



A conclusive test of cold dark matter

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Durham

Modern cosmology emerged from two revolutionary ideas c.a.1980

The new Ogden
Centre at Durham



The big Bang



300 tho

3 minutes

15 thousand million years

The cosmic microwave background is emitted
($t \sim 350,000$ yrs)

II. Production of
particle dark matter

Cowsik & McClelland '73
Marx & Szalay '72

10^{32} degrees

10^{27} degrees

10^{15} degr

degrees

18 degrees

3 degrees K

$t = 13.7$ billion yrs

I. Cosmic inflation
(initial conditions)

Guth, Linde,
Starobinsky,
Mukhanov

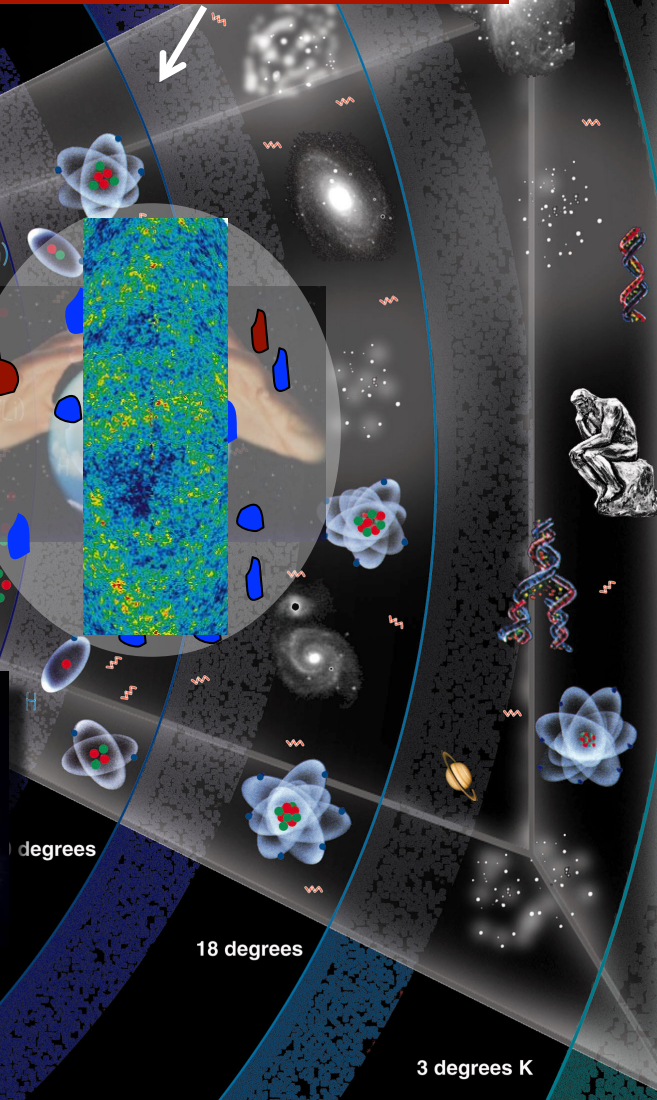
the weak force

quark

anti-quark

electron

e^+ positron (anti-proton)
 n neutron
 m meson
 H hydrogen
 D deuterium
 He helium
 Li lithium



Non-baryonic dark matter candidates

From the early 1980s (Bond & Szalay '83):

Type	example	mass
hot	neutrino	few tens of eV
warm	sterile ν	keV-MeV
cold	axion neutralino	$10^{-5}\text{eV} - 100 \text{ GeV}$

The dark matter power spectrum

$k^3 P(k)$

The linear power spectrum (“power per octave”)

