



The status of cold dark matter

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Durham

... and how to rule it out

The new Ogden
Centre at Durham



The big Bang



The cosmic microwave background is emitted
($t \sim 350,000$ yrs)

Production of
particle dark matter
($t \sim 10^{-10}$ s)

The first
light in our
Universe

$t = 13.7$ billion yrs

Cosmic inflation
(initial conditions)
($t \sim 10^{-35}$ s)

- radiation
- particles
- W^+ heavy particles carrying the weak force
- W^-
- Z
- quark
- anti-quark
- electron
- positron (anti-proton)
- neutron
- meson
- hydrogen
- deuterium
- helium
- lithium

15 thousand million years

300 tho

3 minutes

10^{-43} seconds

10^{32} degrees

10^{27} degrees

10^{15} degr

degrees

18 degrees

3 degrees K

The big Bang



300 thousand

3 minutes

15 thousand million years

The temperature of this radiation should show small irregularities

Production of particle dark matter
($t \sim 10^{-10}$ s)

10^{-43} seconds

10^{32} degrees

10^{27} degrees

10^{15} degrees

1 degrees

18 degrees

3 degrees K

$t = 13.7$ billion yrs

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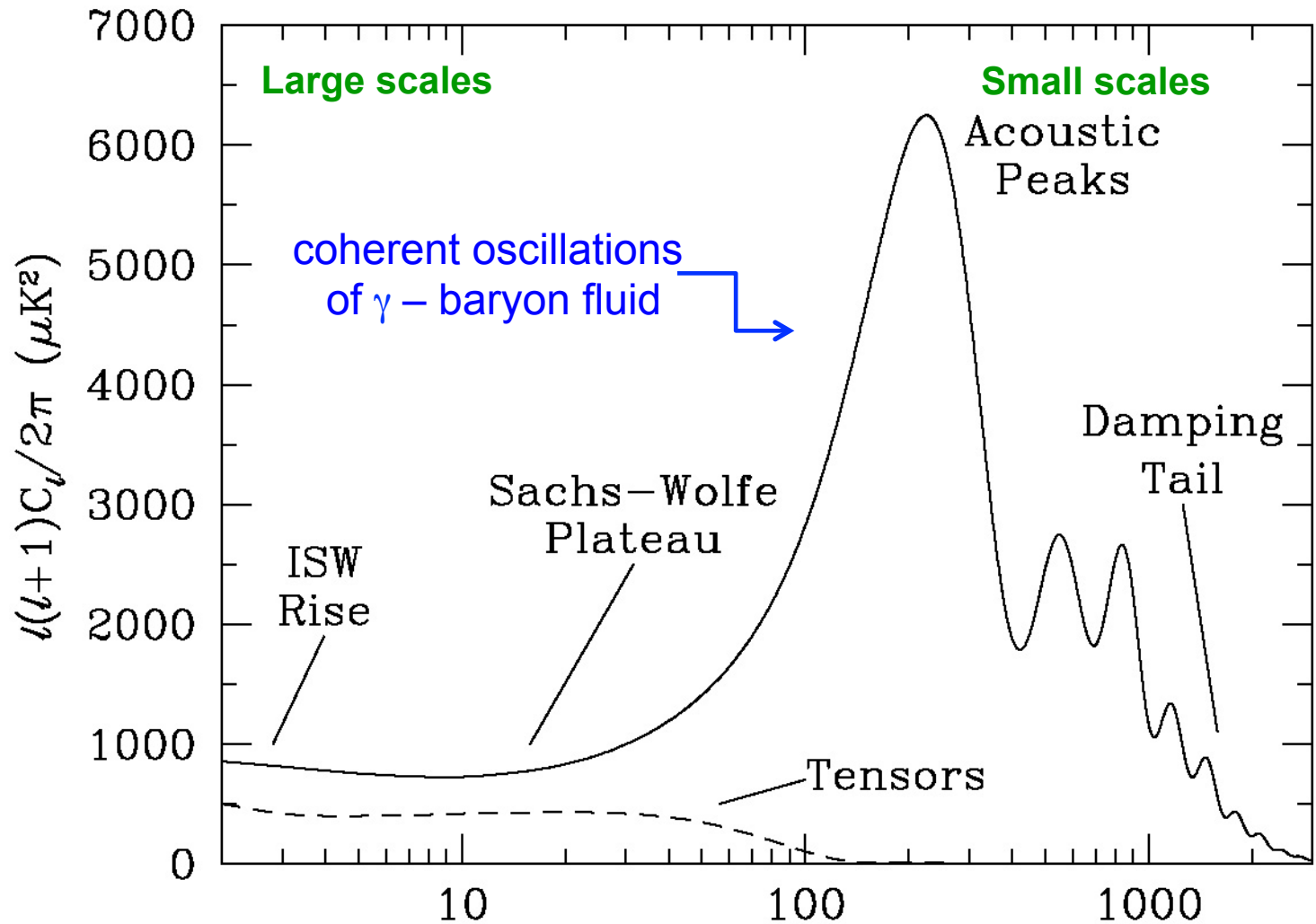
The initial conditions for galaxy formation



Quantum fluctuations from inflation

Temperature anisotropies in CMB

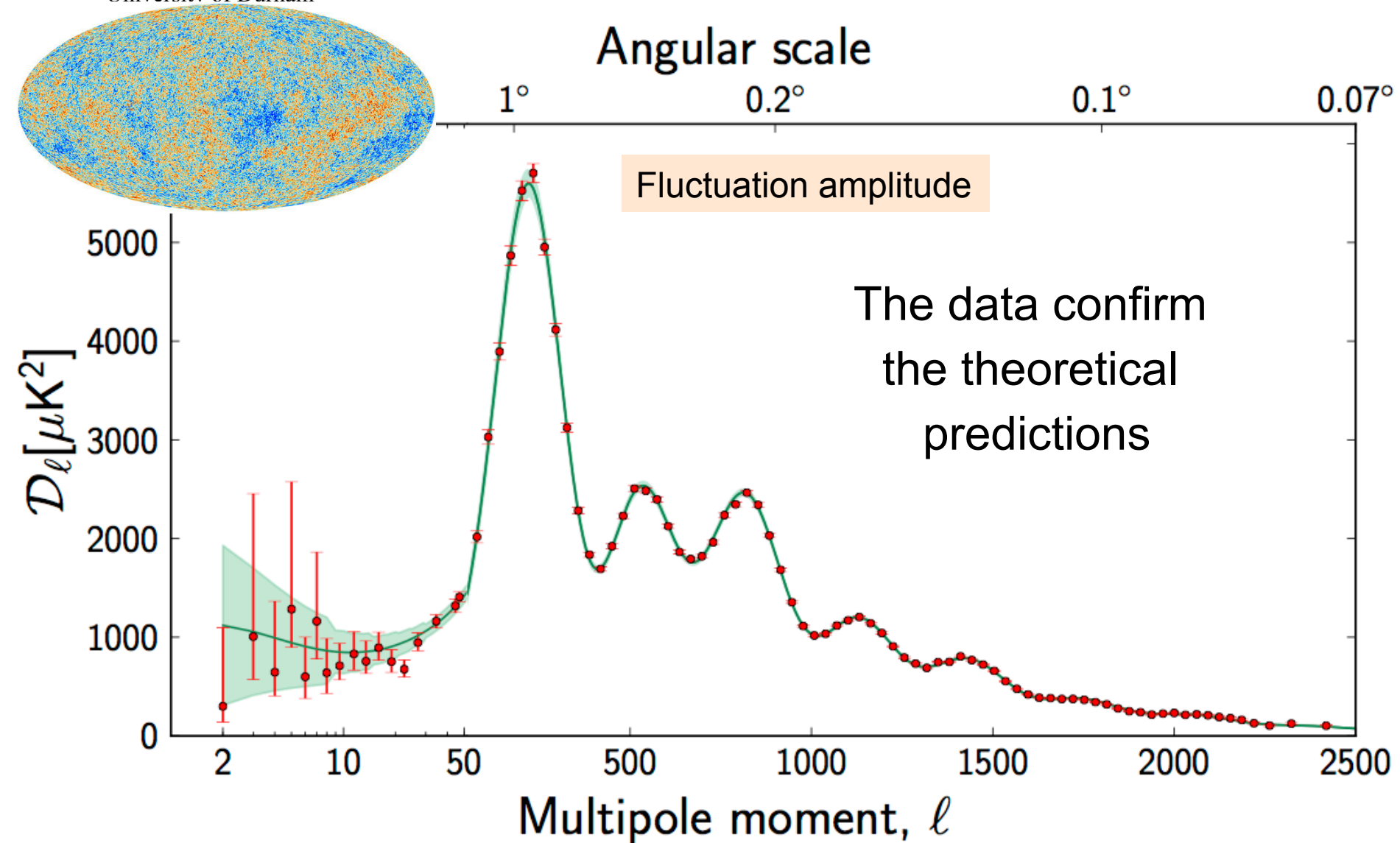
2D power spectrum



Peebles & Yu '70 Sunyev & Zel'dovich '70

For CDM: Peebles '82; Bond & Efstathiou '84

Planck: CMB temperature anisotropies



The six parameters of minimal Λ CDM model

		<i>Planck</i> +WP	
Parameter		Best fit	68% limits
6 model parameters	$\Omega_b h^2$	0.022032	0.02205 ± 0.00028
	$\Omega_c h^2$	0.12038	0.1199 ± 0.0027
	$100\theta_{MC}$	1.04119	1.04131 ± 0.00063
	τ	0.0925	$0.089^{+0.012}_{-0.014}$
	n_s	0.9619	0.9603 ± 0.0073
	$\ln(10^{10} A_s)$	3.0980	$3.089^{+0.024}_{-0.027}$

A 40σ detection of non-baryonic dark matter using only $z=1000$ data!

Non-baryonic dark matter candidates

From the 1980s:

Type	example	mass
hot	neutrino	few tens of eV
warm	sterile ν	keV-MeV
cold	axion neutralino	$10^{-5}\text{eV} - 100 \text{ GeV}$

The dark matter power spectrum

$k^3 P(k)$

The linear power spectrum (“power per octave”)

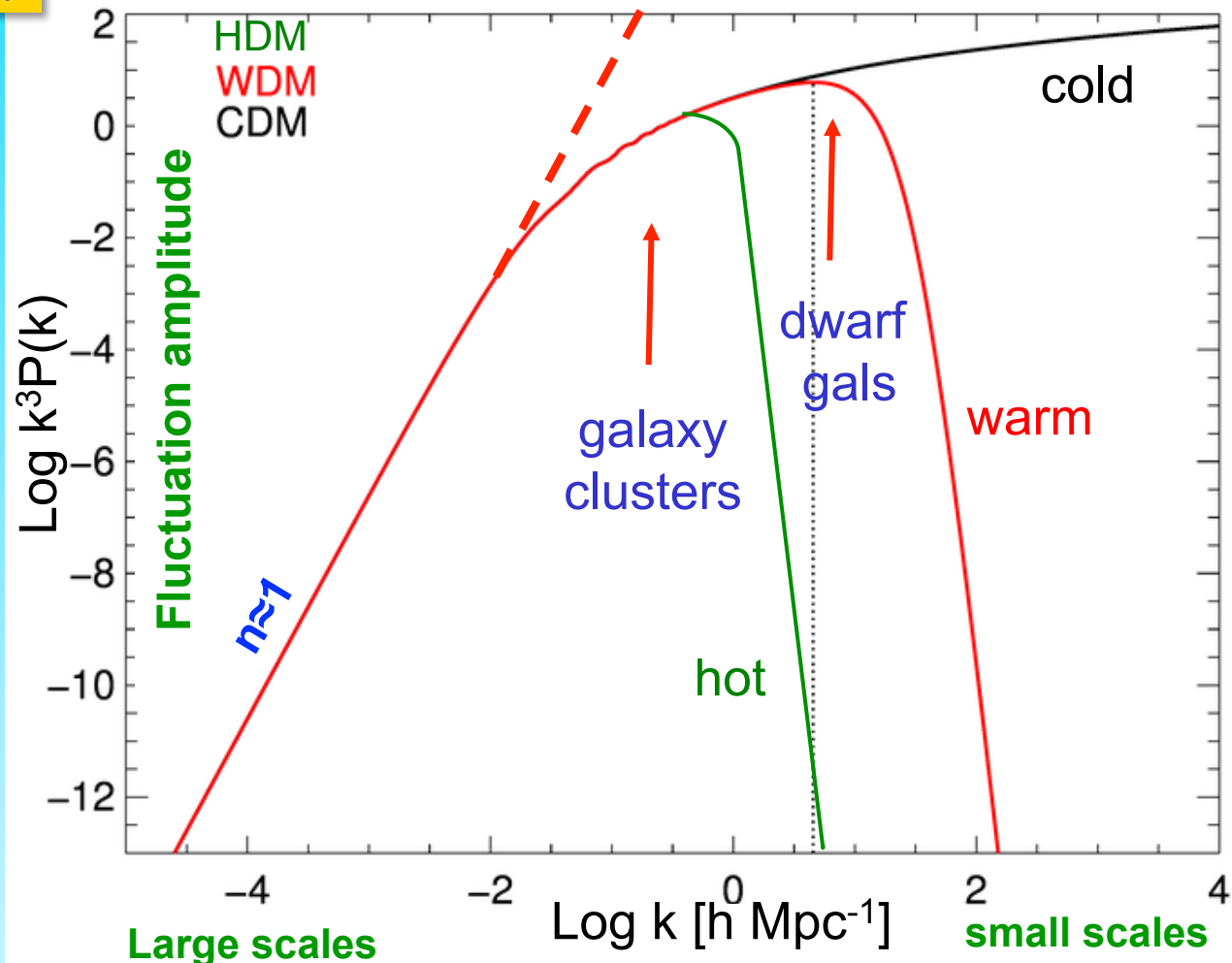
Free streaming \rightarrow

$\lambda_{\text{cut}} \propto m_x^{-1}$
for thermal relic

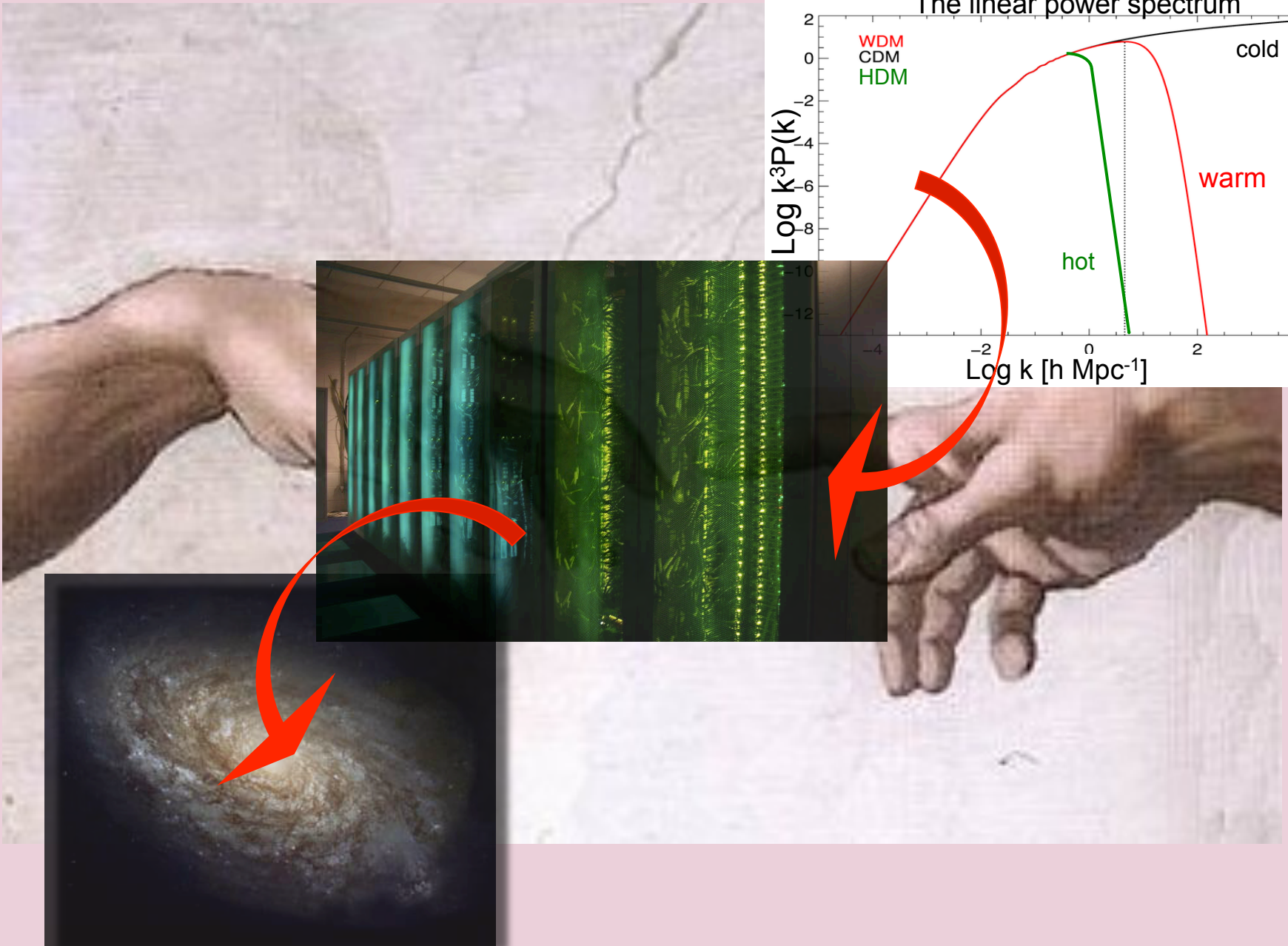
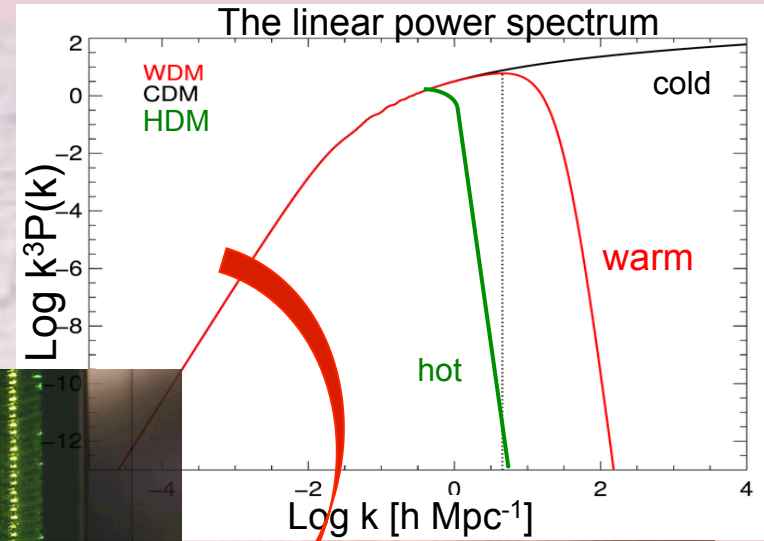
$m_{\text{CDM}} \sim 100 \text{ GeV}$
susy; $M_{\text{cut}} \sim 10^{-6} M_{\odot}$

$m_{\text{WDM}} \sim \text{few keV}$
sterile ν ; $M_{\text{cut}} \sim 10^9 M_{\odot}$

$m_{\text{HDM}} \sim \text{few tens eV}$
light ν ; $M_{\text{cut}} \sim 10^{15} M_{\odot}$



Non-linear evolution

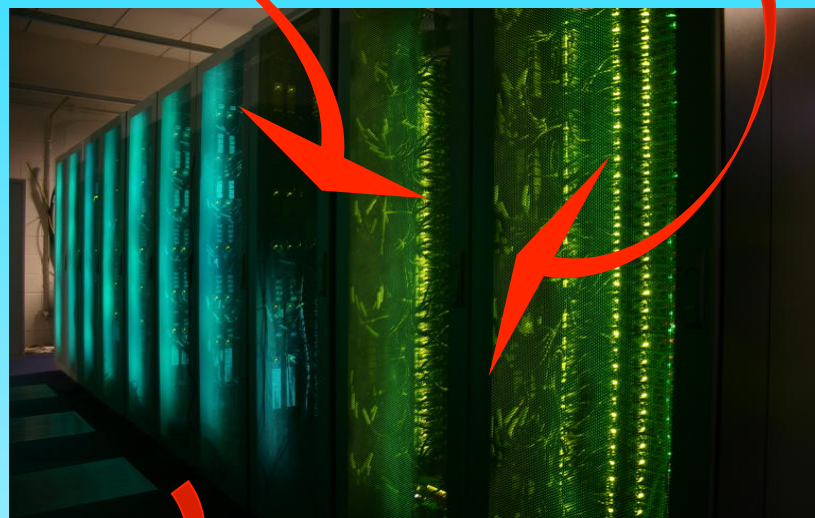


Non-linear evolution: simulations

Initial conditions + assumption about content of Universe

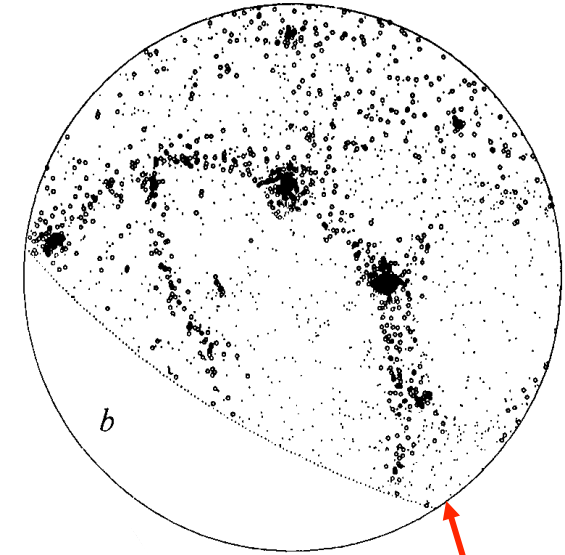
Relevant equations:

Collisionless Boltzmann,
Poisson, Friedmann eqn,
Radiative hydrodynamics
Astrophysics (subgrid)



