

Johannes Hans Daniel Jensen (1907–1973)

Shell model of atomic nucleus





The standard model of cosmology

Carlos S. Frenk
Institute for Computational Cosmology,
Durham





... and how to rule it out



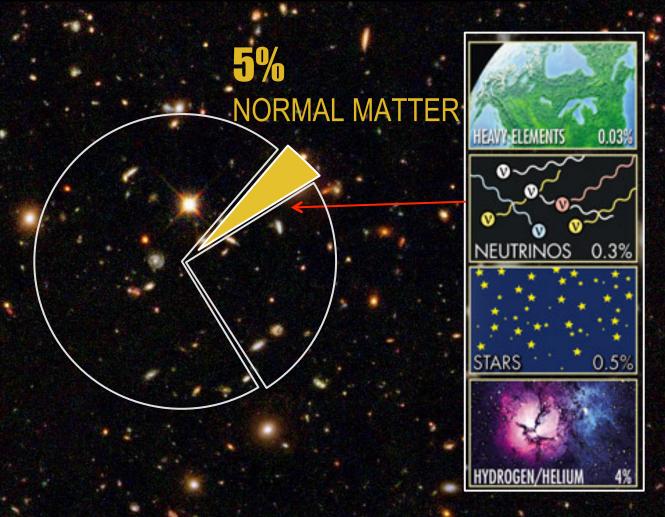
The ACDM model of cosmogony



- Ab initio, fully specified model of cosmic evolution and the formation of cosmic structure
- Has strong predictive power and can, in principle, be ruled out
- Has made a number of predictions that were subsequently verified empirically (e.g. CMB, LSS, galaxy formation)



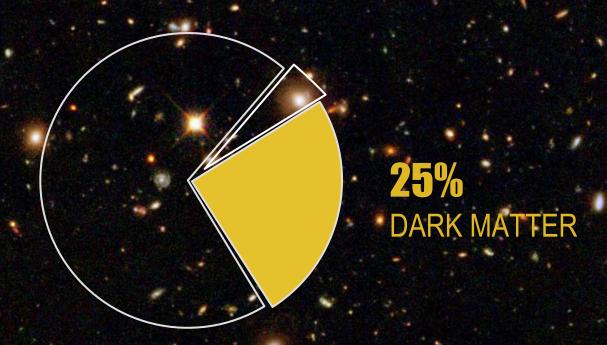
The content of our universe



Normal matter = matter made of ordinary atoms



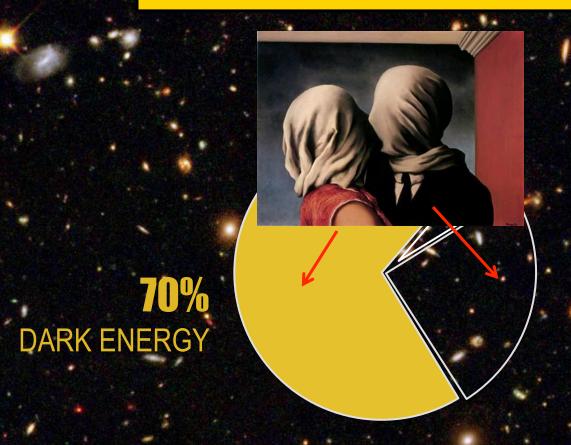
The content of our universe



Dark matter = matter that does not emit light at any wavelength



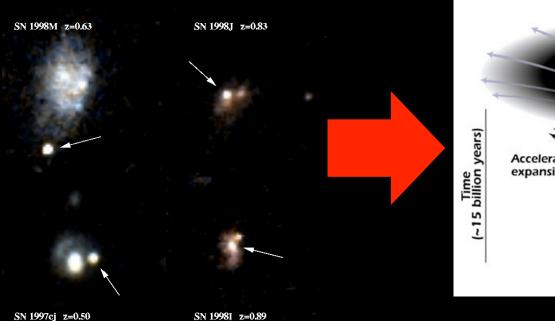
The content of our universe

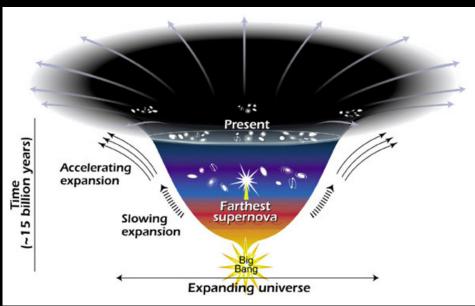


Dark energy = mysterious form of energy which opposes gravity and is causing the cosmic expansion to accelerate

The cosmic expansion

1998





Expansion is rating

2010 Nobel prize in physical k energy

omputational Cosmology



What is the cosmic dark energy?

A form of energy that produces a repulsive force, causing the universal expansion to accelerate

It is likely to be energy associated with empty space – the vacuum

Simplest possibility – Einstein's cosmological constant, A

The cosmic dark energy

Current physics predicts a "natural" value for the cosmological constant (Planck value)

$$\rho_{\Lambda}^{PL} \sim M_{PL}^4 \sim (8\pi G)^{-2} \sim (10^{18} GeV)^4 \sim 2 \times 10^{130} erg / cm^3$$

$$\rho_{\Lambda}^{obs} \sim (10^{-12} GeV)^4 \sim 2 \times 10^{10} erg/cm^3$$

10¹²⁰ larger than observed !!!

- Most inaccurate prediction in physics ever
- Requires new physics!
- But Λ consistent will everything we know



ICC The contents of the Universe

a = cosmic expansion factor

$$\rho_{tot} = \rho_{mass} + \rho_{rel} + \rho_{vac}$$

$$a^{-3} \qquad a^{-4} \qquad const?$$

 ρ_{vac} only became dominant about 4 billion years ago (z=1.5)

Universe dominated by matter in period when most structure forms

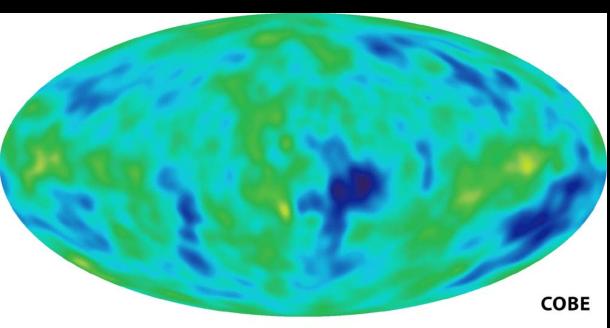
Cosmological constant not important for structure formation



