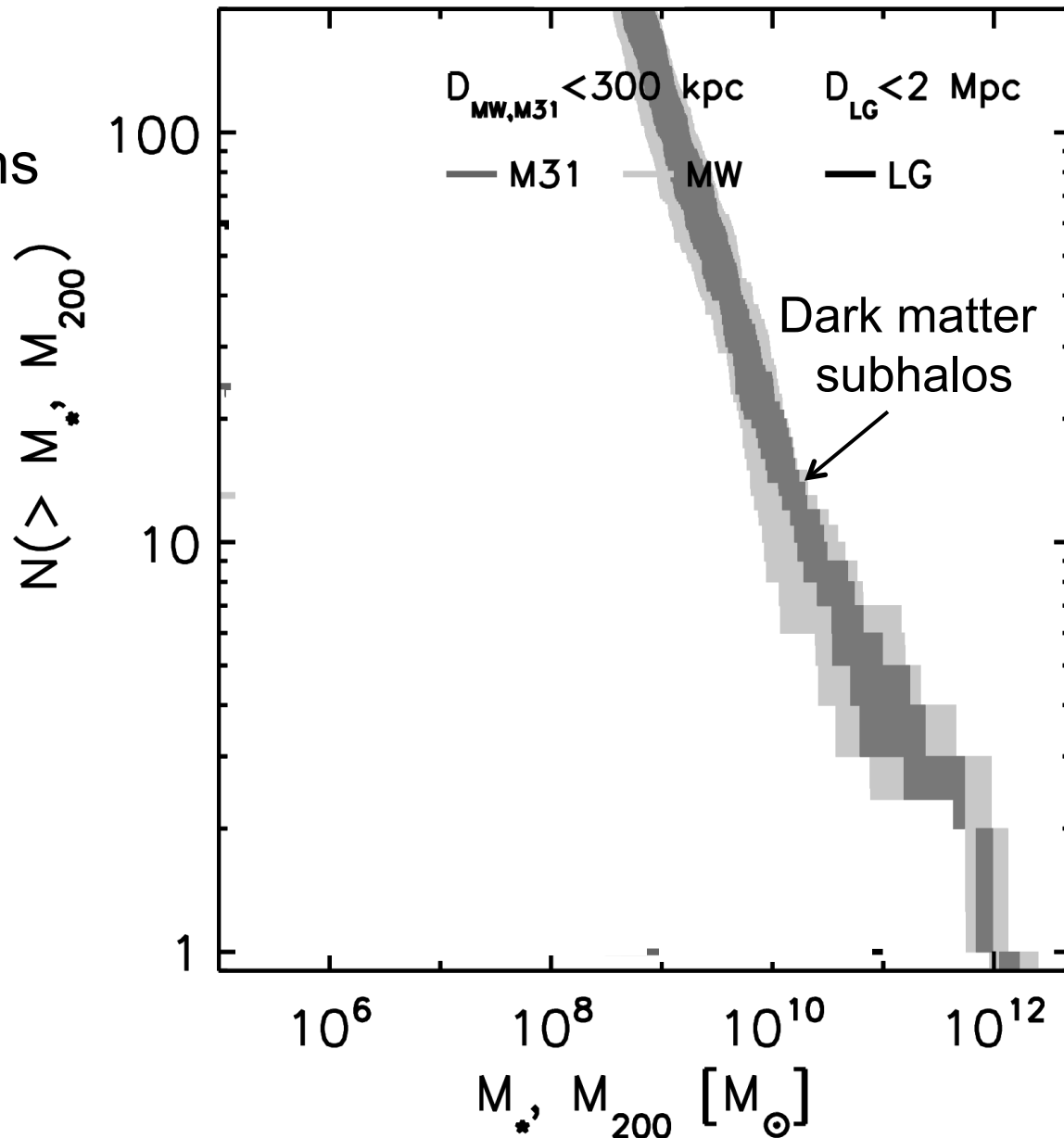
EAGLE full  
hydro  
simulations

Local Group



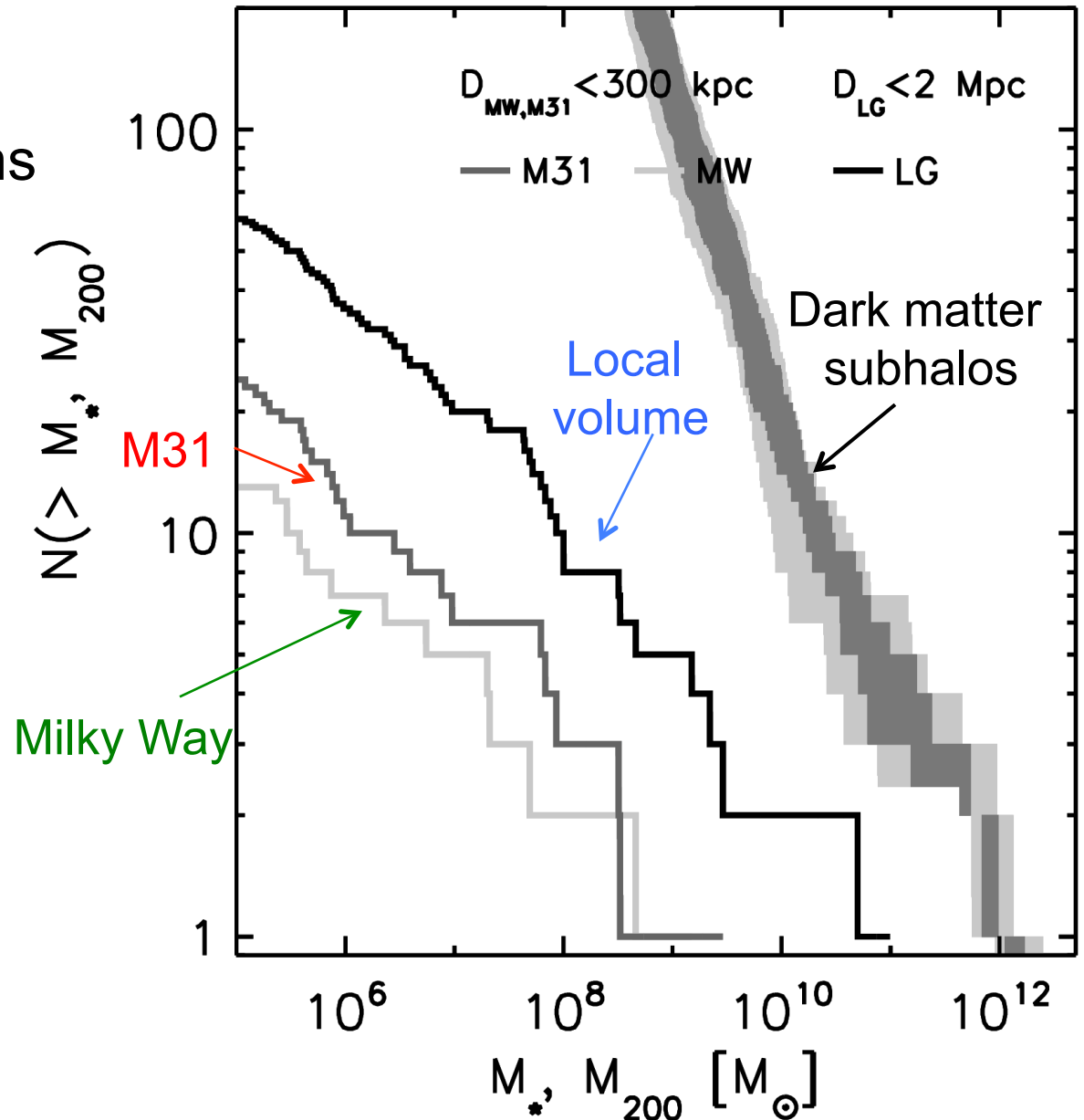
Sawala et al '14

## Subhalo mass functions



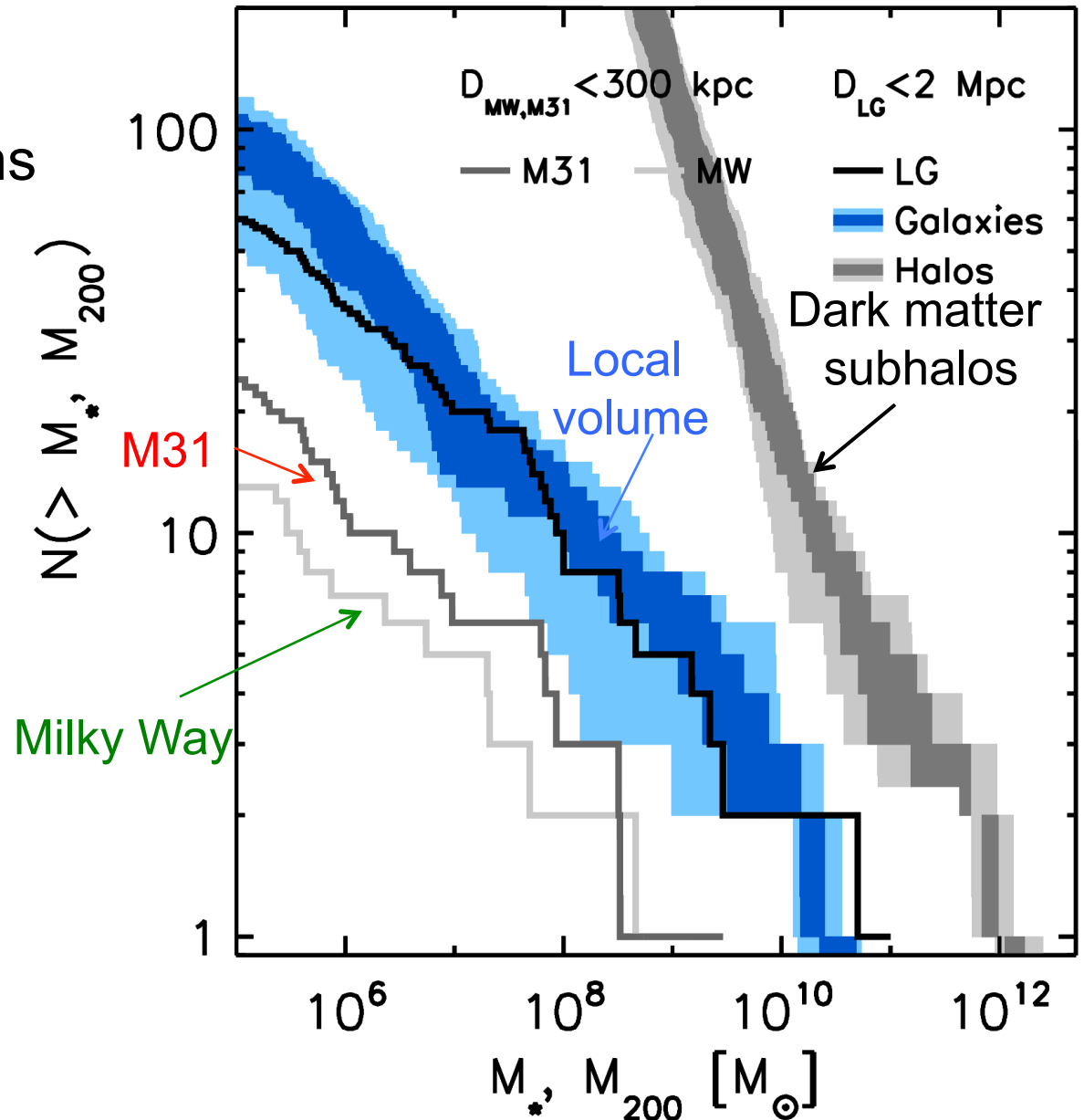


## Stellar mass functions

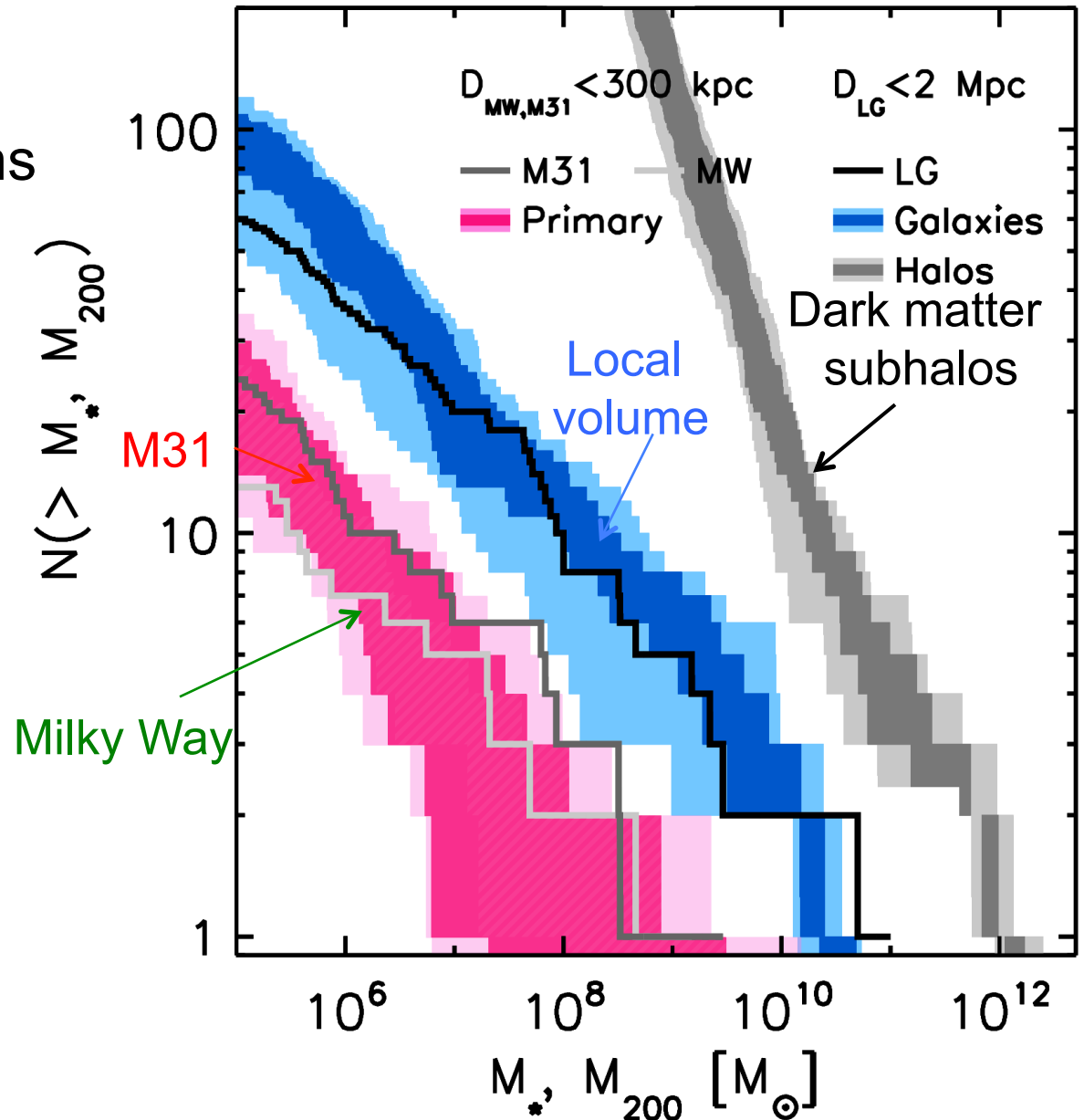




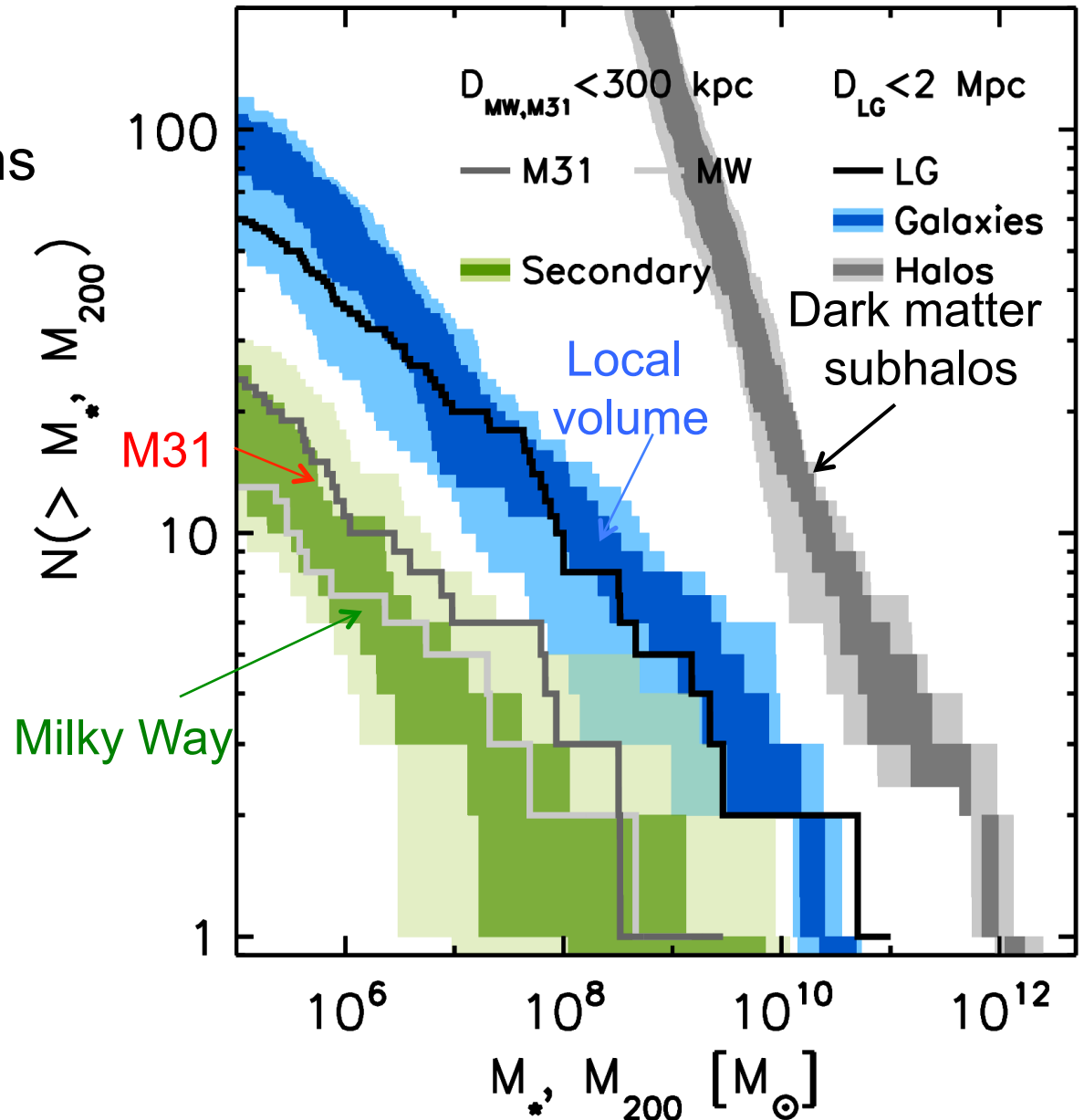
## Stellar mass functions



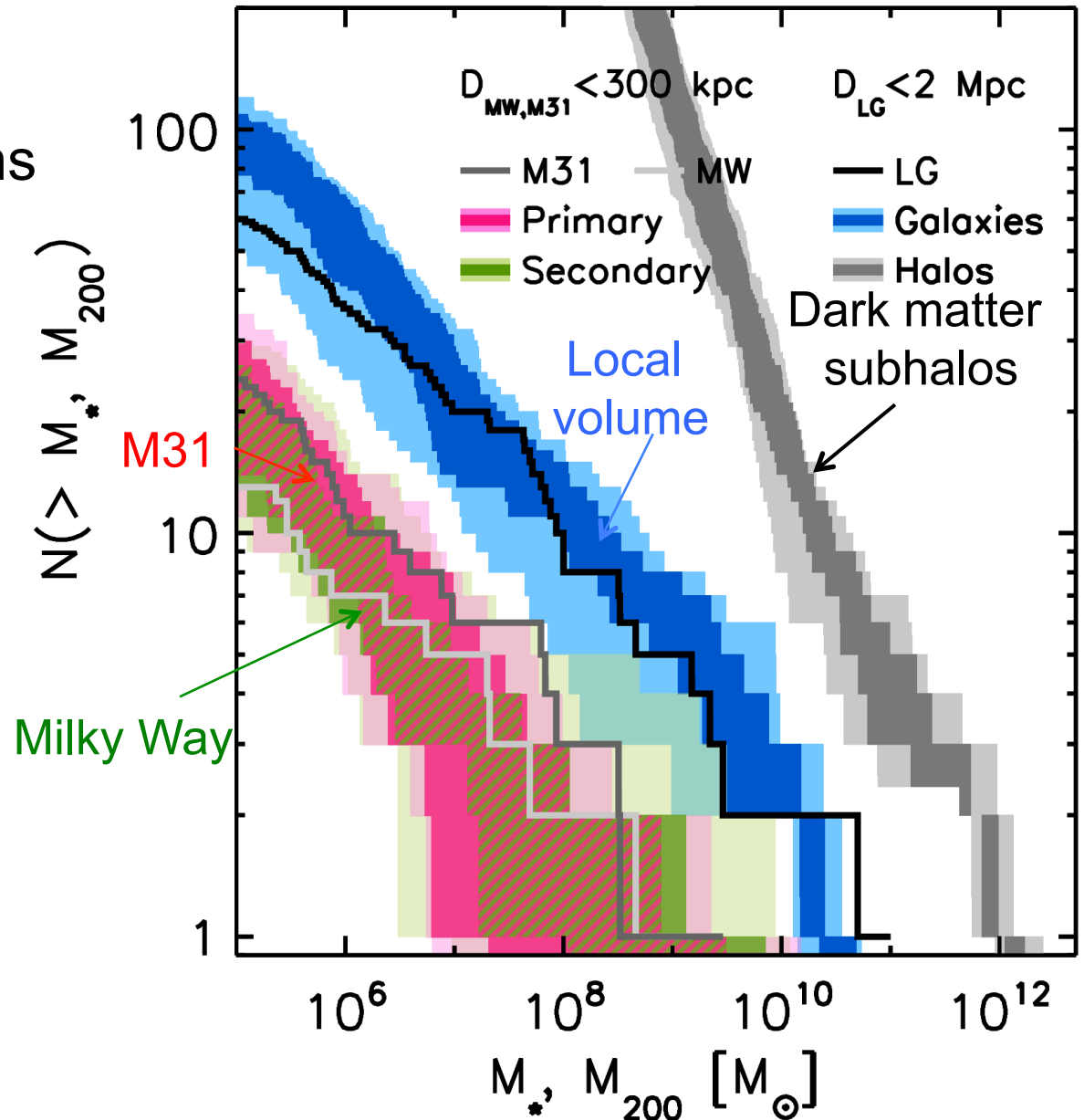
## Stellar mass functions



## Stellar mass functions



## Stellar mass functions





Is there a “satellite problem” in CDM?

No, when galaxy formation is taken into account!

# Four problems for CDM on small scales?

1. The “missing satellites” problem
2. The “too-big-to-fail” problem
3. The “core-cusp” problem
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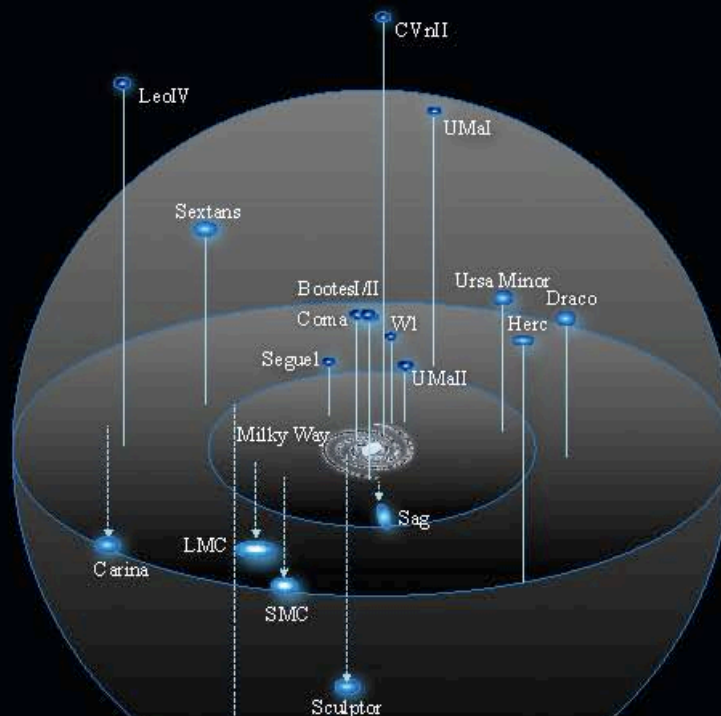