How to make a virtual universe

Non-baryonic dark matter cosmologies



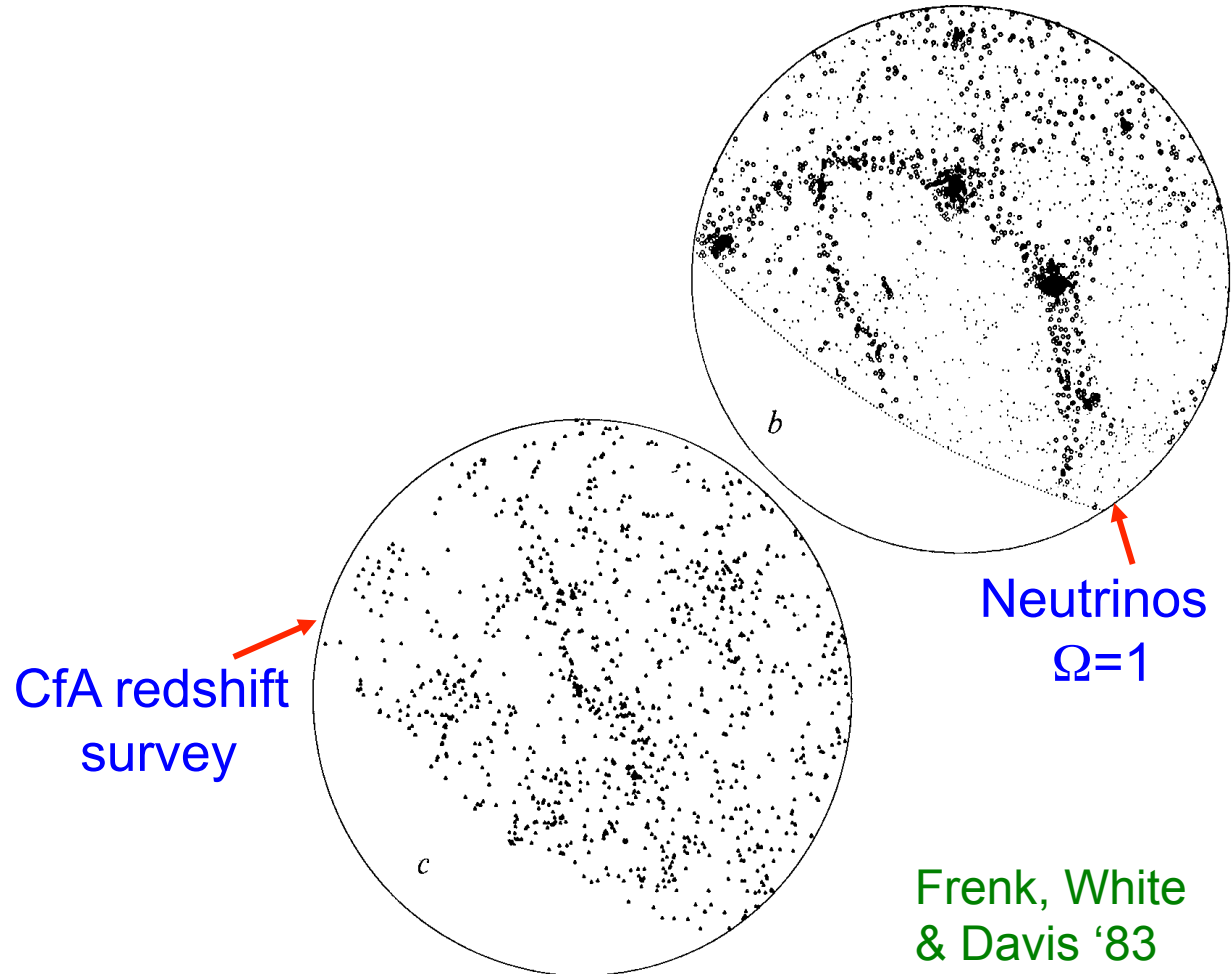
Neutrinos
 $\Omega=1$

Frenk, White
& Davis '83

Non-baryonic dark matter cosmologies

Neutrino DM →
wrong clustering

Neutrinos cannot
make appreciable
contribution to Ω
→ $m_\nu \ll 30 \text{ eV}$



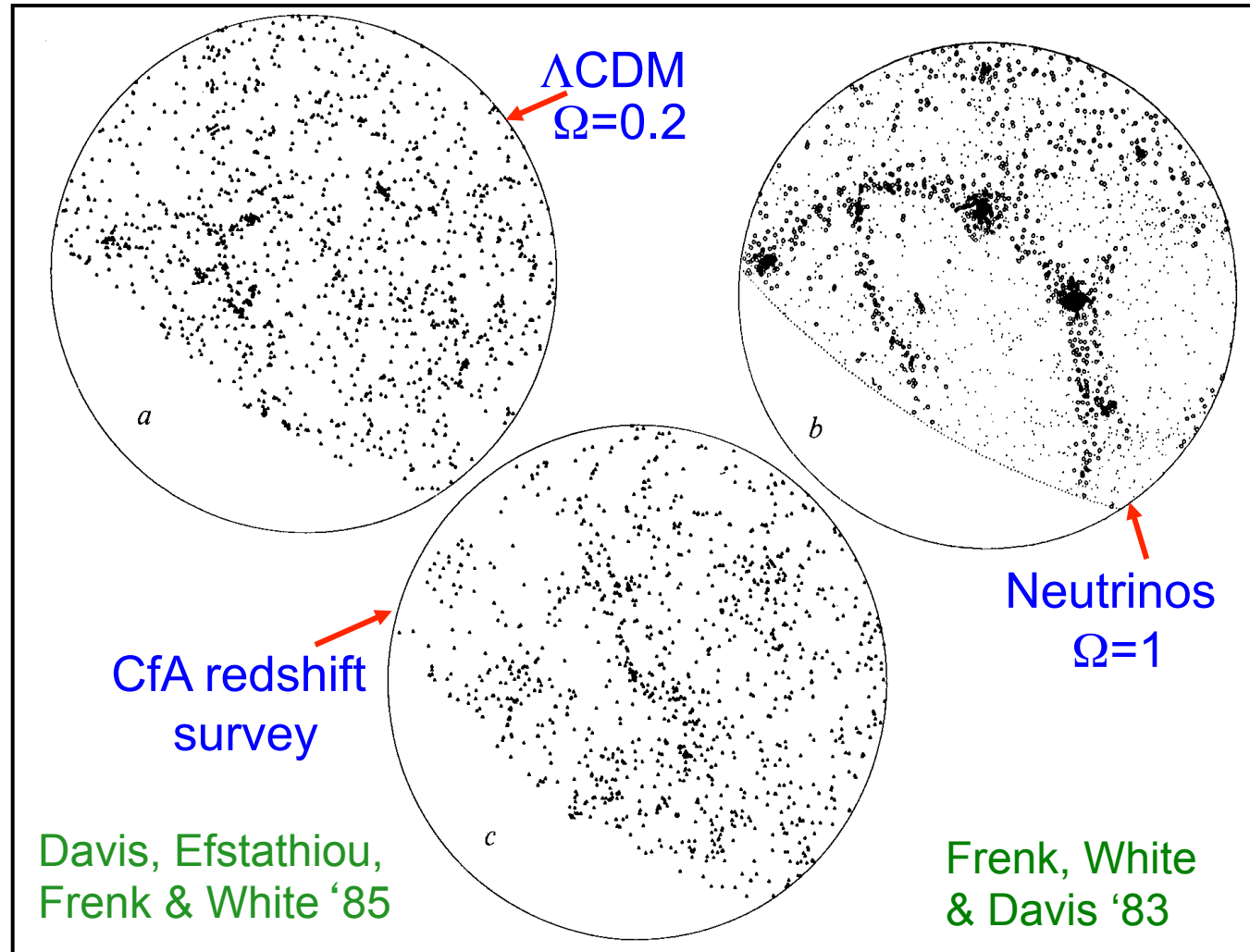
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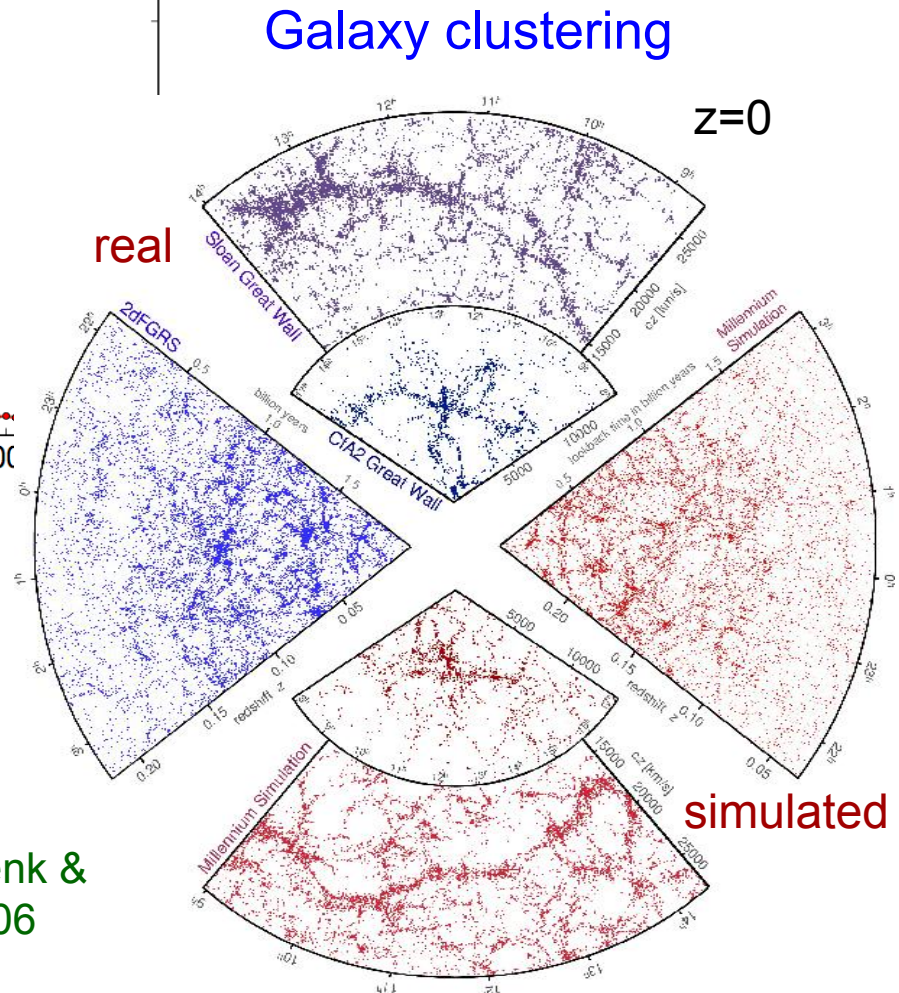
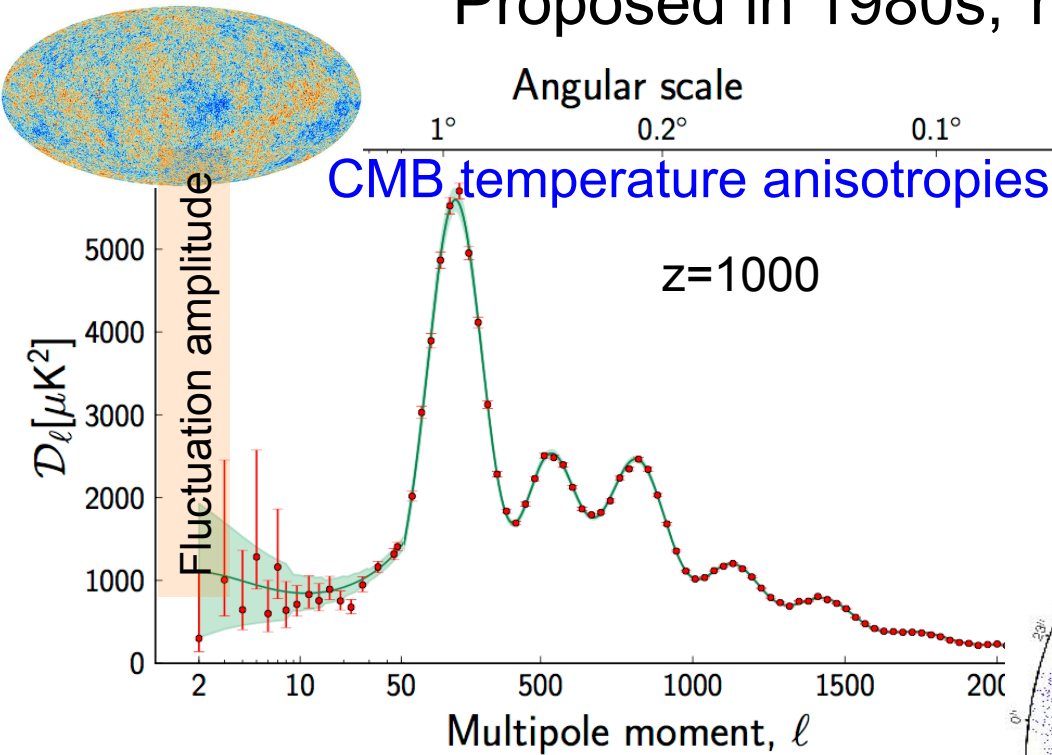
Early CDM N-body
simulations gave
promising results

In CDM structure
forms hierarchically



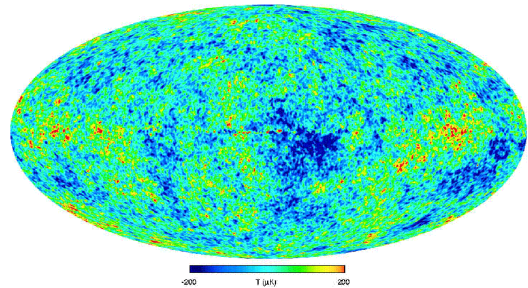
The Λ CDM model of cosmogony

Proposed in 1980s; now empirically supported by:



Springel, Frenk &
White 2006

The cosmic power spectrum: from the CMB to the 2dFGRS

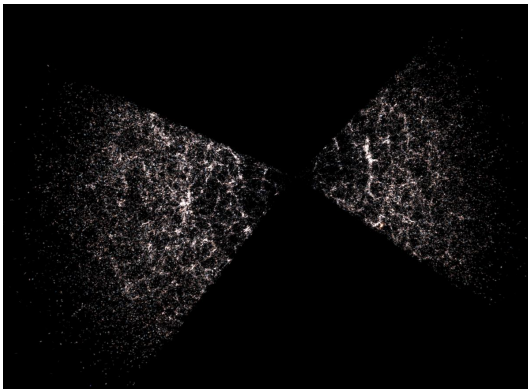


$z \sim 1000$

$\text{Log } k^3 P(k)$

wavelength k^{-1} (comoving h^{-1} Mpc)

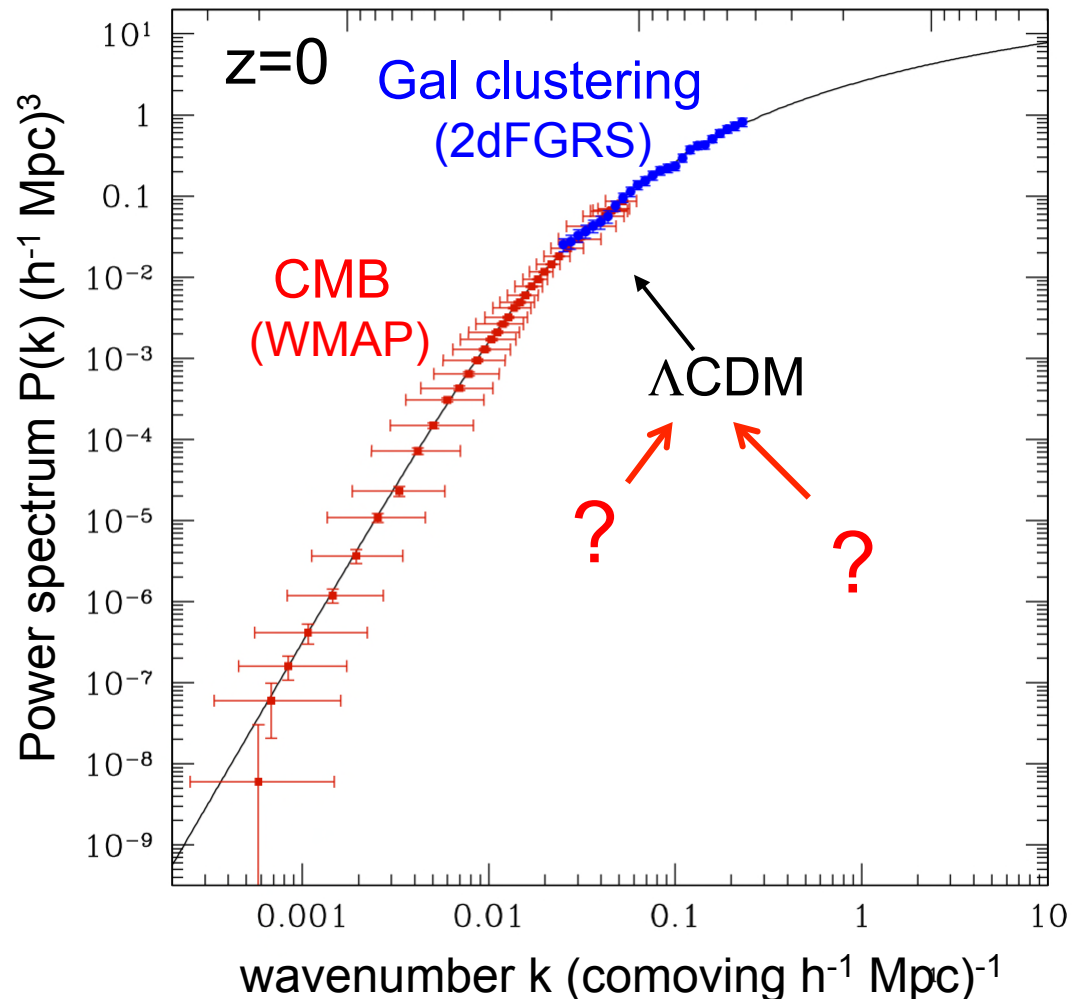
1 000 100 10



$z \sim 0$

⇒ Λ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06



The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming →

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

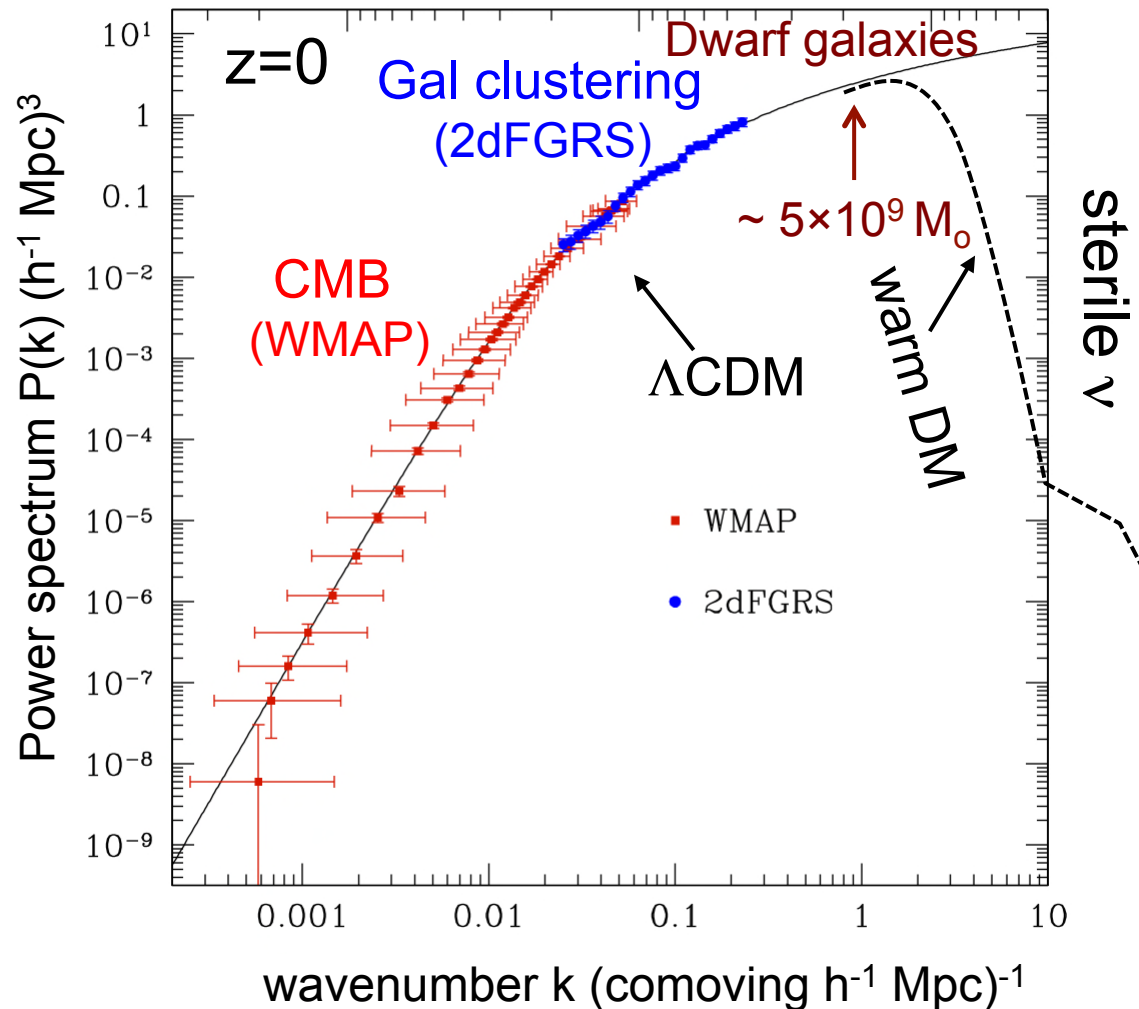
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$$\text{susy}; M_{\text{cut}} \sim 10^{-6} M_{\odot}$$

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$$\text{sterile } \nu; M_{\text{cut}} \sim 10^9 M_{\odot}$$

Log $k^3 P(k)$ wavelength k^{-1} (comoving $h^{-1} \text{ Mpc}$)



Four problems on small scales

Traditionally ascribed to CDM:

1. The “missing satellites” problem
2. The “too-big-to-fail” problem
3. The “plane of satellites” problem
4. The “core-cusp” problem

Sterile neutrinos

Explain:

- Neutrino oscillations and masses
- Baryogenesis
- Absence of right-handed neutrinos in standard model
- Dark matter

Sterile neutrino minimal standard model (ν MSM; Boyarski+ 09):

- Extension of SM w. 3 sterile neutrinos: 2 of GeV; 1 of keV mass
- If $\Omega_N = \Omega_{DM}$, 2 parameters: mass, lepton asymmetry/mixing angle
- GeV particles may be detected at CERN (SHiP)
- Dark matter candidate can be detected by X-ray decay



Both CDM & WDM compatible with CMB & galaxy clustering

Claims that both types of DM have been discovered:

- ◆ CDM: γ -ray excess from Galactic Center
- ◆ WDM (sterile ν): 3.5 X-ray keV line in galaxies and clusters

Very unlikely that both are right!