The CMB







George Smoot - Nobel Prize 2006







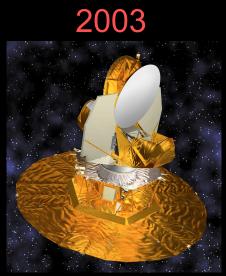
The CMB

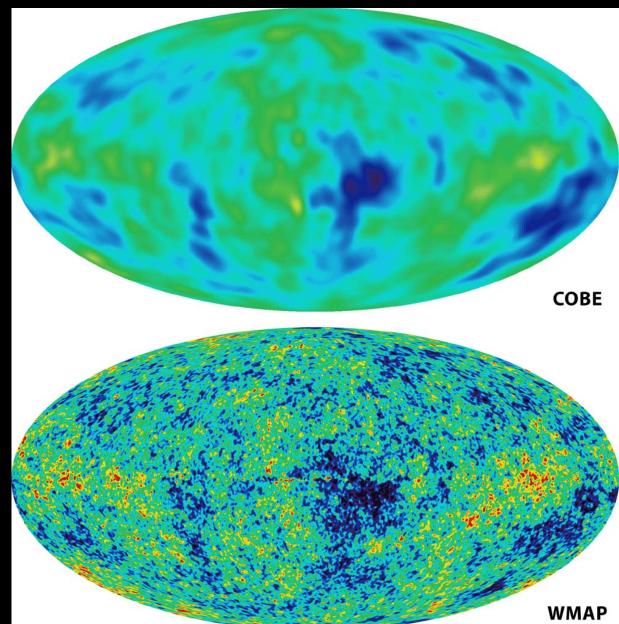
1992











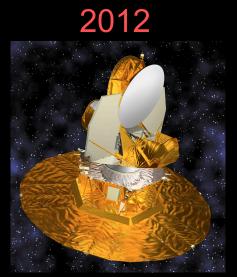


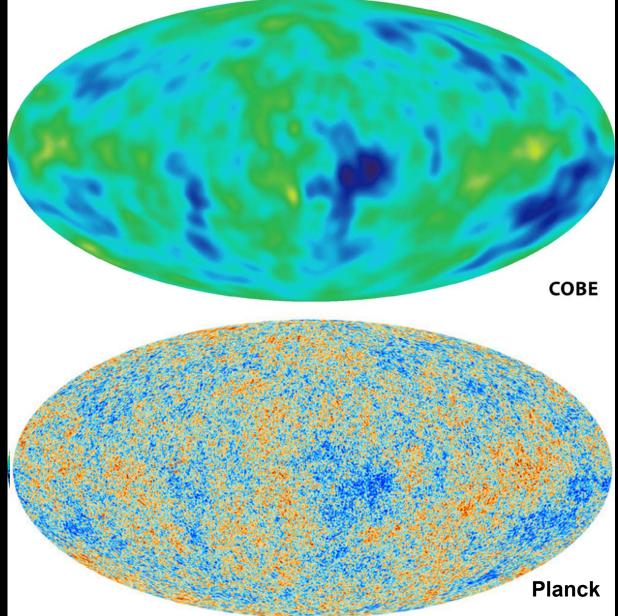
The CMB

1992



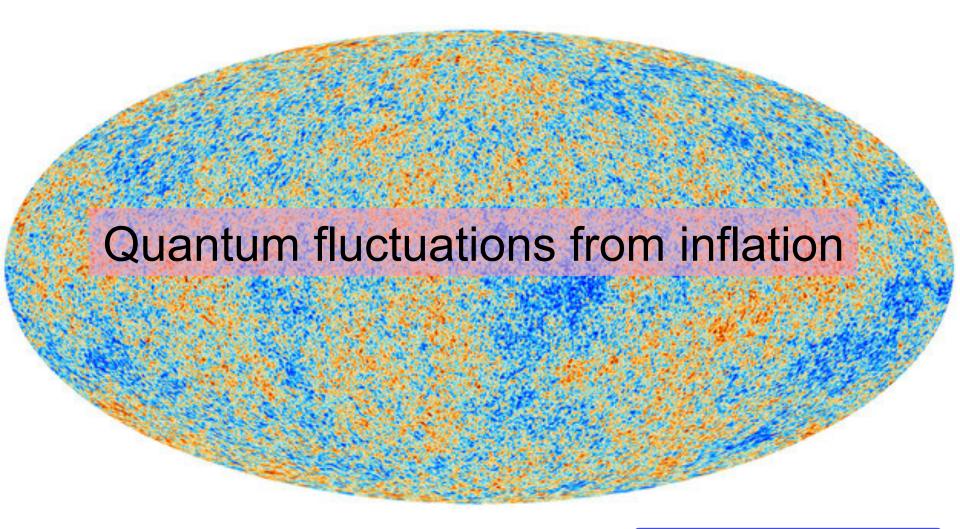






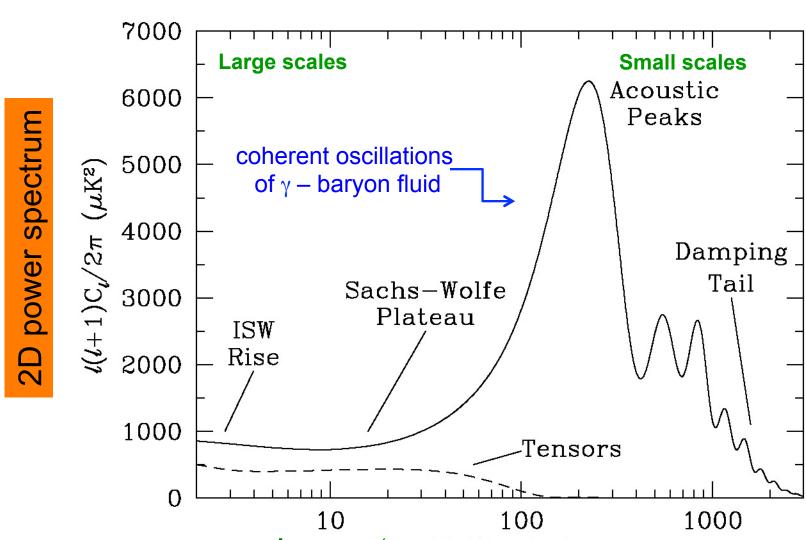


The initial conditions for galaxy formation





Temperature anisotropies in CMB

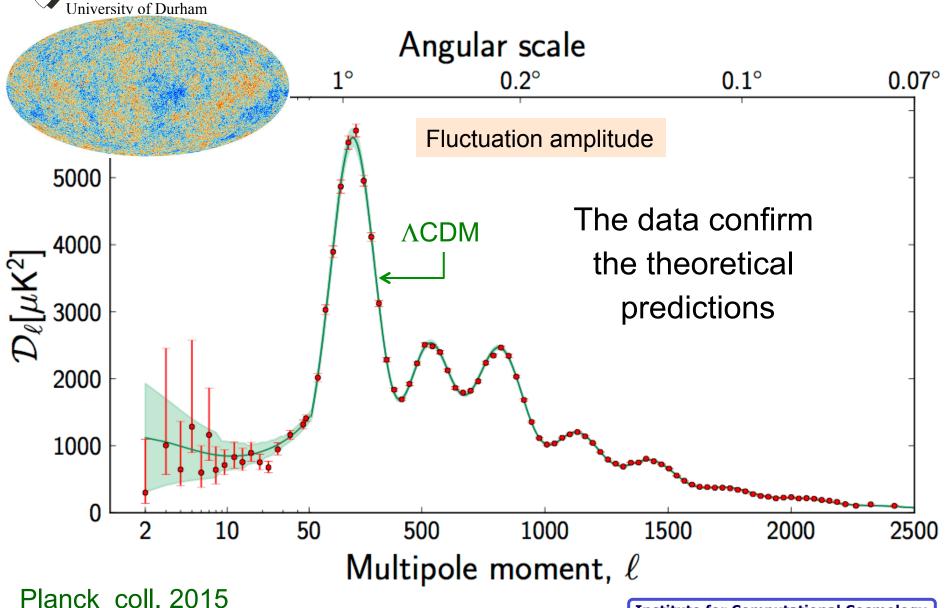


Peebles & Yu '70 Sunyev & Zel' dovich '70 Multipole l

For CDM: Peebles '82; Bond & Efstathiou '84



Planck: CMB temperature anisotropies





The six parameters of minimal \(\Lambda \)CDM model

		Planck+WP		
(0	Parameter	Best fit	68% limits	
lel parameters	Parameter $\frac{\Omega_{\rm b}h^2}{\Omega_{\rm c}h^2}$ $100\theta_{\rm MC}$ 7 $\frac{1}{100} \frac{100}{100} \frac$	0.022032	0.02205 ± 0.00000	data!
	$\Omega_{ m c}h^2$	0.12038	r Using 911 0.0027	
	$100\theta_{\mathrm{MC}}$	darkmatte	1.04131 ± 0.00063	
шос	τ of non-baryonie	0.0925	$0.089^{+0.012}_{-0.014}$	
9	detection of the	0.9619	0.9603 ± 0.0073	
AAUC	$\ln(10^{10}A_{\mathrm{s}})\ldots\ldots$	3.0980	$3.089^{+0.024}_{-0.027}$	

Planck collaboration '13



Non-baryonic dark matter candidates

From the early 1980s:

Т	ype	example	mass

hot	neutrino	few tens of eV
warm	sterile v	keV-MeV
cold	axion neutralino	10-⁵eV - 100 GeV

-7-

$m_v = 30 \text{ ev} \rightarrow \Omega = 1$

HAS THE NEUTRINO A NON-ZERO REST MASS? (Tritium β-Spectrum Measurement)

V. Lubimov, E. Novikov, V. Nozik, E. Tretyakov
Institute for Theoretical and Experimental Physics, Moscow, U.S.S.R.

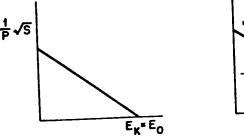
V. Kosik
Institute of Molecular Genetics, Moscow, U.S.S.R.

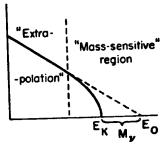
ABSTRACT

The high energy part of the β -spectrum of tritium in the ν molecule was measured with high precision by a toroidal β -spectrum eter. The results give evidence for a non-zero electron antineutrino mass.

Fifty years ago Pauli introduced the neutrino to explain the 2-spectrum shape. Pauli made the first estimate of the neutrino mass (E $_3$ max $\stackrel{?}{=}$ nuclei mass defect): it should be very small or maybe zero. Up to now the study of the β -spectrum shape is the most sensitive, direct method of neutrino mass measurement.

most sensitive, direct method of neutrino mass measurement. For allowed β -transitions, if $M_v = 0$, then $S \simeq (E-E_0)^2$. The Kurie plot is then a straight line with the only kinematic parameter being $E_k = E_0$ (total β -transition energy). If $M_v \neq 0$, then $S \simeq (E_0-E)^{V}(E_0-E)^{2}-M_V^2$. The Kurie plot is then distorted, especially near the endpoint.





1981

Fig. 1. Kurie plot for $M_y = 0$. Fig. 2. Kurie plot for $M_y \neq 0$.

The method for the neutrino mass measurement is to obtain E_0 from the extrapolation and obtain E_k from the spectrum intercept. Then $H_0 = E_0 - E_k$. Qualitatively, $H_0 \neq 0$ if the β -spectrum near the endpoint runs below the extrapolated curve.

things are more complicated. The apparatus resorongly affects the spectrum endpoint and rather e spectrum slope.

M_y=0

M_y<R

Background

E₀

ealistic Kurie plot.

extrapolation. However, we are unable indicate that $M_{\nu} \neq 0$. If $M_{\nu} \leq R$, the changes due to mass and the influence of R are indistinguishable. For M_{ν} cermination the knowledge of R is compulsory. The background determines the statistical accuracy near the endpoint, i.e., in the region of the highest sensitivity to the ν mass. So: 1) R should be ν M_{ν}, 2) the smaller M_{ν} is, the smaller the background (ν M $_{\nu}$) must be and the higher the statistics (ν M $_{\nu}$) must be. For example, suppose that for M_{ν} = 100 eV we need resolution R, background Q, and statistics N. If M_{ν} = 30 eV, to achieve the same ν M/M they should be R/3, Q/10, and N × 30, respectively.

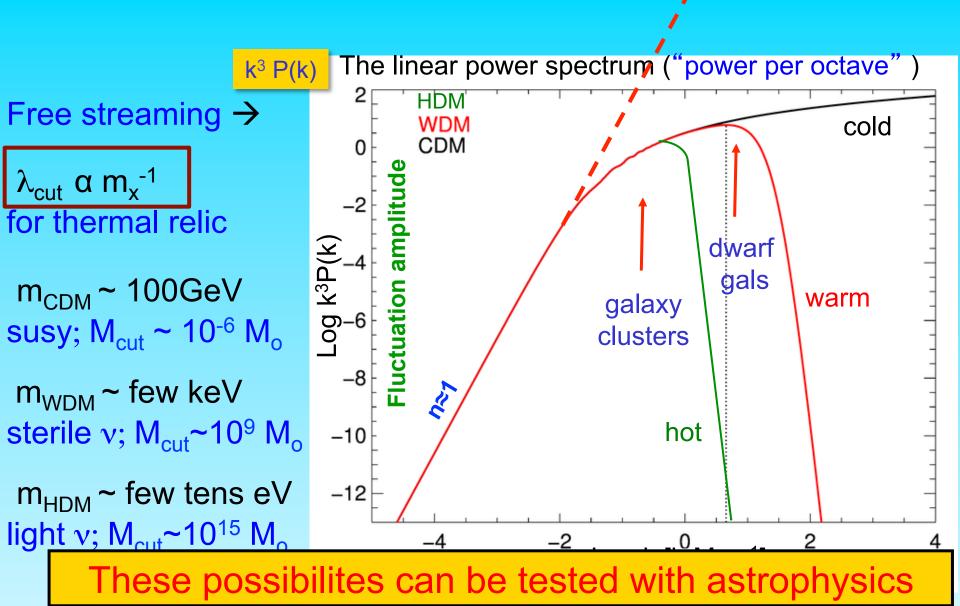
The shorter the β -spectrum, the less it is spread due to R (as R $\sim \Delta p/p = {\rm const.}$). A classical example is 3H β -decay, which has 1) the smallest $E_0 \sim 18.6$ keV, 2) an allowed β -transition, simple nucleus, and simple theoretical interpretation, 3) highly reduced radioactivity. The first experiments with 3H were by S. Curran et al. (1948) and G. Hanna, B. Pontecorvo (1949). Using 3H gas in a proportional counter, they obtained $M_{\odot} \leq 1$ keV. Further progress required magnetic spectrometer development. This allowed the resolution to be improved considerably, and L. Langer and R. Moffat (1952) obtained $M_{\odot} \leq 250$ eV. The best value was obtained by K. Bergkvist (1972): R ~ 50 eV and $M_{\odot} \leq 55$ eV.

The ITEP spectrometer is of a new type: ironless, with toroidal magnetic field (E. Tretyakov, 1973). The principle of the toroidal magnetic field focusing systems was proposed by V. Vladimirsky et al. (An example is a "Horn" of ν -beams.) It turns out that a rectilinear conductor (current) has a focusing ability for particles emitted perpendicular to the rotation axis. This system has infinite periodical focusing structure. The ITEP spectrometer is based on this principle.

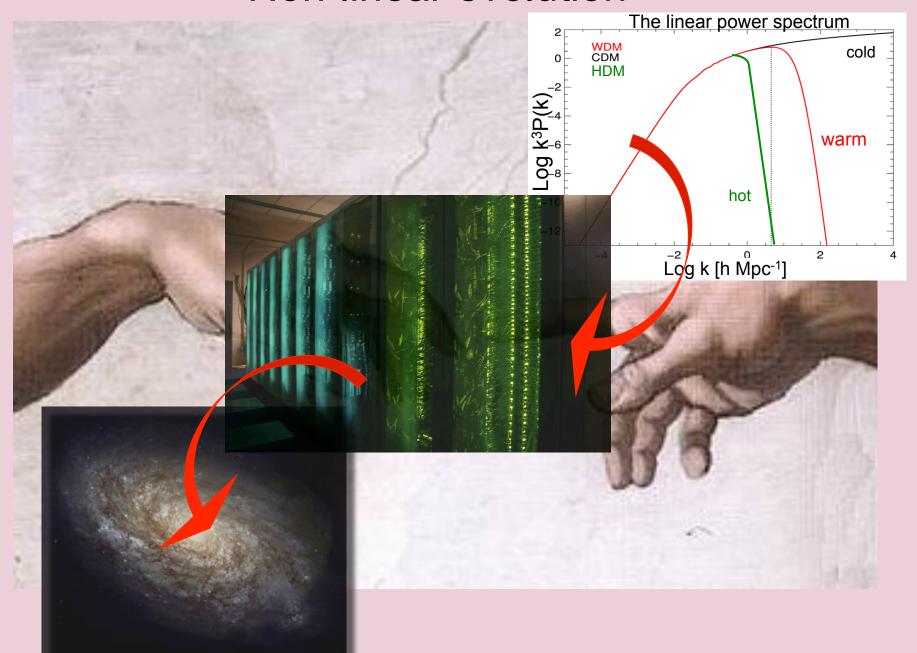
Paper presented by Oleg Egorov.