# The “too-big-to-fail” problem

$$V_c = \sqrt{\frac{GM}{r}}$$

$$V_{\max} = \max V_c$$

The satellites of the MW



MW has only 3 satellites  
with  $V_{\max} > 30$  km/s  
(LMC, SMC, Sgr)

Dark matter subhalos in CDM

CDM has  $\sim 10$  subhalos with  
 $V_{\max} > 30$  km/s

Why did these not make a  
galaxy?

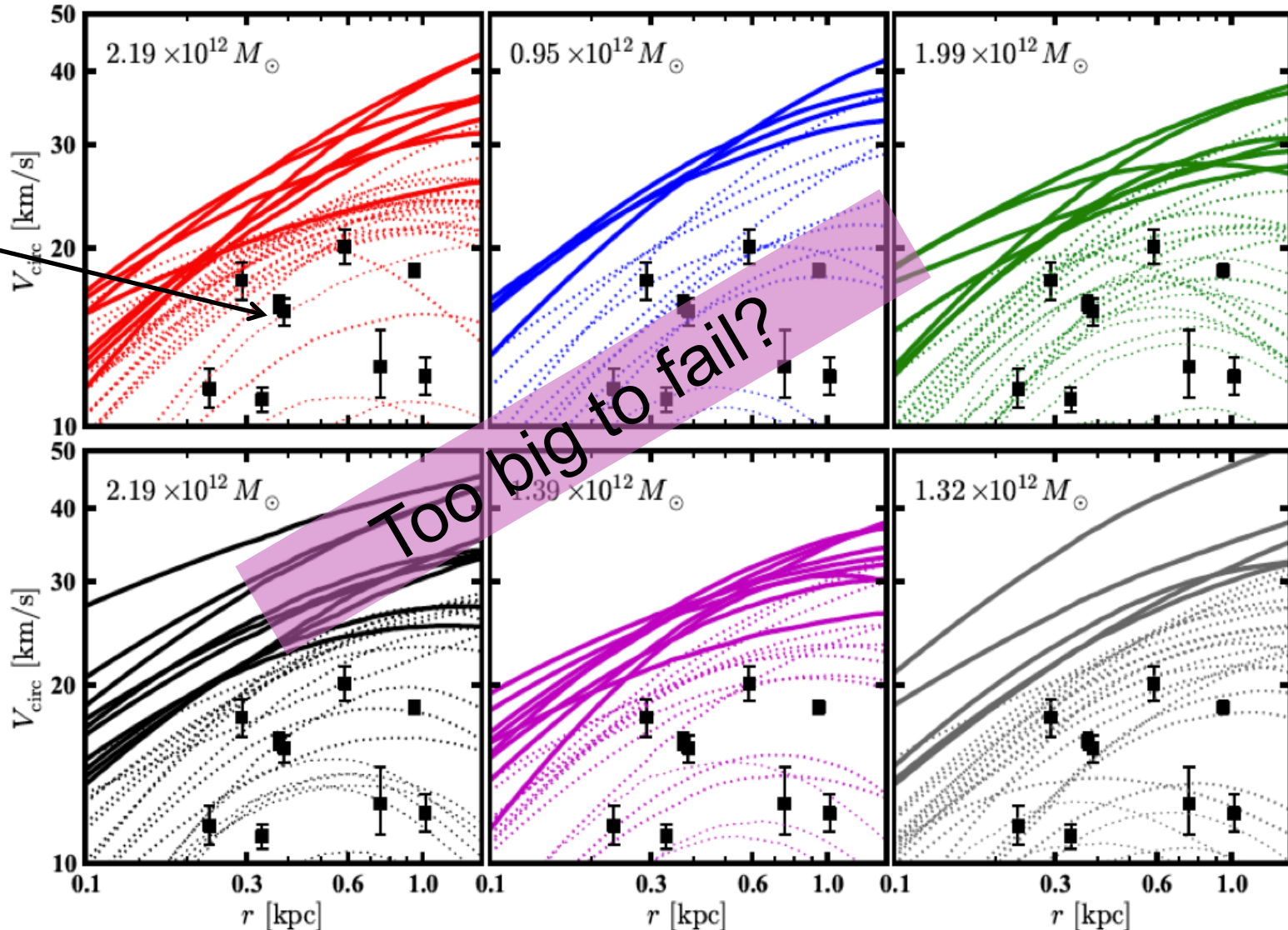
# Rotation curves of Aquarius subhalos

Boylan-Kolchin et al. '11

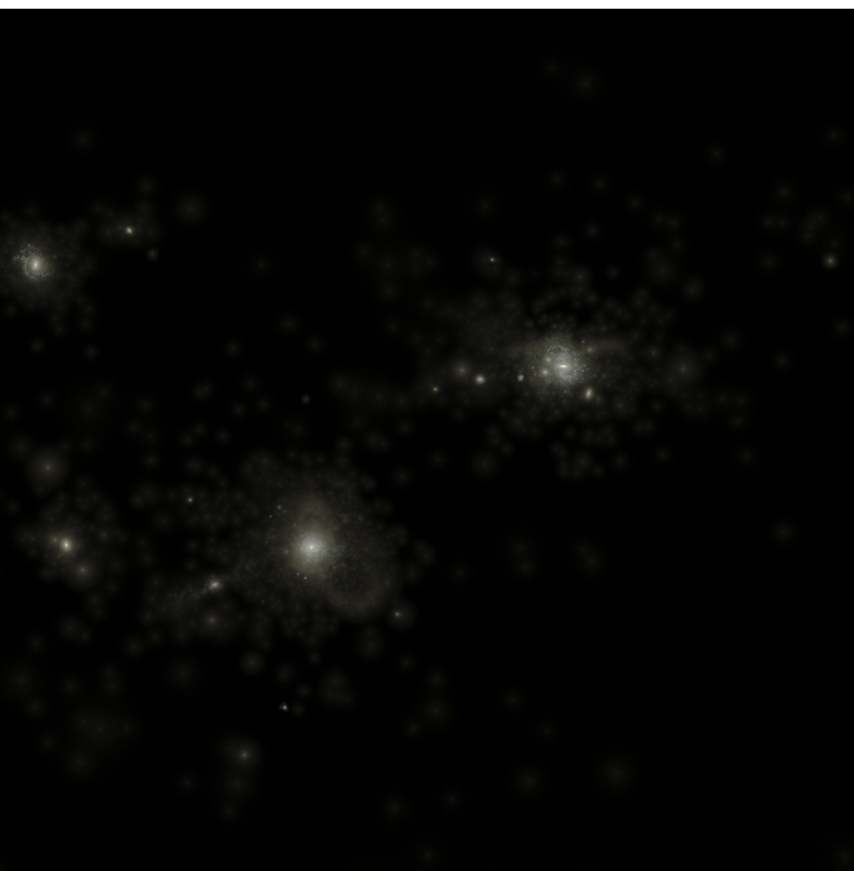
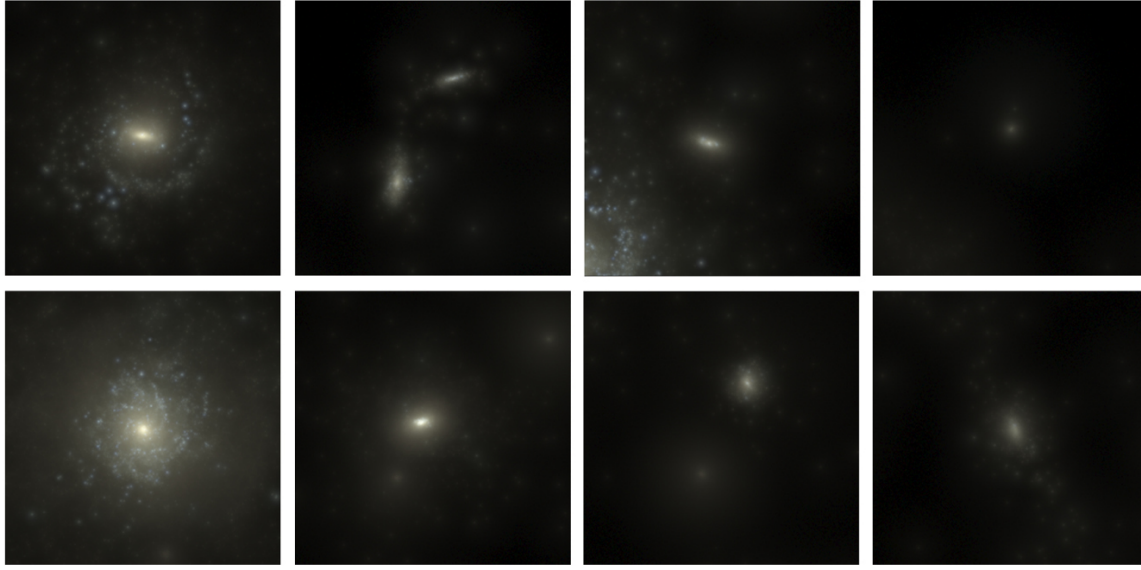
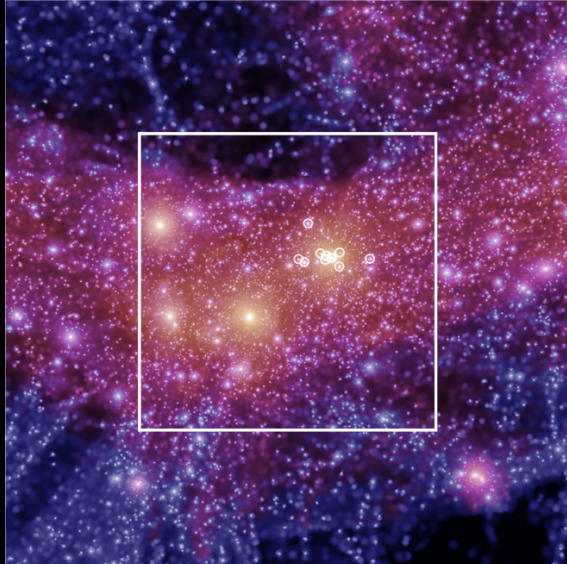
$$V_c = \sqrt{\frac{GM}{r}}$$

9 dwarf  
satellites of  
Milky Way:  
mass within  
half-light  
radius

Excludes  
LMC, SMC,  
Sagittarius





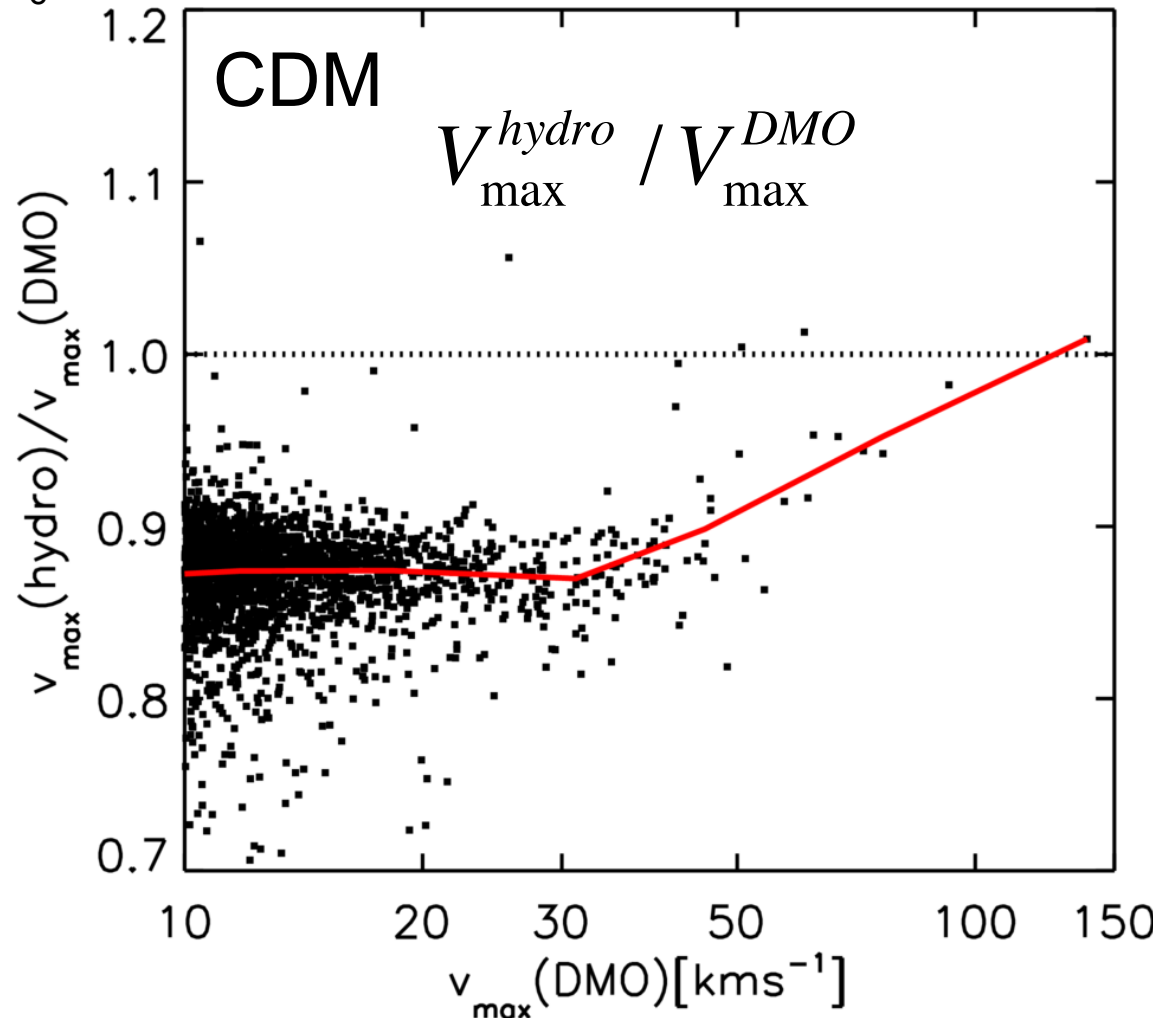
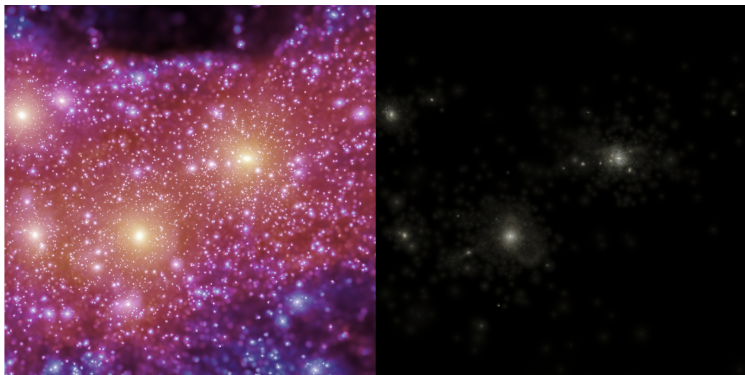