The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming →

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

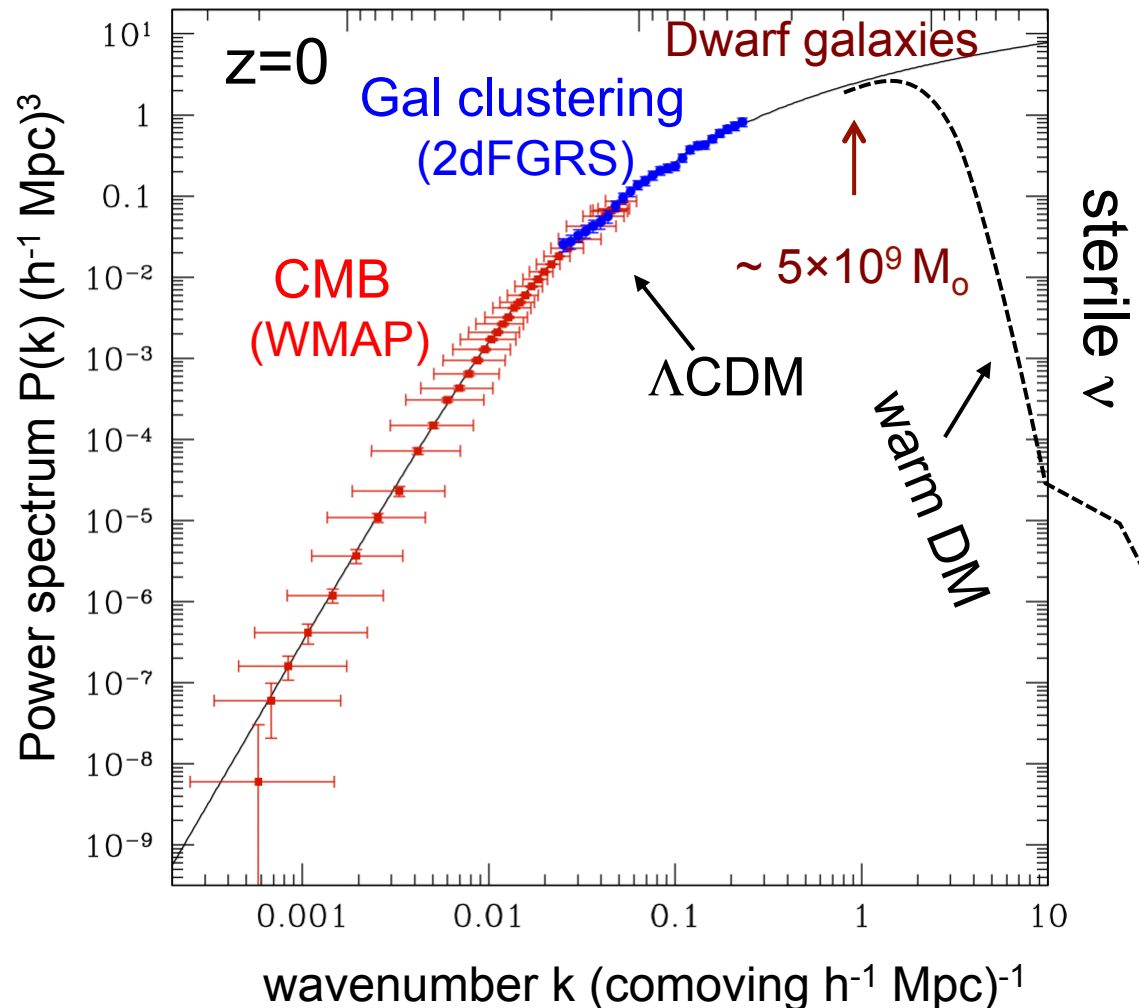
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Log $k^3 P(k)$ wavelength k^{-1} (comoving $h^{-1} \text{ Mpc}$)





The identity of the dark matter is encoded
in dwarf galaxies and in the halo of the MW
(strongly non-linear regime)



Cold Dark Matter

Warm Dark Matter

13.4 billion years ago

cold dark matter

warm dark matter

How can we distinguish between these?

Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,
Boyarski & Ruchayskiy '12

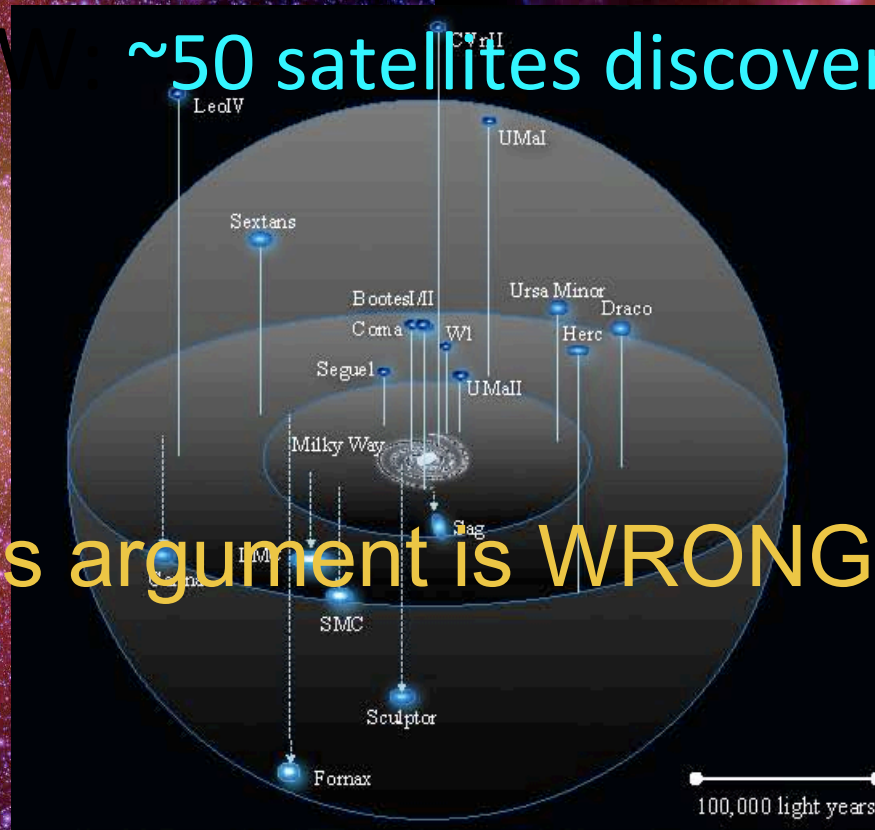
cold dark matter

warm dark matter

Obvious test: count satellites in MW or M31

In the MW ~50 satellites discovered so far

This argument is **WRONG!**



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,
Boyarski & Ruchayskiy '12

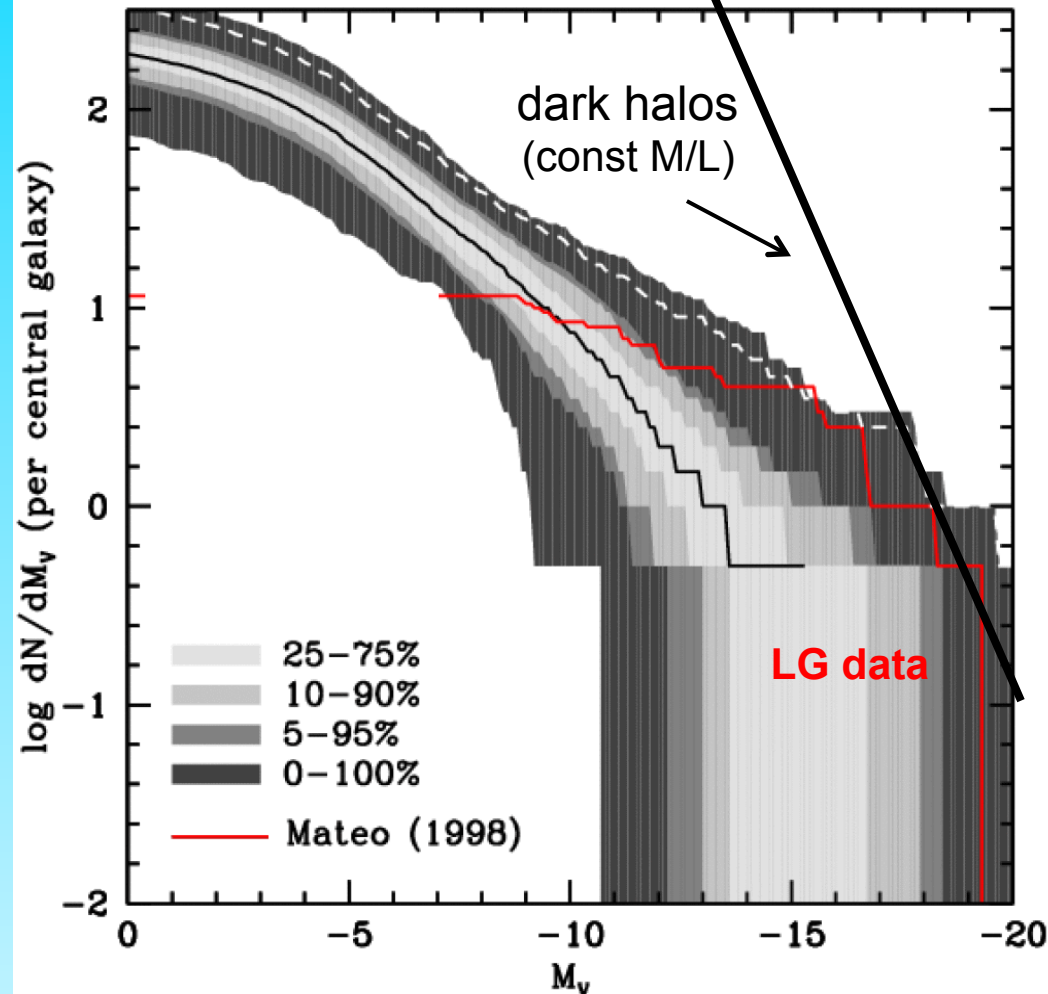
Most subhalos never make a galaxy!

Because:

- Reionization heats gas to 10^4K , preventing it from cooling and forming stars in small halos ($T_{\text{vir}} < 10^4\text{K}$)
- Supernovae feedback expels residual gas in slightly larger halos

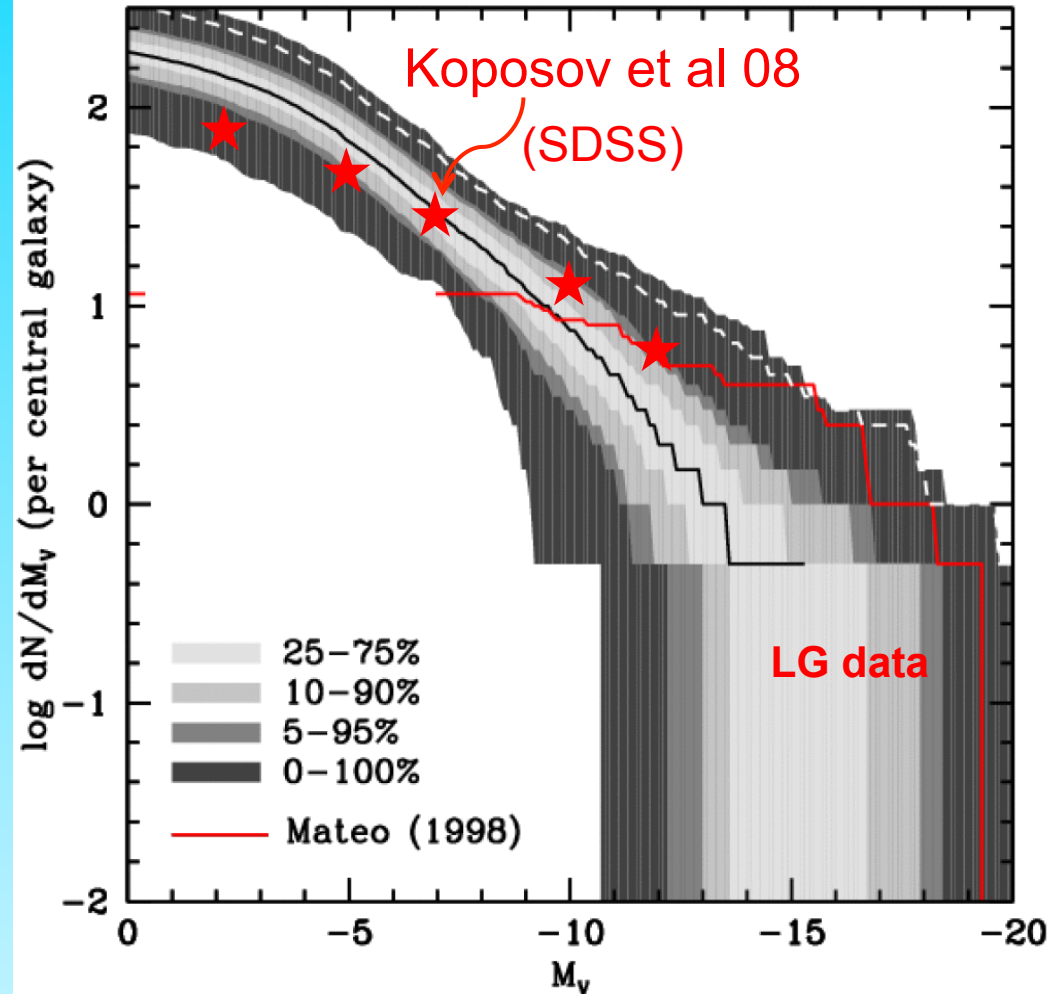
Luminosity Function of Local Group Satellites

- Median model → correct abund. of sats brighter than $M_V = -9$ and $V_{\text{cir}} > 12$ km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare (~10% of cases)



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VIRGO

icc.dur.ac.uk/Eagle

“Evolution and assembly of galaxies and
their environment”

THE EAGLE PROJECT

Virgo Consortium

Durham: Richard Bower, Michelle Furlong, Carlos Frenk, Matthieu Schaller, James Trayford, Yelti Rosas-Guevara, Tom Theuns, Yan Qu, John Helly, Adrian Jenkins.

Leiden: Rob Crain, Joop Schaye.

Other: Claudio Dalla Vecchia, Ian McCarthy, Craig Booth...

The Eagle Simulations

EVOLUTION AND ASSEMBLY OF GALAXIES AND THEIR ENVIRONMENTS

The Hubble Sequence realised in cosmological simulations

E0

E7

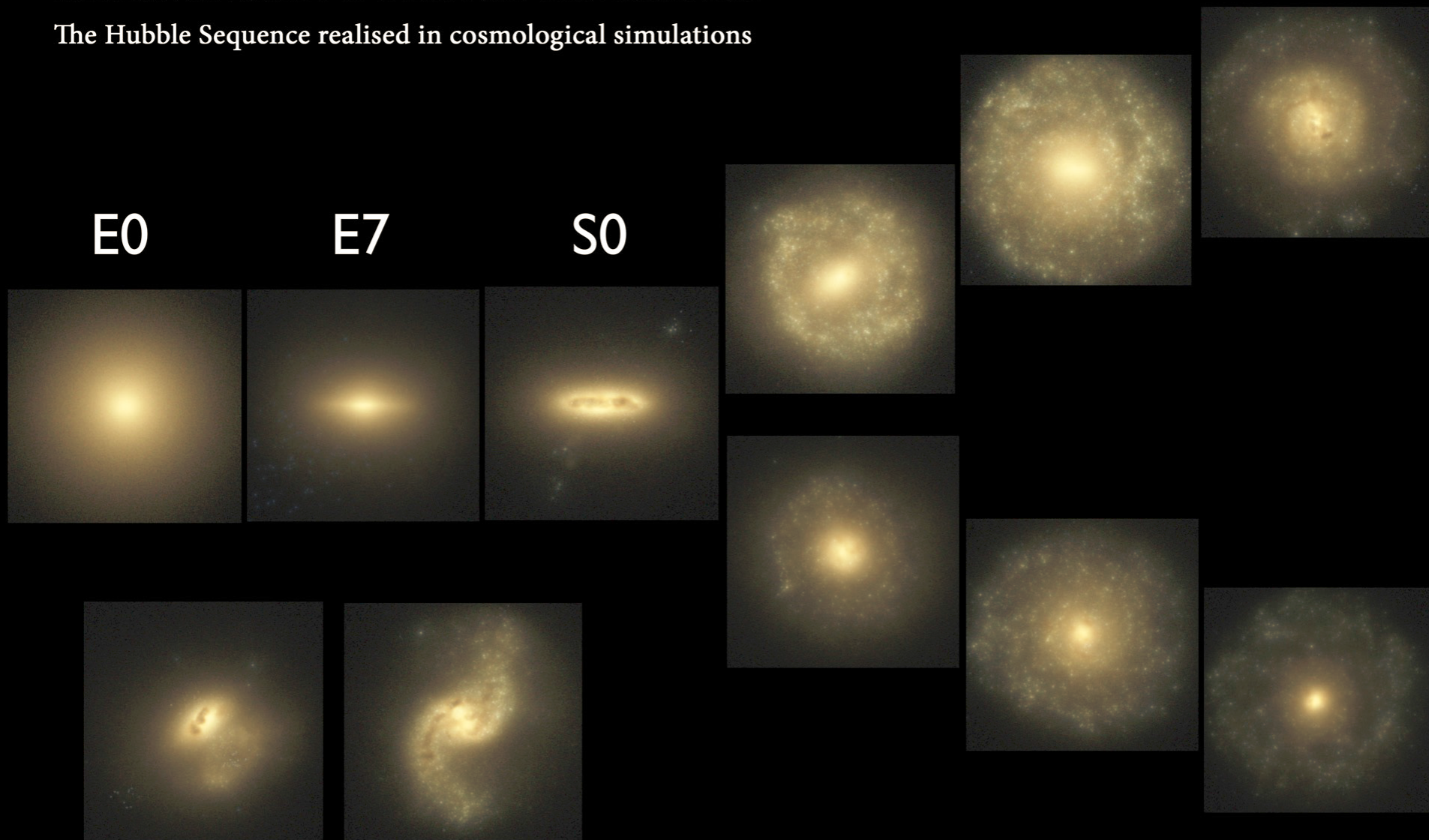
S0

SB

Irr

S

Trayford et al '15



VIRG

Dark matter

APOSTLE
EAGLE full
hydro
simulations

Local Group

CDM

Sawala et al '16



Stars

VIRG

APOSTLE
EAGLE full
hydro
simulations

Local Group

Stars

Far fewer satellite galaxies than CDM halos

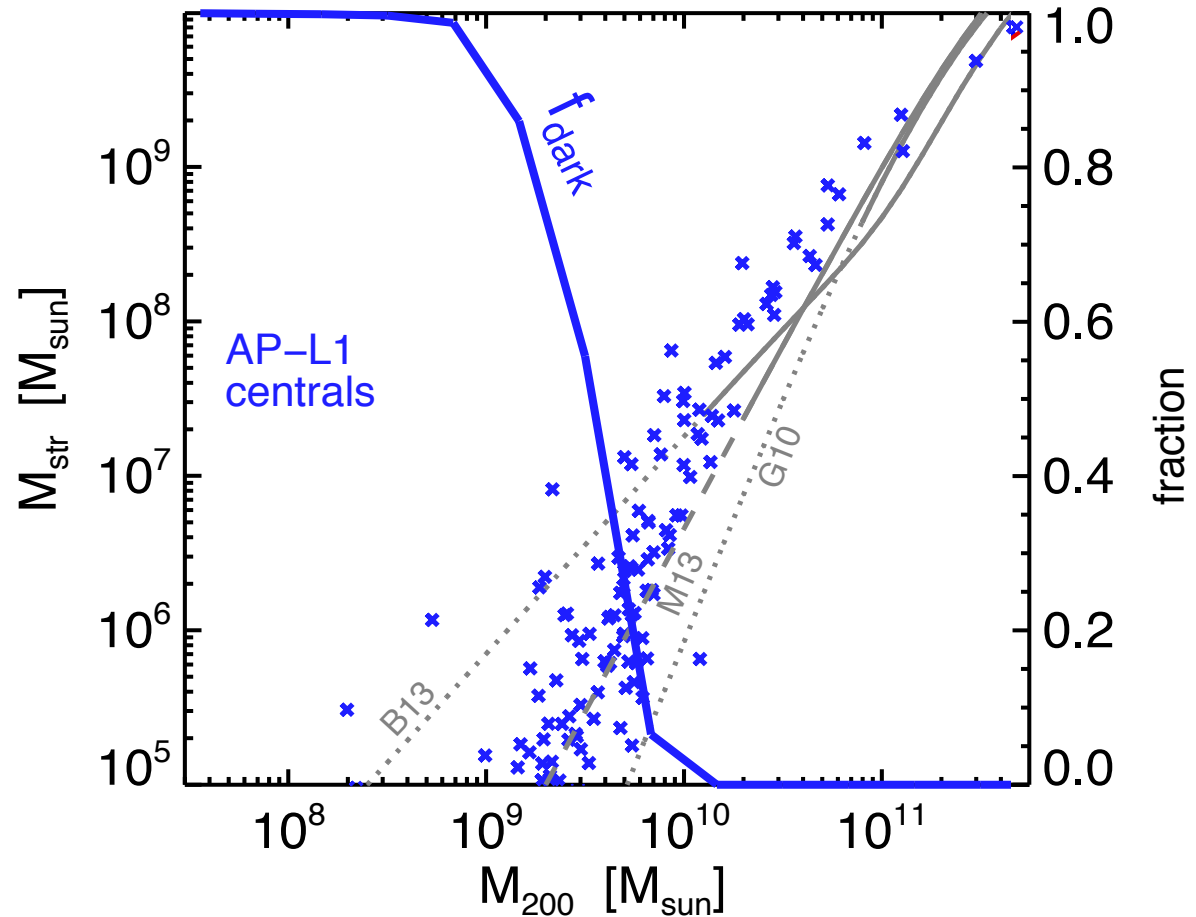
Sawala et al '16



Fraction of dark subhalos

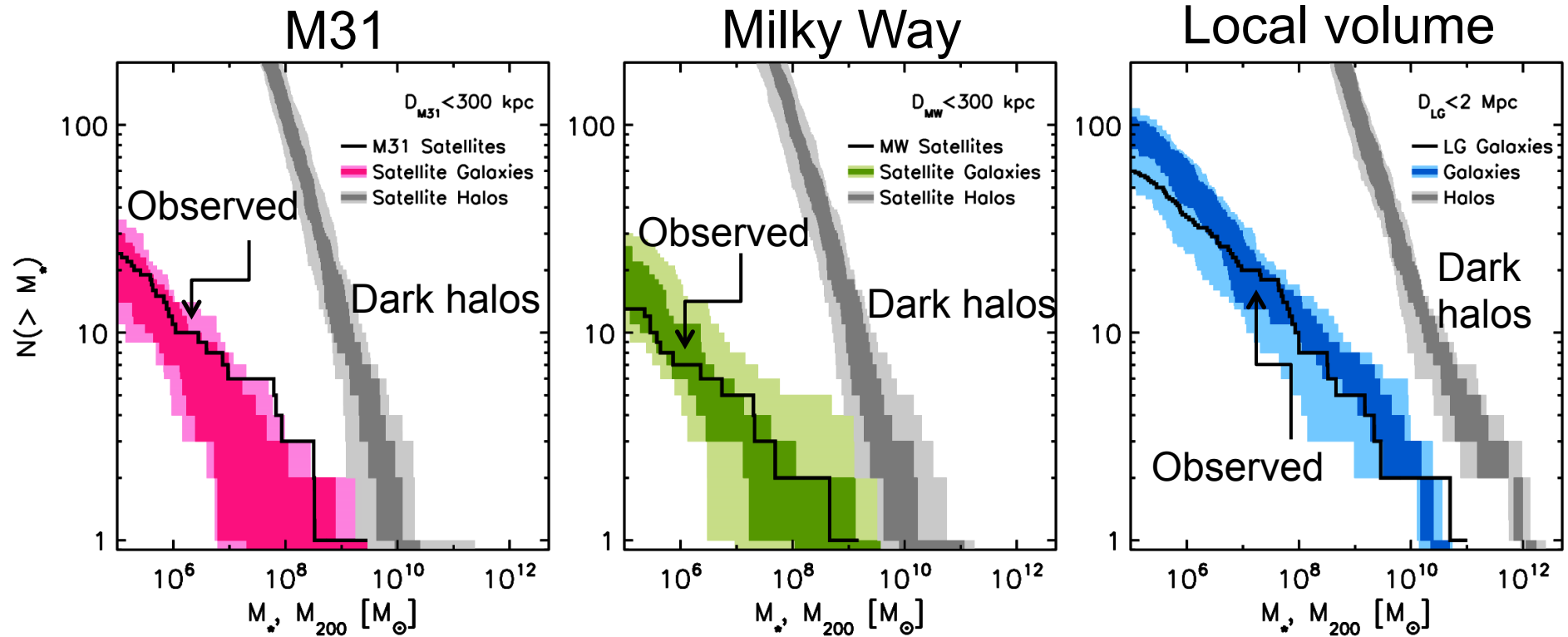
$$V_c = \sqrt{\frac{GM}{r}}$$

$$V_{\max} = \max V_c$$



All halos of mass $< 5 \times 10^8 M_\odot$ or $V_{\max} < 7$ km/s are dark ($m_* < 10^4 M_\odot$)

EAGLE Local Group simulation



When “baryon effects” are
taken into account



Observed abundance of satellites
is compatible with CDM



There is **no** such thing as the
“satellite problem” in CDM!