The dark matter power spectrum



Non-linear evolution





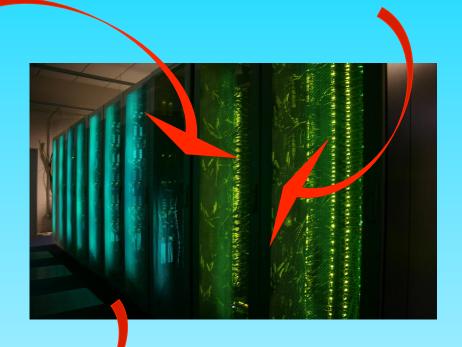
Non-linear evolution: simulations

Initial conditions + assumption about content of Universe

Relevant equations:

Collisionless Boltzmann, Poisson, Friedmann eqn, Radiative hydrodynamics Astrophysics (subgrid)

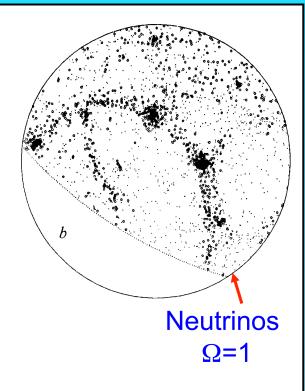




How to make a virtual universe



Non-baryonic dark matter cosmologies



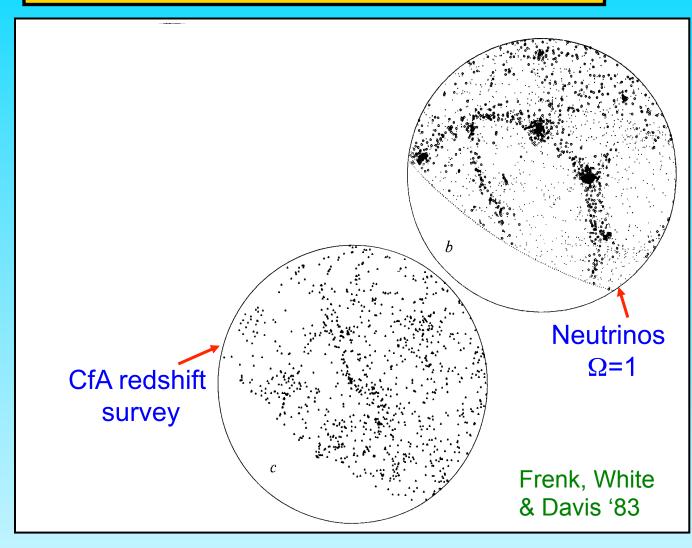
Frenk, White & Davis '83



Neutrino DM → wrong clustering

Neutrinos cannot make appreciable contribution to Ω \rightarrow m_v << 30 ev

Non-baryonic dark matter cosmologies





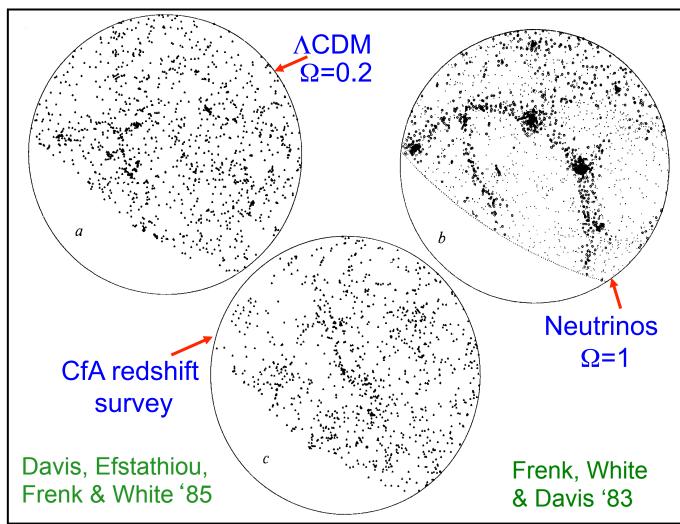
Neutrino DM → wrong clustering

Neutrinos cannot make appreciable contribution to Ω \rightarrow m,<< 30 ev

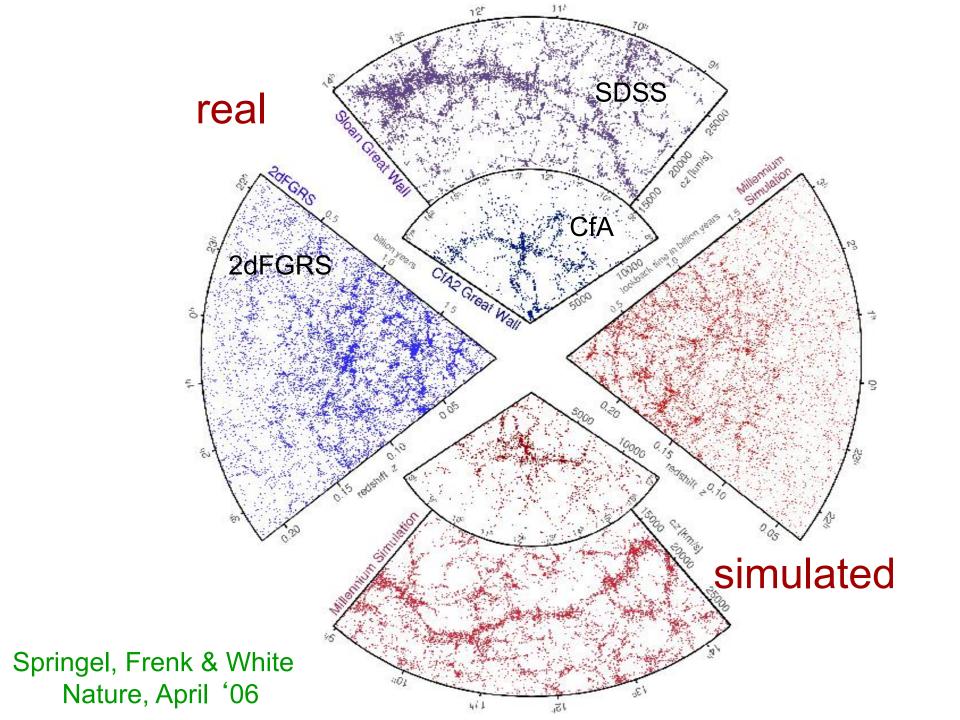
Early CDM N-body simulations gave promising results

In CDM structure [forms hierarchically

Non-baryonic dark matter cosmologies



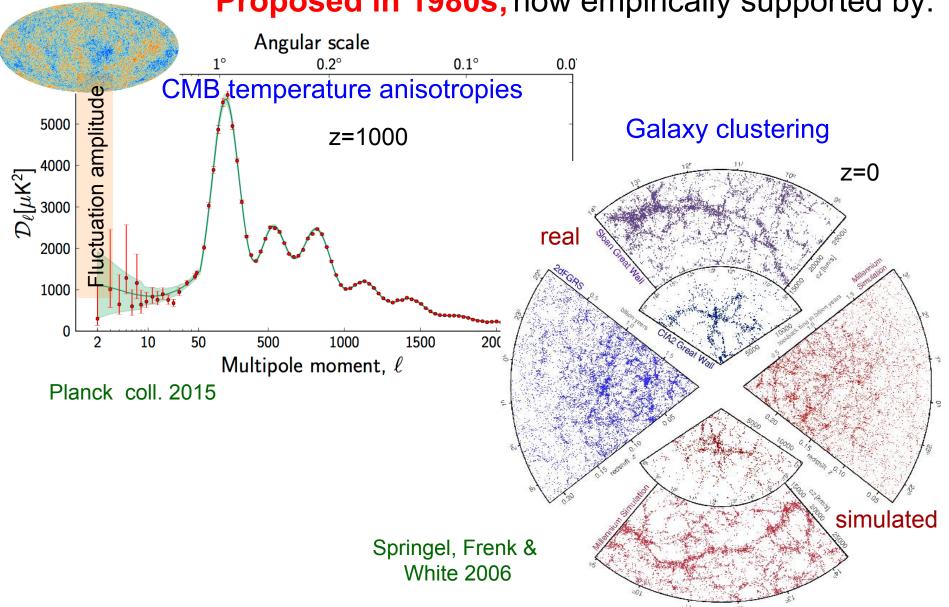






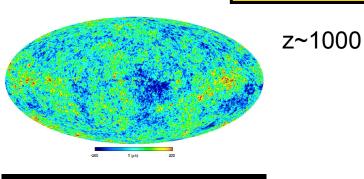
The ACDM model of cosmogony

Proposed in 1980s; now empirically supported by:

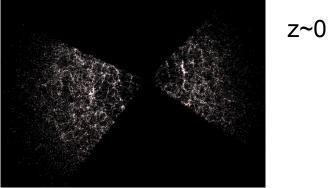




The cosmic power spectrum: from the CMB to the 2dFGRS

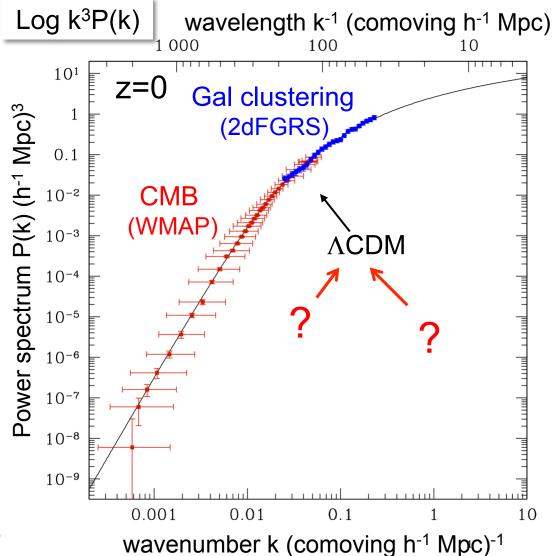


z~0



 \Rightarrow Λ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06





The cosmic power spectrum: from the CMB to the 2dFGRS

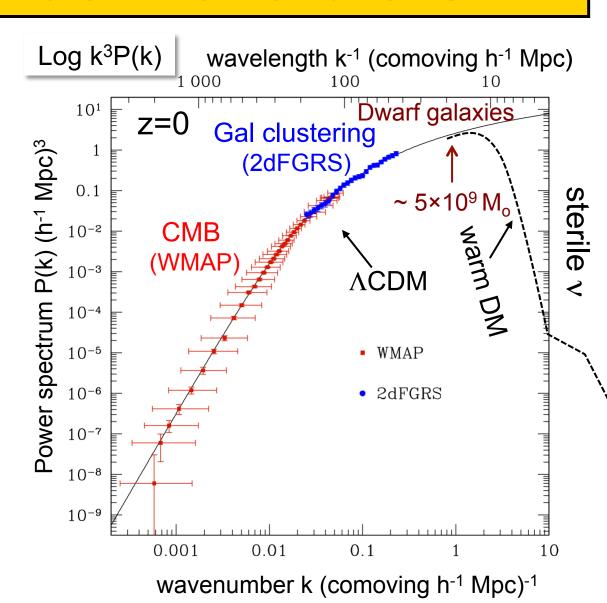
Free streaming →

 $\lambda_{cut} \; \alpha \; m_x^{-1}$

for thermal relic

 $m_{CDM} \sim 100 GeV$ susy; $M_{cut} \sim 10^{-6} M_o$

 $m_{WDM} \sim \text{few keV}$ sterile v; $M_{cut} \sim 10^9 M_o$





Sterile neutrinos

Explain:

- Neutrino oscillations and masses
- Baryogenesis
- Absence of right-handed neutrinos in standard model
- Dark matter

Sterile neutrino minimal standard model (vMSM; Boyarski+ 09):

- Extension of SM w. 3 sterile neutrinos: 2 of GeV; 1 of keV mass
- If $\Omega_N = \Omega_{DM}$, 2 parameters: mass, lepton asymmetry/mixing angle
- GeV particles may be detected at CERN (SHiP)
- Dark matter candidate can be detected by X-ray decay



Both CDM & WDM compatible with CMB & galaxy clustering Claims that both types of DM have been discovered:

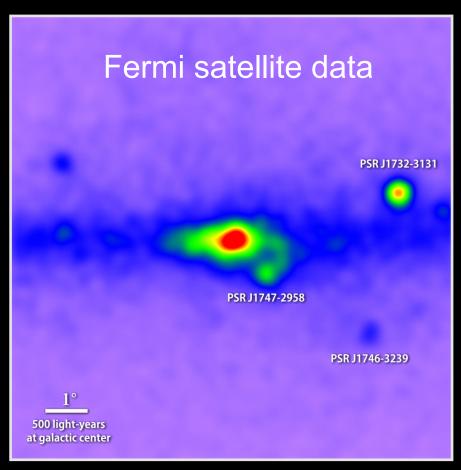
- ♦ CDM: γ-ray excess from Galactic Center
- ♦ WDM (sterile v): 3.5 X-ray keV line in galaxies and clusters

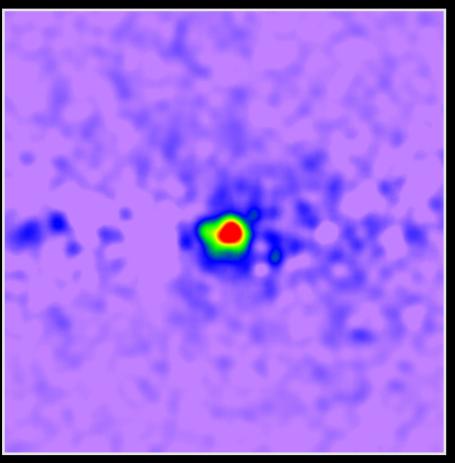
Cold dark matter

The Characterization of the Gamma-Ray Signal from the Central Milky Way:
A Compelling Case for Annihilating Dark Matter