# To-big-to-fail in CDM: baryon effects

$$V_c = \sqrt{\frac{GM}{r}} \quad V_{\max} = \max V_c$$

Reduction in  $V_{\max}$  due to  
SN feedback:

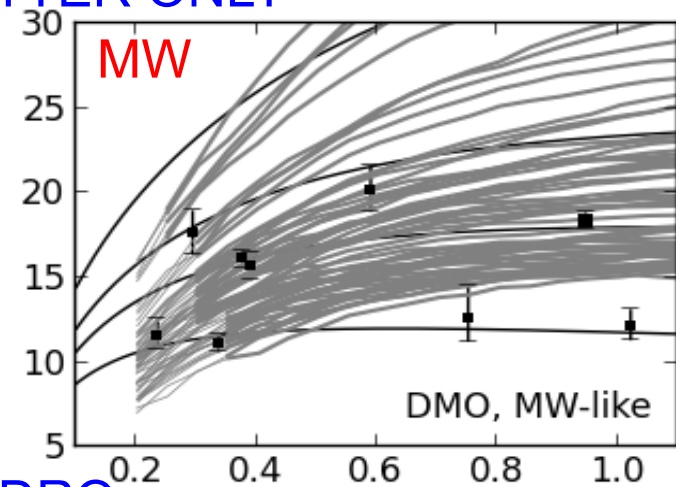
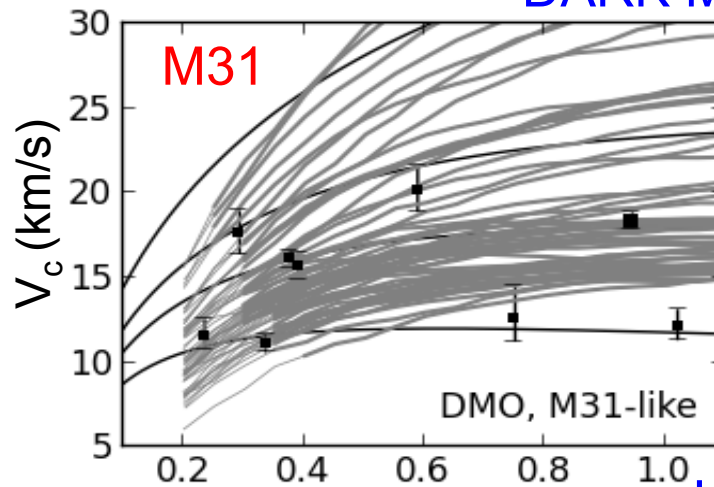
→ Lowers halo mass &  
thus halo growth rate



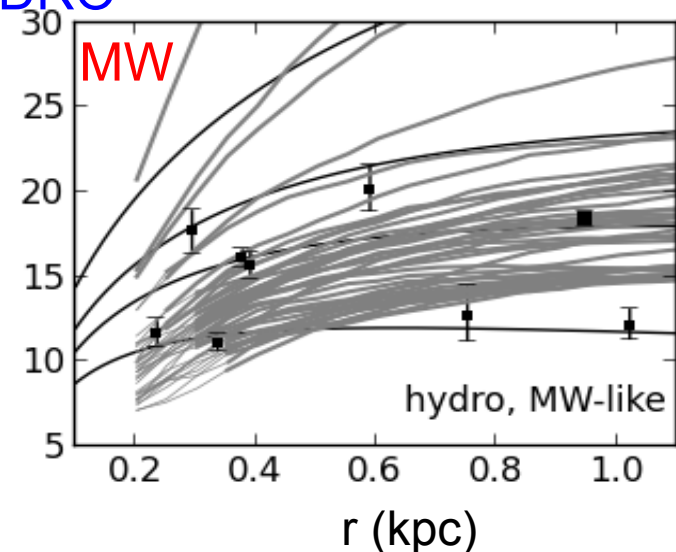
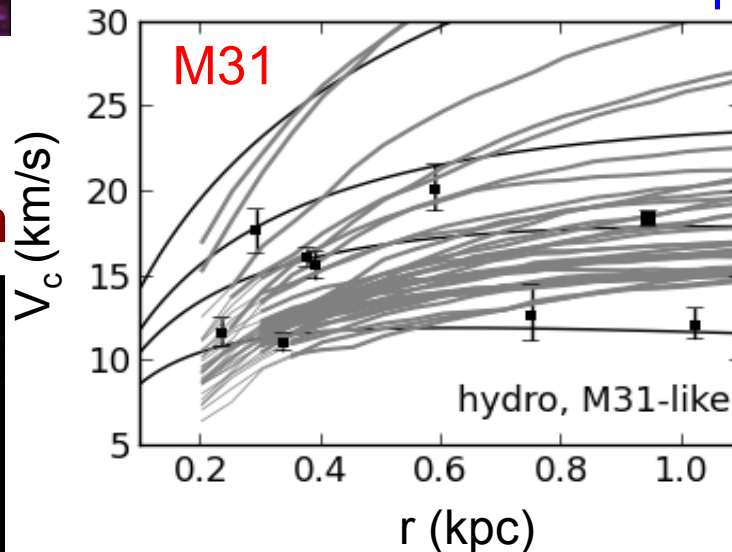
Sawala et al. '13, '14

# Too-big-to-fail: the baryon bailout

DARK MATTER ONLY



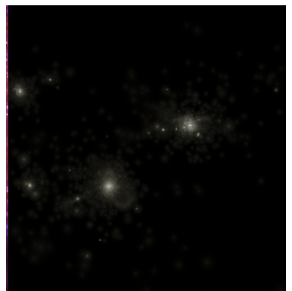
HYDRO



DM-only  
simulation



Gas  
simulation



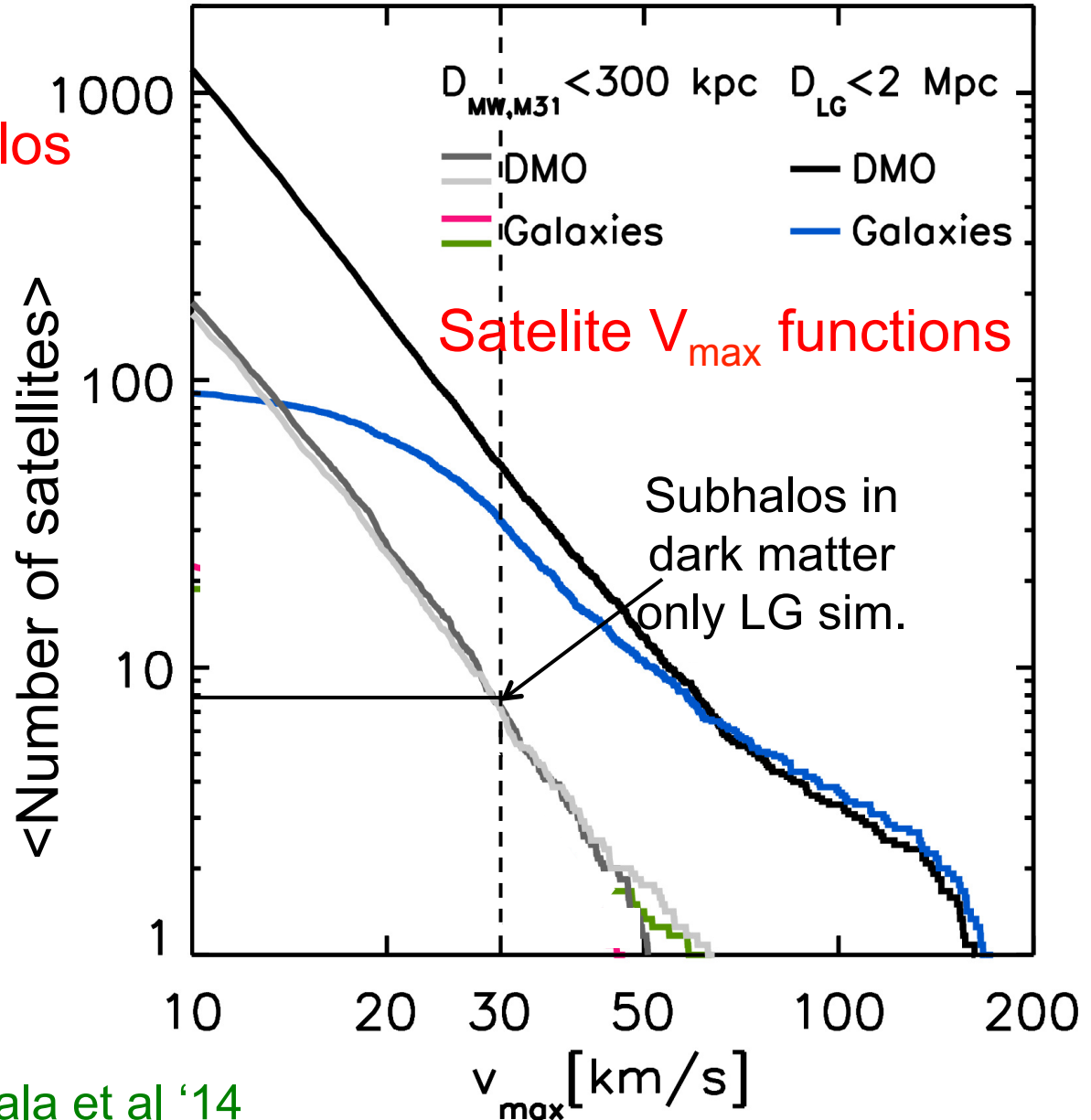
Number of subhalos of given  $V_{\max}$  is greatly reduced in gas simulations

Sawala et al. '14



# Too-big-to-fail: the baryon bailout

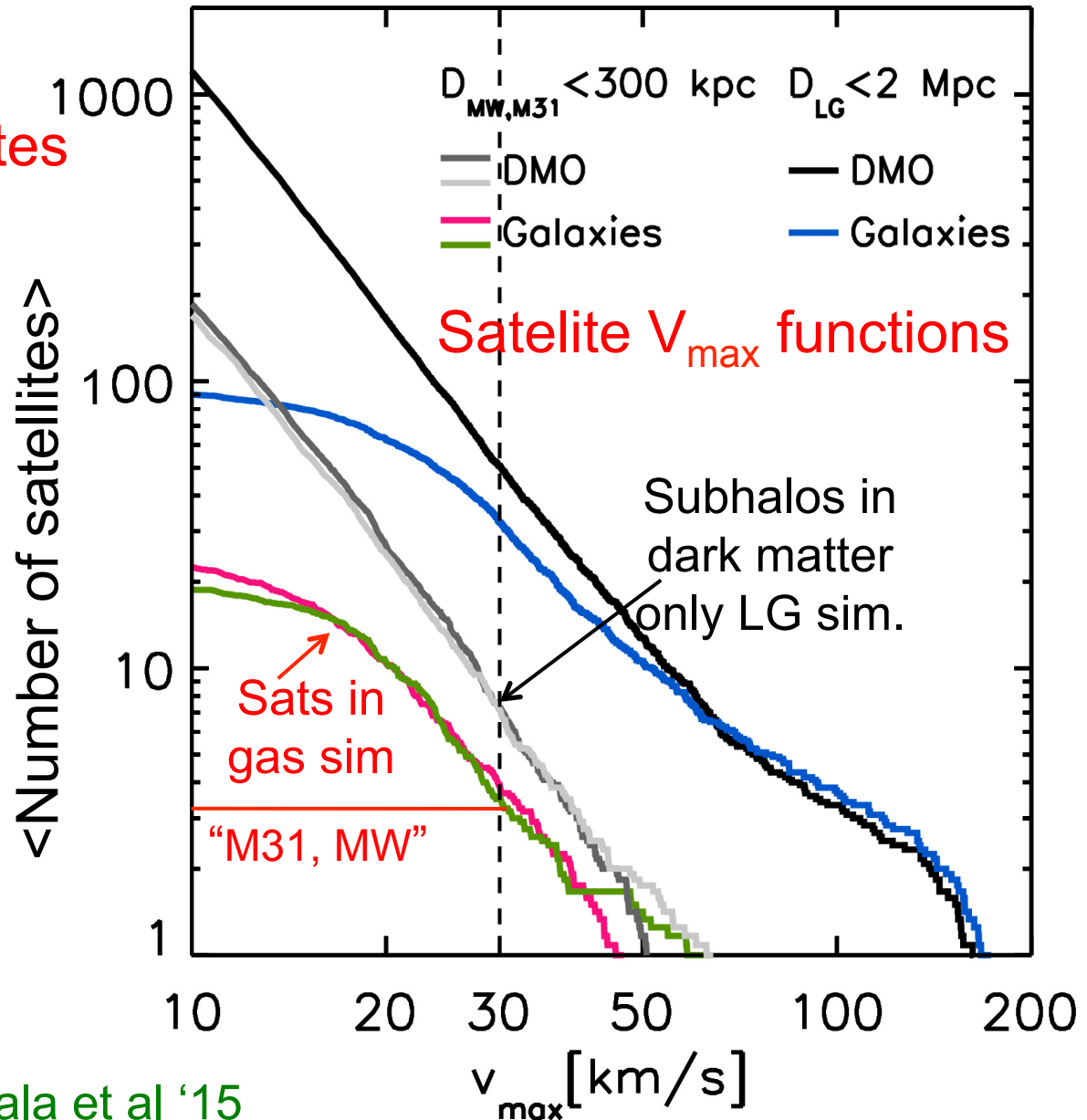
DM only sims  $\rightarrow$   **$\sim 10$  halos**  
with  $V_{\max} > 30$  km/s





# Too-big-to-fail: the baryon bailout

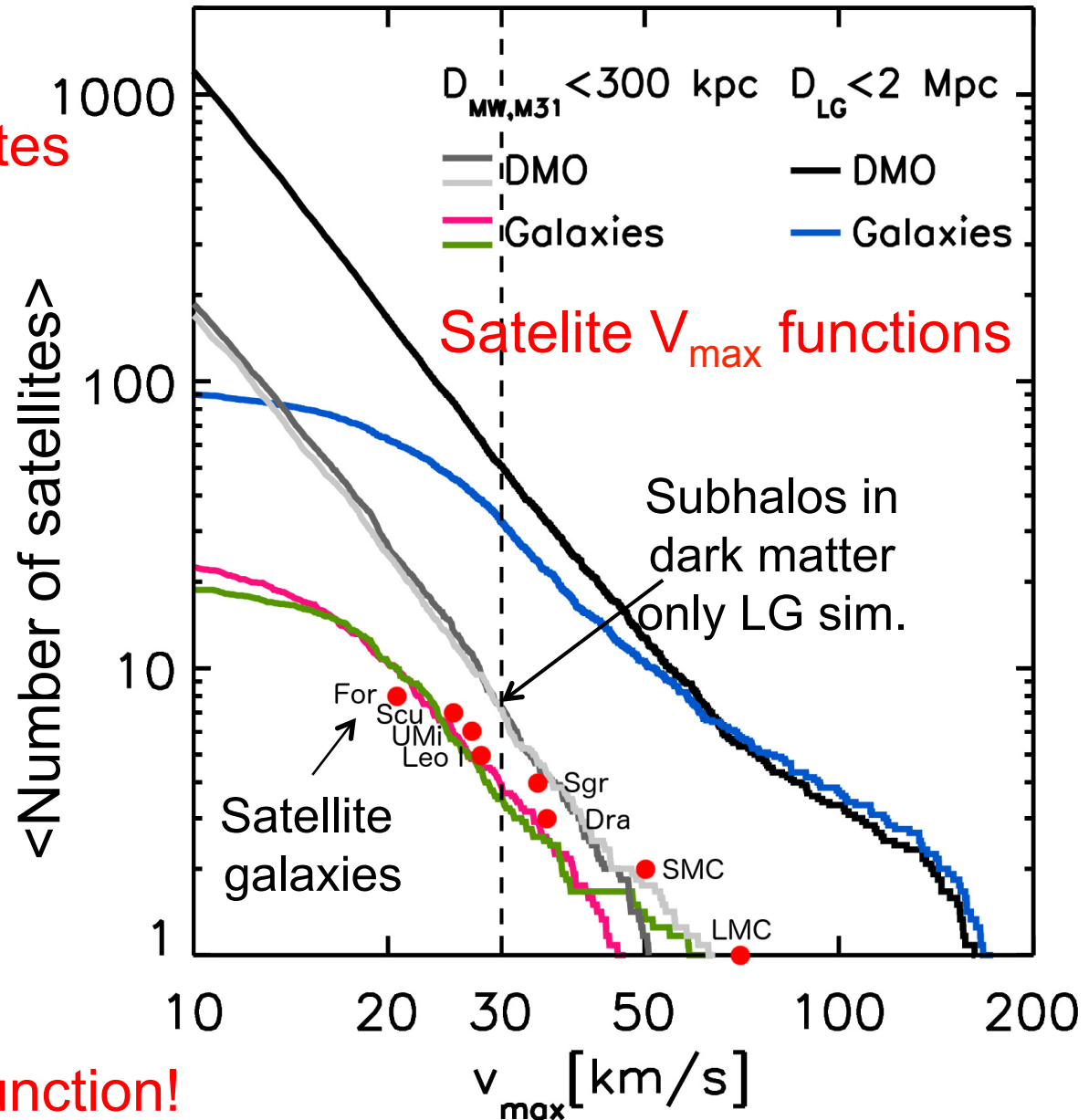
Hydro sims  $\rightarrow$  **~3 satellites**  
with  $V_{\max} > 30$  km/s



Sawala et al '15

# Too-big-to-fail: the baryon bailout

Hydro sims  $\rightarrow$   **$\sim 3$  satellites**  
with  $V_{\max} > 30$  km/s



**and with correct  $V_{\max}$  function!**



Is there a “too-big-to-fail” problem in CDM?