Four problems on small scales

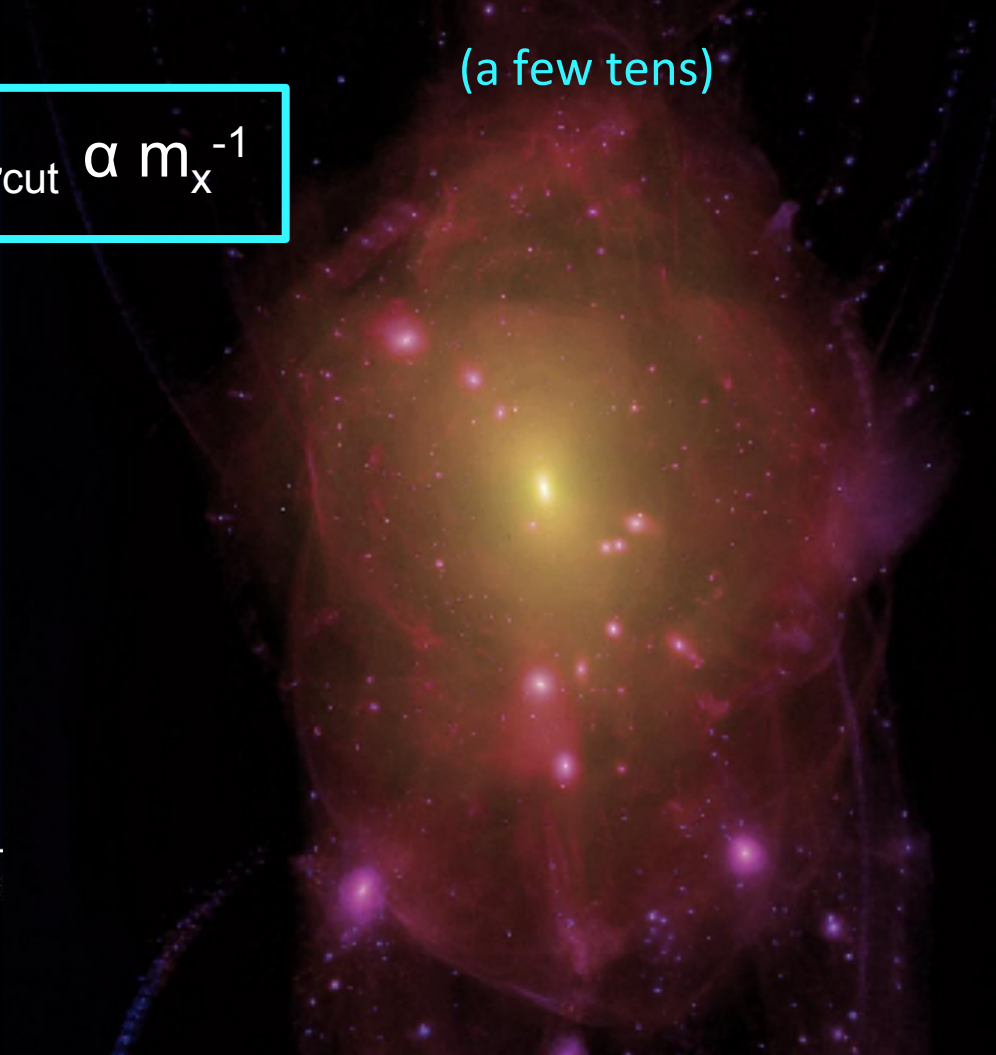
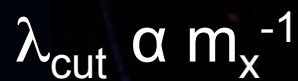
Traditionally ascribed to CDM:

- ~~1. The “missing satellites” problem~~
2. The “too-big-to-fail” problem
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4. The “core-cusp” problem



Dark matter subhalos in WDM

(a few tens)



Warm DM: different ν mass

$z=3$

WDM

2.3 keV

2.0 keV

1.6 keV

1.4 keV

CDM

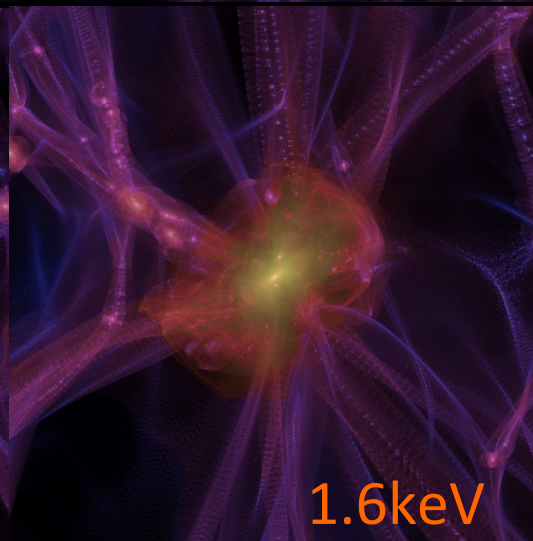
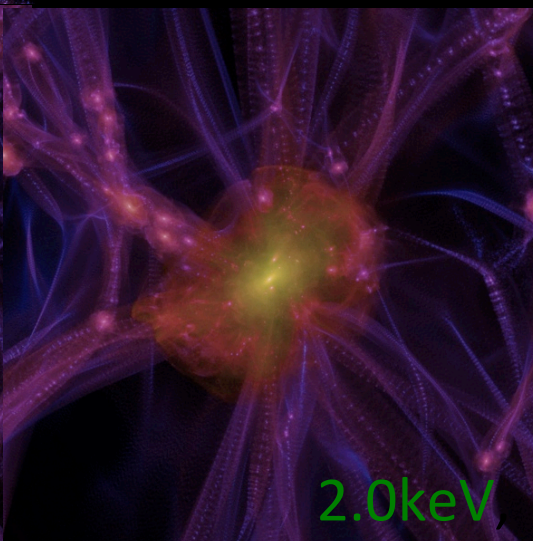
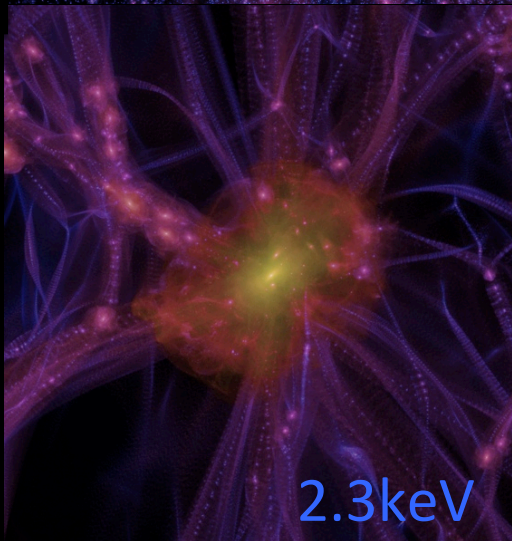
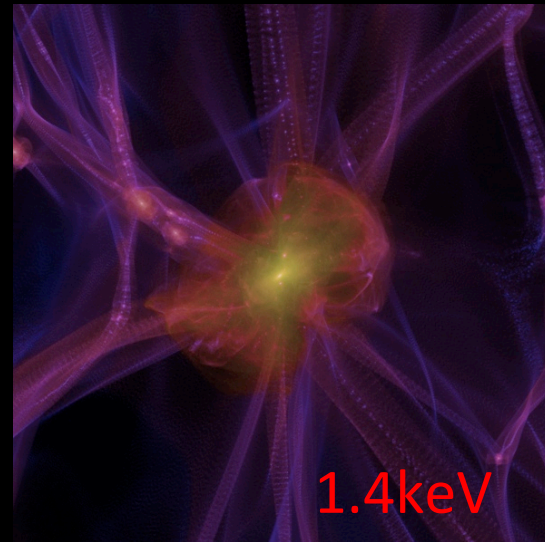
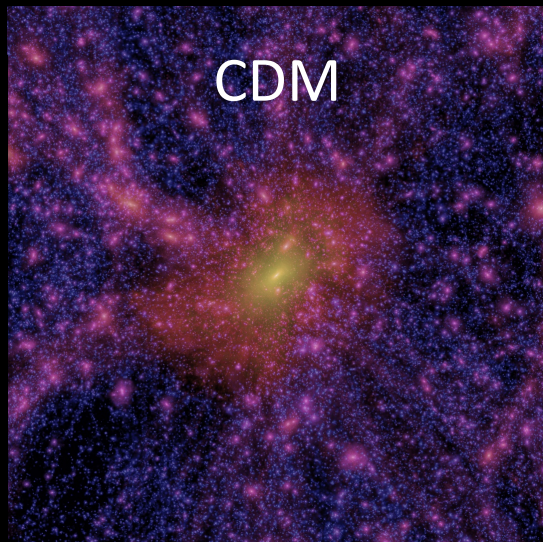
WDM

1.4keV

2.3keV

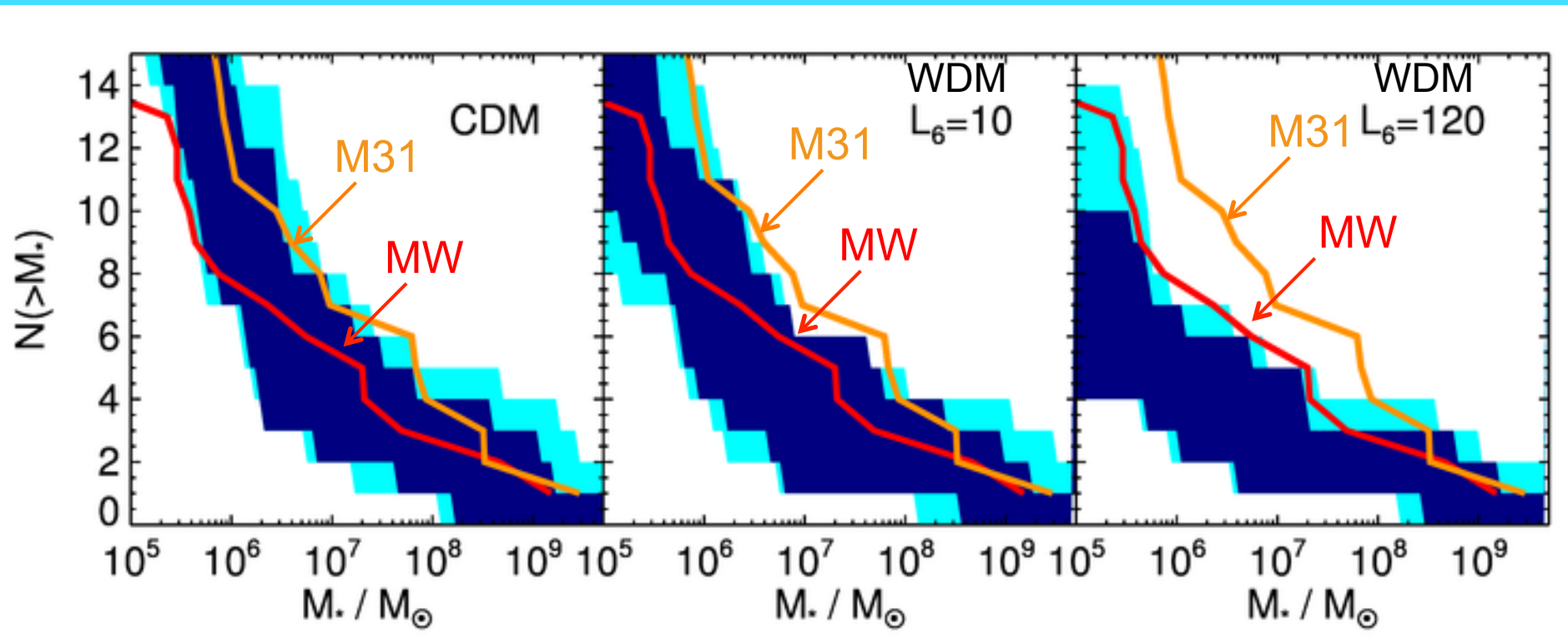
2.0keV

1.6keV



Luminosity Function of Local Group Satellites in WDM

From “Warm Apostle:” 7keV sterile ν $M_h \sim 10^{12} M_\odot$



→ Can rule out parts of sterile ν parameter space

When “baryon effects” are
taken into account



Observed abundance of satellites
is compatible with CDM but rules
out some WDM models



There is no such thing as the
“satellite problem” in CDM!

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$$V_c = \sqrt{\frac{GM}{r}}$$

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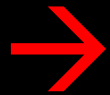
“Too-big-to-fail” problem in CDM:

N-body CDM sims produce too many massive subhalos
(e.g. >10 with $V_{\max} > 30$ km/s)

BUT: Milky Way has only 3 sats with $V_{\max} > 30$ km/s

Why did the big subhalos
not make a galaxy?

When “baryon effects” are
taken into account



No too-big-to-fail **problem** in CDM
similar result for WDM

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The peculiar alignment of the Milky Way satellites

The satellites of the Milky Way

The 11 bright satellites within 250 kpc of the Milky Way lie roughly on a great circle on the sky (Lynden-Bell '67, Kroupa, etal '05)

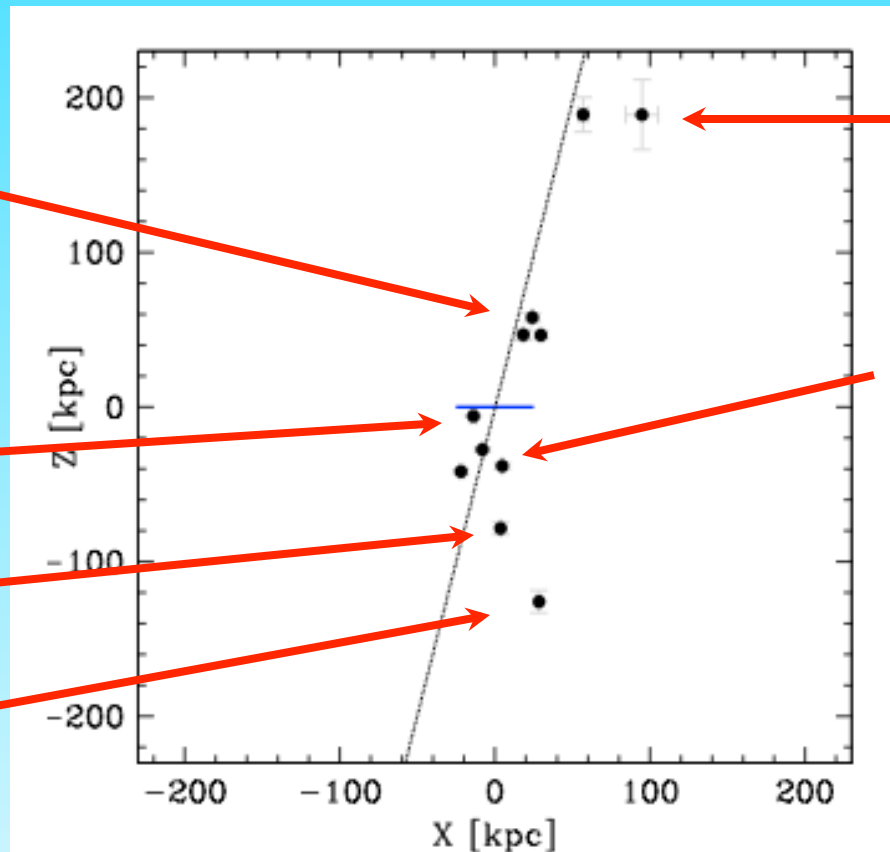
The Great Pancake (Libeskind '05)

Sculptor, Draco,
Sextans

Sagittarius Dw

Carina

Fornax



Leo I & II

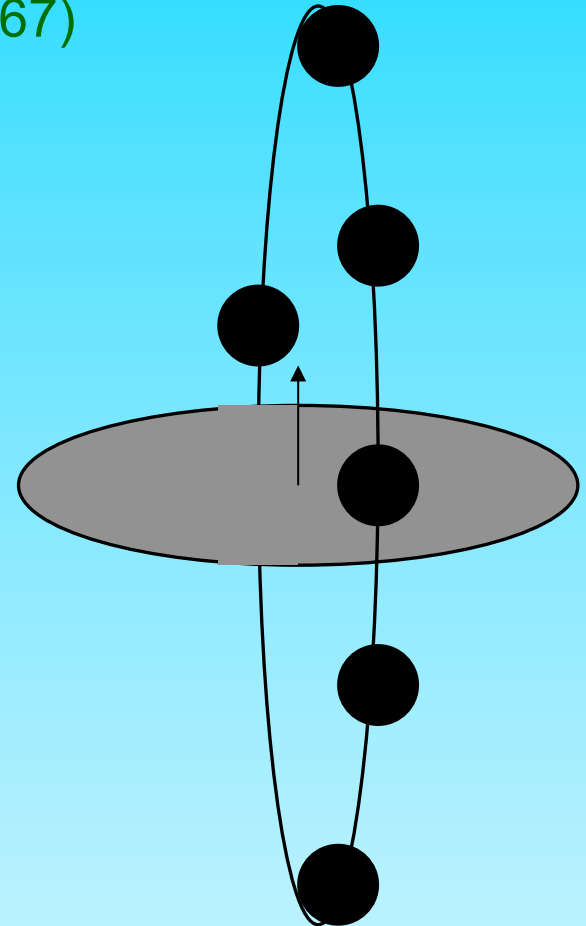
LMC, SMC,
Ursa Minor

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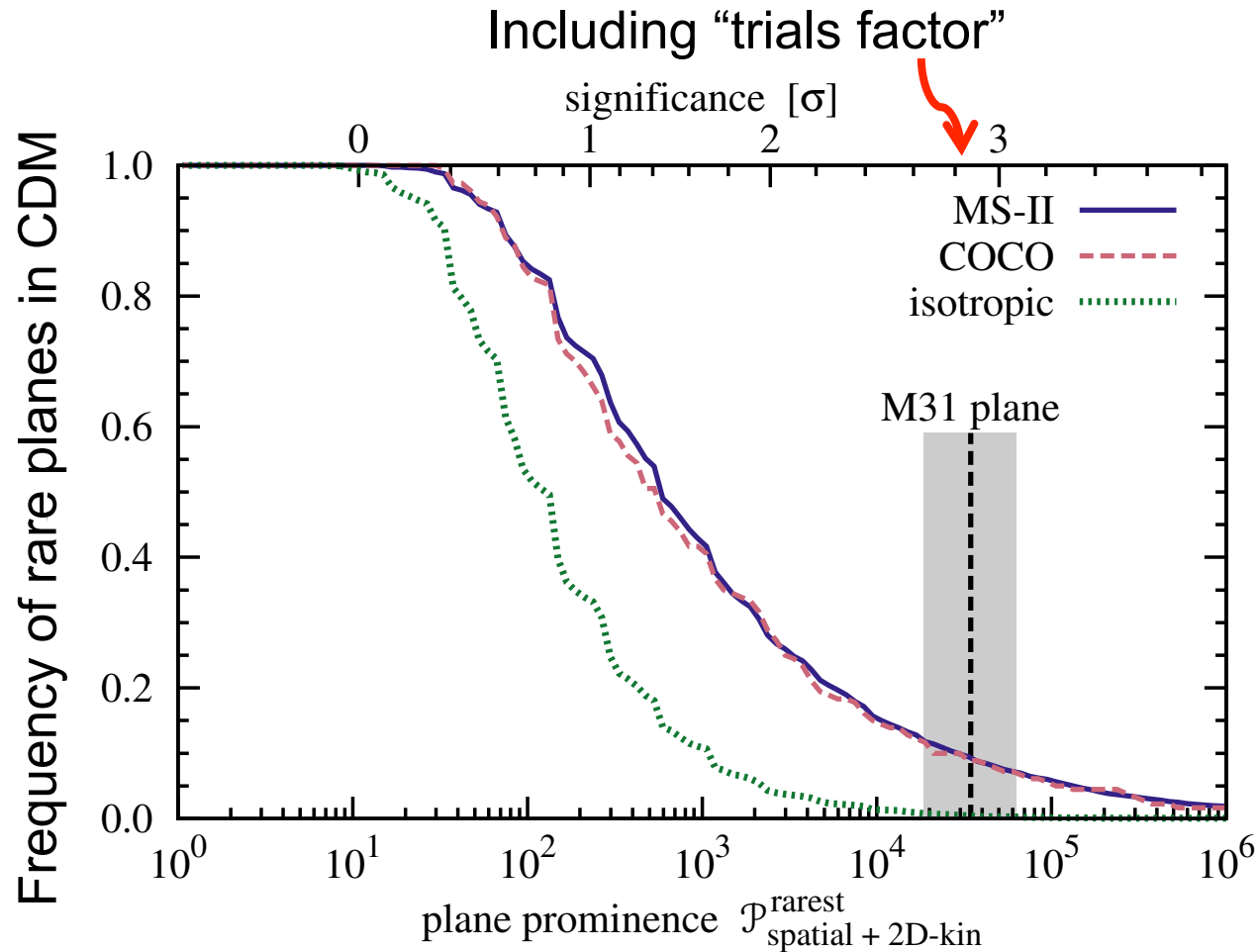
... and ~ 7 of them seem to be rotating coherently (Kroupa+ '05)

Andromeda (Ibata+'15) ; also seems to have a plane of satellites and now Cen A (Pawlowsky+'18) also seems to have one



The significance of Ibata's plane

- Significance of Ibata's plane in M31 is reduced by x100 when trials factor is included
- 8.8% of halos in Λ CDM simulation have even more prominent disks than Ibata's



In random distribution, 1 in 30,000 chance of finding a plane of 15 sats (out of 27) as thin found by Ibata et al.,
 Cautun, CSF, et al '15 with at least 13 having same sense of rotation