Tansu Daylan,¹ Douglas P. Finkbeiner,^{1,2} Dan Hooper,^{3,4} Tim Linden,⁵ Stephen K. N. Portillo,² Nicholas L. Rodd,⁶ and Tracy R. Slatyer^{6,7}

Uncovering a gamma-ray excess at the galactic center





Unprocessed map of 1.0 to 3.16 GeV gamma rays

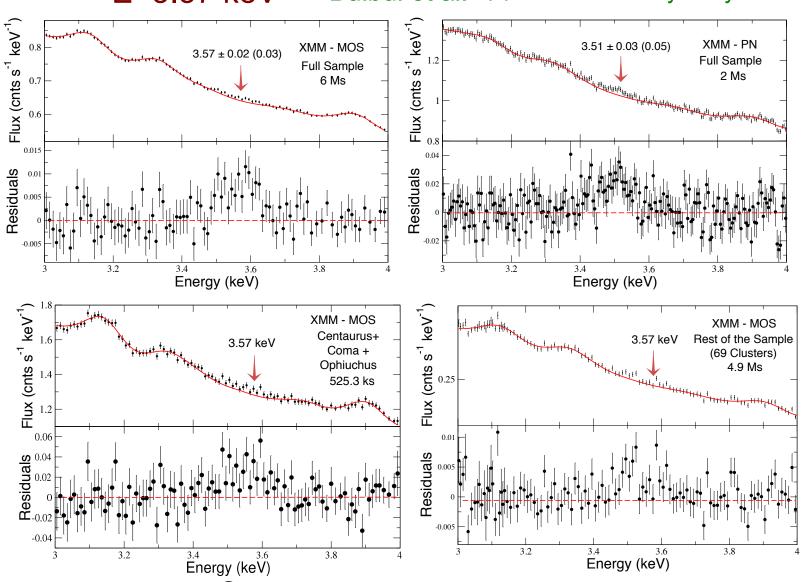
Known sources removed



Warm dark matter WDM decay line in 69 stacked clusters?

E=3.57 keV

Bulbul et al. '14 See also Boyarsky et al. '14





Both CDM & WDM compatible with CMB & galaxy clustering Claims that both types of DM have been discovered:

- ♦ CDM: γ-ray excess from Galactic Center
- ♦ WDM (sterile v): 3.5 X-ray keV line in galaxies and clusters

Very unlikely that both are right!



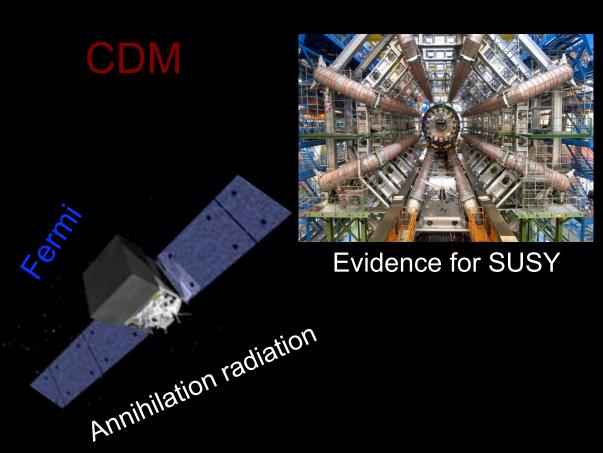
The search for dark matter

Dark matter discovery possible in several ways

Direct detection



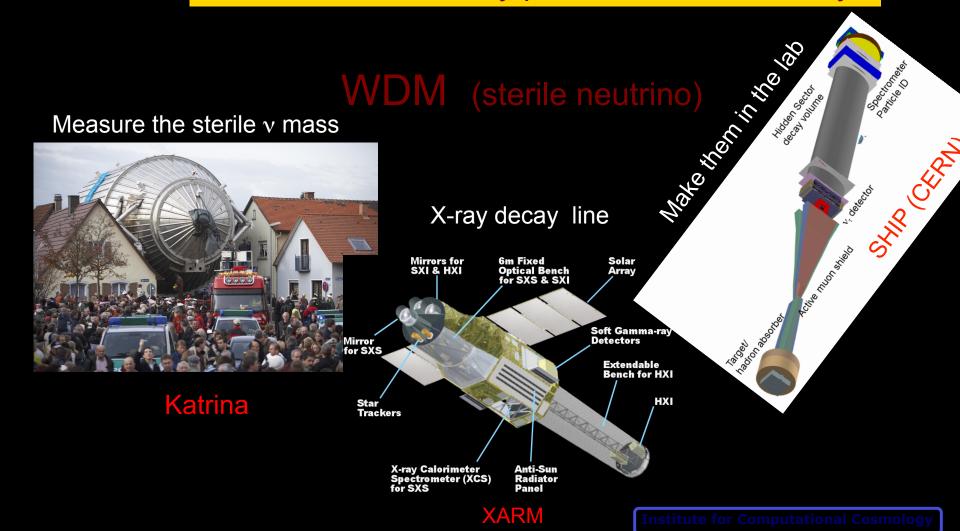
UK DM search (Boulby mine)





The search for dark matter

Dark matter discovery possible in several ways





The identity of the dark matter is encoded in dwarf galaxies and in the halo of the MW

(strongly non-linear regime)



Cold Dark Matter

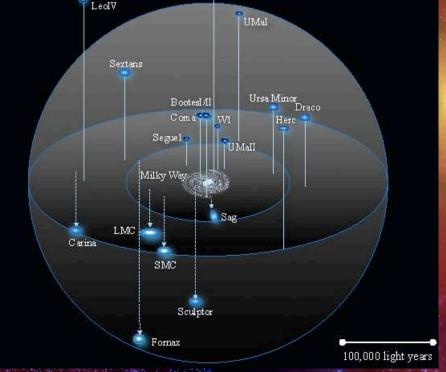
Warm Dark Matter



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns, Boyarski & Ruchayskiy '12

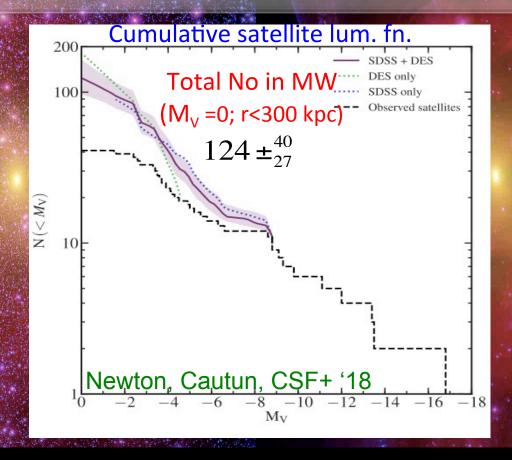
Obvious test: count satellites in MW or M31

In the MW: ~55 satellites discovered so far



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns, Boyarski & Ruchayskiy '12

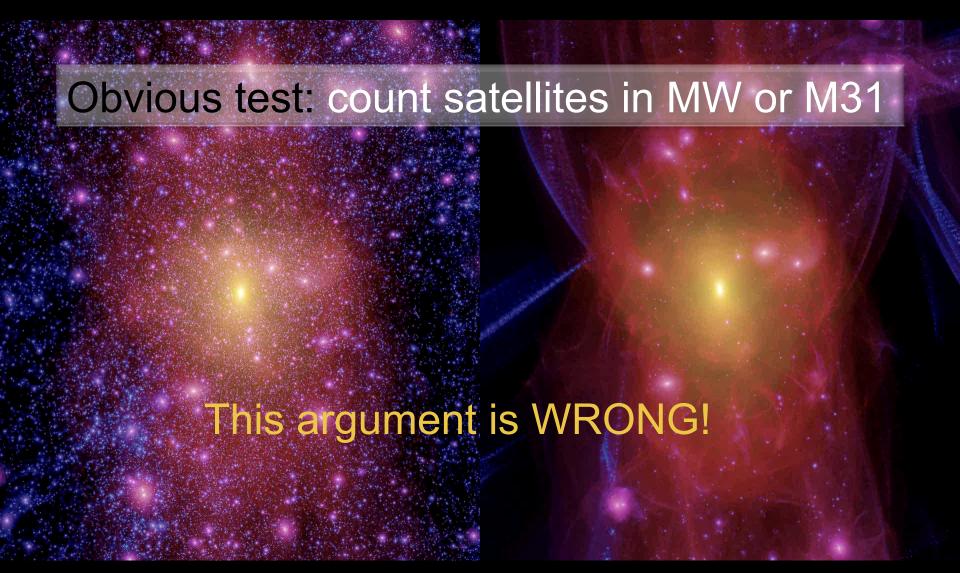
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Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns, Boyarski & Ruchayskiy '12

cold dark matter

warm dark matter

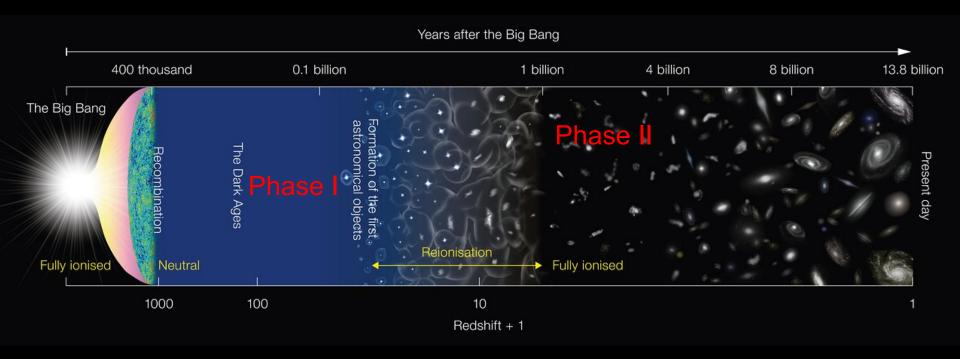


Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns, Boyarski & Ruchayskiy '12





The two phases of galaxy formation



Phase I: Galaxies begin to form during the "dark ages"

First stars reionize H and heat it up to 10⁴K → prevents gas from cooling in halos of "T_{vir}" < 10⁴K − galaxy formation is interrupted

Phase II: Halos with "T_{vir}" > 10⁴K form → galaxy formation resumes



Evolution of baryons

Basic differential equations of Durham SA model:

$$M_{\star} = (1 - R)\psi$$

$$\dot{M}_{\rm hot} = -\dot{M}_{\rm cool} + \beta \psi$$

$$\dot{M}_{\rm cold} = \dot{M}_{\rm cool} - (1 - R + \beta)\psi$$

$$\dot{M}_{\star}^{Z} = (1 - R) Z_{\rm cold} \psi$$

$$\dot{M}_{\rm hot}^Z = -\dot{M}_{\rm cool}Z_{\rm hot} + (pe + \beta Z_{\rm cold})\psi$$

$$\dot{M}_{\rm cold}^Z = \dot{M}_{\rm cool} Z_{\rm hot}$$

+
$$(p(1-e) - (1+\beta - R)Z_{\text{cold}})\psi$$
,

SFR & mass ejection

SFR
$$\psi = \frac{M_{\rm cold}}{\tau_{\star}(r_{\rm disk}, V_{\rm disk})}$$

$$\dot{
m SN}_{
m edback} \dot{M}_{
m eject} = eta(V_{
m disk}) \, \psi$$

feedback

AGN
$$M_{BH} = f_{RH} \psi_{burst} + -$$

feedback

$$M_{BH} = f_{BH} \psi_{burst} + \frac{L_{cool}}{c^2 \varepsilon_{SMBH}}$$

Mass conservation

R = recycled fraction

 ψ = star formation rate

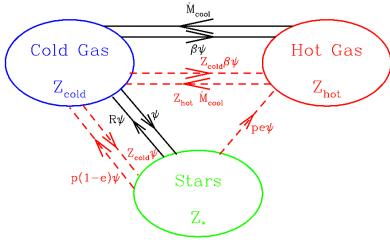
Conservation of metals

 β = SN feedback parameter

p = metal yield

e = fraction of metals ejected

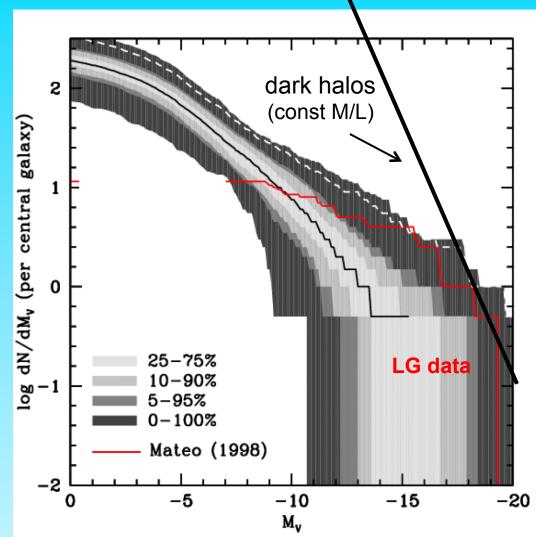
White & Frenk '91 Cole et al '00





Luminosity Function of Local Group Satellites

- Median model → correct abund. of sats brighter than M_V=-9 and V_{cir} > 12 km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare (~10% of cases)