No, when galaxy formation is taken into account!

# Four problems for CDM on small scales?

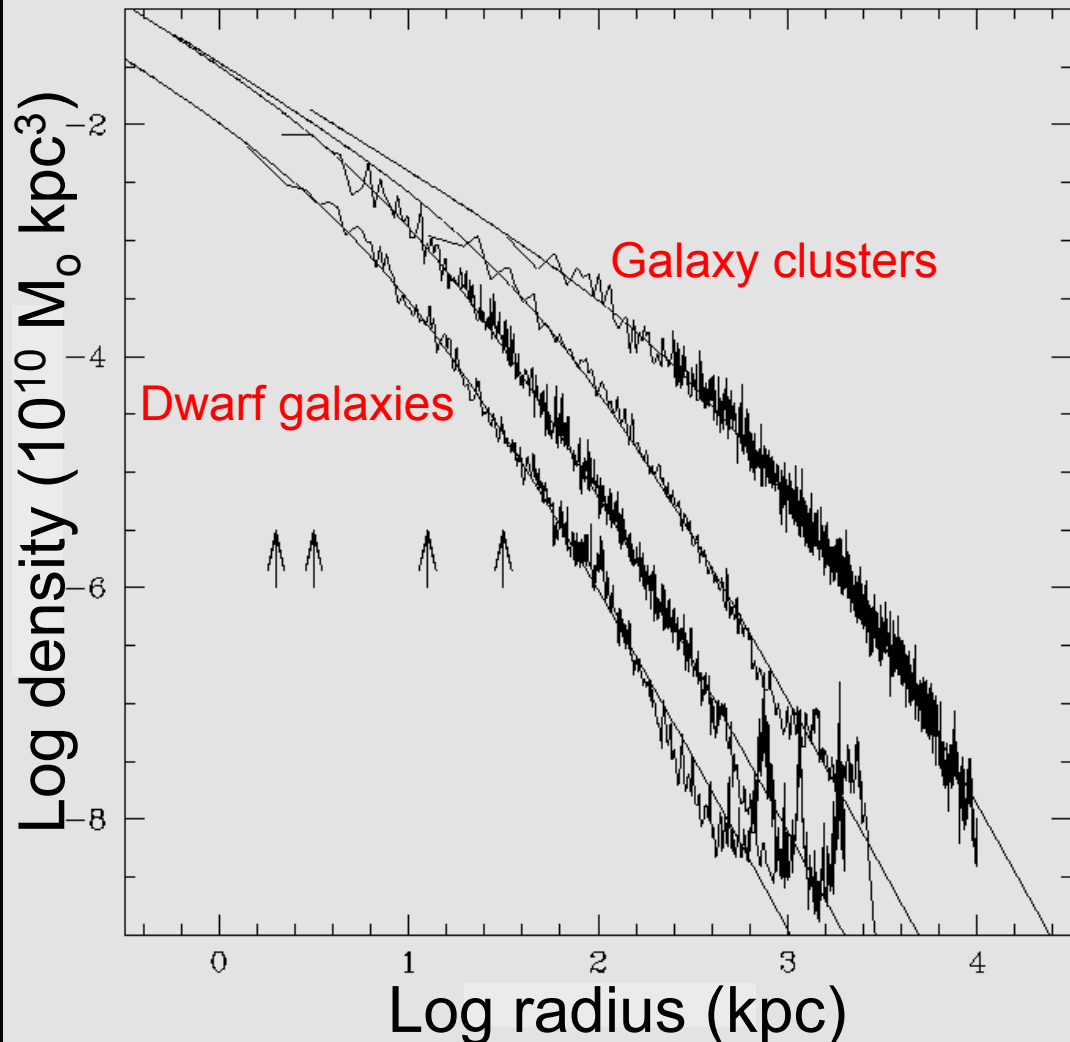
1. The “missing satellites” problem
2. The “too-big-to-fail” problem
3. The “core-cusp” problem
4. The “satellite disk” problem





# A challenge to Andi Burkert

# The Density Profile of Cold Dark Matter Halos



Shape of halo profiles  
~independent of halo mass &  
cosmological parameters

Density profiles are “cuspy” -  
no ‘core’ near the centre

Fitted by simple formula:

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

(Navarro, Frenk & White '97)

More massive halos and  
halos that form earlier have  
higher densities (bigger  $\delta$ )

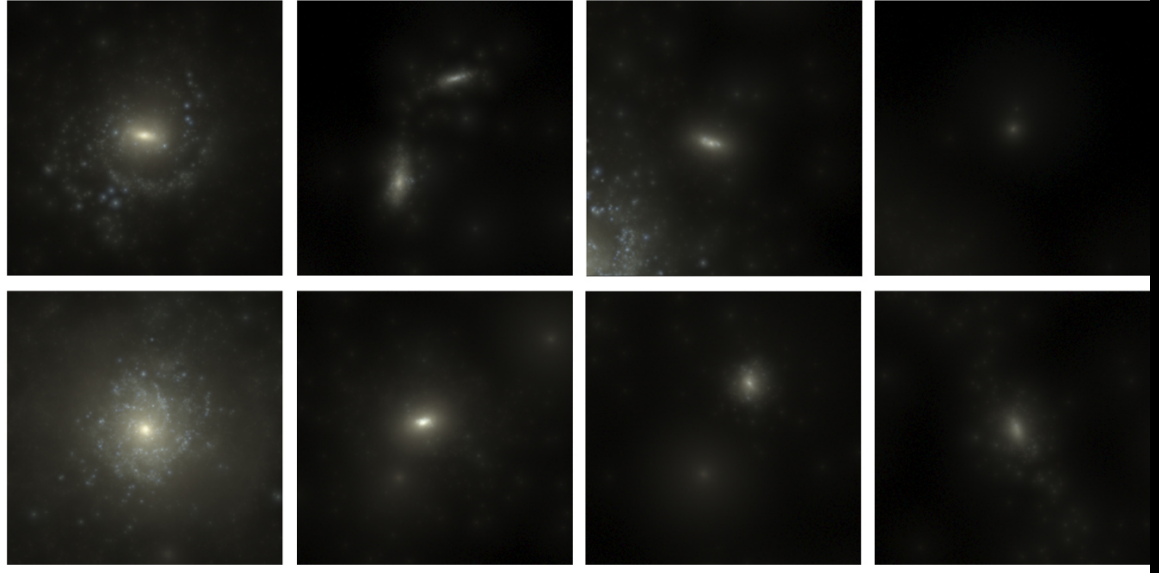
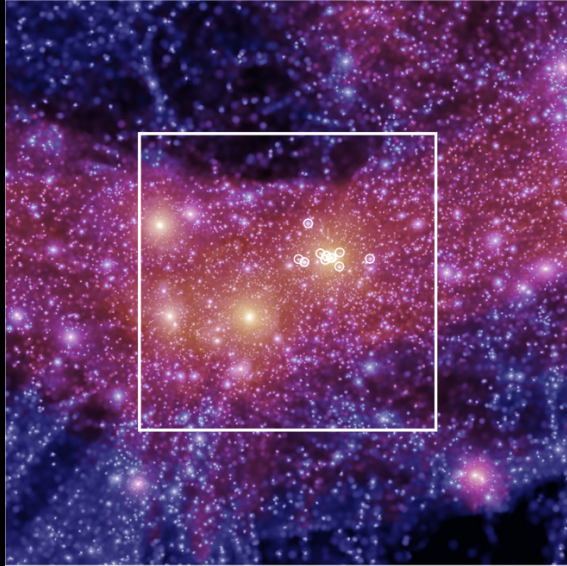
# The core-cusp problem

“Core-cusp” problem:

CDM & subhalos have **cuspy** profiles

**BUT:** kinematical data are said to “show” that the dwarf satellites of the Milky Way have **cores**





Dwarf galaxies in Eagle have NFW cusps!

Sawala et al '15





# Dwarf galaxies around the Milky Way

Many claims that dwarf spheroidal satellites have density cores

e.g. Gilmore et al. '07, Kuzio de Naray '08 and many more

Fornax

Sculptor

Leo I

© Anglo-Australian Observatory

Carina

Sextans

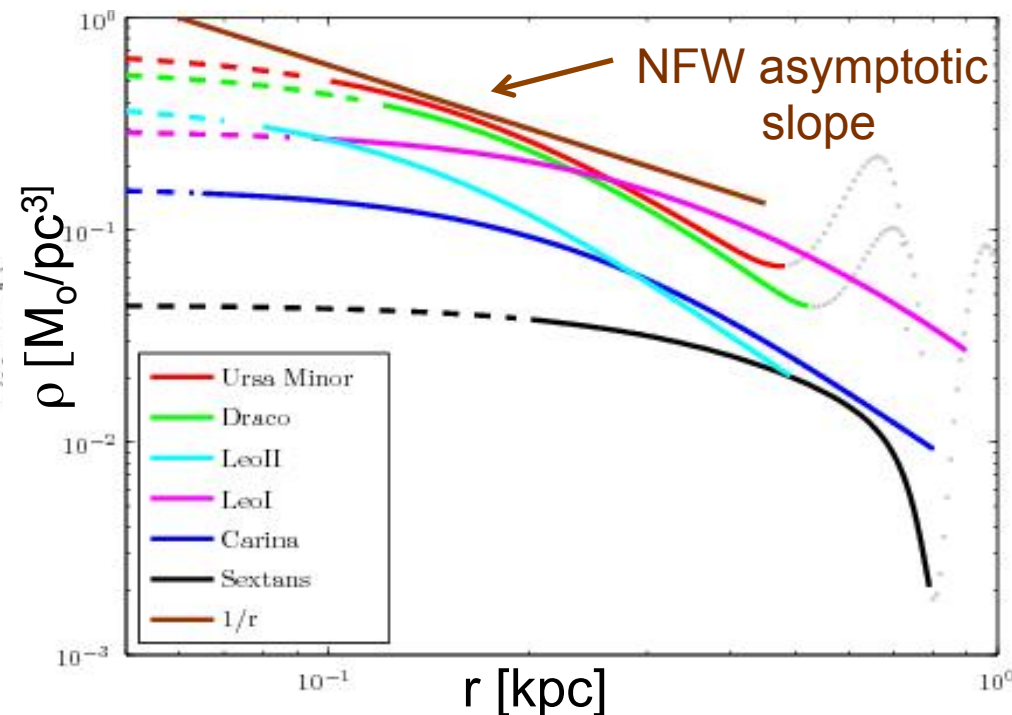
Sagittarius

# Evidence for warm dark matter?

THE ASTROPHYSICAL JOURNAL, 663:948–959, 2007 July 10

THE OBSERVED PROPERTIES OF DARK MATTER ON SMALL SPATIAL SCALES

GERARD GILMORE,<sup>1</sup> MARK I. WILKINSON,<sup>1,2</sup> ROSEMARY F. G. WYSE,<sup>3</sup> JAN T. KLEYNA,<sup>4</sup> ANDREAS KOCH,<sup>5,6</sup>  
N. WYN EVANS,<sup>1</sup> AND EVA K. GREBEL<sup>6,7</sup>



Inferred density profiles  
for 6 dwarf spheroidals

“...dark matter forms cored  
mass distributions, with a core  
scale length of greater than  
about 100pc, and always has a  
maximum central density in a  
narrow range...”

“...(keV) sterile neutrino particles have been discussed as relevant in just the  
spatial and density range we have derived here.”

# Dwarf sphs: cores or cusps?

Jeans eqn:

$$\frac{GM(r)}{r} = -\sigma_r^2 \left[ \frac{d \ln \rho_*}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right]$$

from Aquarius sim

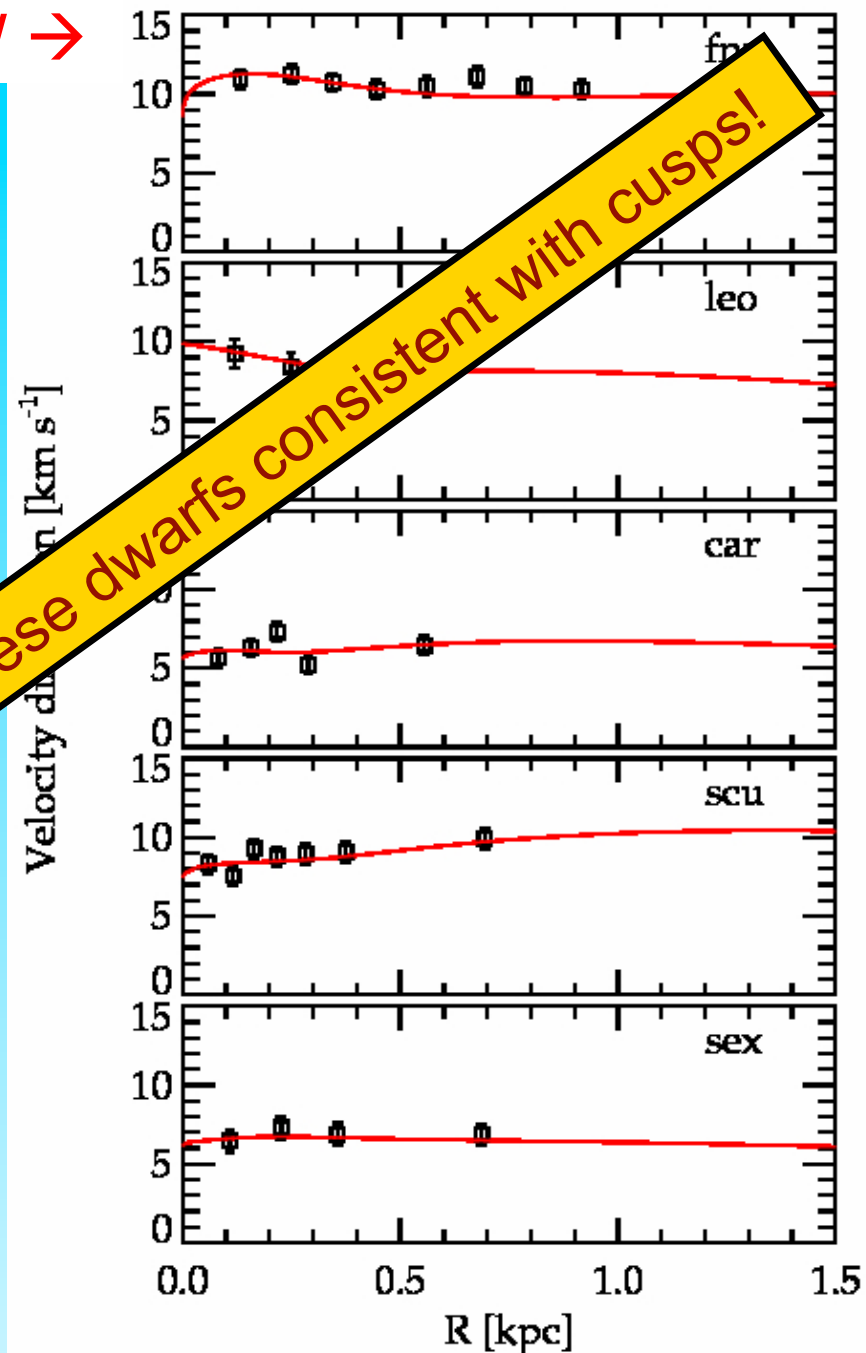
Cuspy!

vel. an...

- Assume isotropic
- Solve for
- Compare with observed  $\sigma_r(r)$
- "best fit" subhalo

Photometric and kinematical data for these dwarfs consistent with cusps!

Strigari, Frenk & White '10







# Dwarf galaxies around the Milky Way

Fornax

Sculptor

Leo I

© Anglo-Australian Observatory

Carina

Sextans

Sagittarius



# The DM halo of the Sculptor dwarf

Sculptor has two stellar pops:

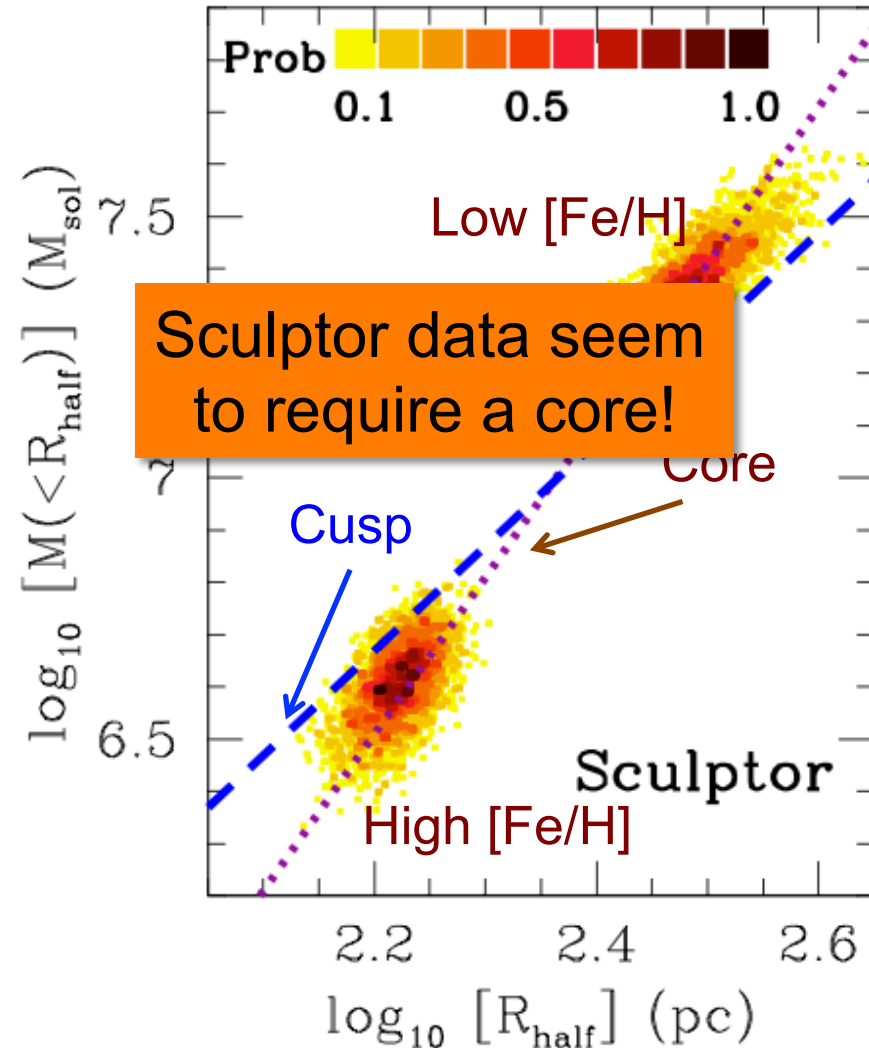
(i) centrally concentrated, high [Fe/H]

(ii) extended, low [Fe/H]

$$M(< r) = \mu \frac{r < \sigma_{los}^2 >}{G}$$

Walker '10; Wolf et al '10 →

if  $r=r_{1/2}$ ,  $\mu=2.5$ , independently of model assumptions!