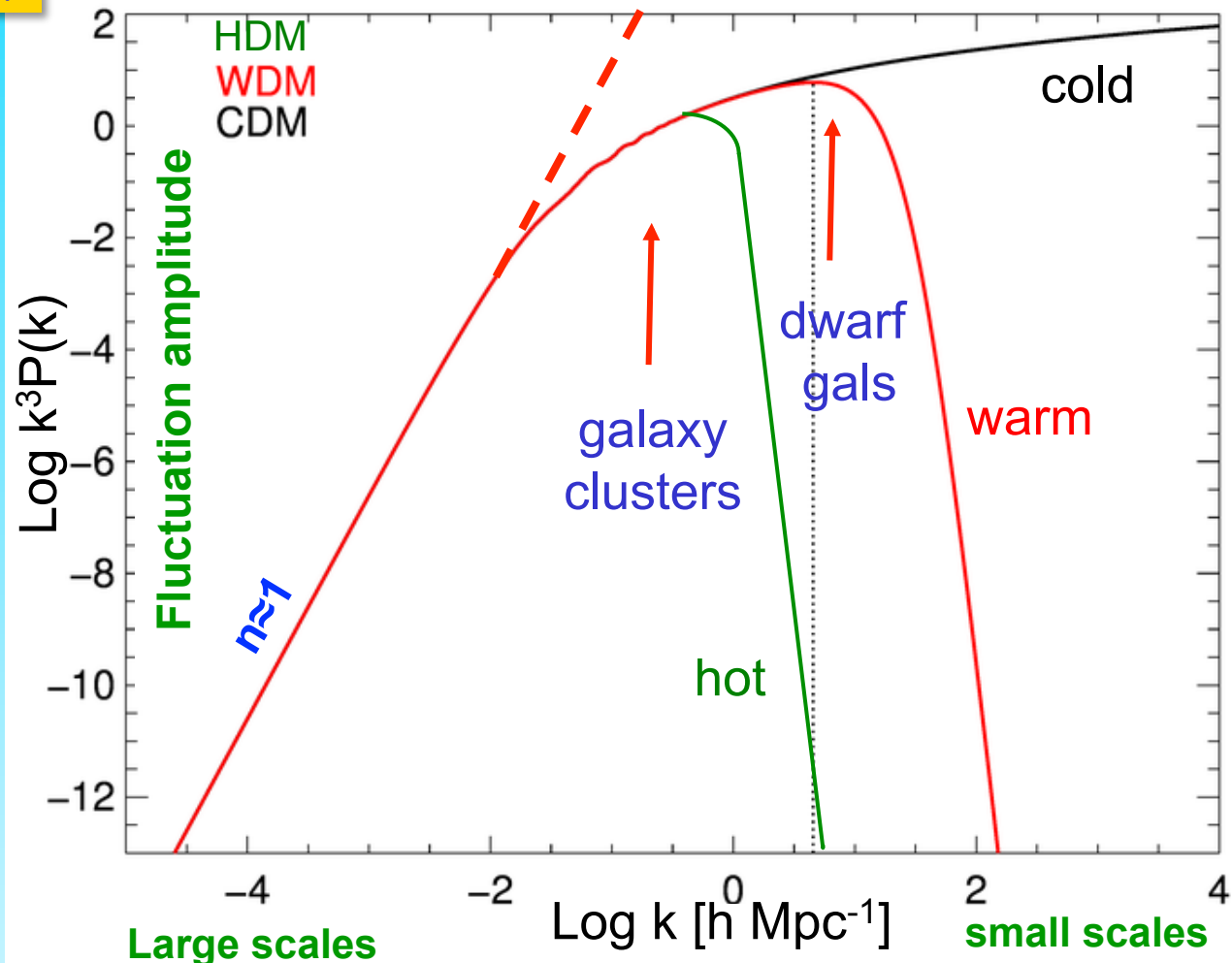
Free streaming \rightarrow

$\lambda_{\text{cut}} \propto m_x^{-1}$
for thermal relic

$m_{\text{CDM}} \sim 100 \text{ GeV}$
susy; $M_{\text{cut}} \sim 10^{-6} M_{\odot}$