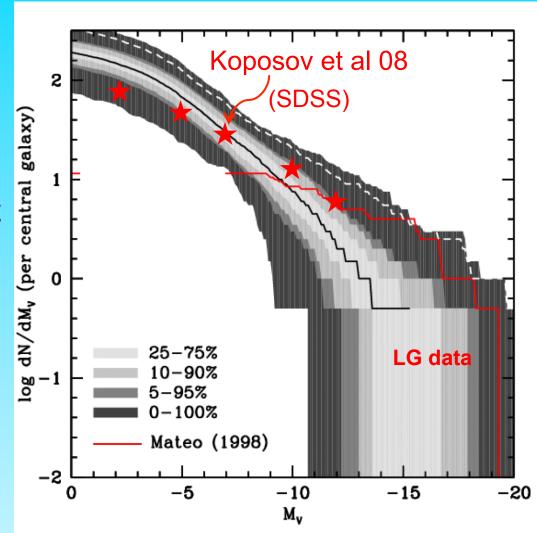
Benson, Frenk, Lacey, Baugh & Cole '02 (see also Kauffman+ '93, Bullock+ '00, Somerville '02)

Institute for Computational Cosmology



Luminosity Function of Local Group Satellites

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Benson, Frenk, Lacey, Baugh & Cole '02 (see also Kauffman+ '93, Bullock+ '00, Somerville '02)

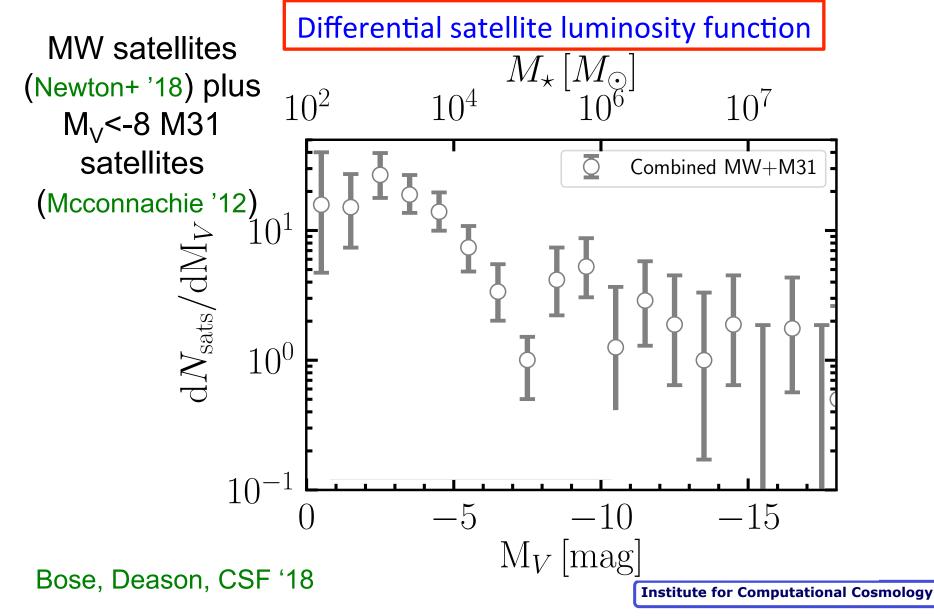
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An aside: have the first galaxies been discovered?



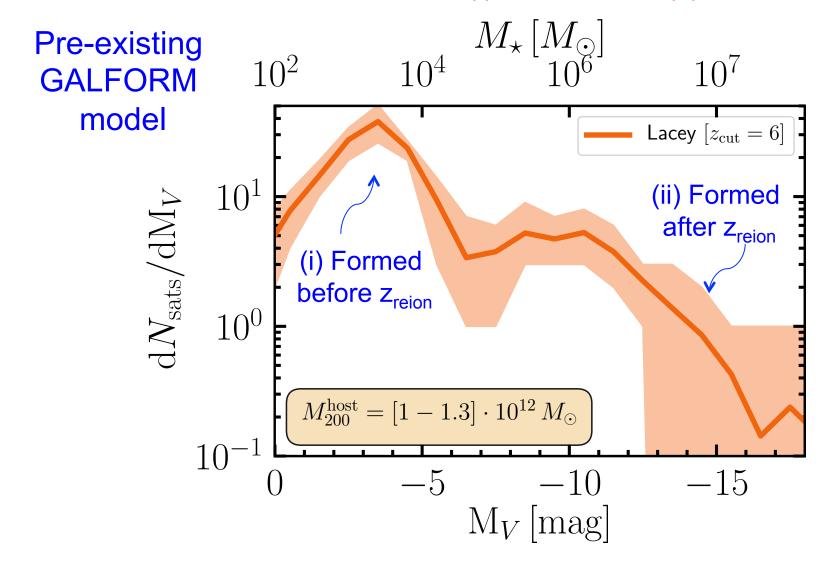
The MW/M31 sat. luminosity function





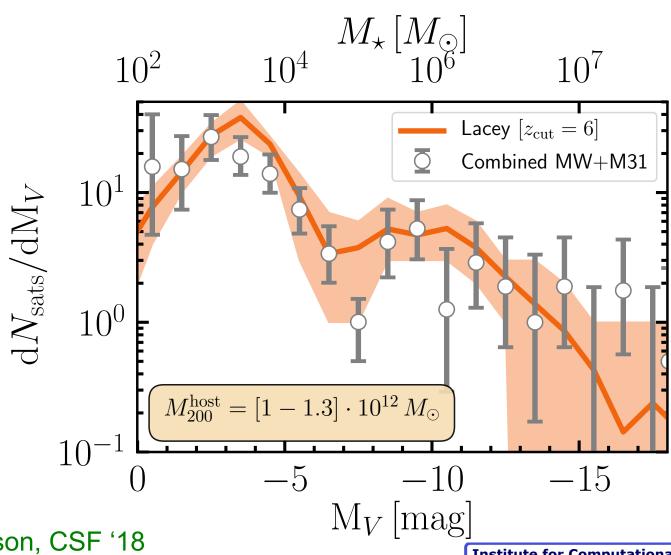
The satellite luminosity function

Two populations of sats formed: (i) before and (ii) after reionization





Theory vs data



Bose, Deason, CSF '18

Institute for Computational Cosmology

"Evolution and assembly of galaxies and their environment"

THE EAGLE PROJECT

Virgo Consortium

Durham: Richard Bower, Michelle Furlong, Carlos Frenk, Matthieu Schaller, James Trayford, Yelti Rosas-Guevara, Tom Theuns, Yan Qu, John Helly, Adrian Jenkins.

Leiden: Rob Crain, Joop Schaye.

Other: Claudio Dalla Vecchia, Ian McCarthy, Craig Booth...



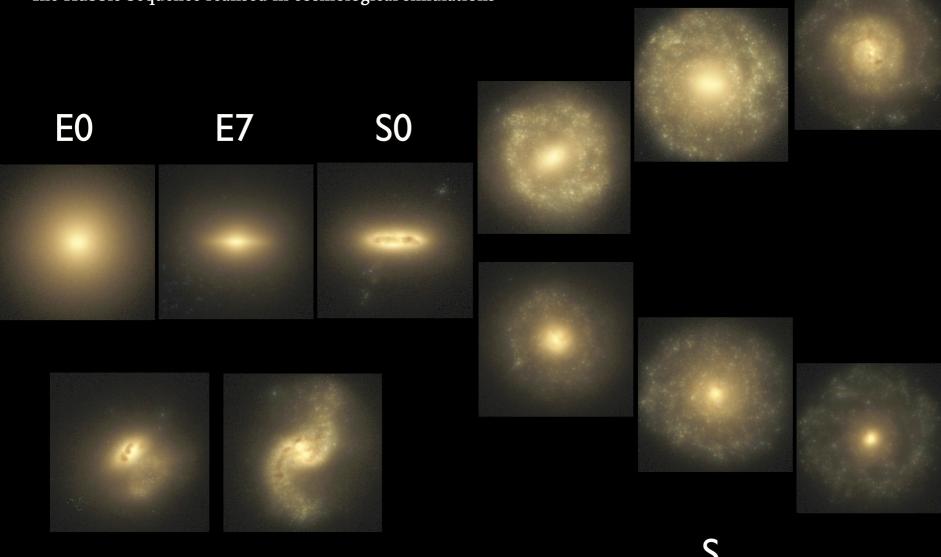




The Eagle Simulations

EVOLUTION AND ASSEMBLY OF GALAXIES AND THEIR ENVIRONMENTS

The Hubble Sequence realised in cosmological simulations



Trayford et al '15

SB

VIRG

APOSTLE
EAGLE full
hydro
simulations

Local Group

CDM

Sawala et al '16





Stars



Local Group

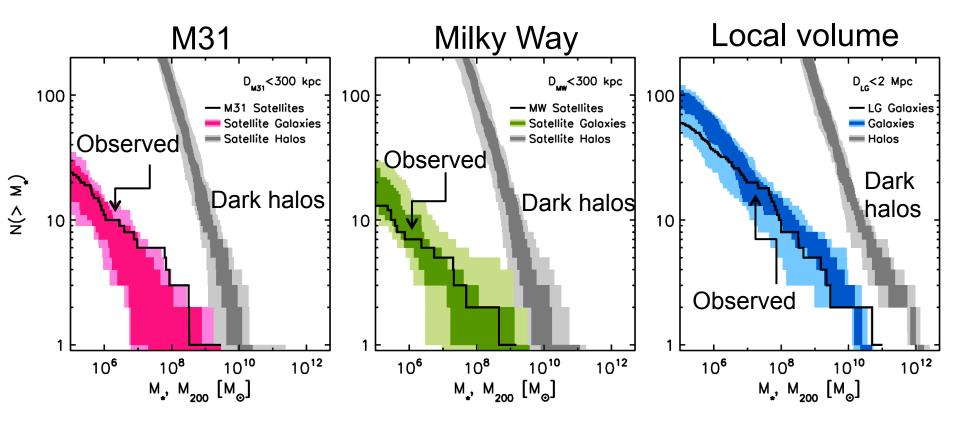
Stars

Far fewer satellite galaxies than CDM halos

Sawala et al '16

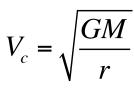


EAGLE Local Group simulation

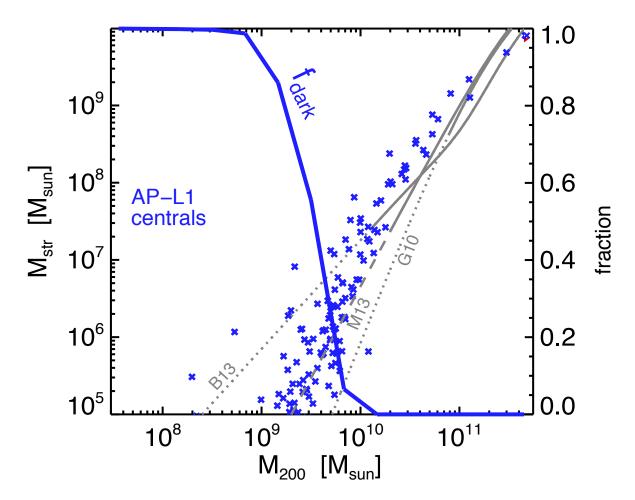




Fraction of dark subhalos



$$V_{max} = max V_{c}$$



All halos of mass $< 5 \times 10^8 M_o$ or $V_{max} < 7$ km/s are dark (m_{*} $< 10^4 M_o$)



How about in WDM?