# The DM halo of the Sculptor dwarf

Strigari, Frenk & White '14

Distribution function analysis of 2 metallicity pop. data of Battaglia et al.

Assume pops in equil. in NFW halo:  $\rho(r) = \frac{\rho_s}{x(1+x)^2}$

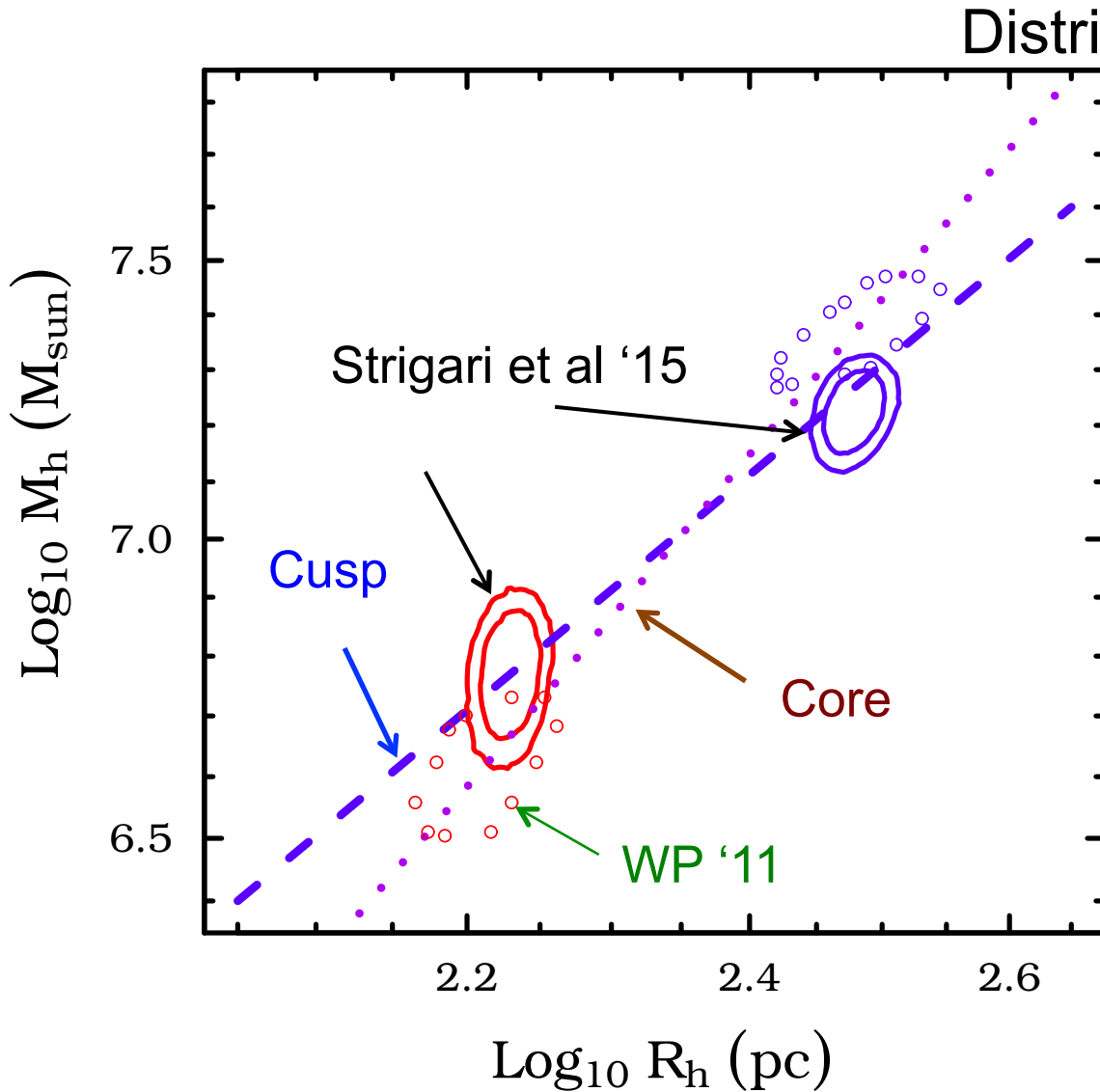
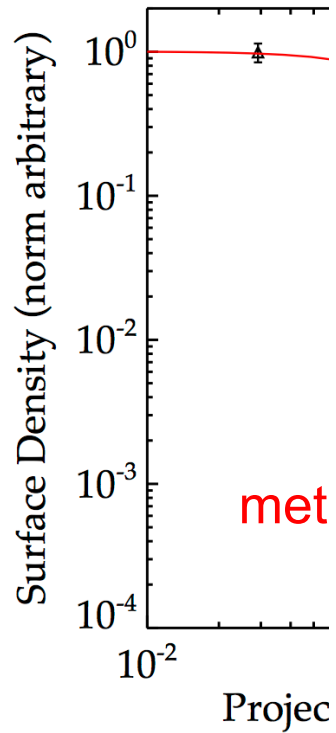
For each population:  $f(E, J) = g(J)h(E),$

Parametrize:  $g(J) = \left[ \left( \frac{J}{J_\beta} \right)^{\frac{b_0}{\alpha}} + \left( \frac{J}{J_\beta} \right)^{\frac{b_1}{\alpha}} \right]^\alpha$

$$h(E) = \begin{cases} N E^a (E^q + E_c^q)^{d/q} (\Phi_{lim} - E)^e & \text{for } E < \Phi_{lim} \\ 0 & \text{for } E \geq \Phi_{lim}, \end{cases}$$

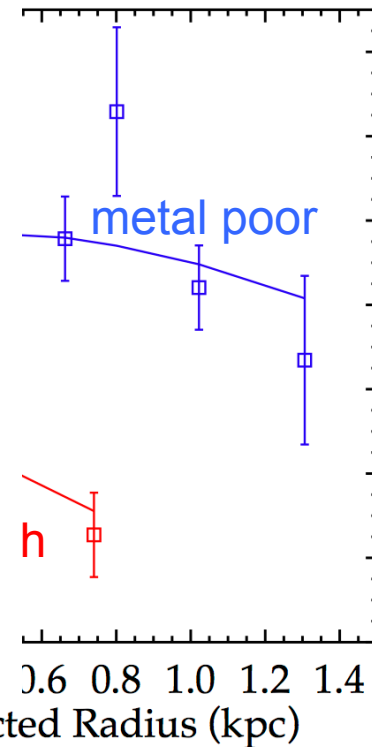
Find best-fit parameters using MCMC

# The DM halo of the Sculptor dwarf



Distribution function analysis

y dispersion



Data consistency

Strigari, Freeman & White (2015)



# Cores or cusps in the dwarf sph. satellites of the MW?

When sufficiently general models are considered, even best kinematical data cannot distinguish cores from NFW cusps in the dwarf spheroidal satellites of the Milky Way

How about in field dwarf galaxies?

Data are not as detailed, but some dwarfs have disks:

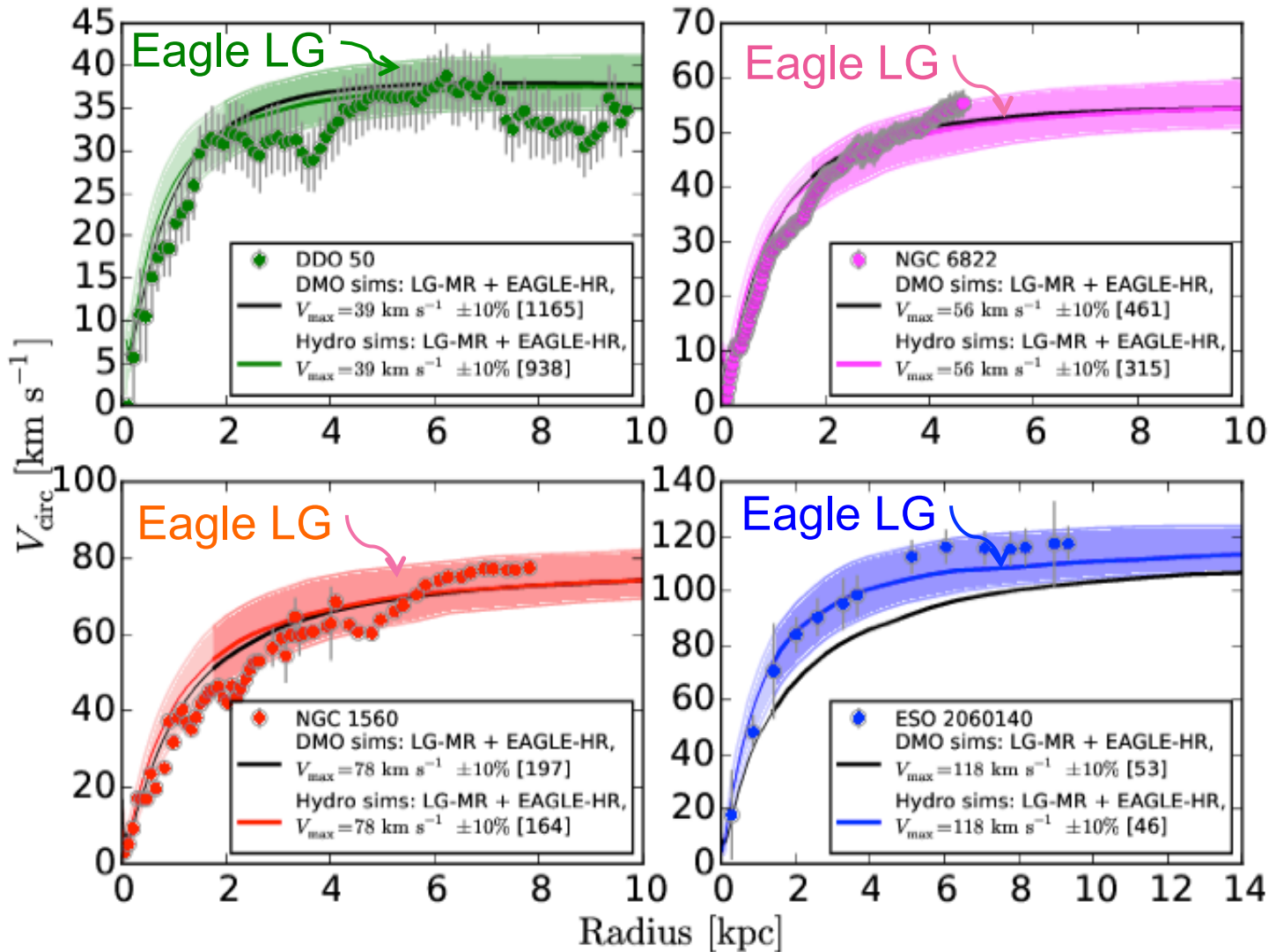
- (i) Rotation curves
- (ii) 2D velocity fields



# The diversity of gal rotation curves

Four rotation curves that are well fit by  $\Lambda$ CDM

(from dwarfs to  $\sim L_*$ )

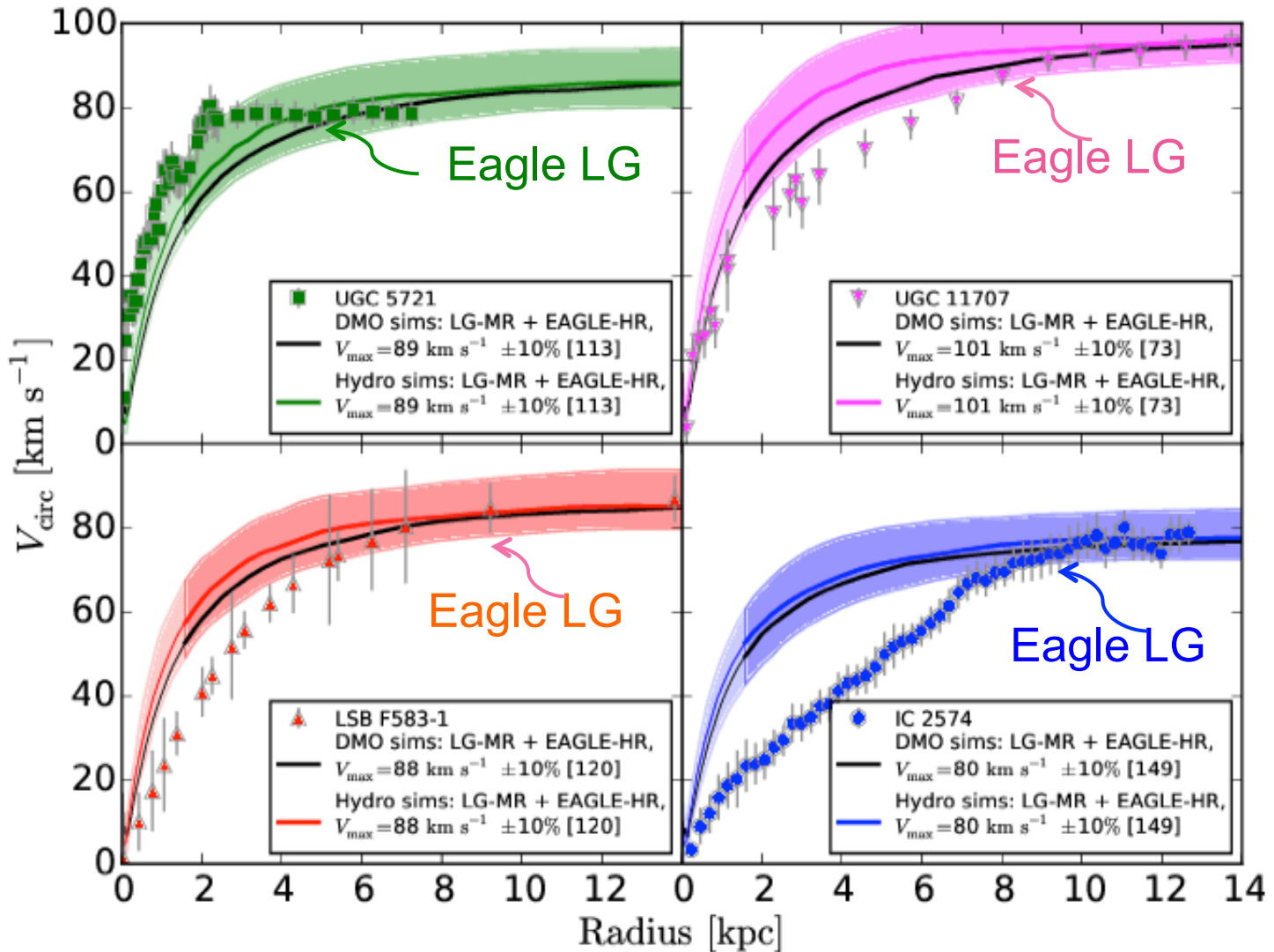


Oman, Navarro, Frenk et al. '15

# The diversity of gal rotation curves

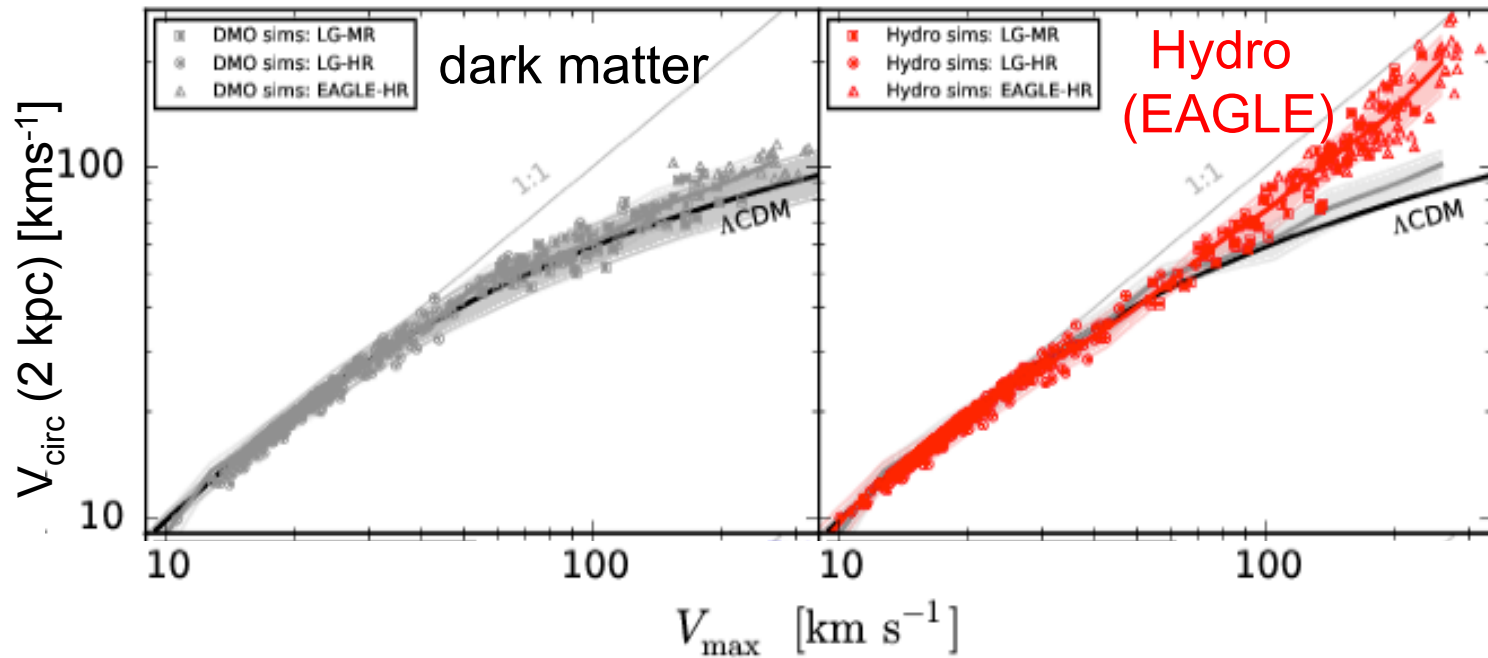
Four rotation curves that are NOT well fit by  $\Lambda$ CDM

(from dwarfs to  $\sim L_*$ )