$m_{\text{WDM}} \sim \text{few keV}$
sterile ν ; $M_{\text{cut}} \sim 10^9 M_{\odot}$

$m_{\text{HDM}} \sim \text{few tens eV}$
light ν ; $M_{\text{cut}} \sim 10^{15} M_{\odot}$



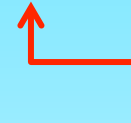
Inflationary non-baryonic dark matter cosmogonies

- *Ab initio*, fully specified models of cosmic evolution and the formation of cosmic structure
- Have strong predictive power than can be tested by astronomical observations (esp CMB and large-scale structure)

Linear theory

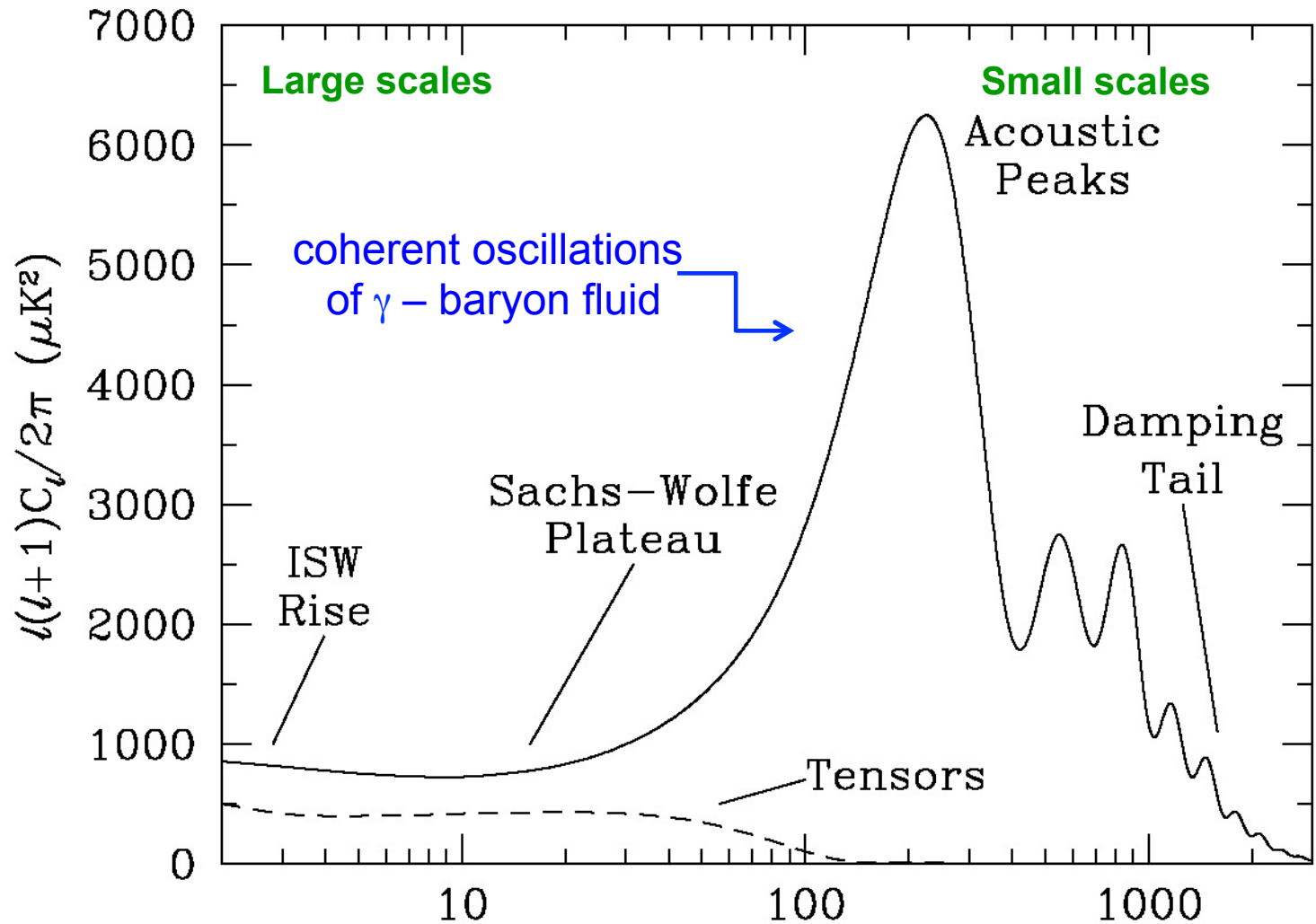


Non-linear



Temperature anisotropies in CMB

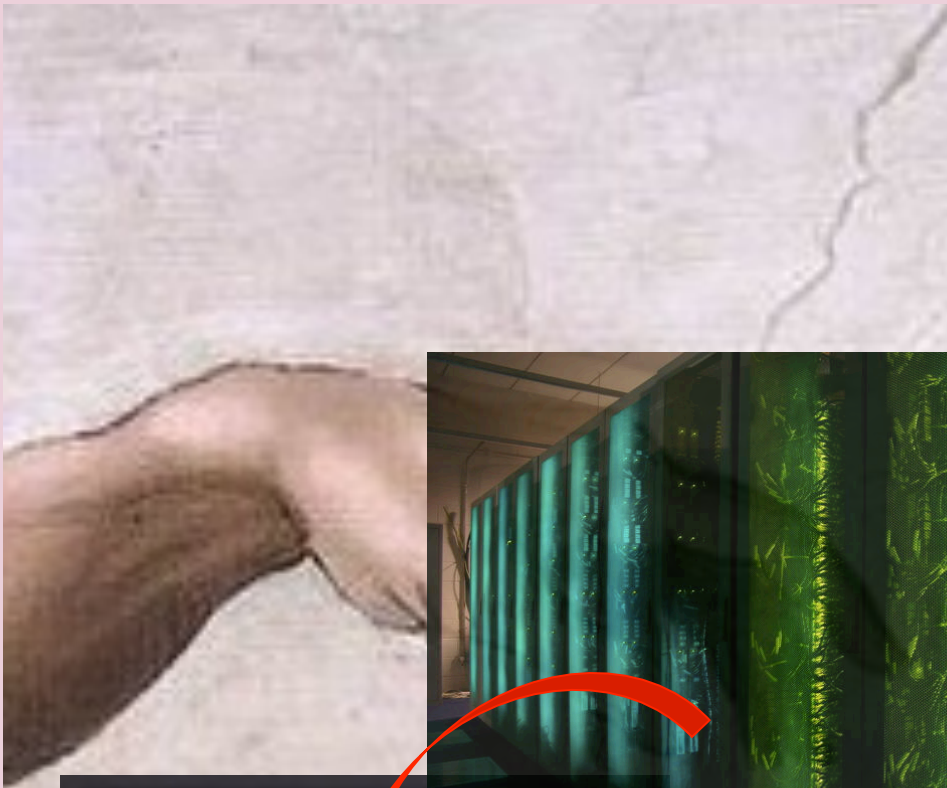
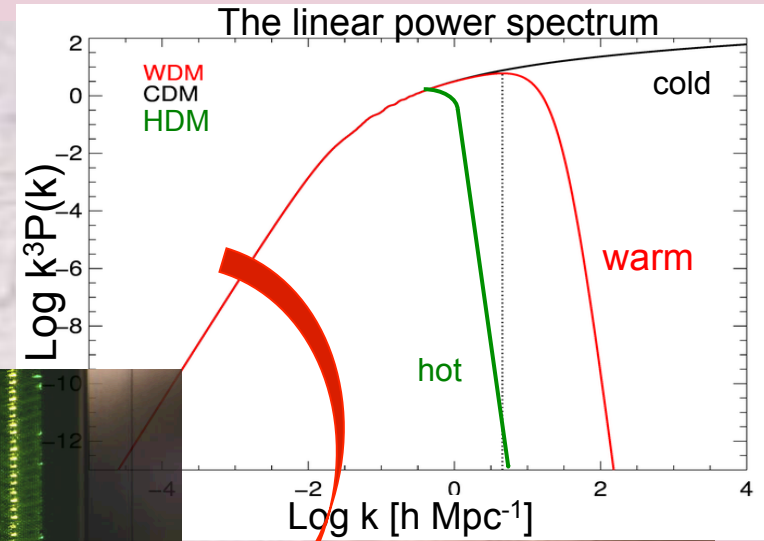
2D power spectrum