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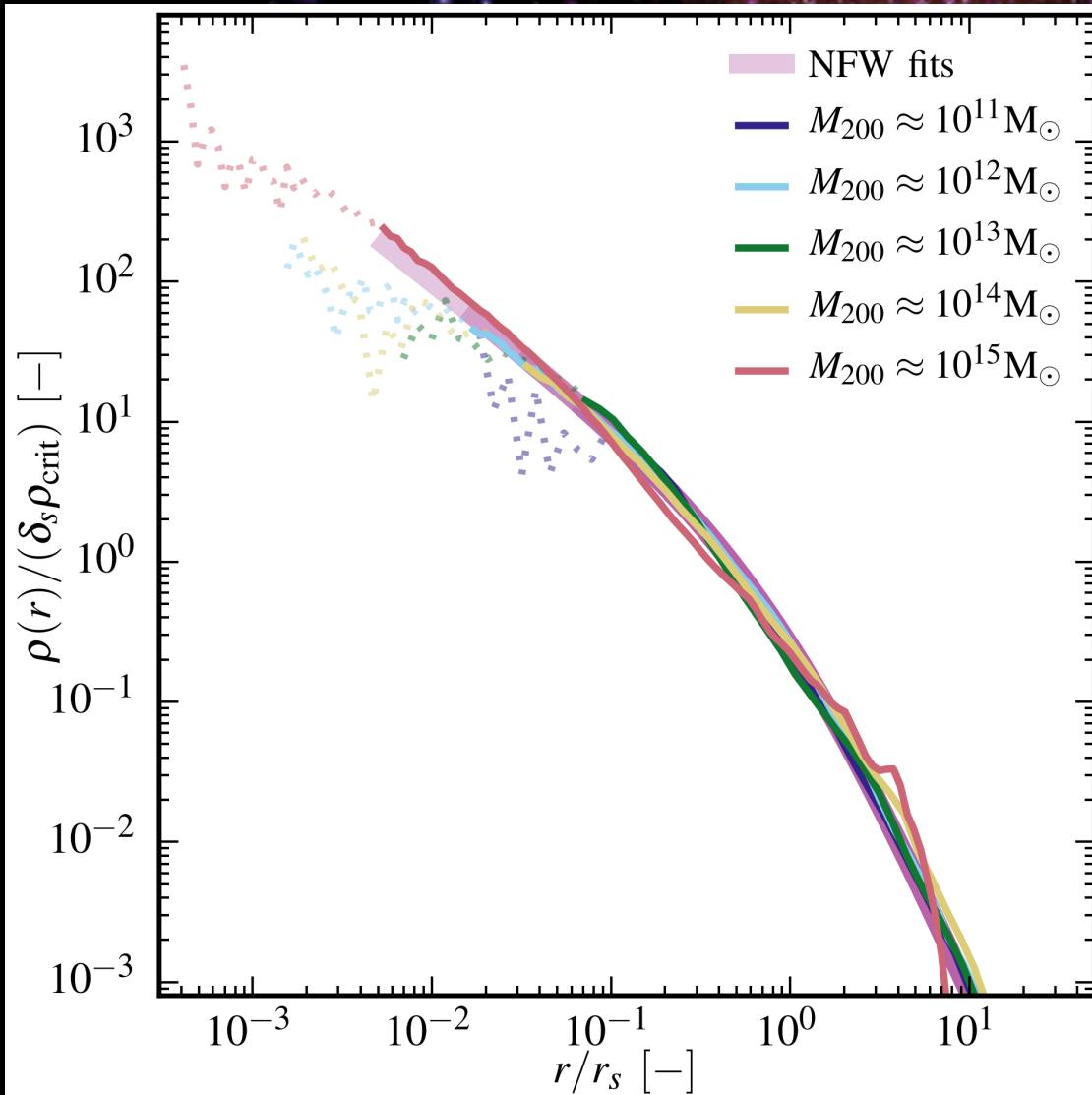
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The Density Profile of Cold Dark Matter Halos



Shape of halo profiles
~independent of halo mass &
cosmological parameters

Density profiles are “cuspy” -
no ‘core’ near the centre

Fitted by simple formula:

$$\frac{\rho(r)}{\rho_{\text{crit}}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

(Navarro, Frenk & White '97)

More massive halos and
halos that form earlier have
higher densities (bigger δ)



The core-cusp problem

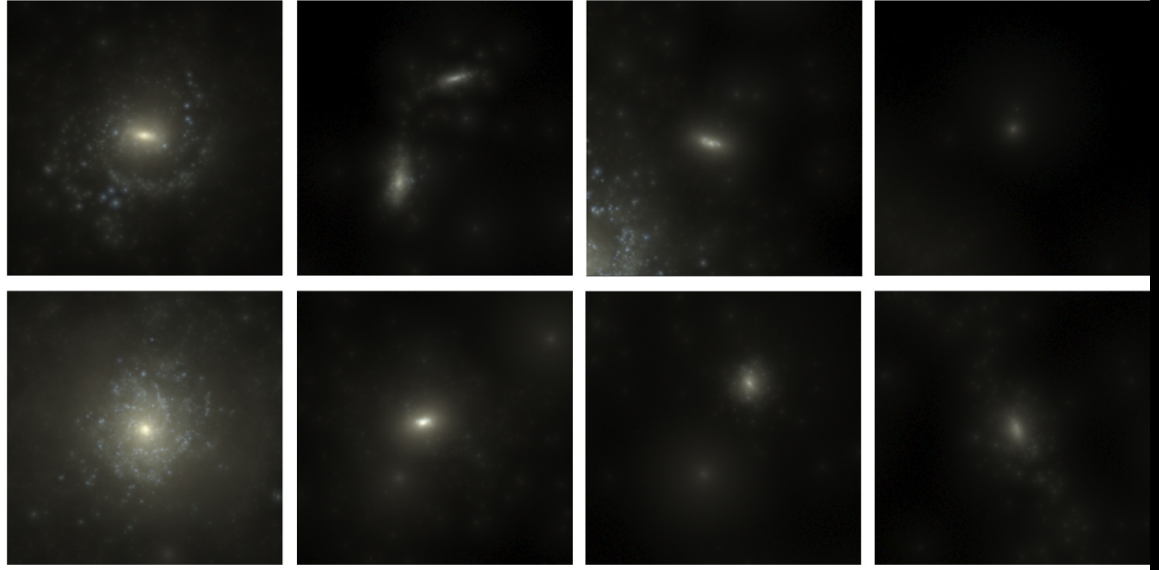
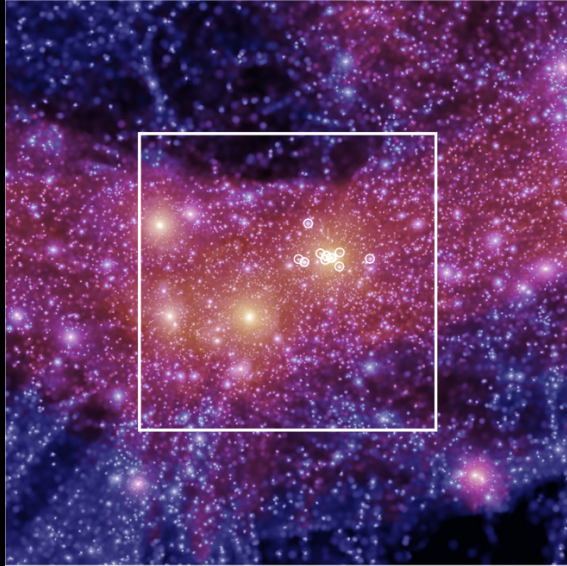
cold dark matter

warm dark matter

Halos and subhalos in CDM & WDM have
cuspy NFW profiles

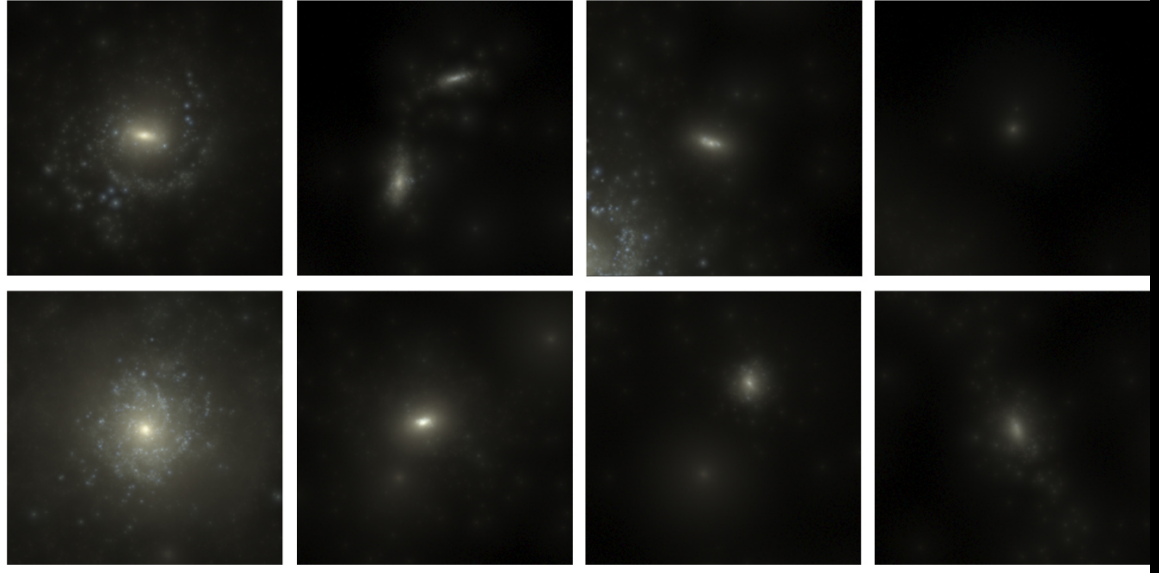
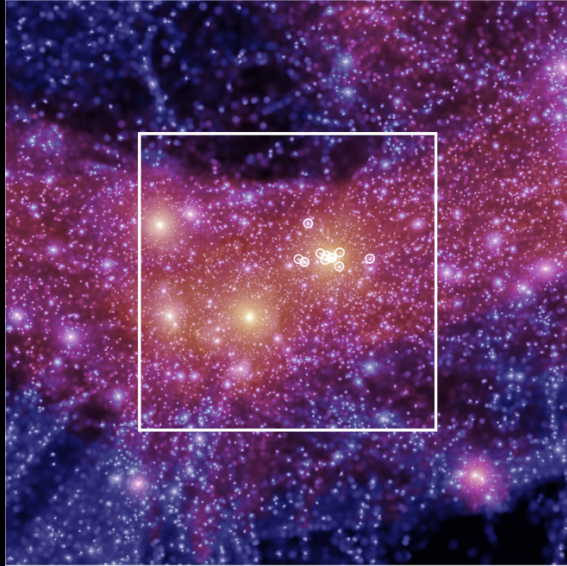
$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r / r_s)(1 + r / r_s)^2}$$

Lovell, Eke, Frenk, Gao, Jenkins, Theuns '12



EAGLE/Apostle/
Auriga galaxies have
NFW cusps

Sawala et al '15



Does Nature have them?



Sawala et al '15



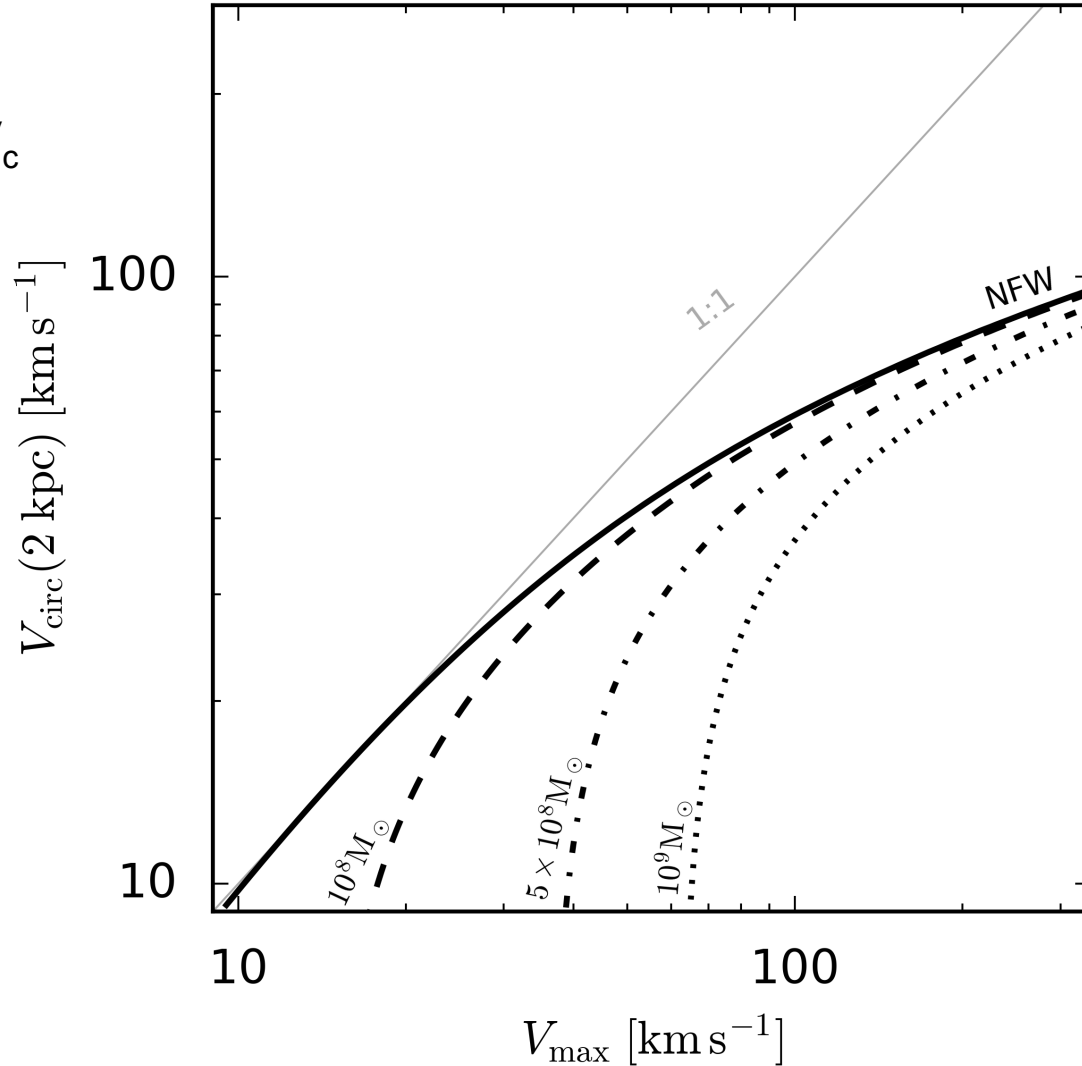
Many nearby galaxies now have hi-res 2D HI velocity fields → ideal for inferring potential

Assume: gas is in centrifugal equilibrium on approximately circular orbits

The diversity of rotation curves

$$V_c = \sqrt{\frac{GM}{r}}$$

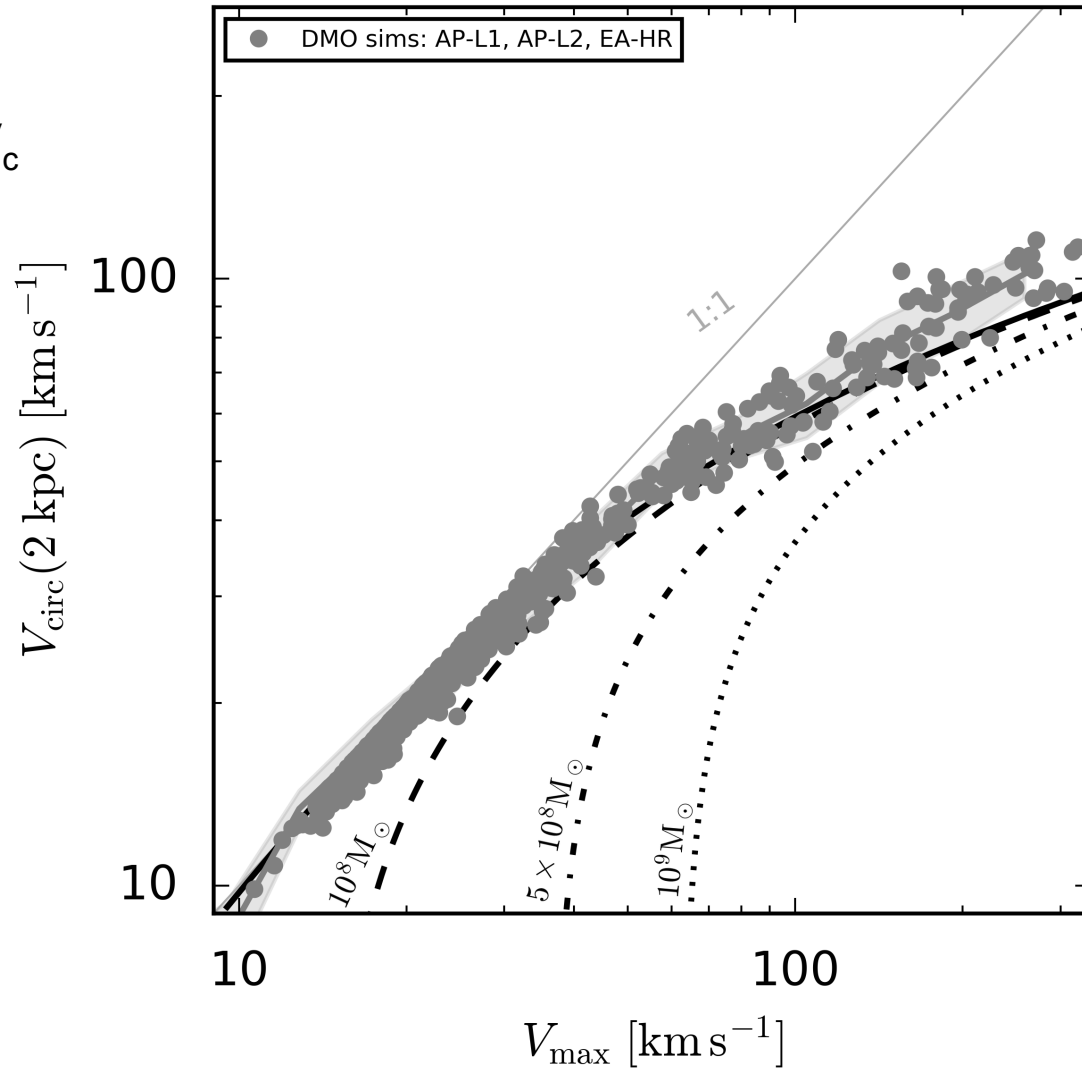
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The diversity of rotation curves