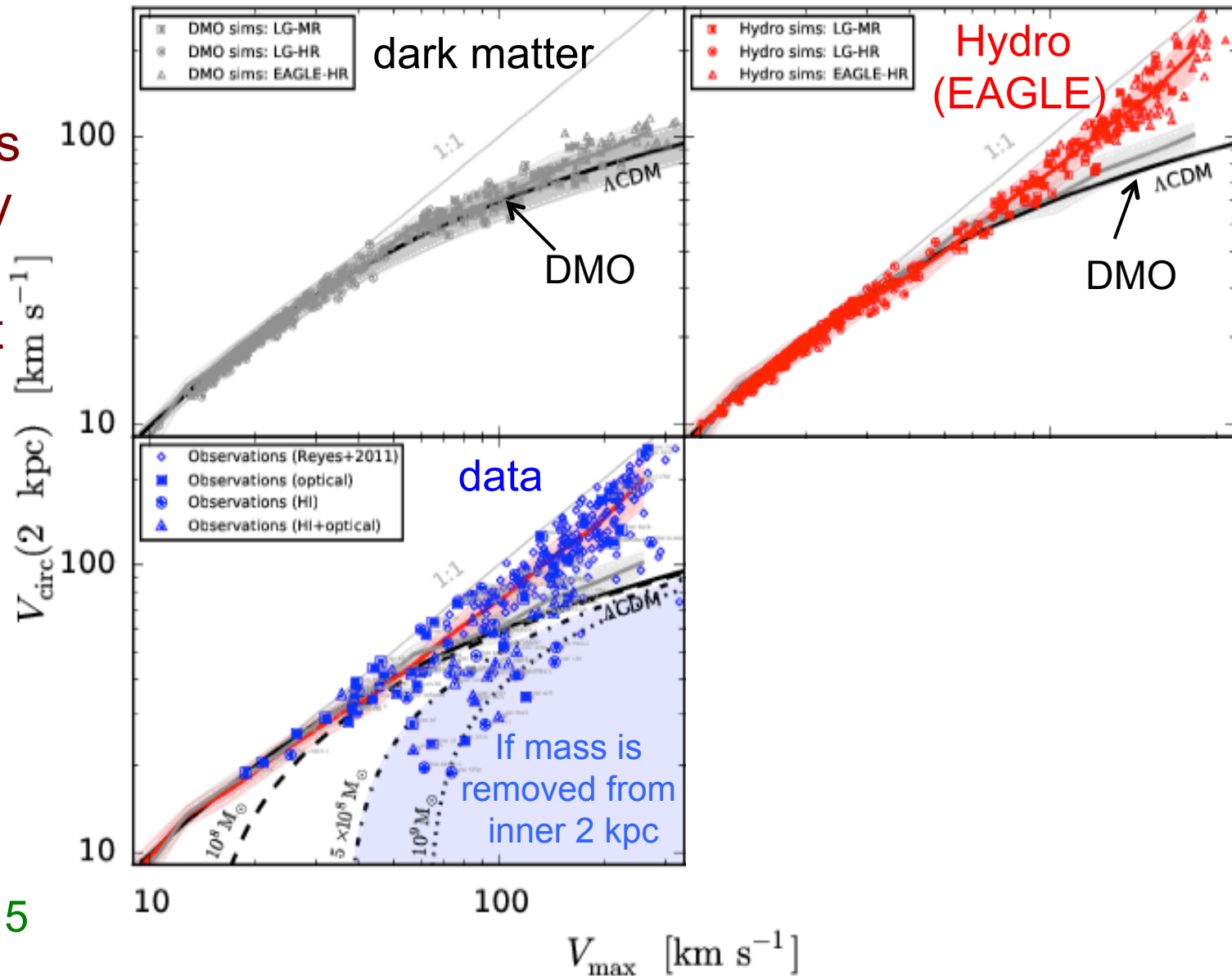
Oman et al. '15

# The diversity of gal rotation curves



# The diversity of gal rotation curves

Most galaxies are well fit by EAGLE; others not fit by any simulation







Are there other baryon effects that could make cores but are not present in Eagle?

## The cores of dwarf galaxy haloes

Julio F. Navarro,<sup>1,2★</sup> Vincent R. Eke<sup>2</sup> and Carlos S. Frenk<sup>2</sup>

<sup>1</sup>*Steward Observatory, The University of Arizona, Tucson, AZ 85721, USA*

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Accepted 1996 September 2. Received 1996 August 28; in original form 1996 June 26

### ABSTRACT

We use  $N$ -body simulations to examine the effects of mass outflows on the density profiles of cold dark matter (CDM) haloes surrounding dwarf galaxies. In particular, we investigate the consequences of supernova-driven winds that expel a large fraction of the baryonic component from a dwarf galaxy disc after a vigorous episode of star formation. We show that this sudden loss of mass leads to the formation of a core in the dark matter density profile, although the original halo is modelled by a coreless (Hernquist) profile. The core radius thus created is a sensitive function of the mass and radius of the baryonic disc being blown up. The loss of a disc with mass and size consistent with primordial nucleosynthesis constraints and angular momentum considerations imprints a core radius that is only a small fraction of the original scalelength of the halo. These small perturbations are, however, enough to reconcile the rotation curves of dwarf irregulars with the density profiles of haloes formed in the standard CDM scenario.

Let gas cool and condense to the galactic centre

→ gas self-gravitating  
→ star formation/burst

Rapid ejection of gas during starburst → a core in the halo dark matter density profile

Navarro, Eke, Frenk '96

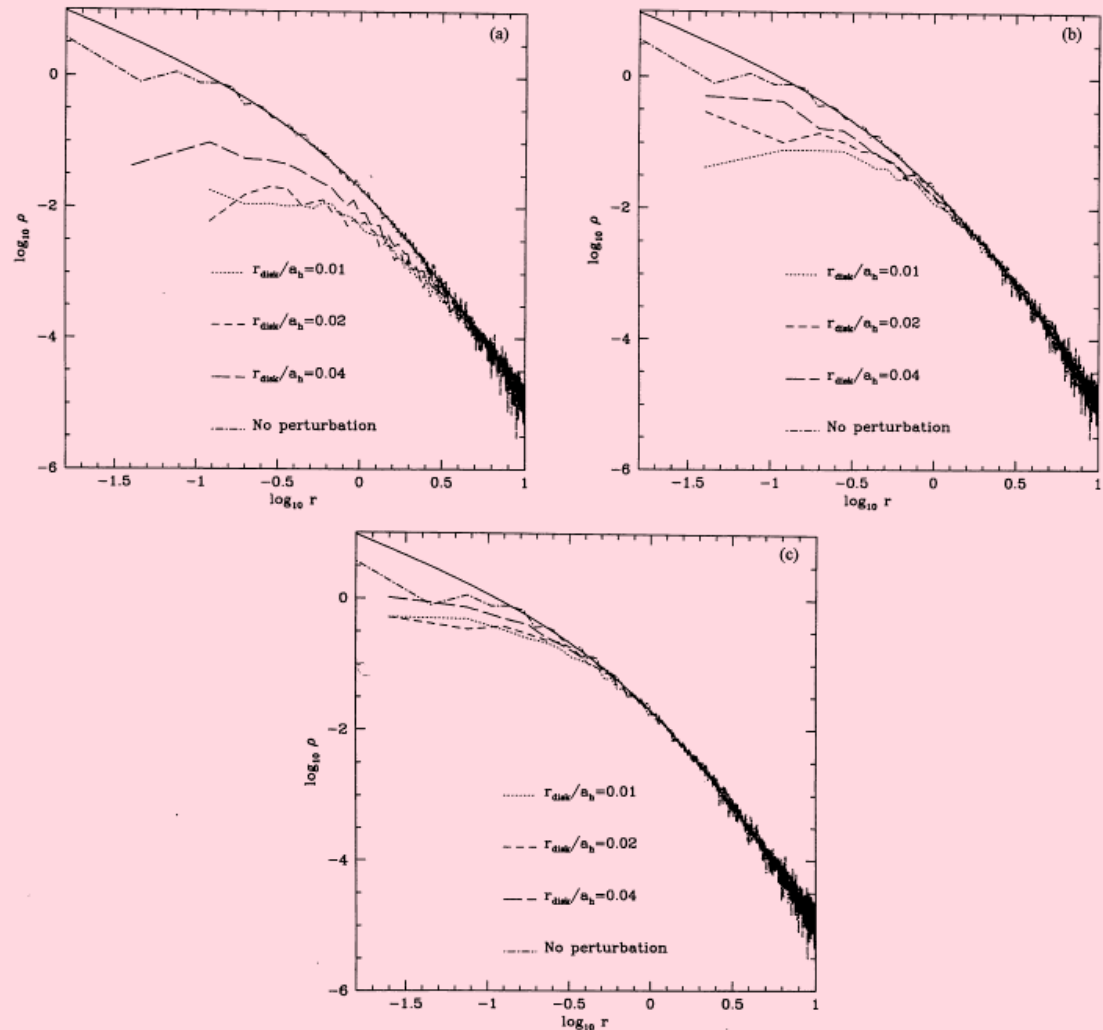
Governato et al. '12

Pontzen & Governato '12

Brooks et al. '12

Navarro, Eke, Frenk '96

*The cores of dwarf galaxy haloes* L75



**Figure 3.** Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10 000-particle realization of the Hernquist model run in isolation at  $t=200$ . (a)  $M_{\text{disc}}=0.2$ . (b)  $M_{\text{disc}}=0.1$ . (c)  $M_{\text{disc}}=0.05$ .

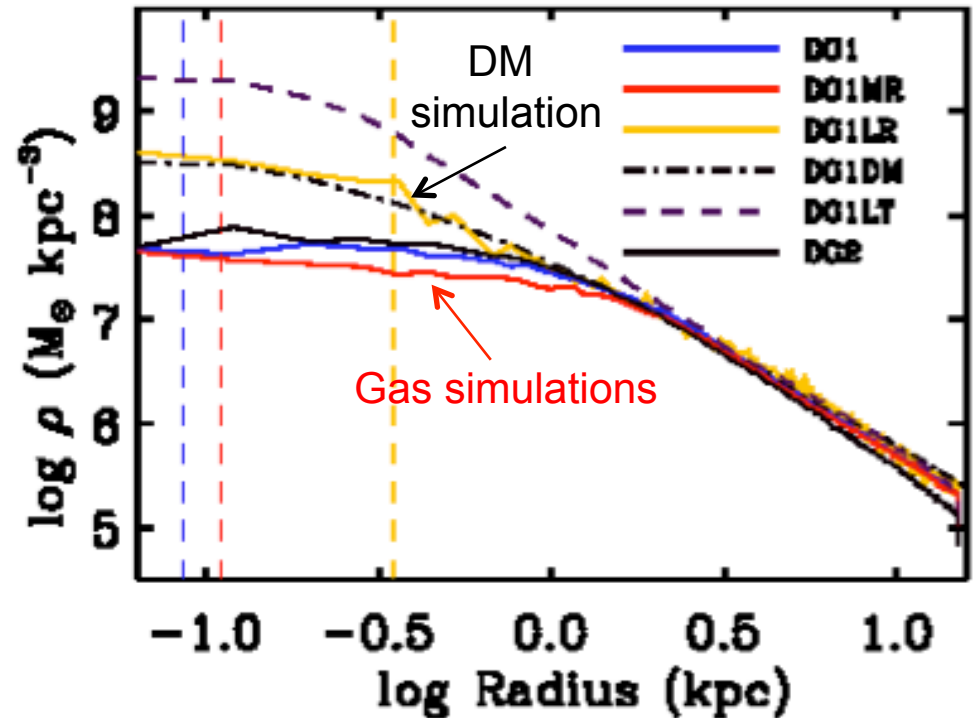
# Cores in dwarf galaxy simulations

Governato et al. assume  
high density threshold for  
star formation.

EAGLE does not

→ High threshold allows  
large gas mass to  
accumulate in centre

→ Sudden repeated  
removal of gas transfers  
binding energy



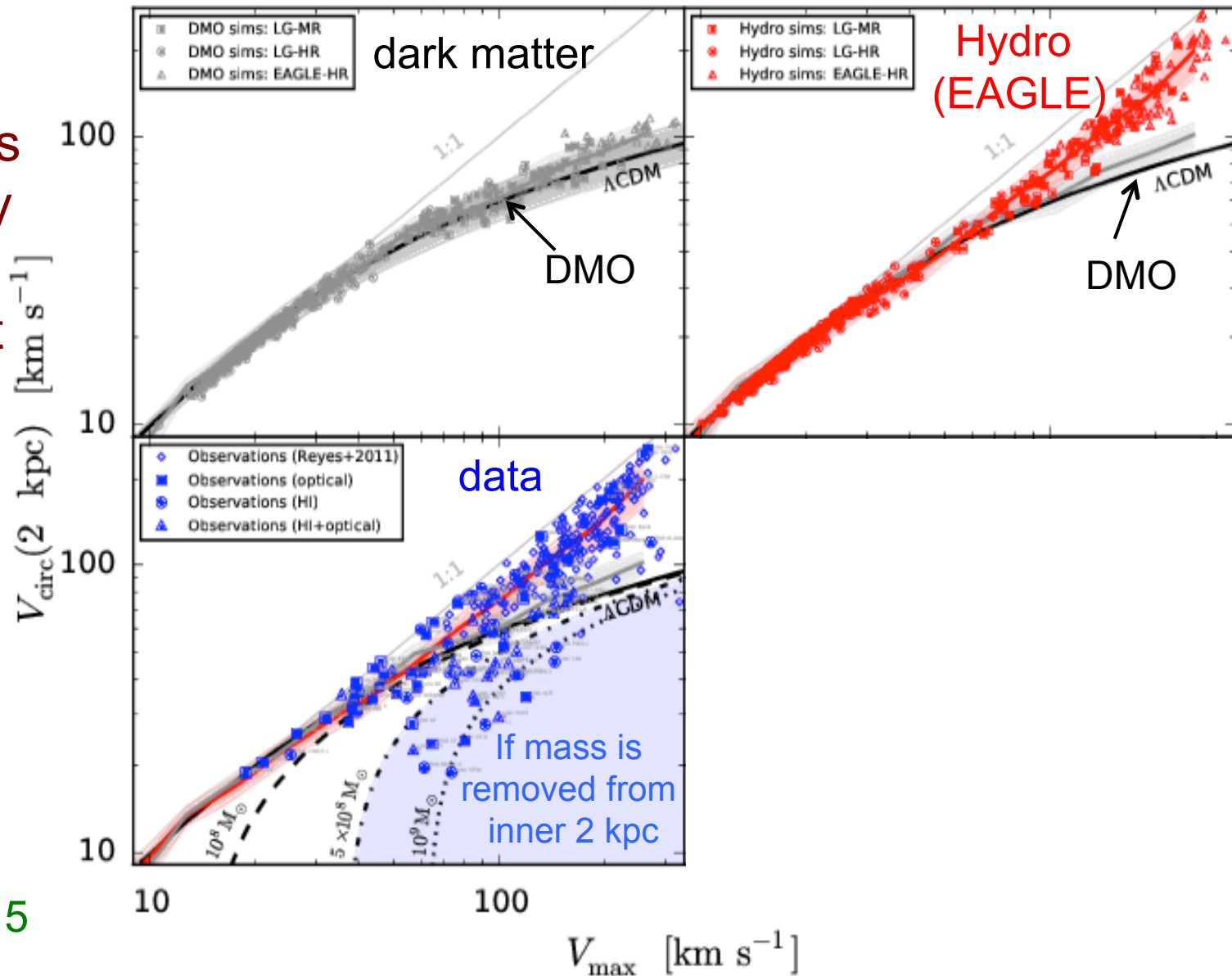
Governato et al. '10

Pontzen et al. 2011



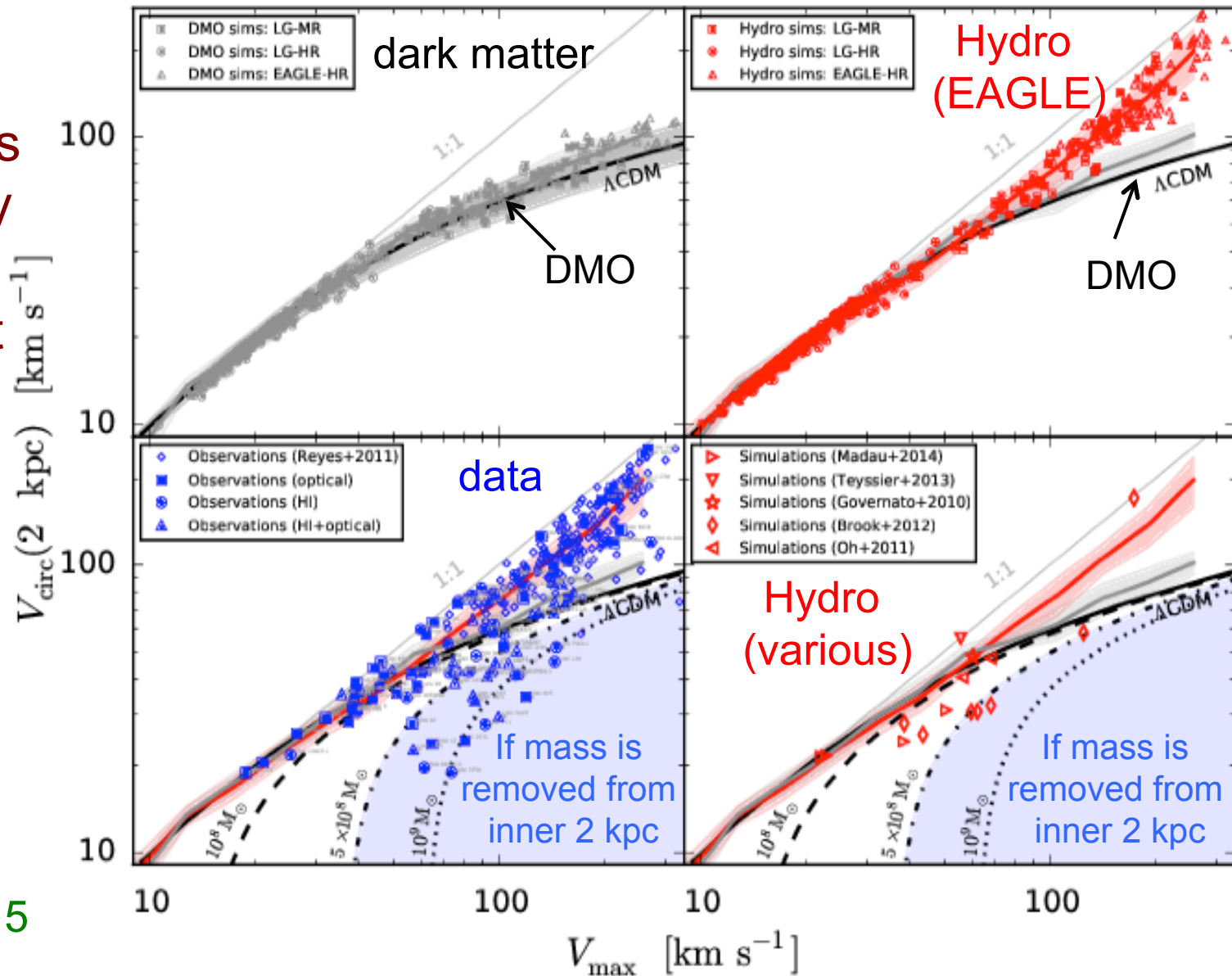
# The diversity of gal rotation curves

Most galaxies are well fit by EAGLE; others not fit by any simulation



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# Cores or cusps in dwarf gals?