The satellites of the MW

Sculptor

Dark mattter subhalos in WDM

(~55 discovered so far) $\begin{array}{c} \text{CVrII} \\ \text{LeoIV} \\ \text{Sextans} \\ \text{Some of the content of the c$

100,000 light

(a few tens)

Can rule out low WDM particle masses



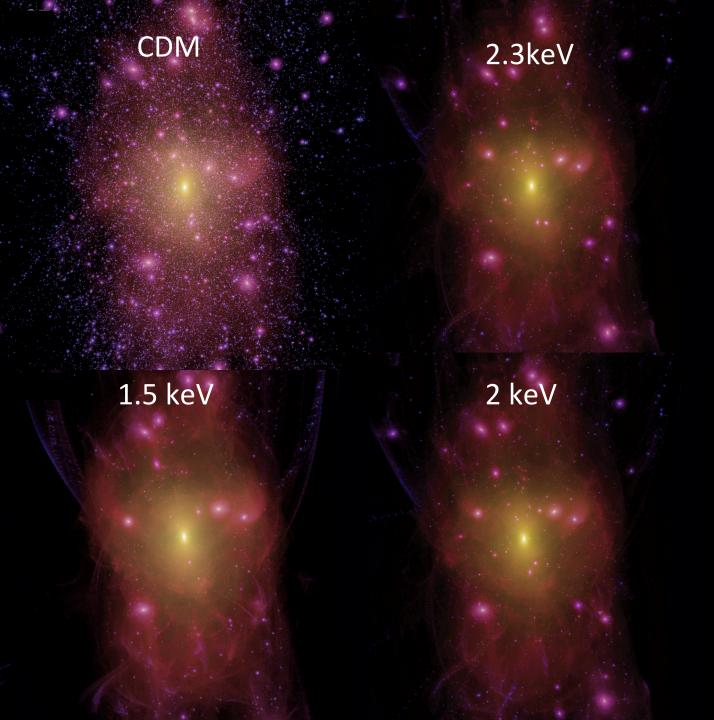
Warm DM: different v mass

WDM

2.3 keV

2.0 keV

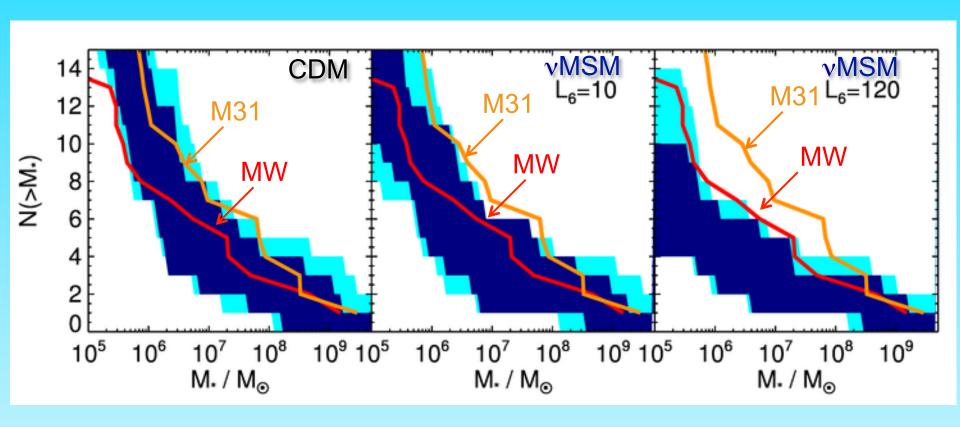
1.5 keV





Luminosity Function of Local Group Satellites in WDM

From "Warm Apostle:" 7keV sterile $v = M_h \sim 10^{12} M_o$



Lovell et al. '16

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When "baryon effects" are taken into account

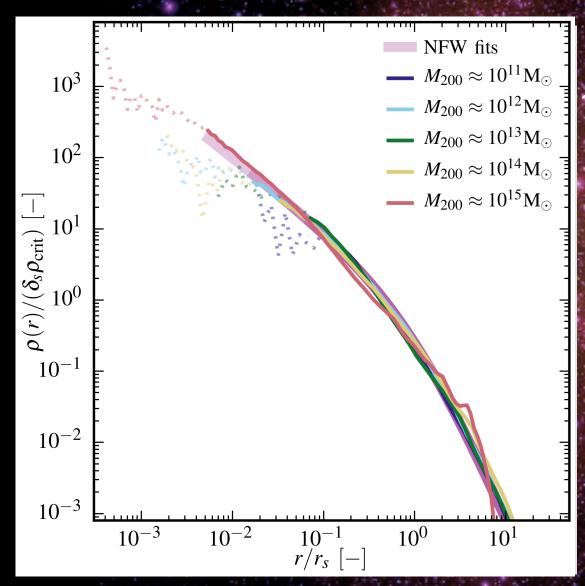


Observed abundance of satellites is compatible with CDM but rules out some WDM models



There is no such thing as the "satellite problem" in CDM!

The Density Profile of Cold Dark Matter Halos



Shape of halo profiles
~independent of halo mass &
cosmological parameters

Density profiles are "cuspy" - no `core' near the centre

Fitted by simple formula:

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

(Navarro, Frenk & White '97)

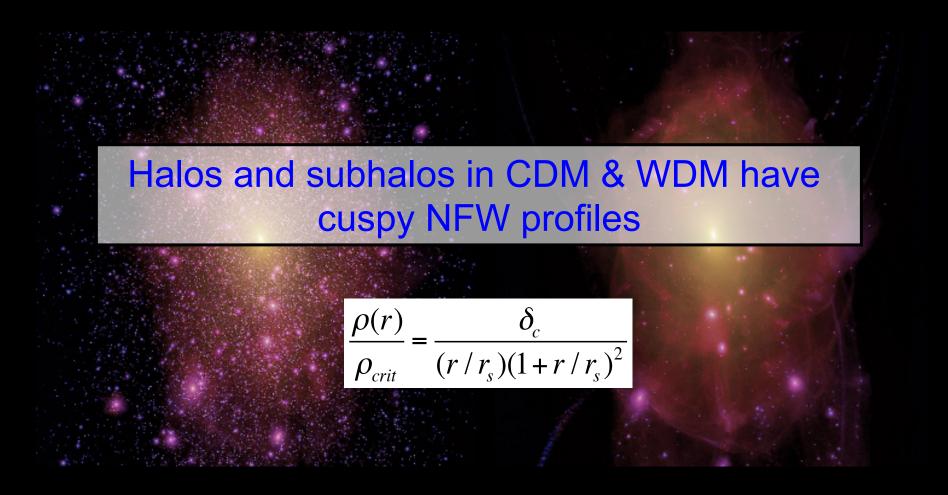
More massive halos and halos that form earlier have higher densities (bigger δ)



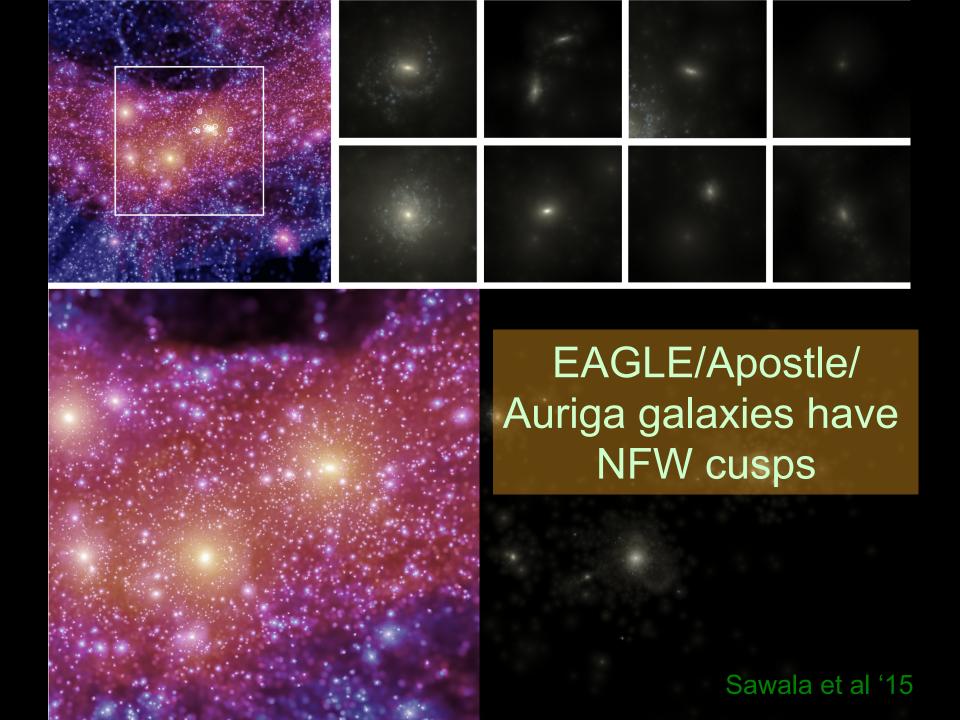
The core-cusp problem

cold dark matter

warm dark matter



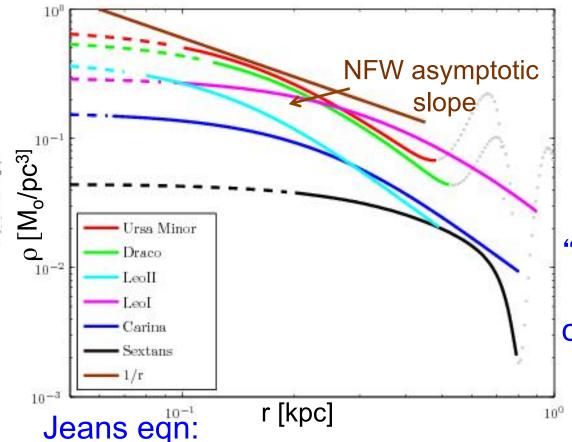
Lovell, Eke, Frenk, Gao, Jenkins, Theuns '12







The DM halos of dwarf spheroidals



Gilmore etal '07

Inferred density profiles for 6 dwarf spheroidals

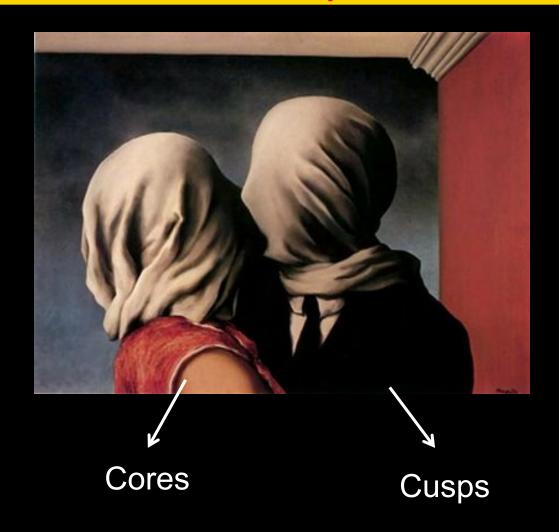
...dark matter forms cored mass distributions, with a core scale length of greater than about 100pc..."

$$\frac{GM(r)}{r} = -\sigma_r^2 \left[\frac{d \ln \rho_*}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right]$$
vel. anisotropy

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Cores or cusps in nature?



No convincing evidence for cores in observed galaxies



But, if cores we found to exist in galaxies, would this rule out CDM (& WDM)?

No!



The physics of core formation

Cusps → cores

Perturb central halo region by growing a galaxy adiabatically and removing it suddenly (Navarro, Eke & Frenk '96)

Cores may also form by repeated fluctuations in central potential (e.g. by SN explosions) (Read & Gilmore '05; Pontzen & Governato '12,'14; Bullock & Boylan-Kolchin '17)

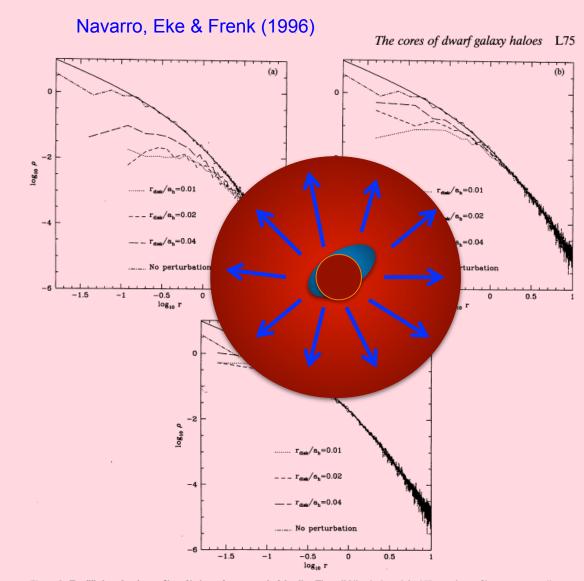


Figure 3. Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10 000-particle realization of the Hernquist model run in isolation at t = 200. (a) $M_{\rm disc} = 0.1$. (c) $M_{\rm disc} = 0.05$.