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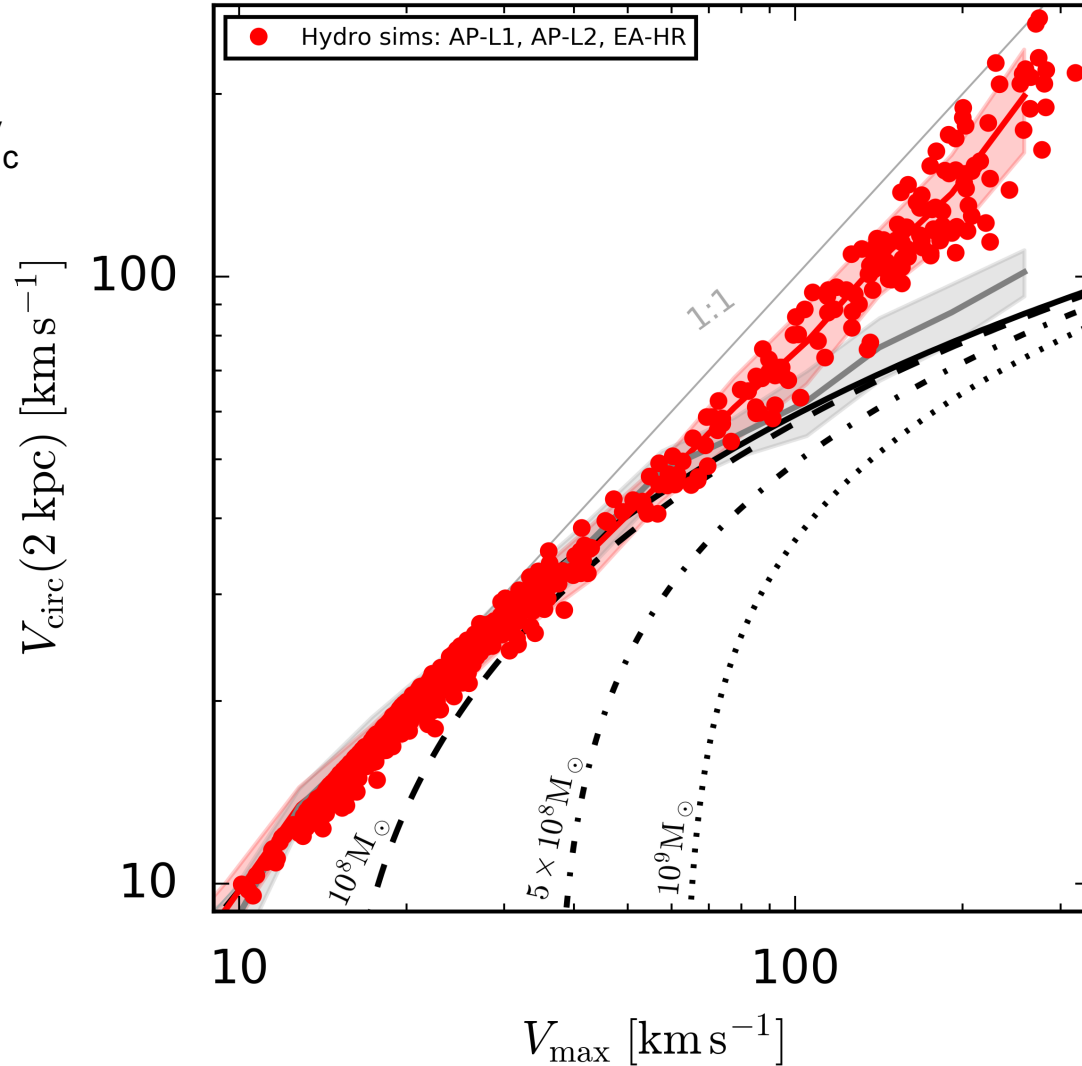
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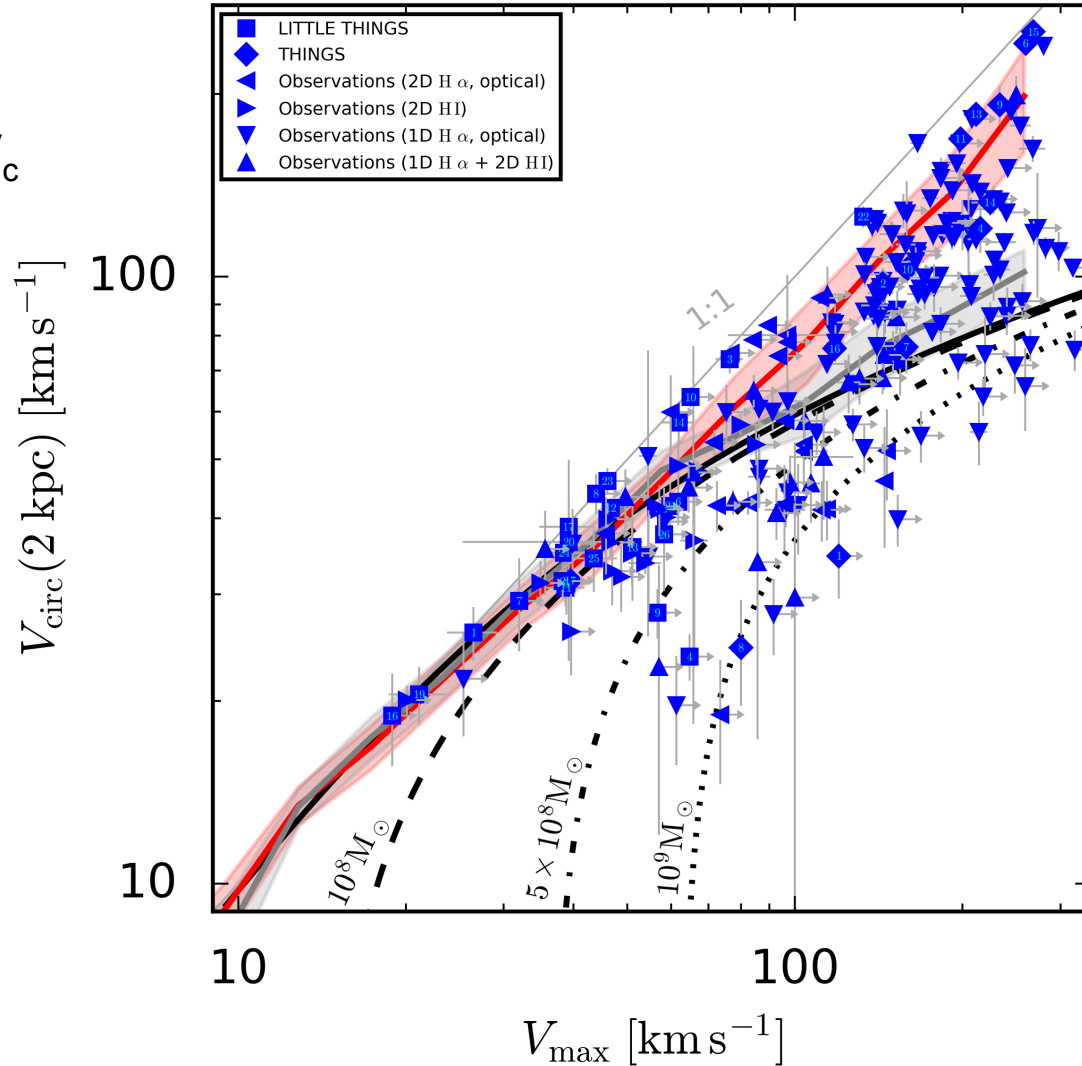
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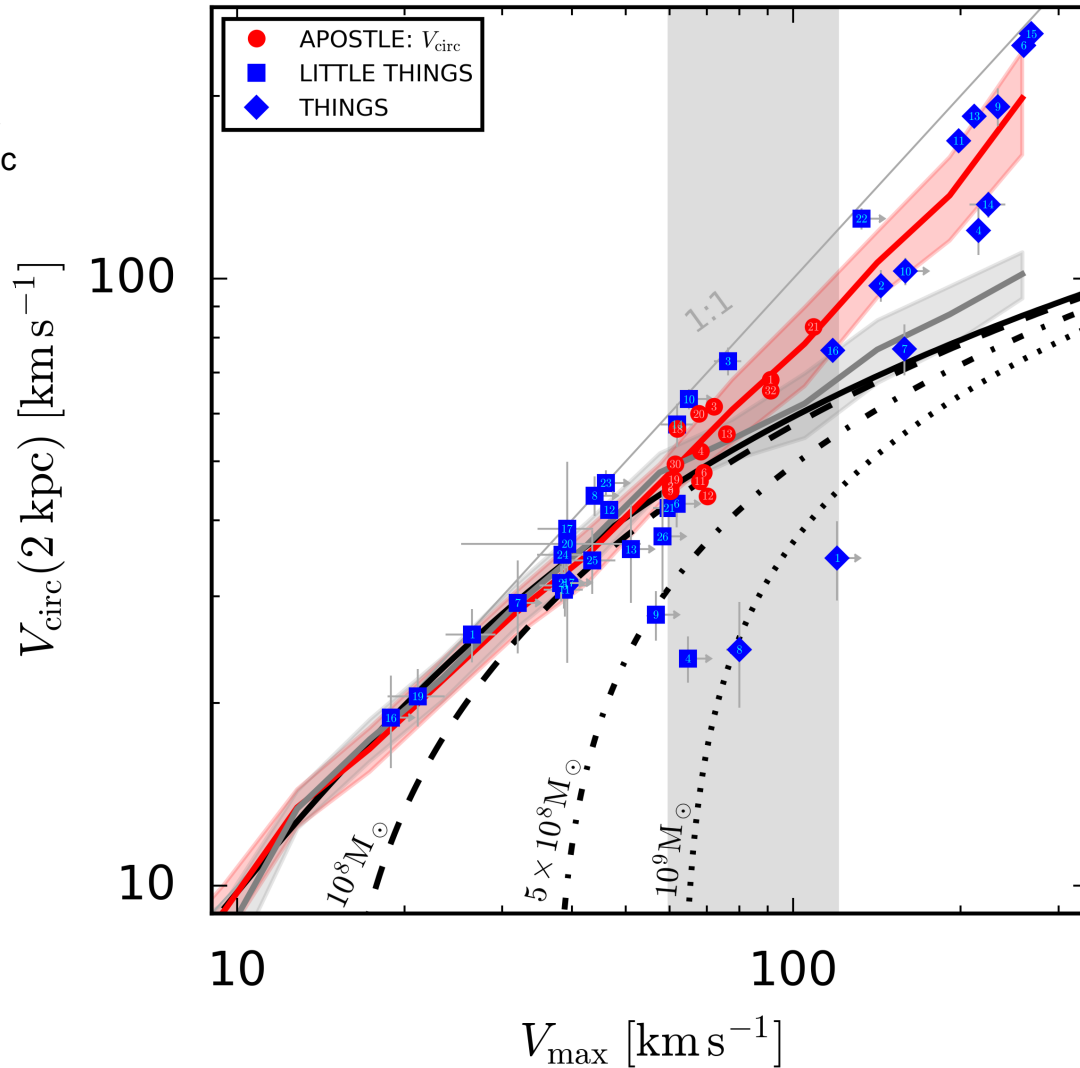
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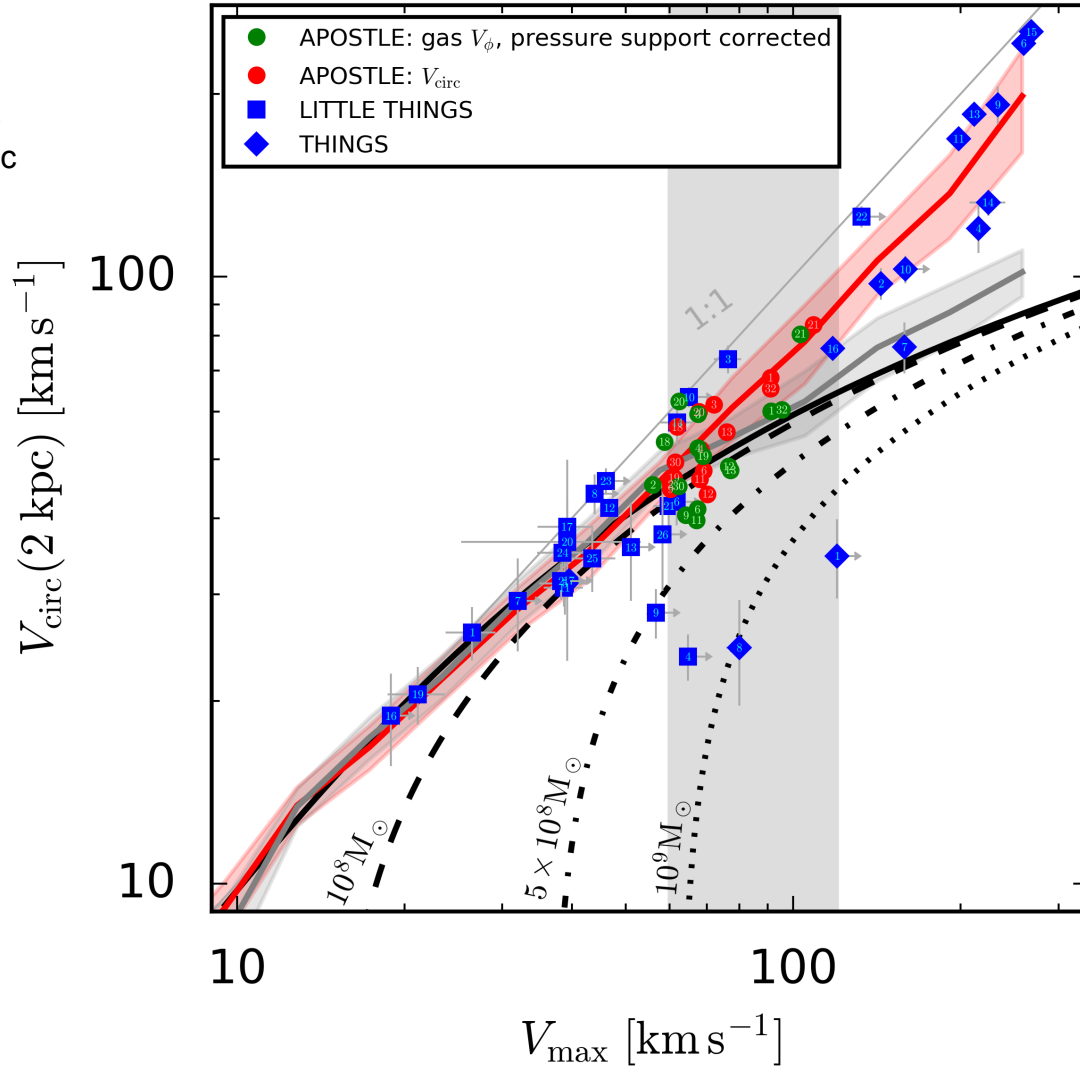
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$$V_c = \sqrt{\frac{GM}{r}}$$

$$V_{\max} = \max V_c$$



Analysis of 2D velocity fields

2D velocity field $\rightarrow V_c(r)$ (rotn curve); in dynamical equilibrium: $V_c = \sqrt{\frac{GM(< r)}{v}}$

\downarrow

\bullet 3D BAROLO fit

Tilted-ring model corrected for asymmetric drift

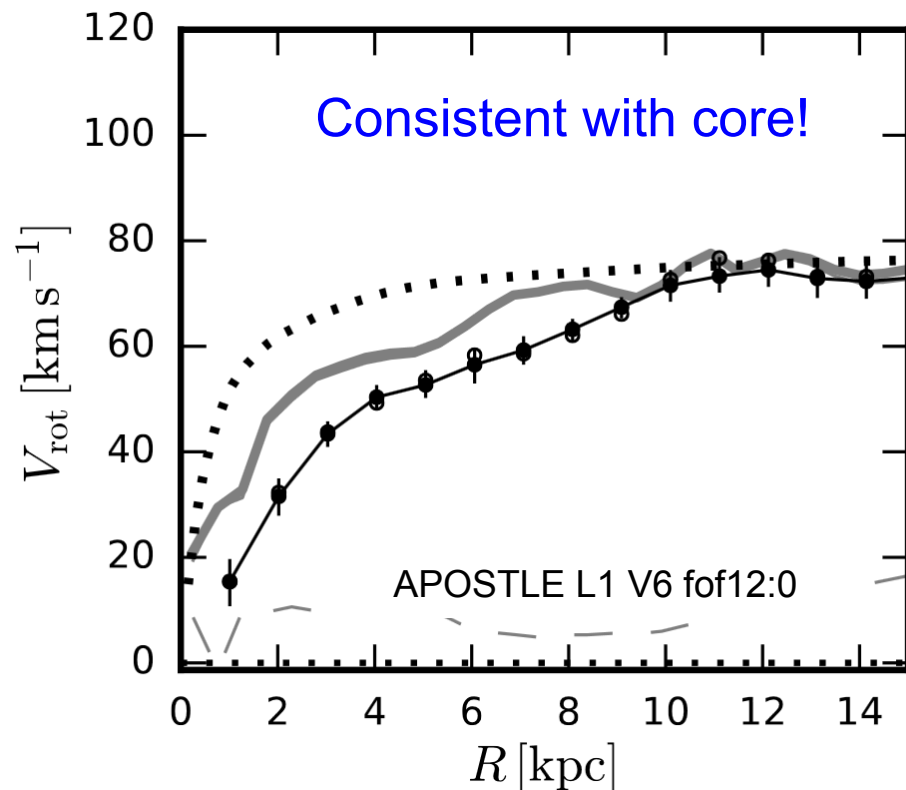
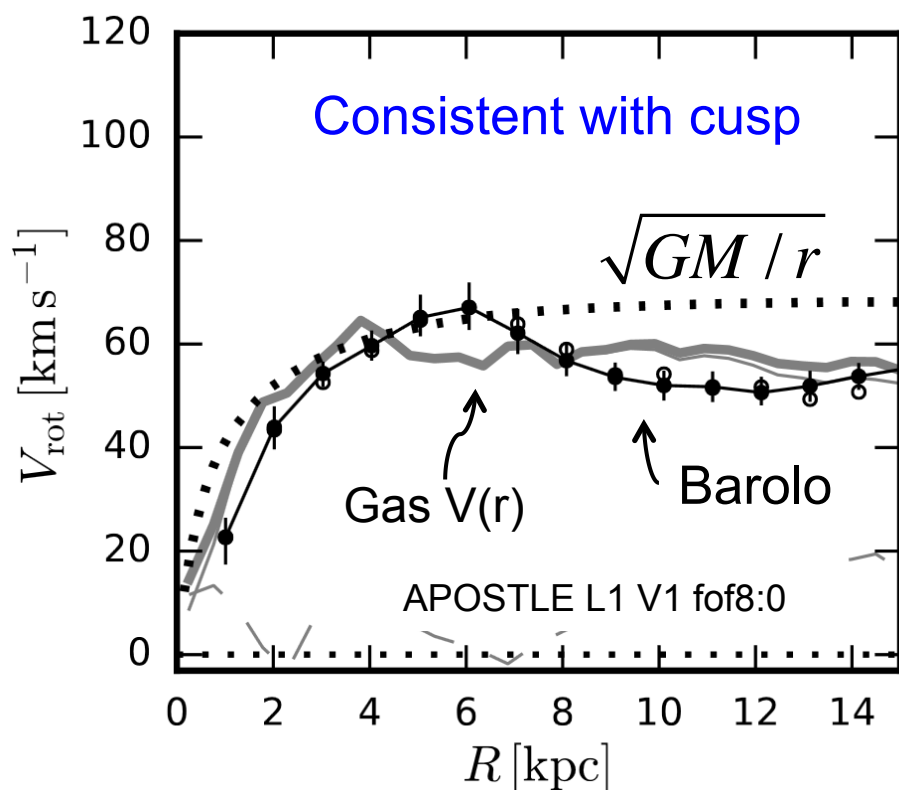
Let's apply this to APOSTLE galaxies by making a mock 2D velocity field data cube and analysing it just as the real data

Rotation curves of 2 APOSTLE dwarfs

APOSTLE galaxies all have NFW cusps

2D velocity field $\rightarrow V_c(r)$ (rotn curve); in dynamical equilibrium: $V_c = \sqrt{\frac{GM(<r)}{v}}$

\downarrow Tilted-ring model corrected for asymmetric drift
 \bullet ${}^3\text{D}$ BAROLO fit



Oman et al '18; Marasco et al '18

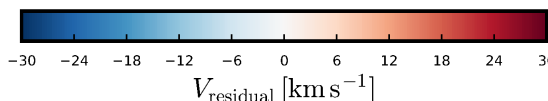
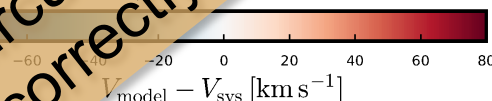
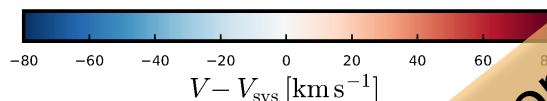
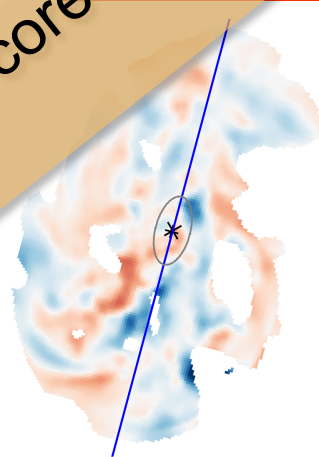
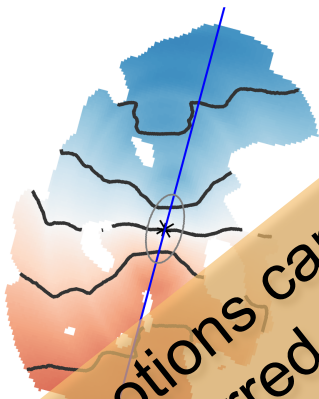
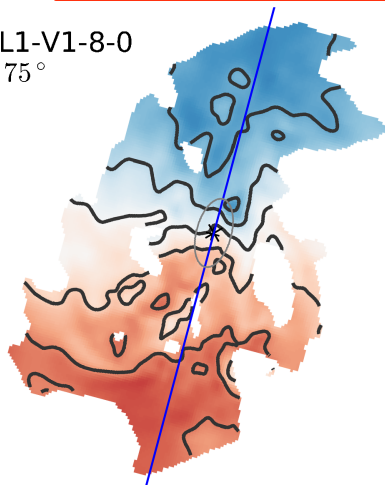
Non-circular motions

Obs. vel field

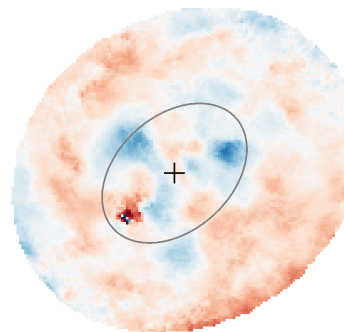
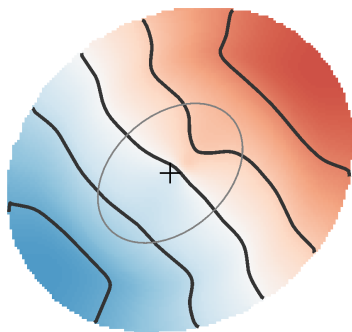
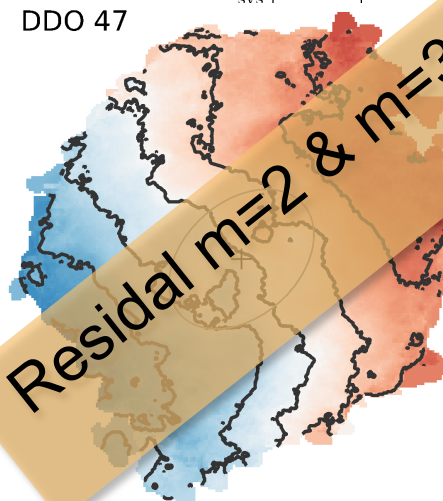
Barolo model

Residuals

AP-L1-V1-8-0
 $\Phi = 75^\circ$



DDO 47

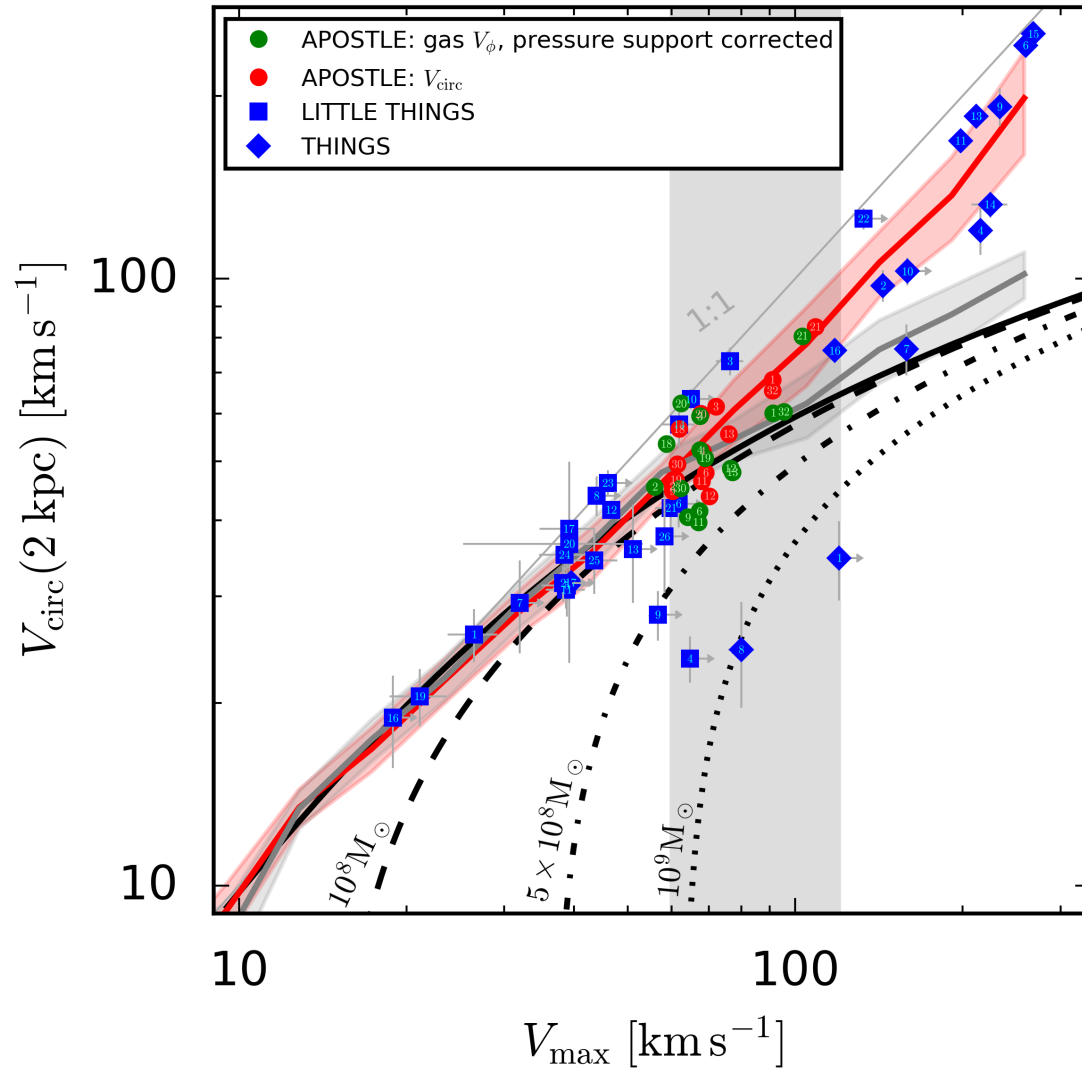


APOSTLE

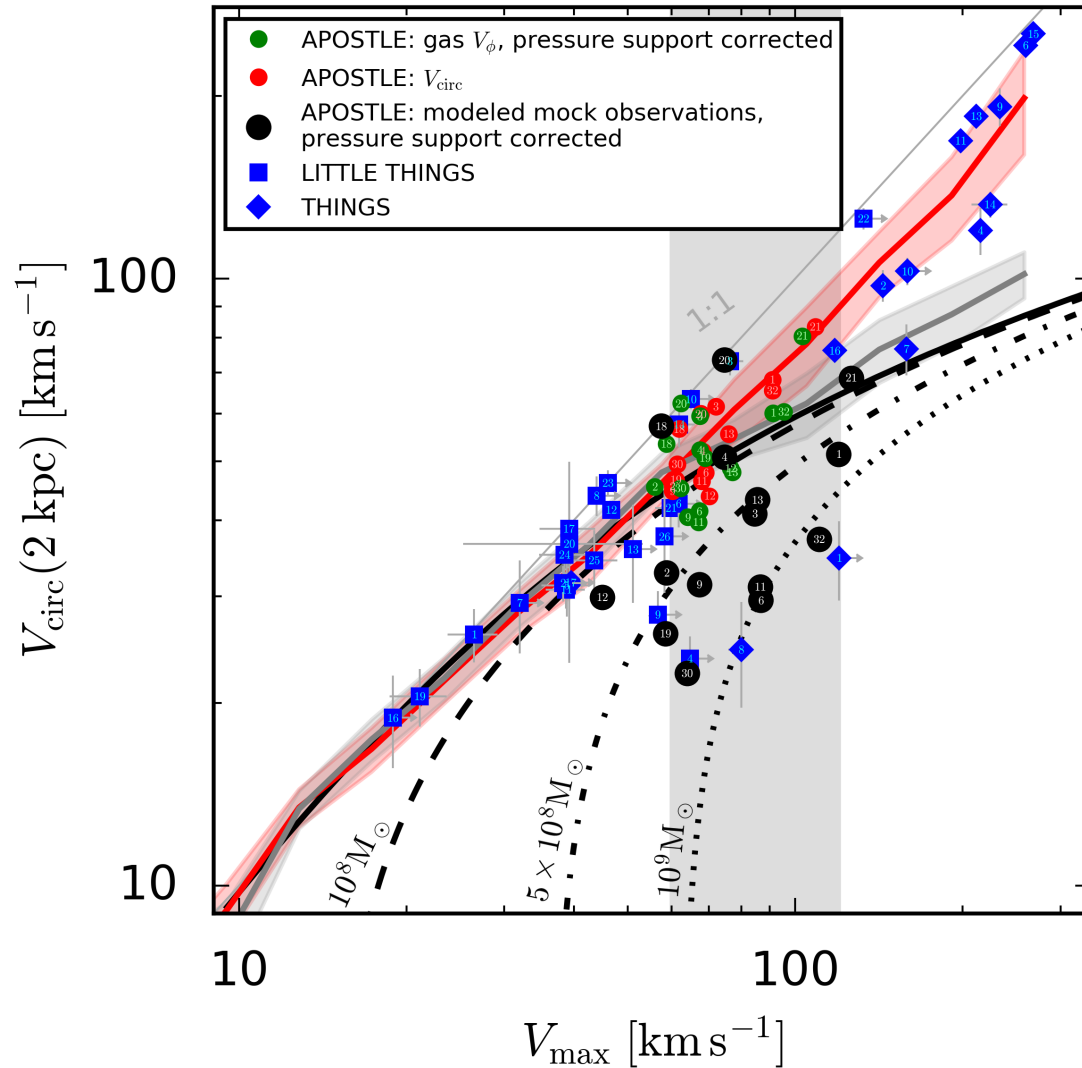
DDO 47

Residual $m=2$ & $m=3$ non-circular motions can cause a core to be incorrectly inferred

The diversity of rotation curves



The diversity of rotation curves





Cores or cusps in nature?