- Some dwarfs have rotation curves that agree well with EAGLE
- Others have inner mass deficits compared to  $\Lambda$ CDM expectation
- In many cases, inner deficit much larger than seen in simulations that make cores

EITHER (i) dark matter more complex than in any current model

OR (ii) current simulations fail to reproduce effects of baryons on inner regions of dwarfs

AND/OR (iii) the mass profiles of “inner mass deficit” galaxies inferred from kinematic data are incorrect.

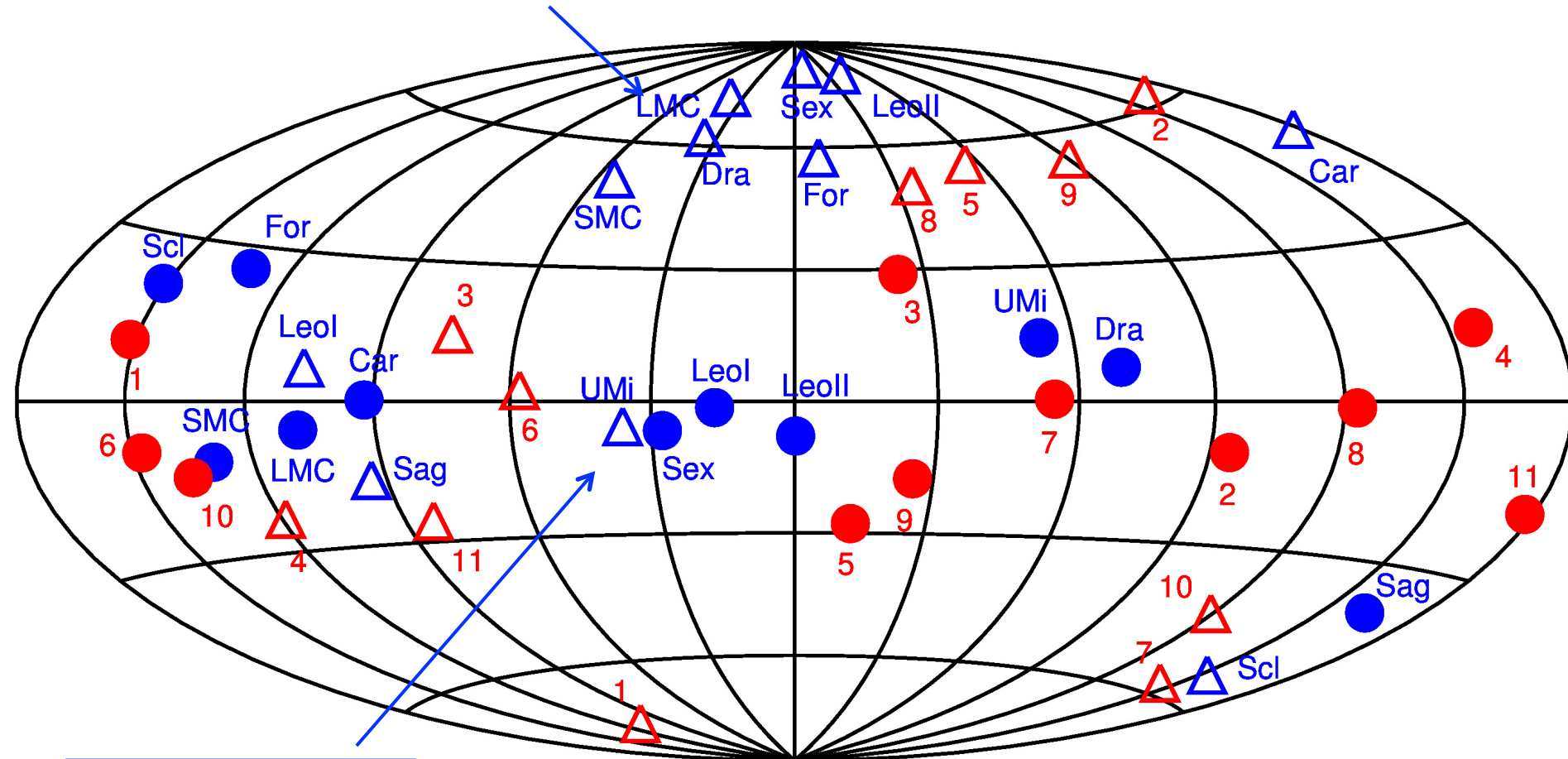
# Four problems for CDM on small scales?

1. The “missing satellites” problem
2. The “too-big-to-fail” problem
3. The “core-cusp” problem
4. The “satellite disk” problem



# The “satellite disk” problem

Direction of ang. mom. Milky Way

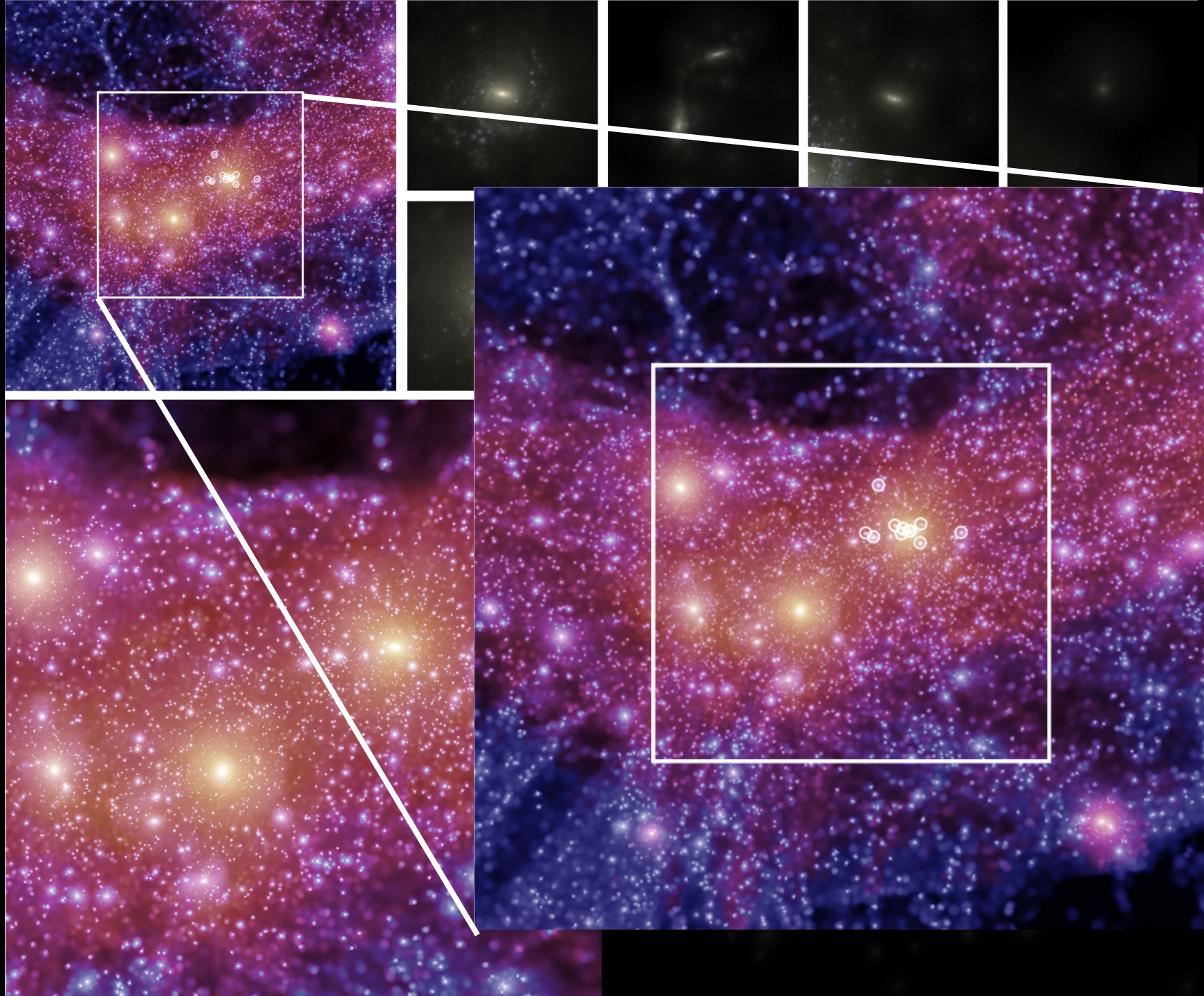


MW satellites

Lynden-Bell '76

Sawala et al '15

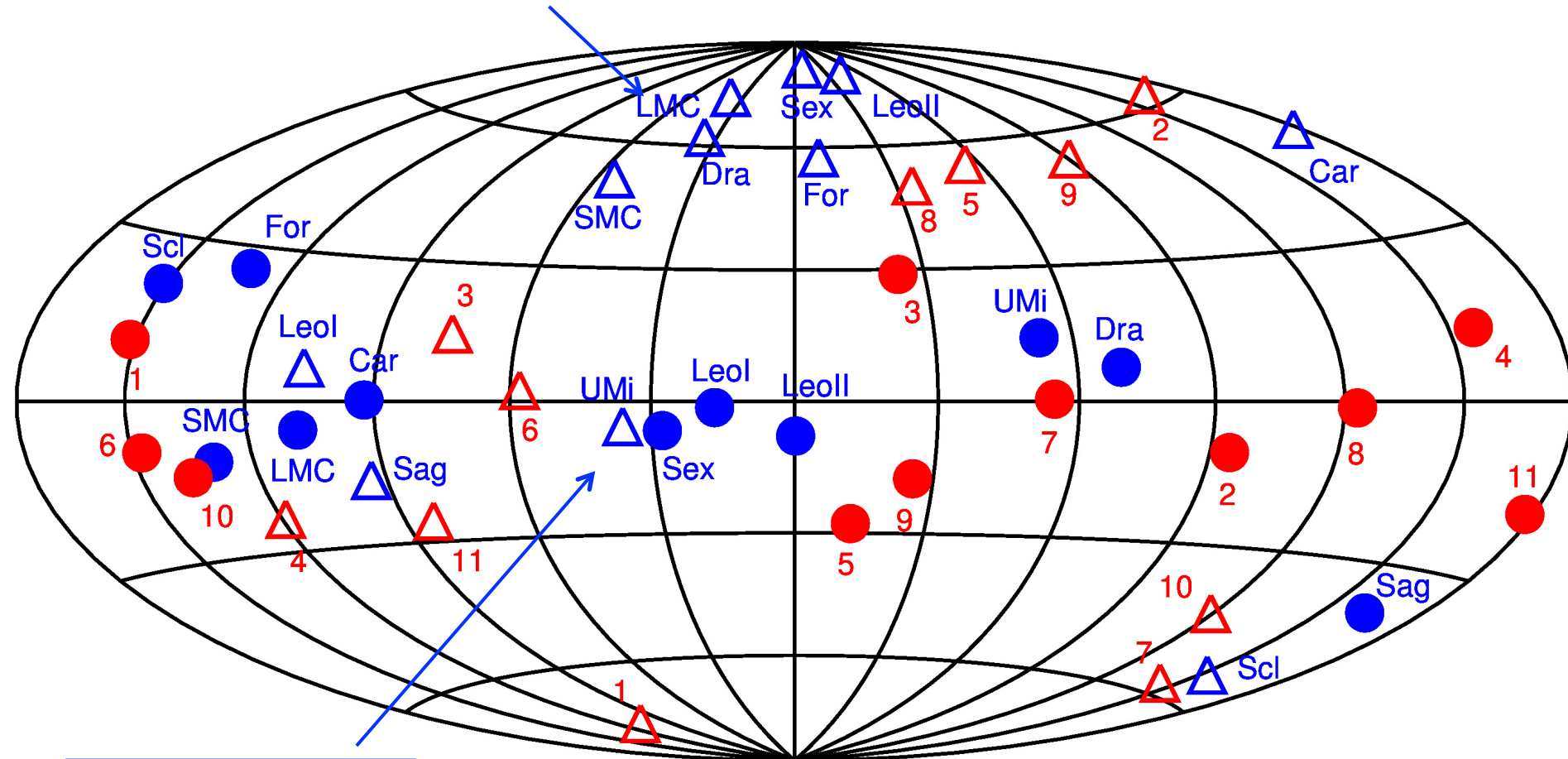
Institute for Computational Cosmology





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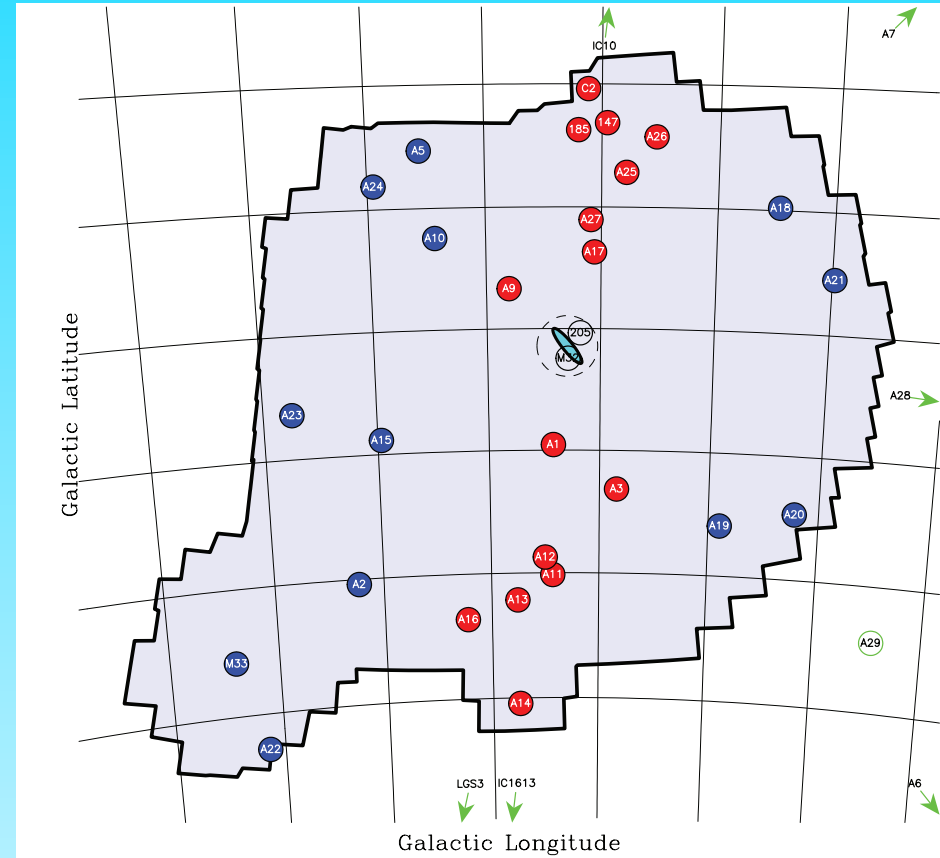
Institute for Computational Cosmology

# The curious case of a thin, “rotating” plane of sats in M31

Ibata et al ‘13 found a **plane** of **15 satellites** in Andromeda (out of 27) of which **13** have the same sense of **rotation**

They claim a  **$4.3\sigma$  detection**

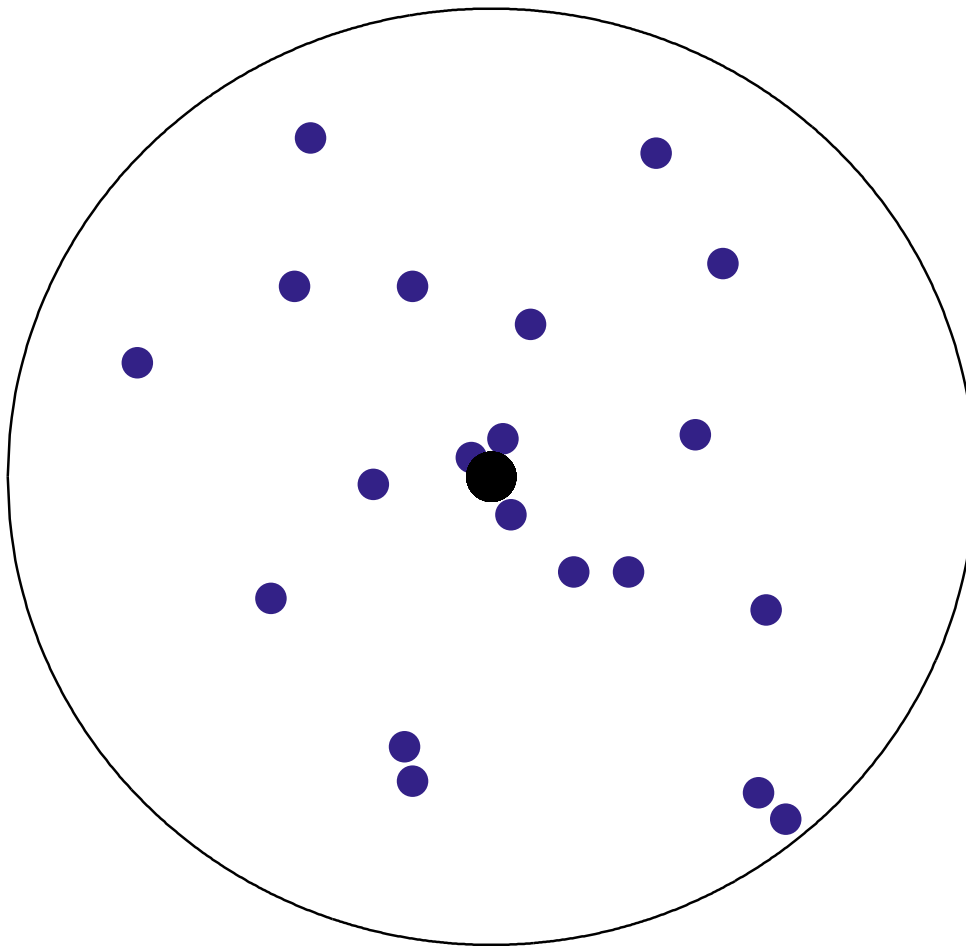
“We find that **0.04%** of host galaxies [in **Millennium II**] display satellite alignments that are at least as extreme as the observations, when we consider their extent, thickness, and number of members rotating in the same sense.”