Peebles & Yu '70 Sunyev & Zel'dovich '70

For CDM: Peebles '82; Bond & Efstathiou '84

Non-linear evolution

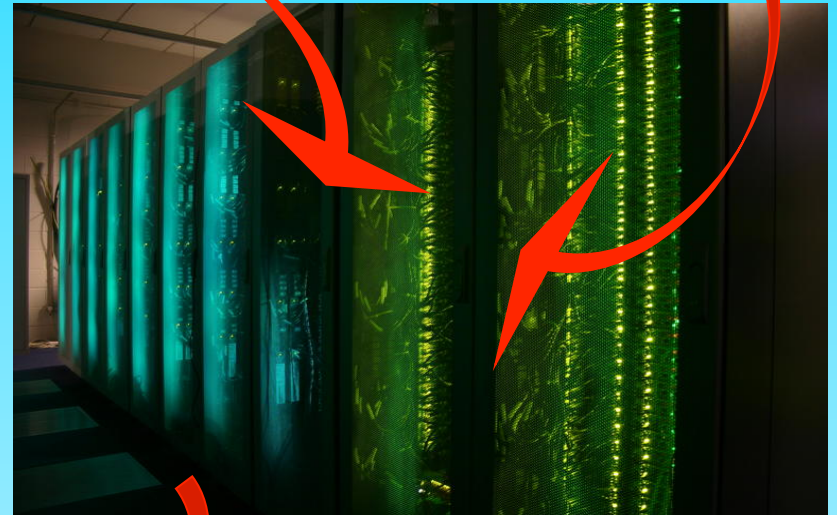


Non-linear evolution: simulations

Inflation + material content of Universe \rightarrow Initial conditions

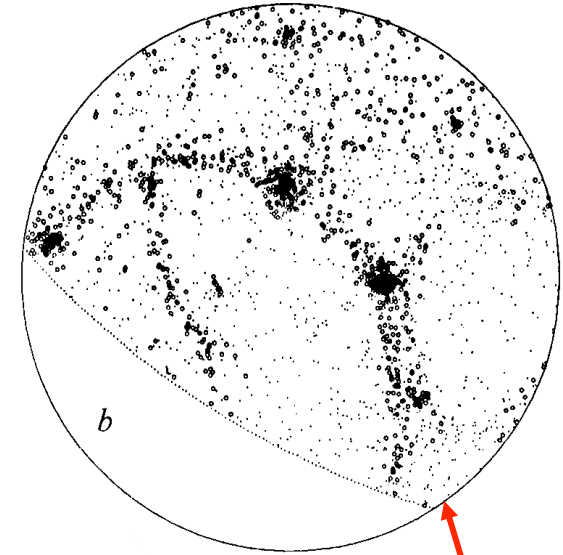
Relevant equations:

Collisionless Boltzmann,
Poisson, Friedmann eqn,
Radiative hydrodynamics
Astrophysics (subgrid)