↓
Cores

↓
Cusps

No convincing evidence for cores in observed galaxies



But if cores were found in halos, would this rule out CDM (and WDM)?

The physics of core formation

Cusps → cores

Perturb central halo region
by growing a galaxy
adiabatically and removing
it suddenly (Navarro, Eke
& Frenk '96)

Cores may also form by
repeated fluctuations in
central potential (e.g. by
SN explosions) (Pontzen &
Governato '12,'14; Bullock
& Boylan-Kolchin '17)

Navarro, Eke & Frenk (1996)

The cores of dwarf galaxy haloes L75

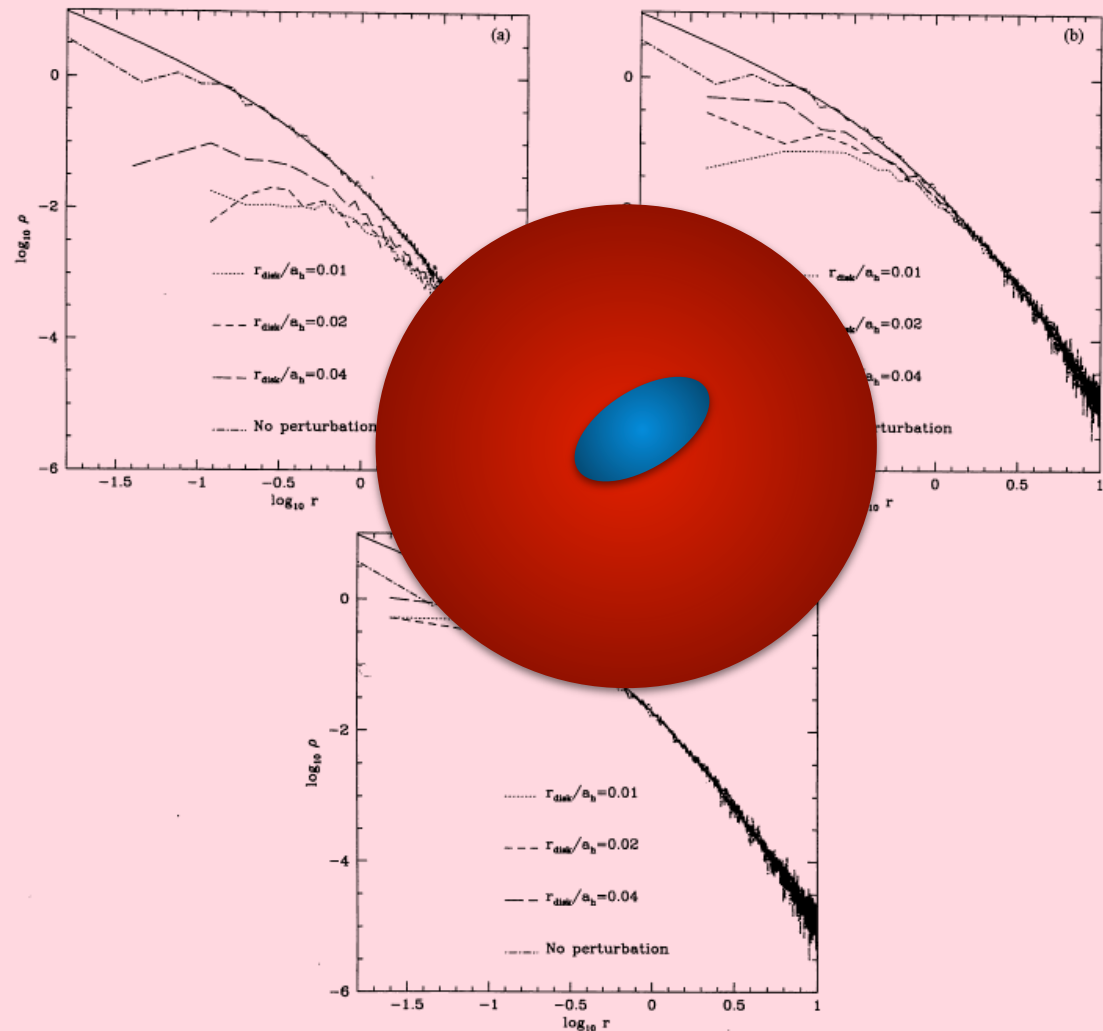


Figure 3. Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10 000-particle realization of the Hernquist model run in isolation at $t=200$. (a) $M_{\text{disc}}=0.2$. (b) $M_{\text{disc}}=0.1$. (c) $M_{\text{disc}}=0.05$.

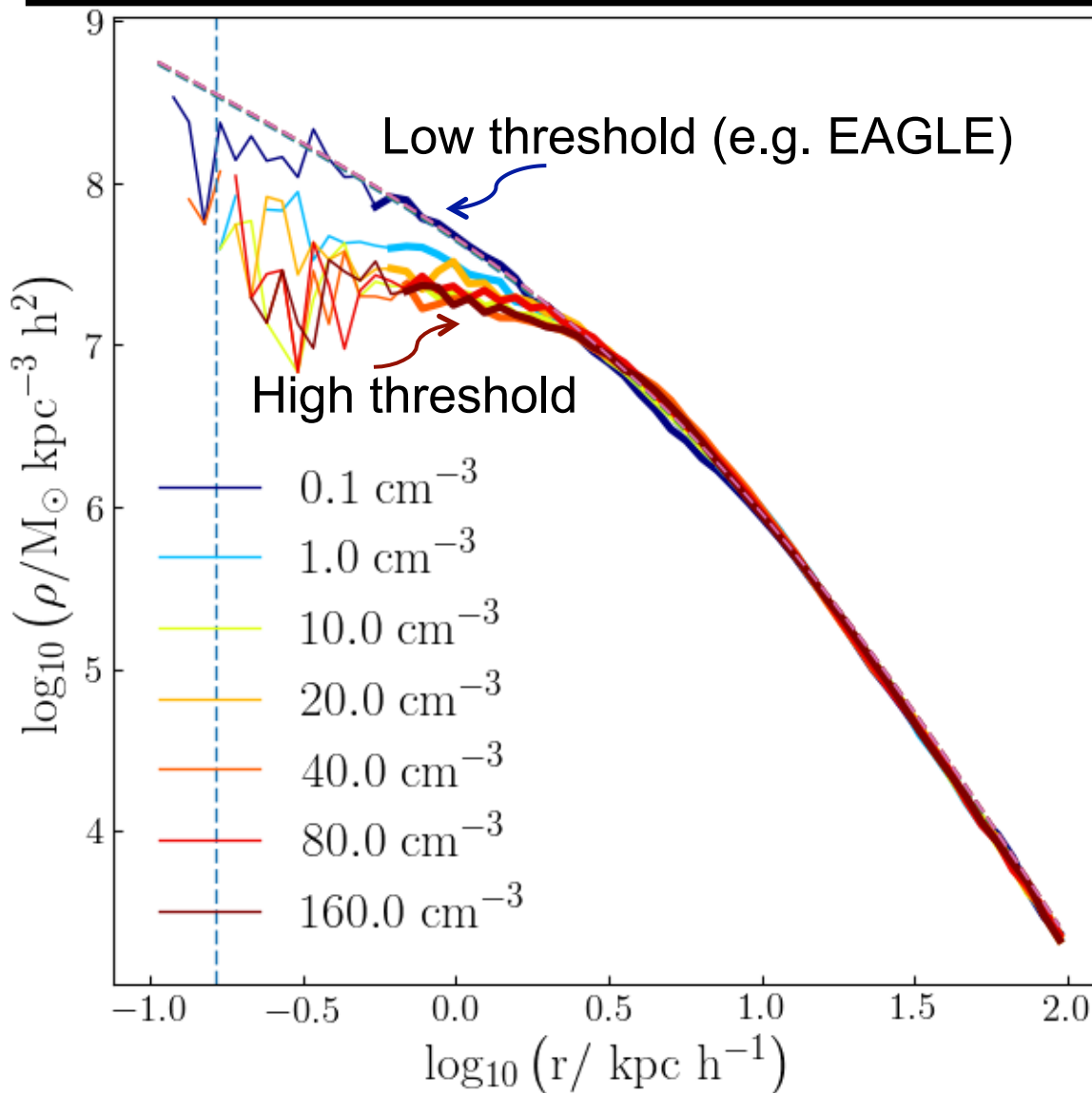
Cores or cusps in simulations?

Key parameter: gas density threshold for star formation

High density → NEF mechanism

Low density → not enough central gas density to perturb DM

Cores or cusps in simulations?



Four problems on small scales

Traditionally ascribed to CDM:

~~1. The “missing satellites” problem~~

~~2. The “too-big-to fail” problem~~

~~3. The “plane of satellites” problem~~

~~4. The “core-cusp” problem~~



Is there any way can
distinguish CDM from
WDM?

There is no need for
despair: there is a way
to distinguish them





Can we distinguish CDM/WDM?

cold dark matter

warm dark matter

Rather than counting faint galaxies,
count the number of dark halos

The subhalo mass function

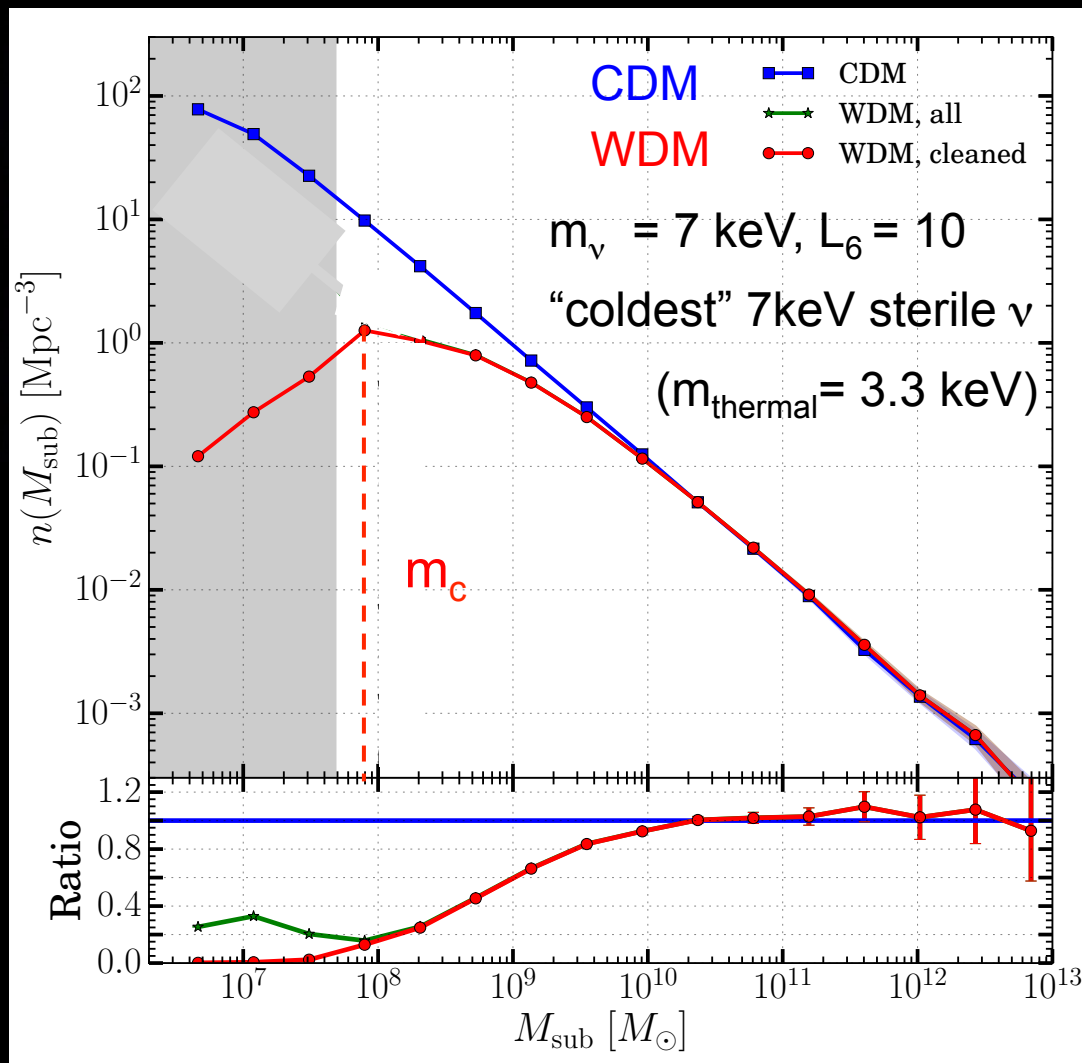


CDM

WDM

3 x fewer WDM subhalos at $3 \times 10^9 M_\odot$

10 x fewer at $10^8 M_\odot$





Can we distinguish CDM/WDM?

cold dark matter

warm dark matter

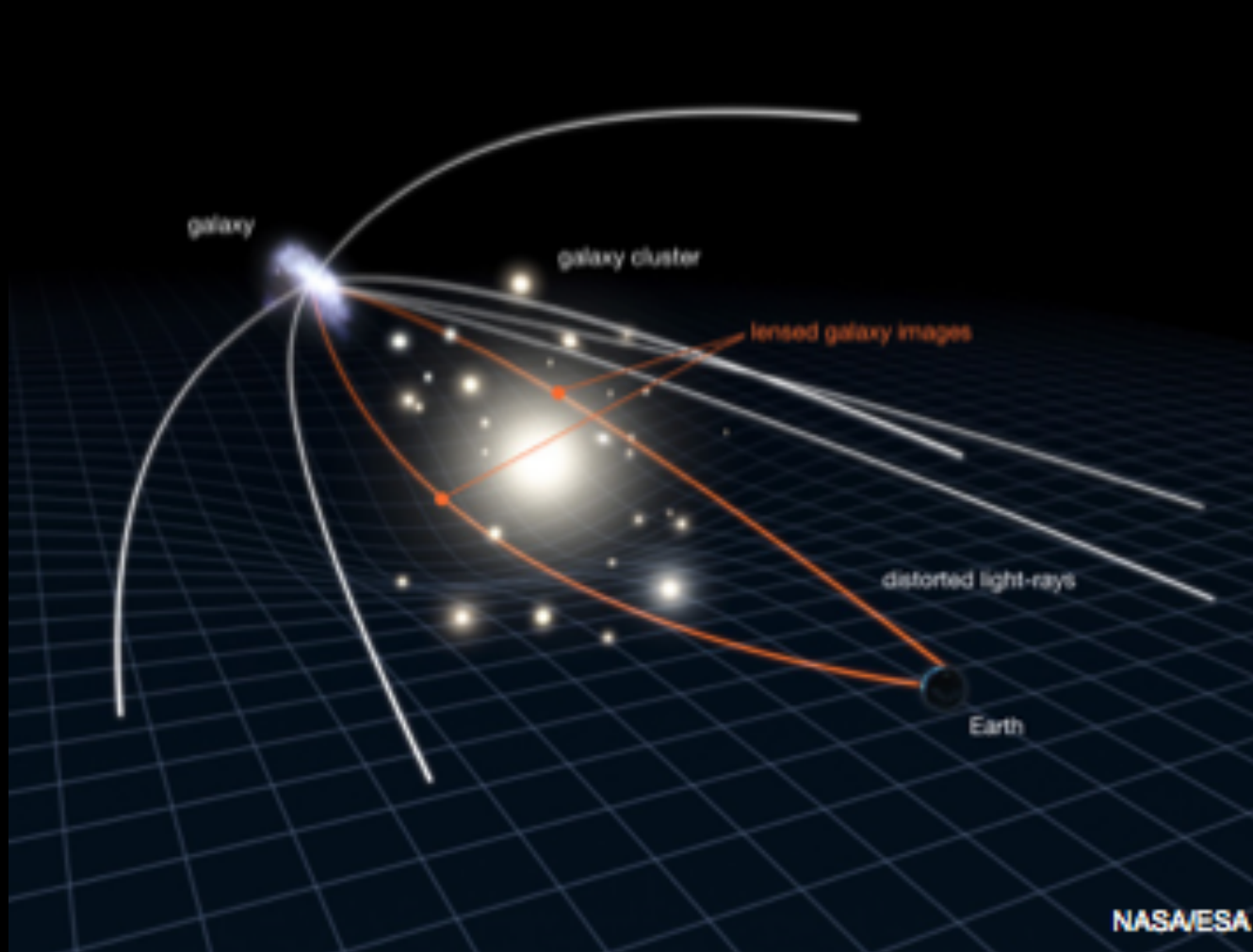
Dark halos can be detected through
gravitational lensing



Gravitational lensing: Einstein rings

How to rule out CDM

Gravitational lensing: Einstein rings



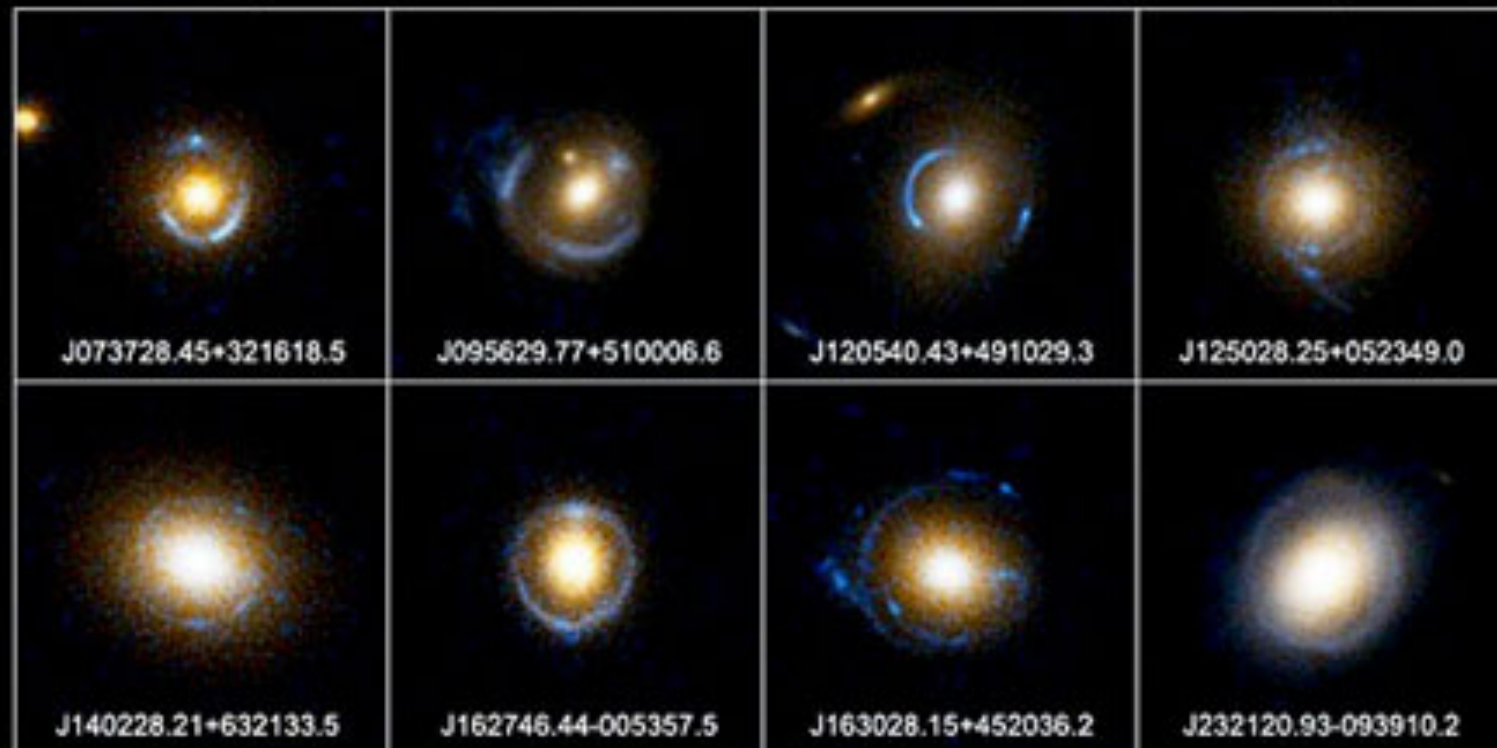
When the source and the lens are well aligned → strong arc or an Einstein ring