Ibata et al ‘13

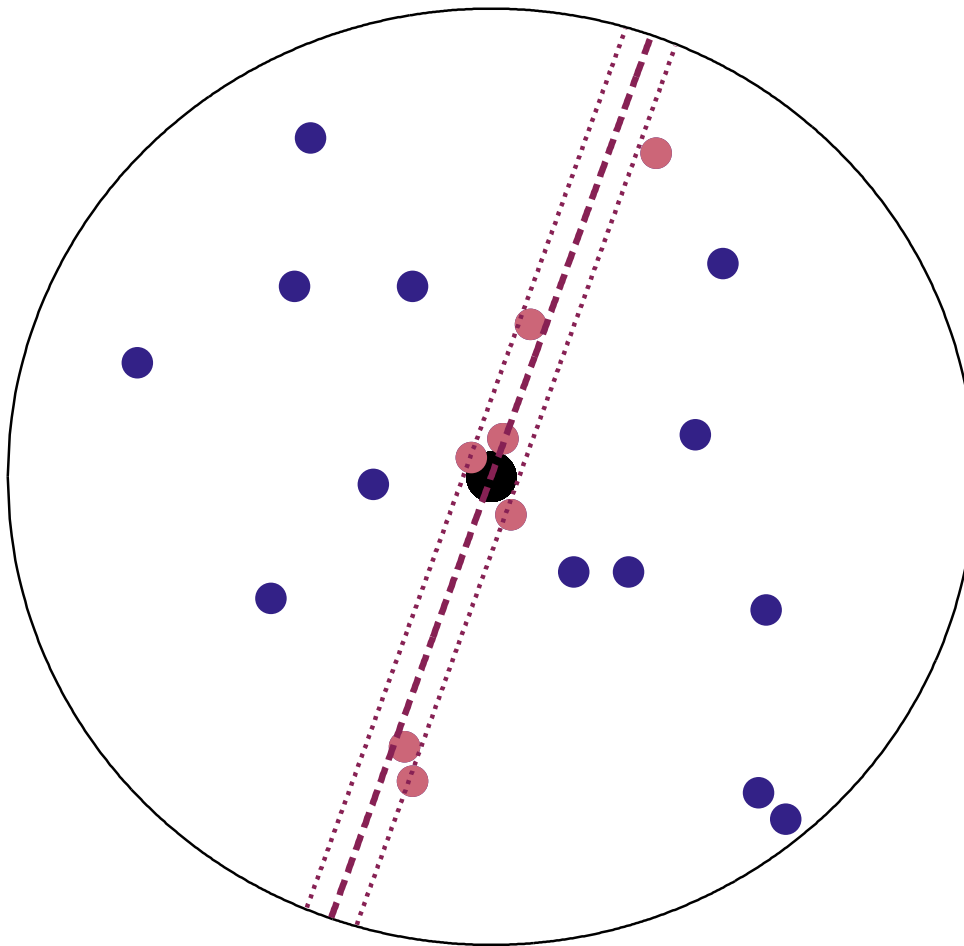


# Finding disks of satellites



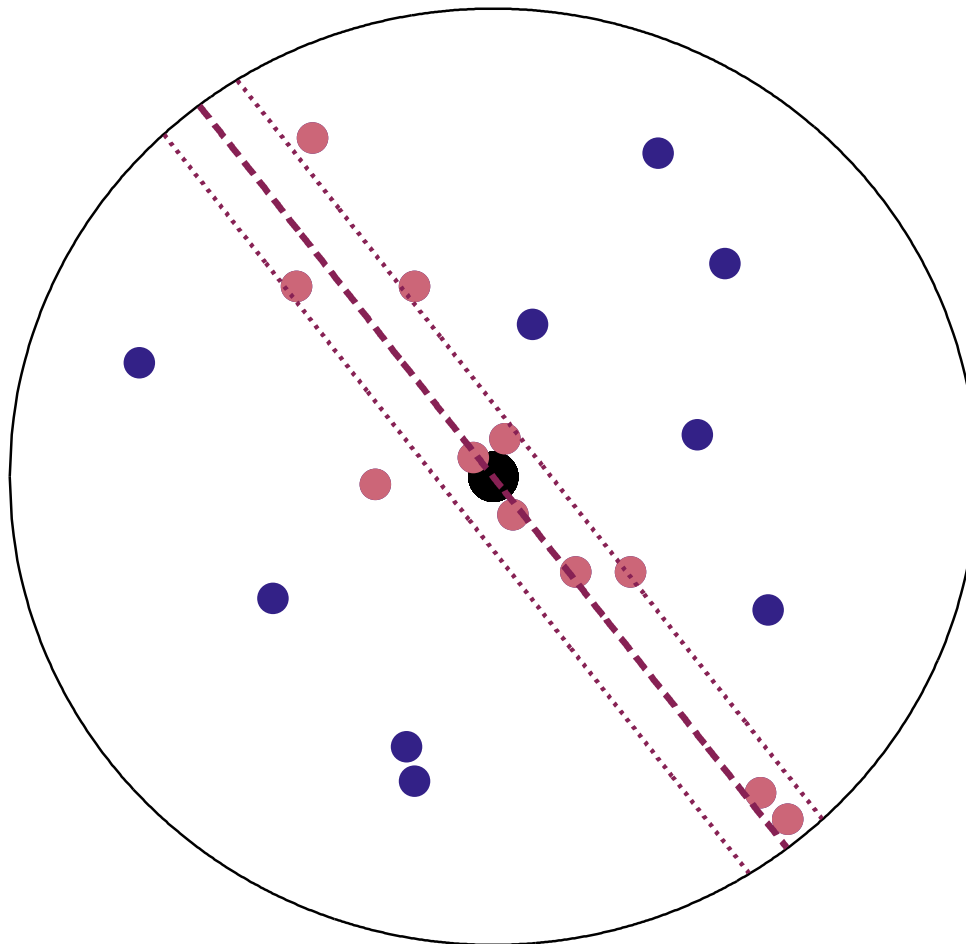
# Finding disks of satellites

Plane 1:  $N_{\text{sat}} = 7$ ,  $\mathcal{P} = 410$



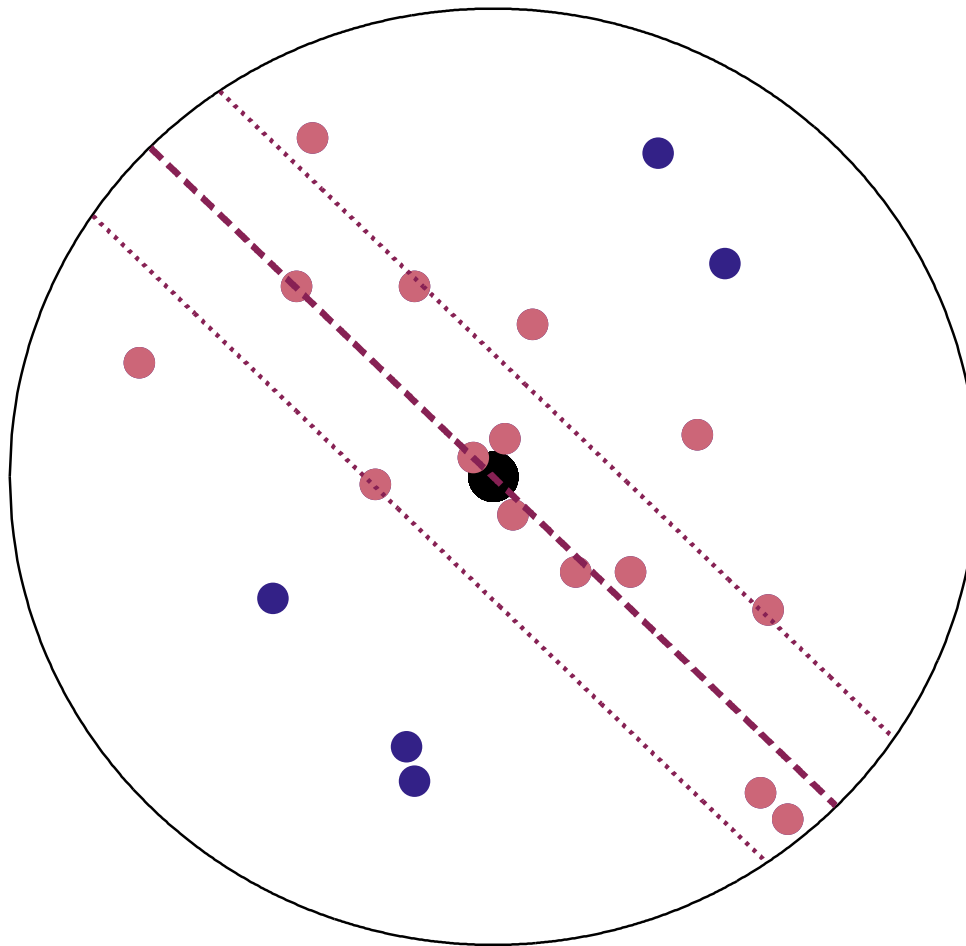
# Finding disks of satellites

Plane 2:  $N_{\text{sat}} = 11$ ,  $\mathcal{P} = 660$



# Finding disks of satellites

Plane 3:  $N_{\text{sat}} = 15$ ,  $\mathcal{P} = 450$





# The “satellite disk” problem

Prominence of a plane =  $\frac{1}{\text{Probability of finding plane in random distr}}$

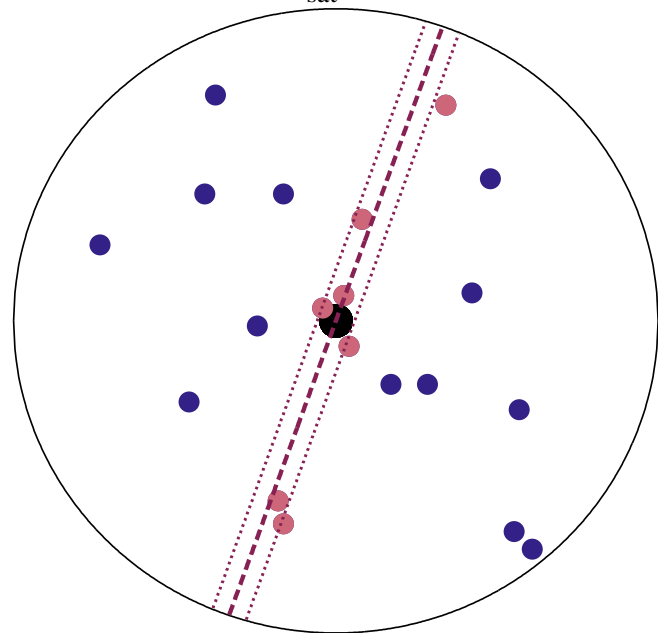
Prominence of plane thinner than  $r_{\perp}$  having  $N_{\text{sat}}$  galaxies  $\mathcal{P}_{\text{spatial}}^{\text{plane } i} = \frac{1}{p(\leq r_{\perp}; i \mid N_{\text{sat}; i})}$

Prominence of plane of  $N_{\text{sat}}$  gals,  $N$  same sense of rotation  $\mathcal{P}_{2\text{D-kin}}^{\text{plane } i} = \frac{1}{p(\geq N_{\text{s.s.r.}; i} \mid N_{\text{sat}; i})}$

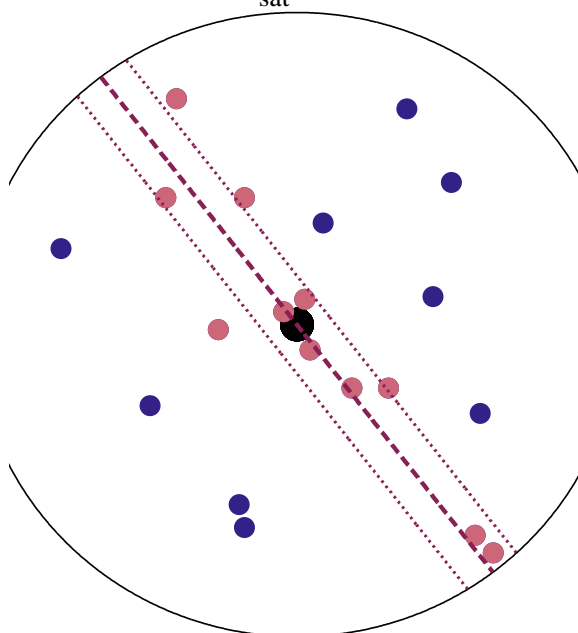
$$\mathcal{P}_{\text{spatial}}^{\text{rarest}} = \max_{\text{all planes } i} \left[ \mathcal{P}_{\text{spatial}}^{\text{plane } i} \right] ;$$

# Finding disks of satellites

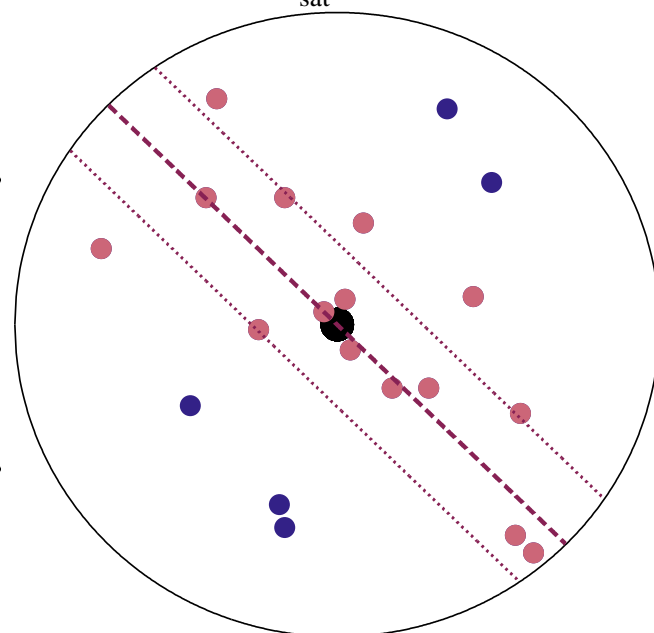
Plane 1:  $N_{\text{sat}} = 7$ ,  $\mathcal{P} = 410$



Plane 2:  $N_{\text{sat}} = 11$ ,  $\mathcal{P} = 660$



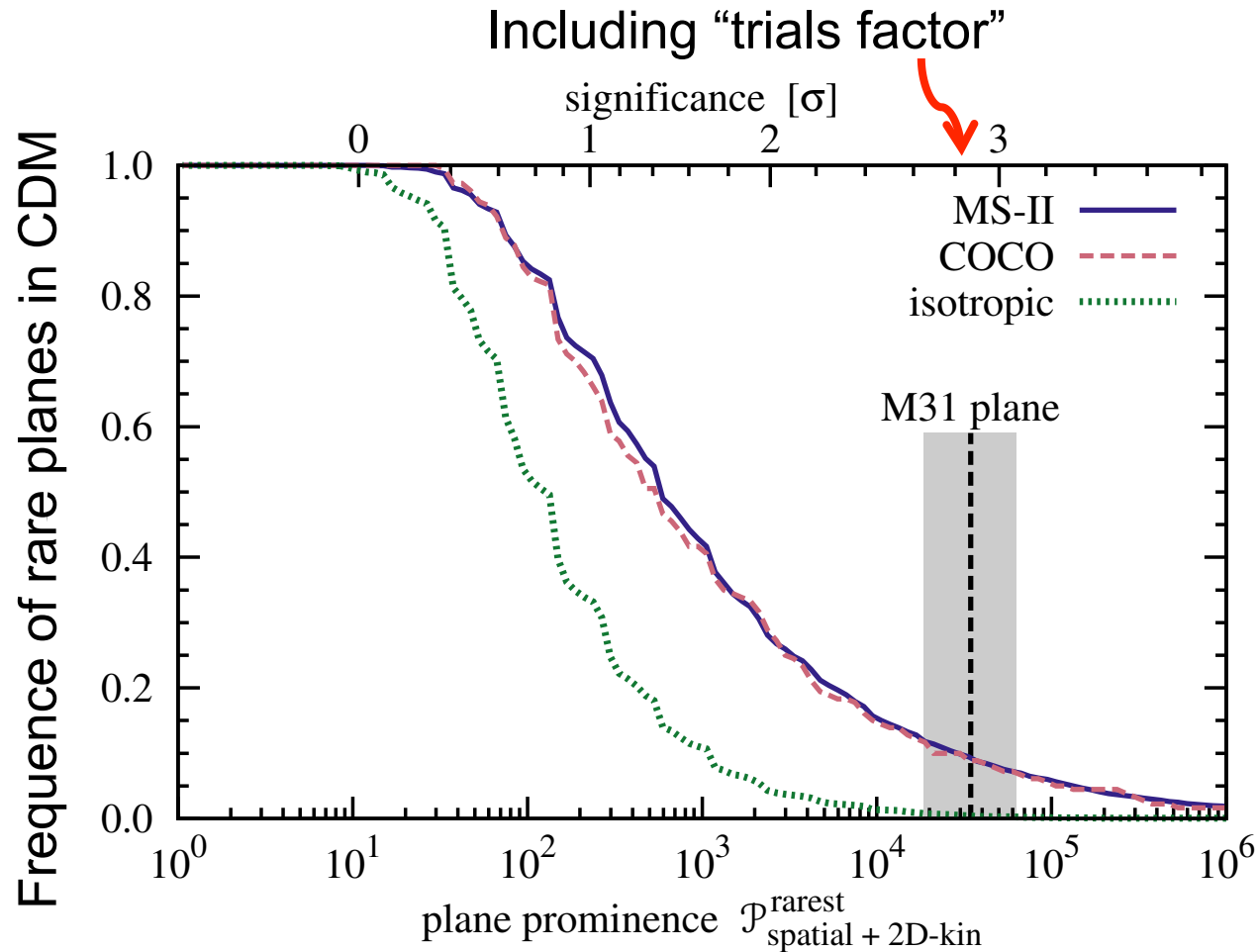
Plane 3:  $N_{\text{sat}} = 15$ ,  $\mathcal{P} = 450$



Cautun, Bose, Frenk et al '15

# The significance of Ibata's plane

- Significance of Ibata's plane is reduced by x100 when trials factor is included
- 8.8% of halos in  $\Lambda$ CDM simulation have even more prominent disks than Ibata's



1 in 30,000 chance of finding a plane of 15 sats (out of 27) as thin as the one found by Ibata et al., with at least 13 having the same sense of rotation

Cautun et al '15



Is there a “satellite disks problem” in CDM?

No, when statistics are properly calculated

Satellite planes are v. common in  $\Lambda$ CDM: 5 & 9% of halos have even more prominent planes than Milky Way and Andromeda





# Conclusions

- $\Lambda$ CDM: great **success** on scales  $> 1\text{Mpc}$ : CMB, LSS, gal evolution

Four “problems” on small scales:

1. Abundance of sats
2. Too-big-to-fail
3. Core-cusp
4. Disk of satellites



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- But on these scales  **$\Lambda$ CDM** cannot be distinguished from **WDM**
- The **identity** of the DM makes a big difference on **small scales**

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1. Abundance of sats: simply galaxy formation!
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3. Core-cusp: **No** evidence for cores in satellites; (Baryon effects?)
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# Conclusions

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- The **identity** of the DM makes a big difference on **small scales**

Four “problems” on small scales:

1. Core-cusp: **Not** a problem? (Baryon effects?)
2. Abundance of sats: **CDM** OK; **WDM** OK if  $m_{\text{WDM}} > 3\text{ KeV}$
3. Too-big-to-fail: **CDM**, **WDM** OK
4. Disk of satellites: **CDM**, **WDM** OK