Core formation

In the absence of a treatment of the (multi-phase) interstellar medium, need a "subgrid" model for star formation

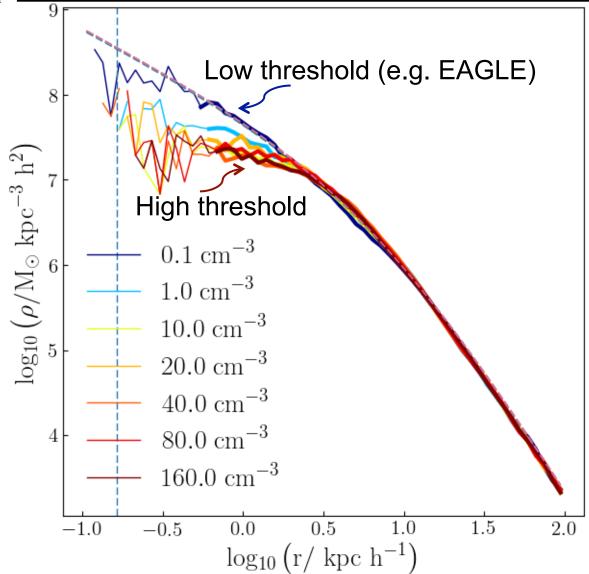
Key parameter: gas density threshold for star formation

Physically meaningless





Cores or cusps in simulations?





Many halos are consistent with NFW cusps; there is no convincing evidence for cores

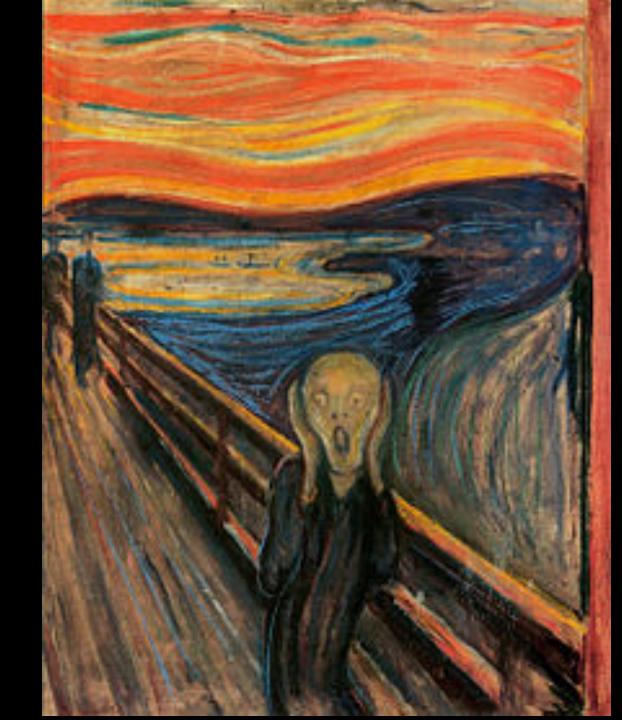
And if cores do exist, they inform us about baryon astrophysics not about the nature of the dark matter





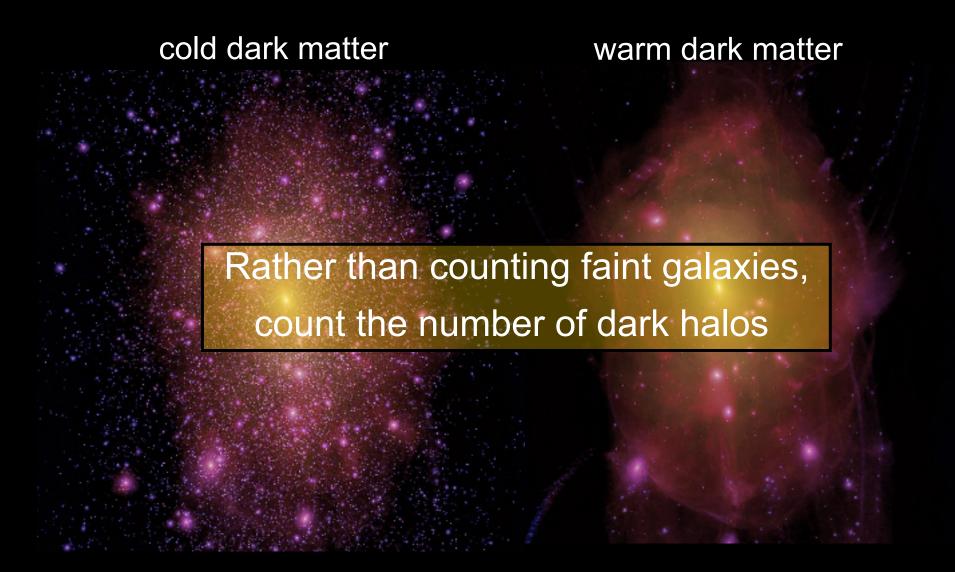
Is there any way can distinguish CDM from WDM?

There is no need for despair: there is a way to distinguish them



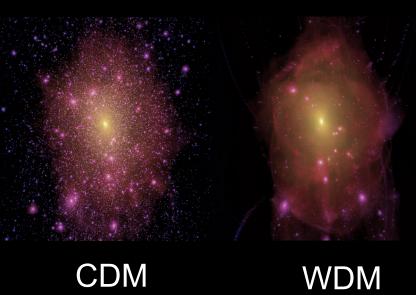


Can we distinguish CDM/WDM?



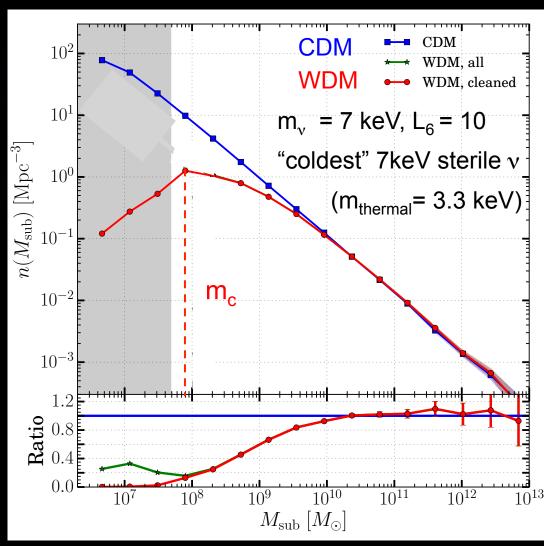


The subhalo mass function



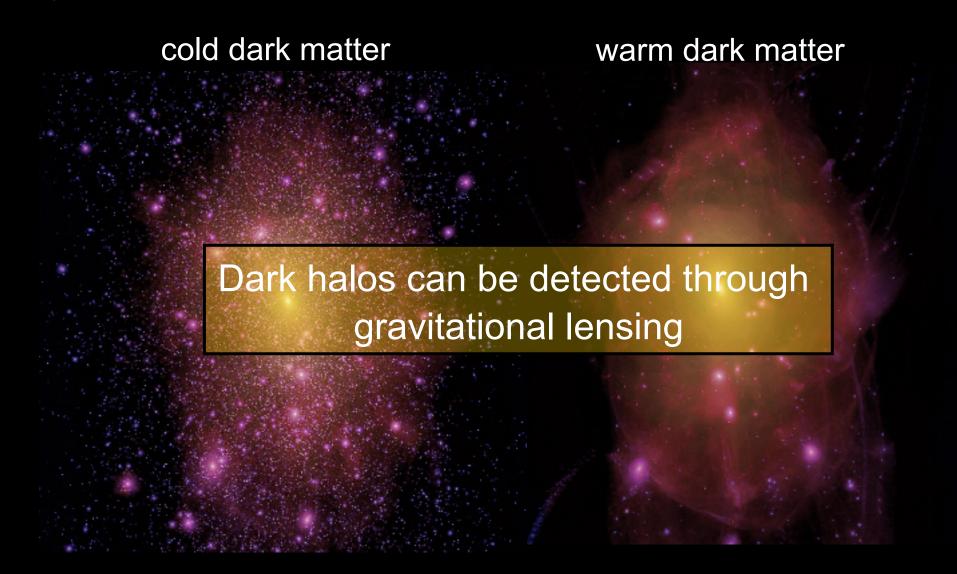
3 x fewer WDM subhalos at $3 \text{x} 10^9 \, \text{M}_{\text{o}}$

10 x fewer at 108 M_o





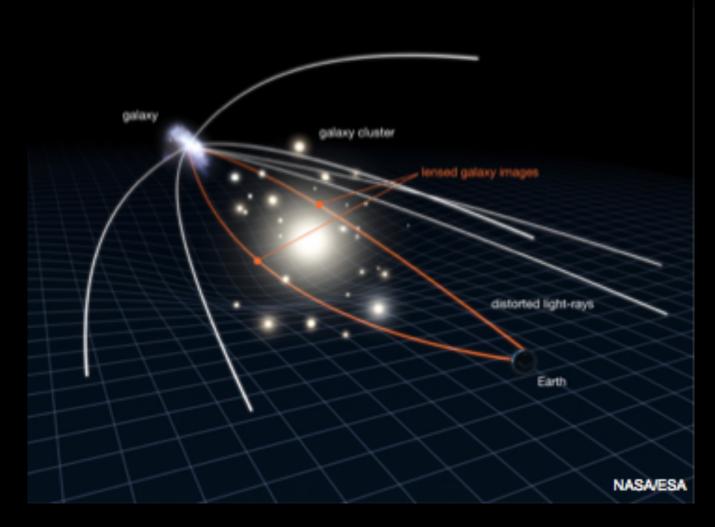
Can we distinguish CDM/WDM?





How to rule out CDM





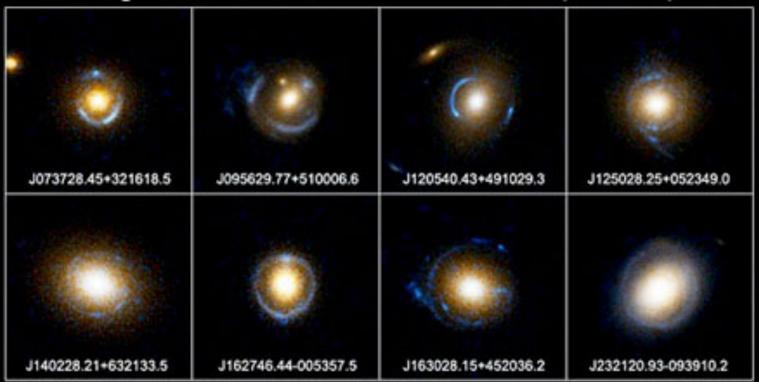
When the source and the lens are well aligned -> strong arc or an Einstein ring