SLAC sample of strong lenses

Einstein Ring Gravitational Lenses

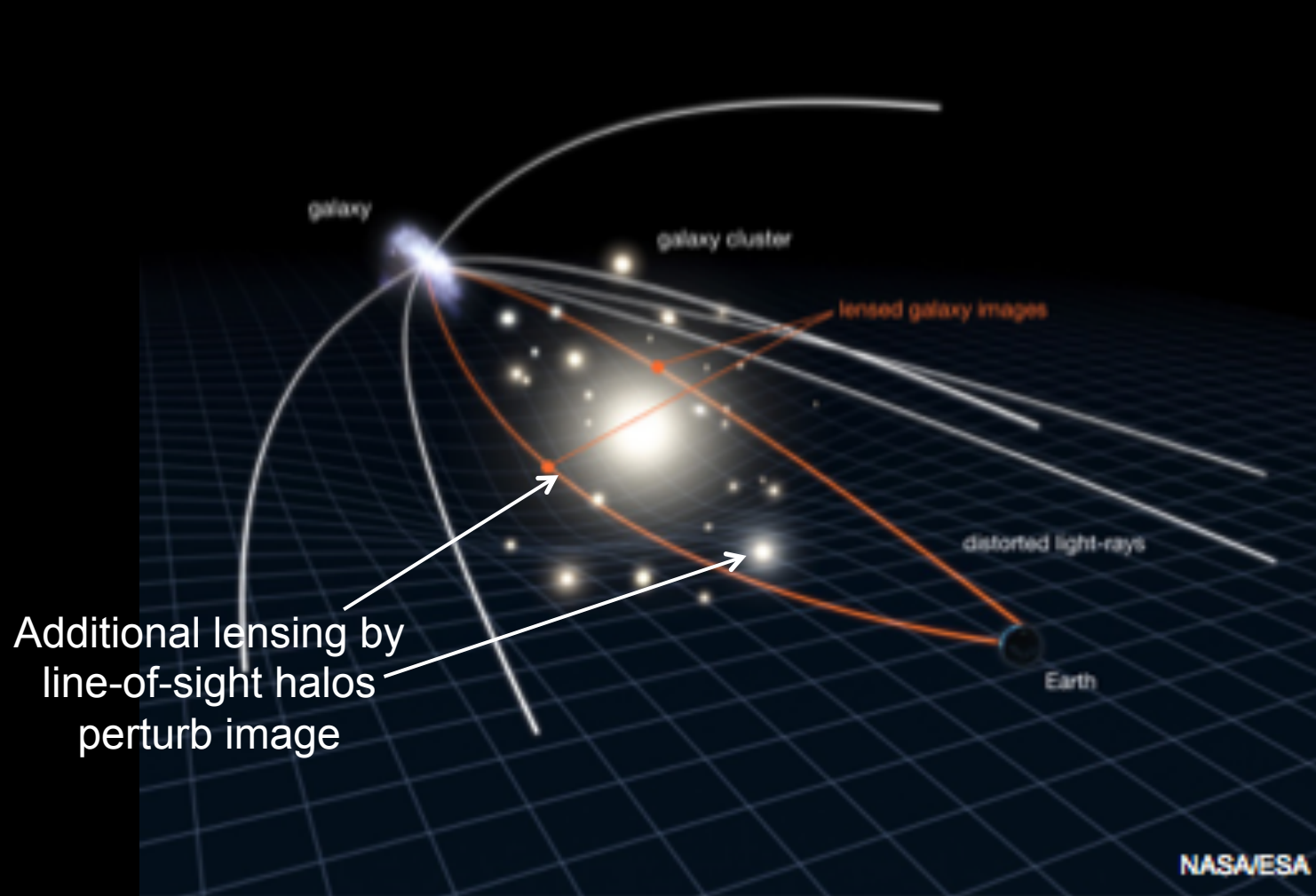
Hubble Space Telescope • ACS



NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

STScI-PRC05-32

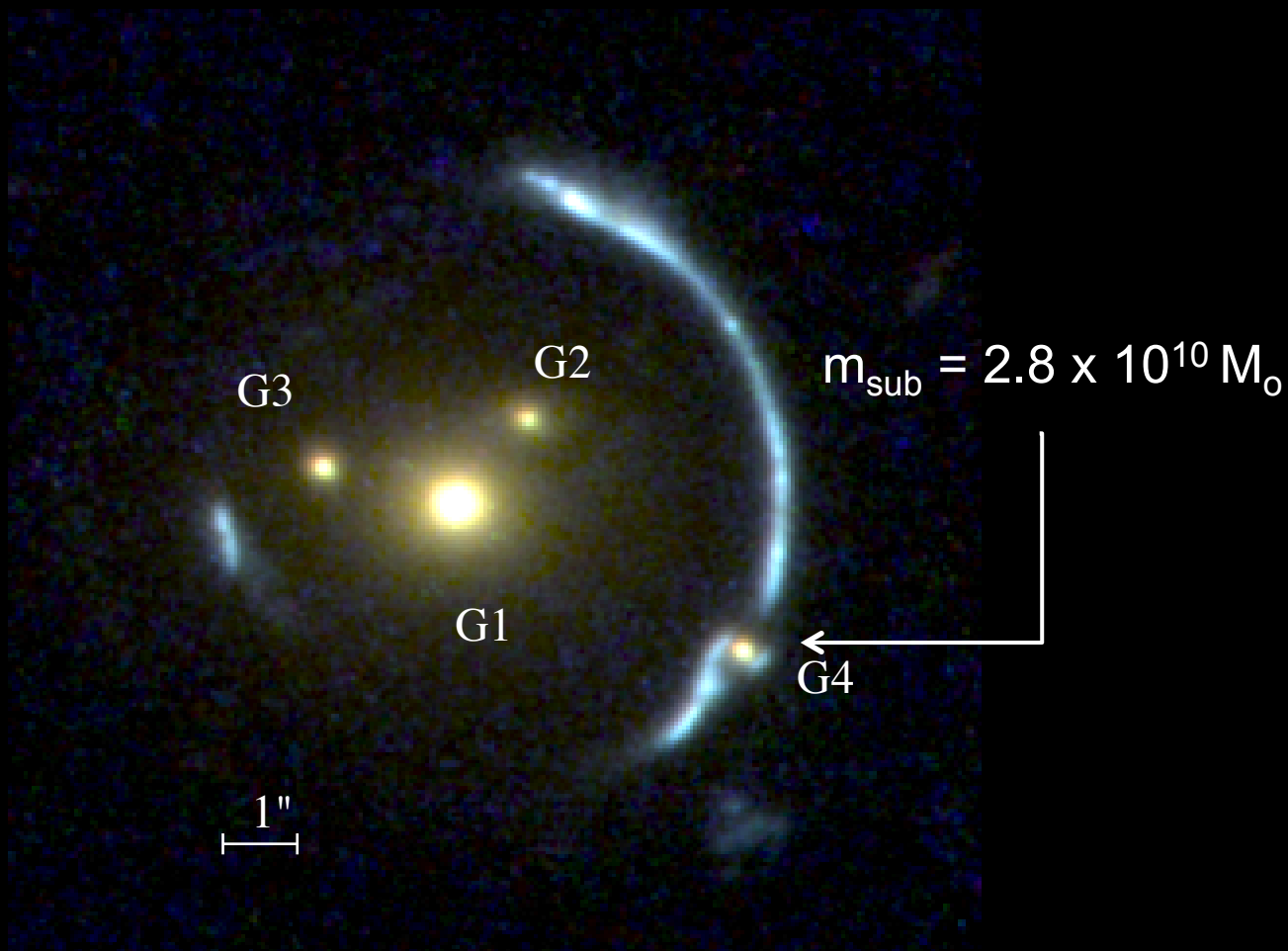
Gravitational lensing: Einstein rings



When the source and the lens are well aligned → strong arc or an Einstein ring

Gravitational lensing: Einstein rings

Halos projected onto an Einstein ring distort the image

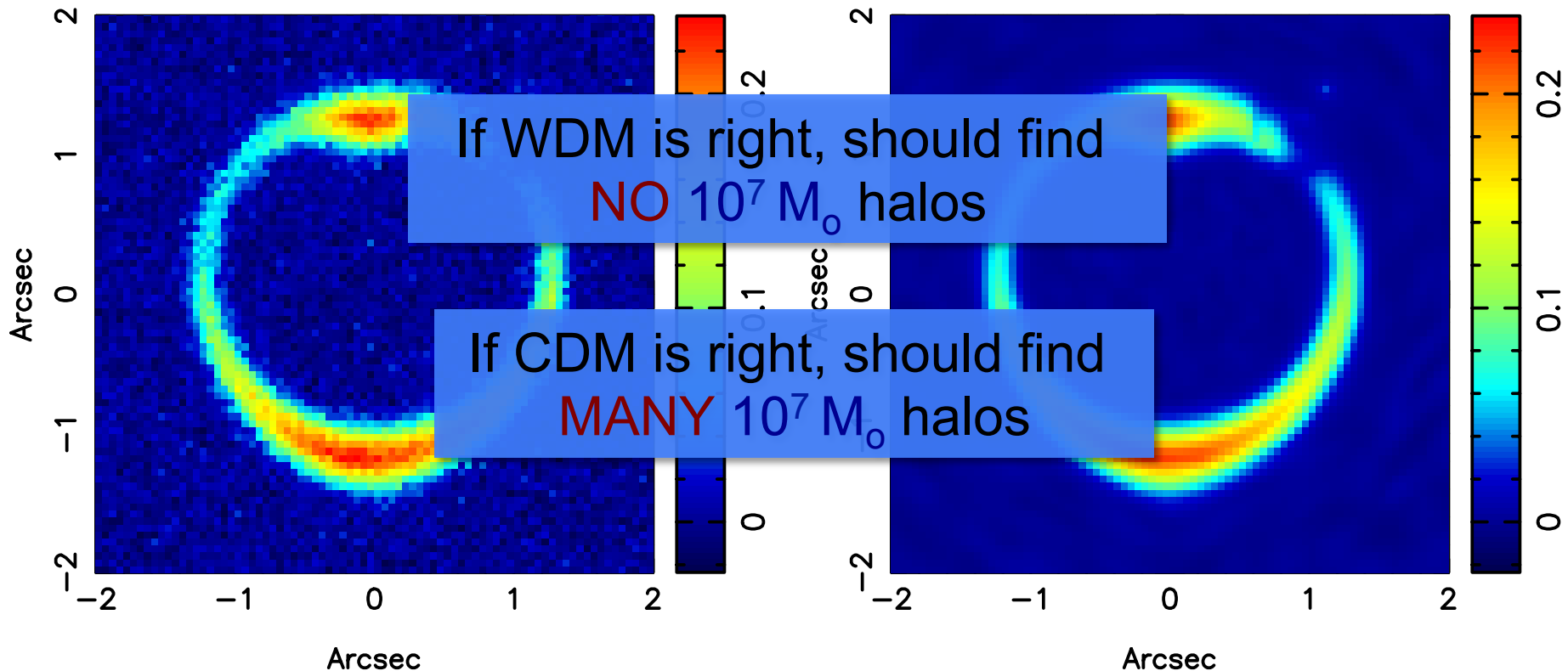


Detecting substructures with strong lensing

Can detect subhalos as small as $10^7 - 10^8 M_\odot$

Data

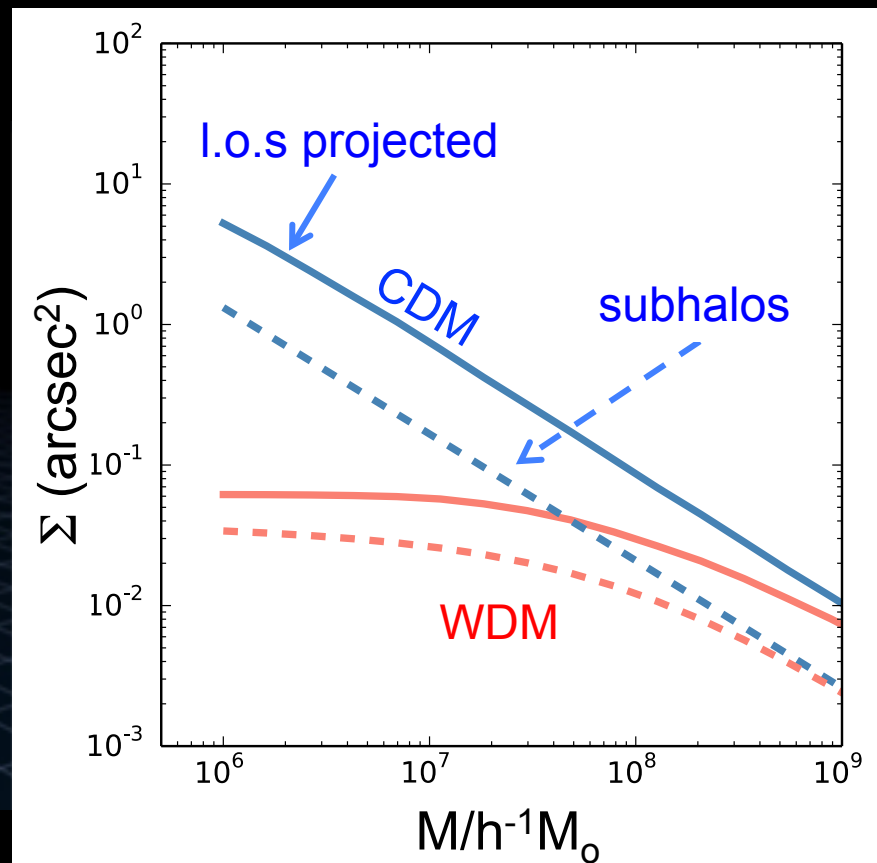
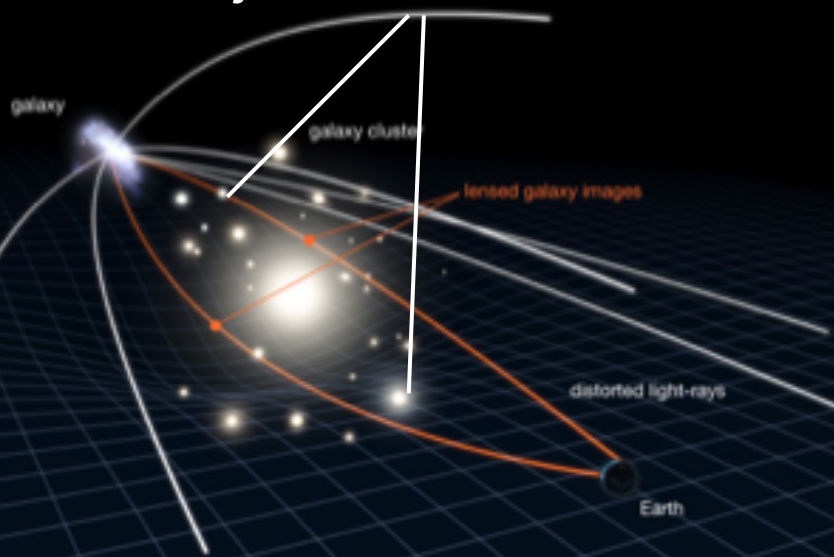
Model



Substructures vs interlopers

Subhalos & halos projected along the l.o.s both lens: who wins?

Projected l.o.s halos

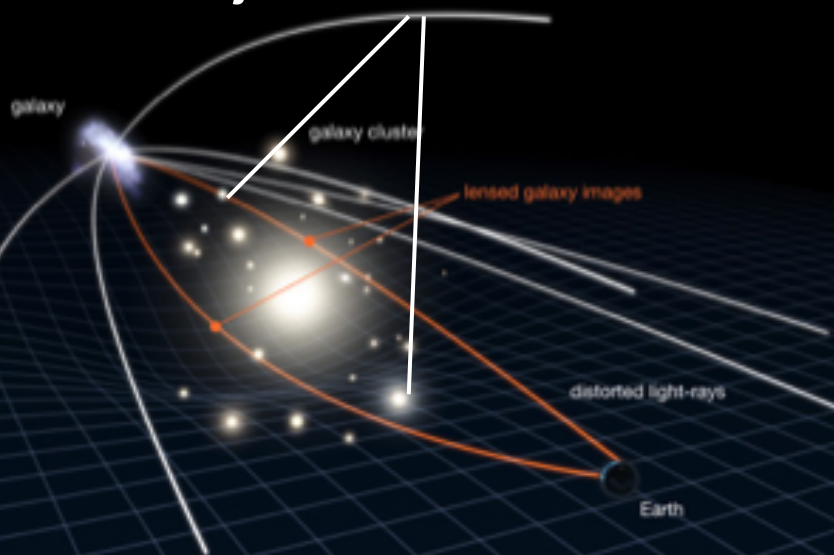


The number of line-of-sight haloes is larger than that of subhaloes

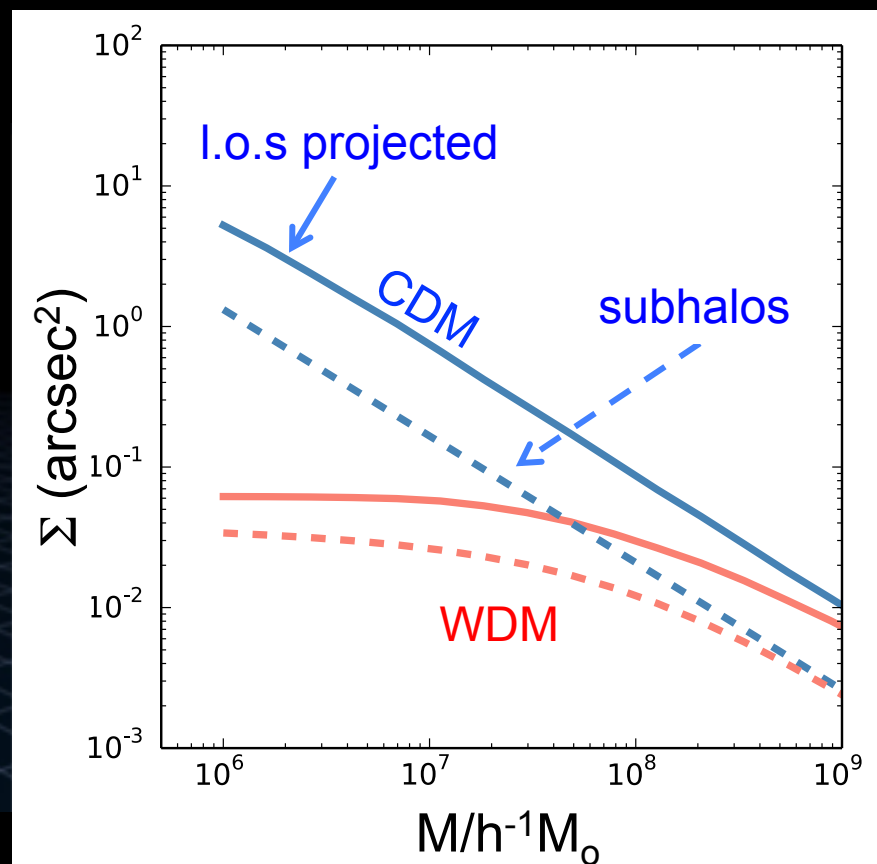
Substructures vs interlopers

Subhalos & halos projected along the l.o.s both lens: who wins?

Projected l.o.s halos



Li, CSF et al. '16



→ This is the **cleanest** possible **test**: it depends **ONLY** on the **small-mass** end of the “**field**” halo mass function which we know how to calculate and is **unaffected by baryons**

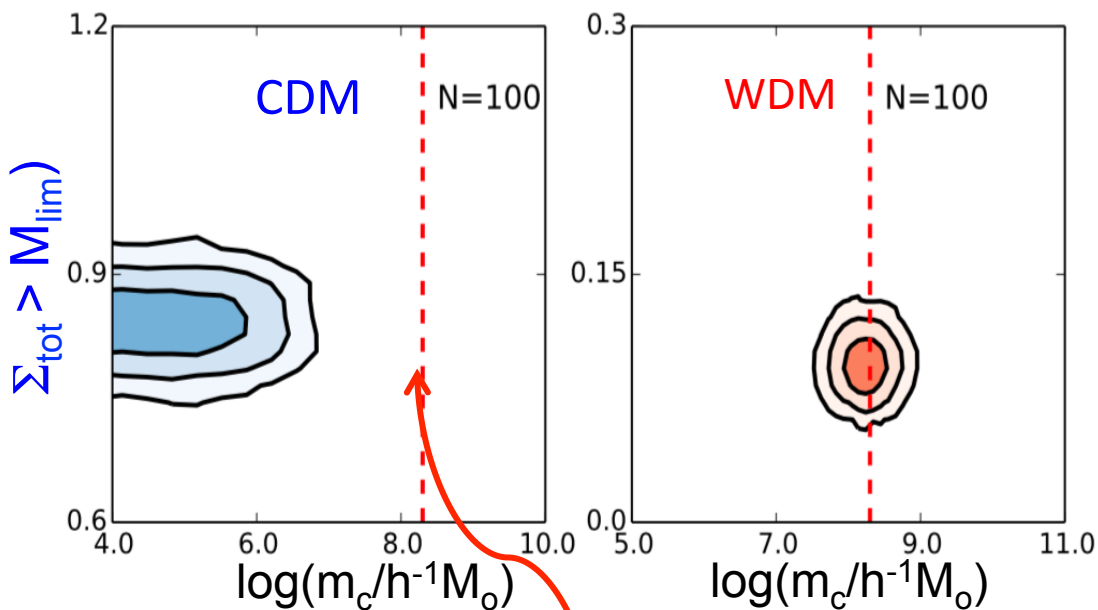
Detecting substructures with strong lensing

Σ_{tot} = projected halo number density within Einstein ring

m_c = halo cutoff mass

100 Einstein ring systems and detection limit: $m_{\text{low}} = 10^7 h^{-1} M_\odot$

Detection limit = $10^7 h^{-1} M_\odot$



m_c = halo cutoff mass

$m_c = 1.3 \times 10^8 h^{-1} M_\odot$ for coldest 7 keV sterile neutrino

- If DM is 7 keV sterile $\nu \rightarrow$ **exclude** CDM at $\gg \sigma$!
- If DM is CDM \rightarrow **exclude** 7 keV sterile ν at $\gg \sigma$



Conclusions

- Λ CDM: great **success** on scales $> 1\text{Mpc}$: CMB, LSS, gal evolution
 - But on these scales Λ CDM cannot be distinguished from WDM
 - The identity of the DM makes a big difference on small scales
1. Halos $< \sim 5 \cdot 10^8 M_\odot$ are dark; halos $> 10^{10} M_\odot$ are bright
 2. No evidence for cores; baryon effects can make them
 3. When **baryons** taken into account \rightarrow **No satellite, too-big-to-fail, plane of sats, core/cusp** problems in CDM
 4. Distortions of **strong** gravitational **lenses** offer a **clean test** of CDM vs WDM \rightarrow and can potentially **rule out** CDM!