How to make a virtual universe

Non-baryonic dark matter cosmologies



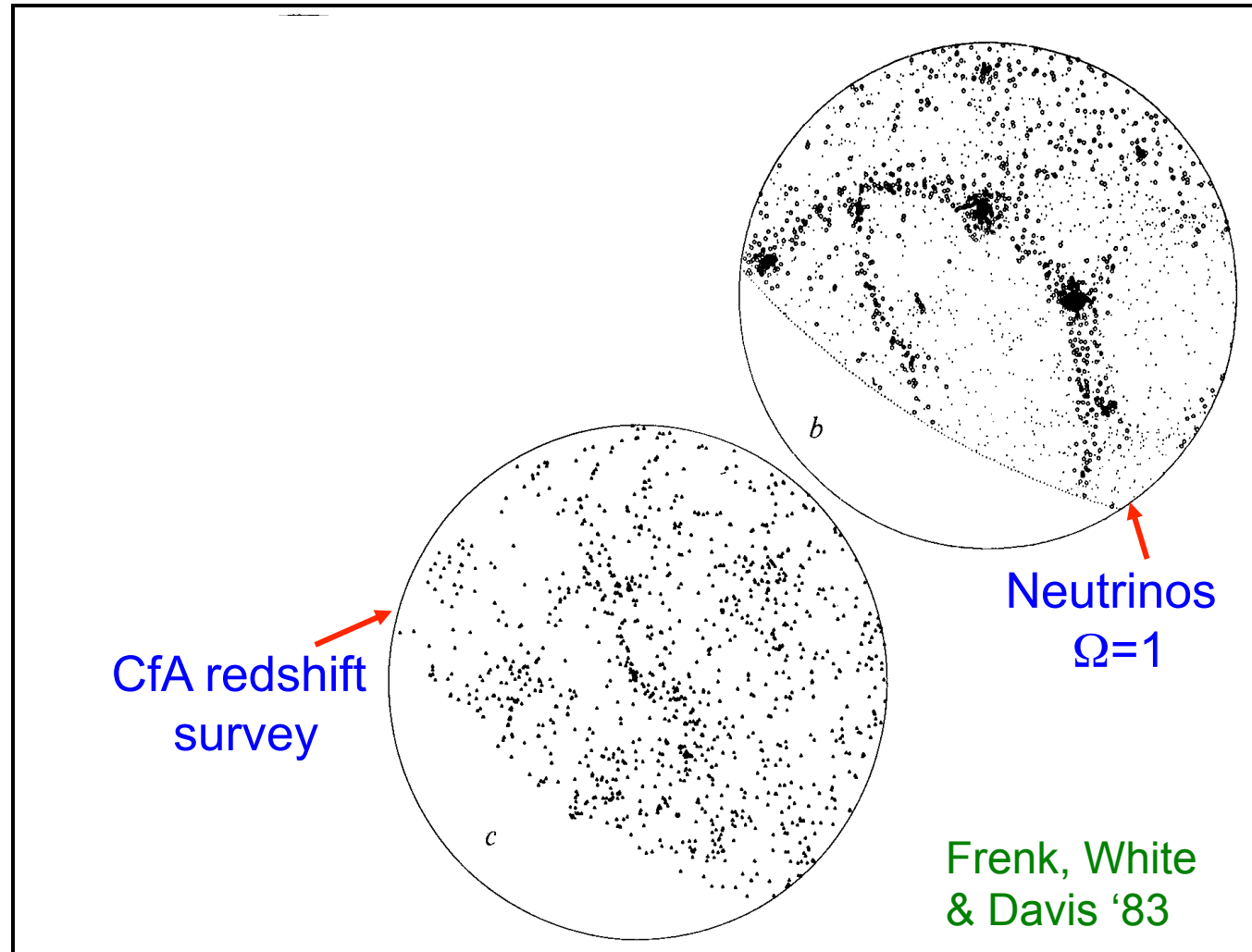
Neutrinos
 $\Omega=1$

Frenk, White
& Davis '83

Non-baryonic dark matter cosmologies