SLAC sample of strong lenses

Einstein Ring Gravitational Lenses

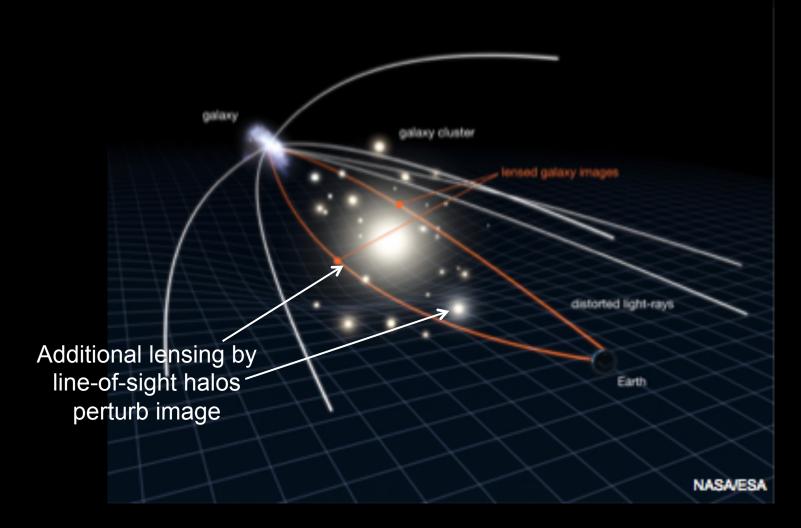
Hubble Space Telescope . ACS



NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

STScI-PRC05-32

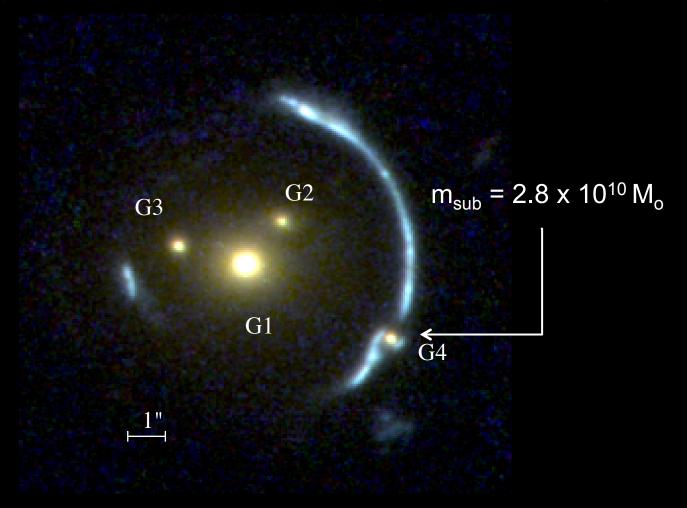




When the source and the lens are well aligned -> strong arc or an Einstein ring



Halos projected onto an Einstein ring distort the image





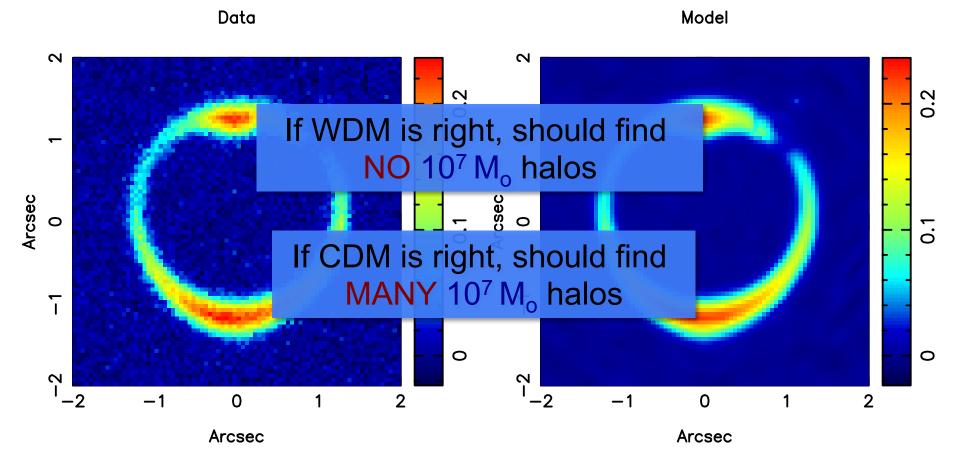
Halos projected onto an Einstein ring distort the image





Detecting substructures with strong lensing

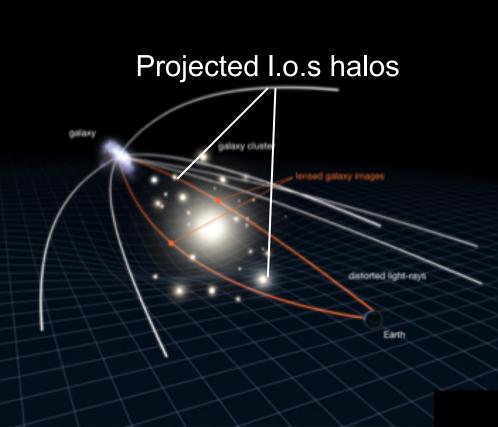
Can detect subhalos as small as $10^7 - 10^8 M_o$

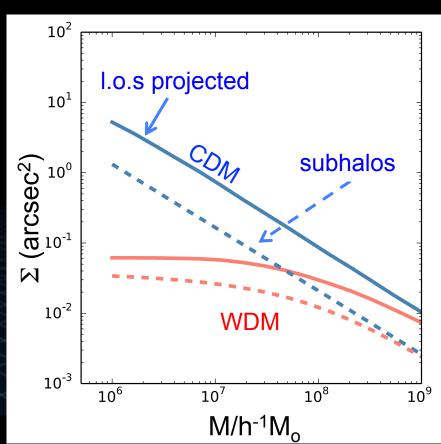




Substructures vs interlopers

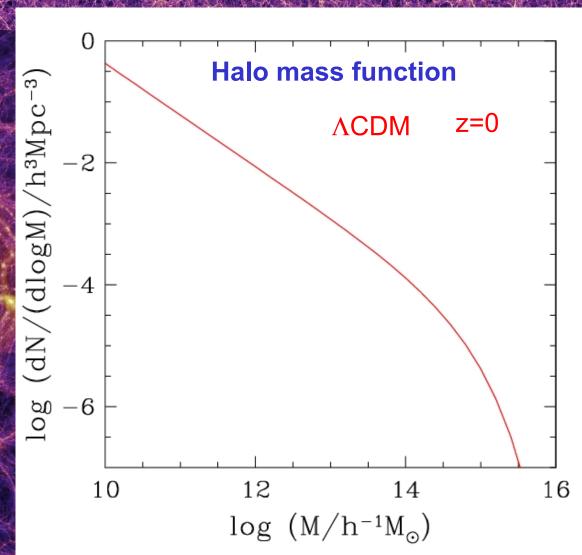
Subhalos & halos projected along the l.o.s both lens: who wins?





The number of line-of-sight haloes is larger than that of subhaloes

The Millennium/Aquarius/Phoenix simulation series

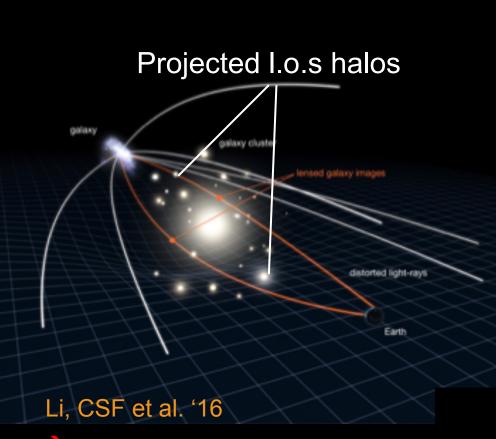


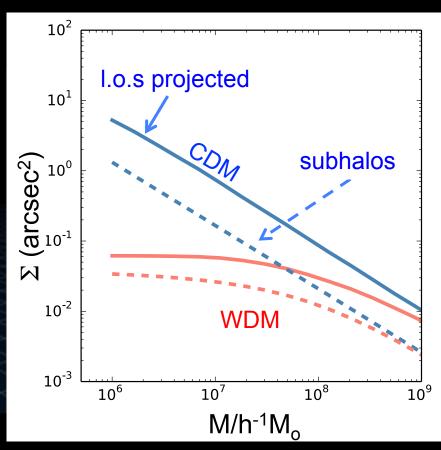
Springel et al '05, '08, Gao et al '11



Substructures vs interlopers

Subhalos & halos projected along the l.o.s both lens: who wins?





→ This is the cleanest possible test: it depends ONLY on the small-mass end of the "field" halo mass function which we know how to calculate and is unaffected by baryons



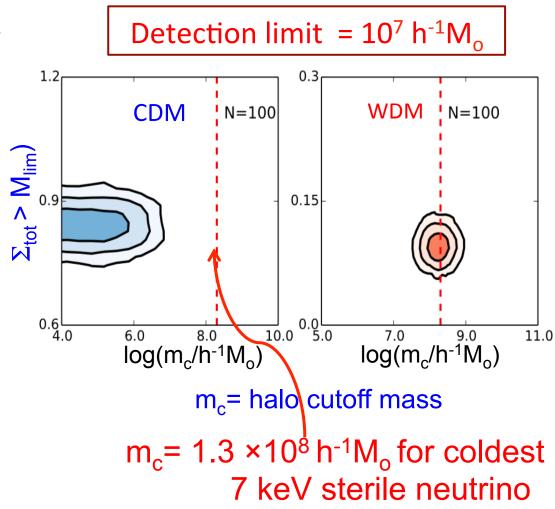
Detecting substructures with strong lensing

 Σ_{tot} = projected halo number density within Einstein ring

m_c= halo cutoff mass

100 Einstein ring systems and detection limit: $m_{low} = 10^7 h^{-1} M_o$

- If DM is 7 keV sterile v → exclude CDM at >>σ!
- If DM is CDM → exclude
 7 keV sterile v at >>σ



Li, CSF et al '16

Institute for Computational Cosmology



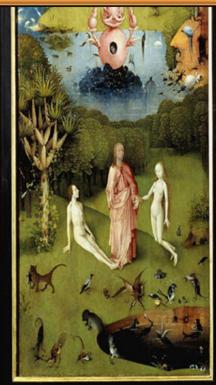
Conclusions

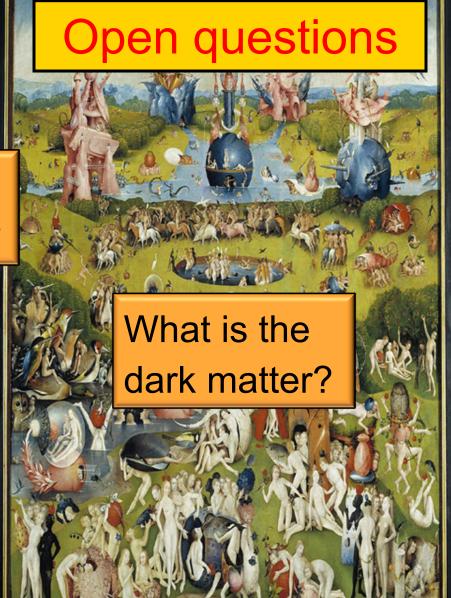
- ΛCDM: great success on scales > 1Mpc: CMB, LSS, gal evolution
- Λ makes little difference to formation of cosmic structure
- But the identity of DM makes a big difference on small scales

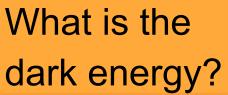
- CDM makes many small subhalos but most (<5.10⁸M₀)
 are dark → No satellite problem in CDM or WDM
- 2. No evidence for cores; baryon effects can make them
 - → No "core/cusp" problem in CDM or WDM
- 3. Distortions of strong gravitational lenses offer a clean test of CDM vs WDM → and can potentially rule out CDM!



How did the universe begin?



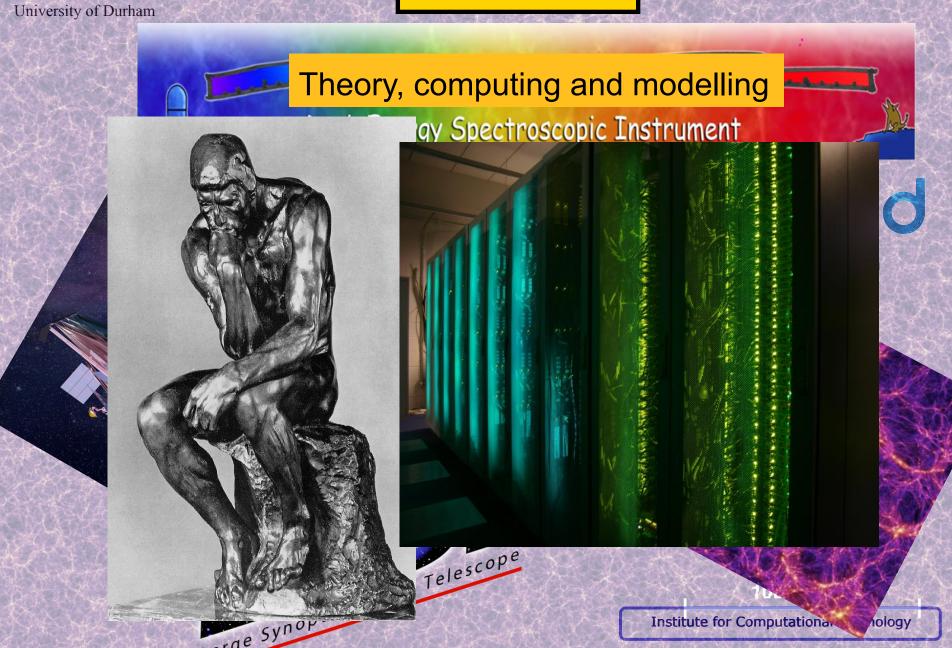








The future



There has been great progress in cosmology in the past 30 years