Neutrino DM →
wrong clustering

Neutrinos cannot
make appreciable
contribution to Ω
→ $m_\nu \ll 30$ eV



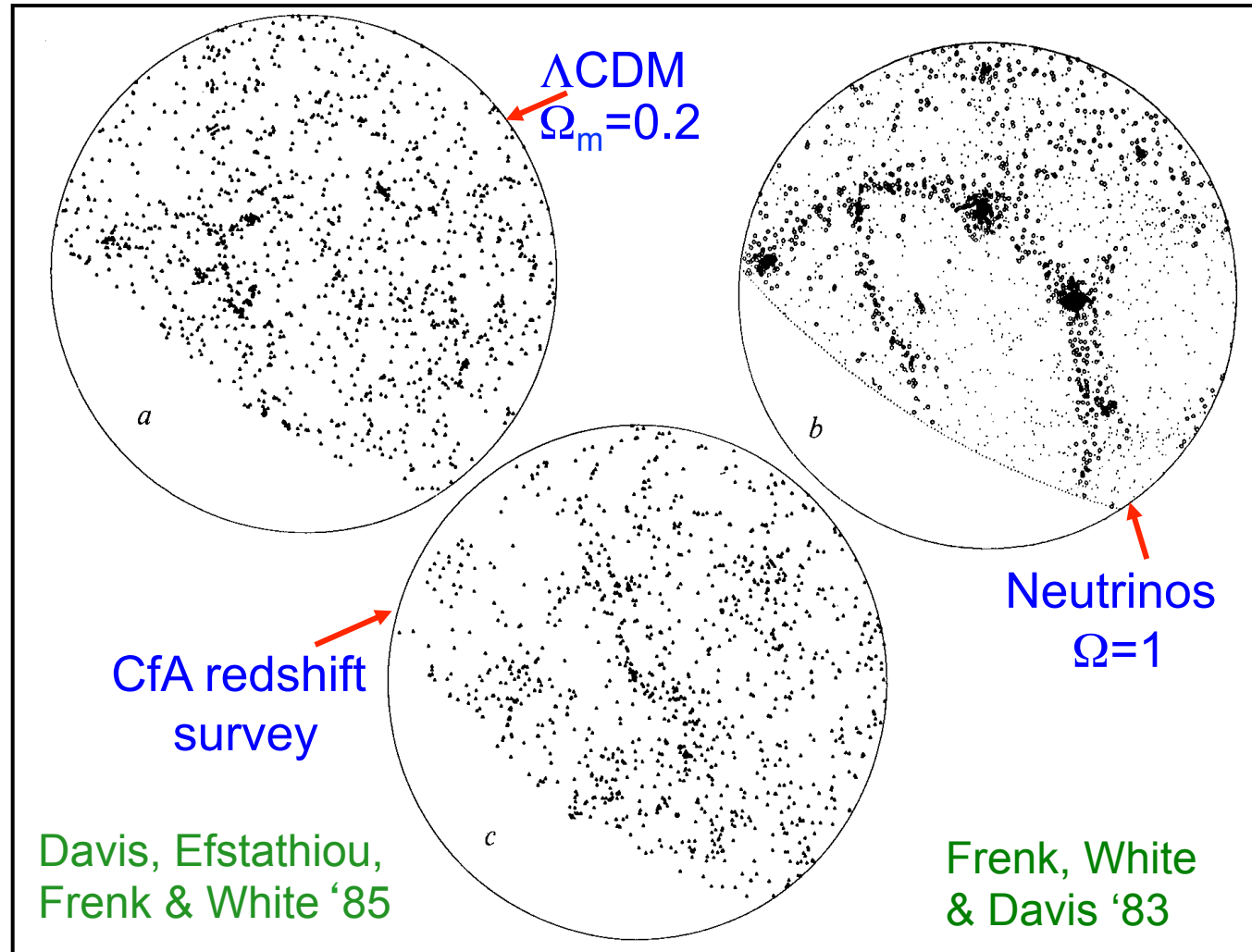
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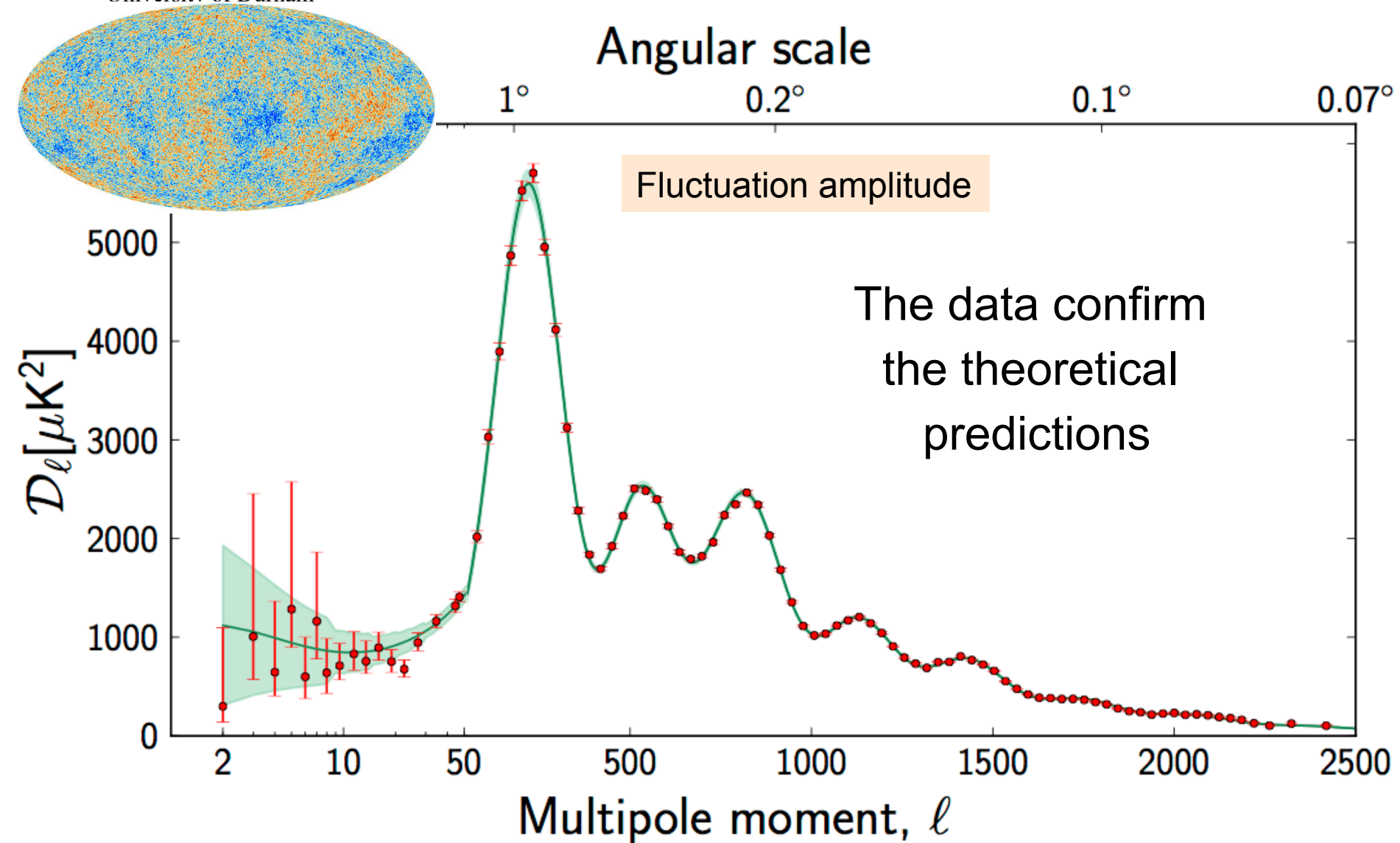
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Early CDM N-body
simulations gave
promising results

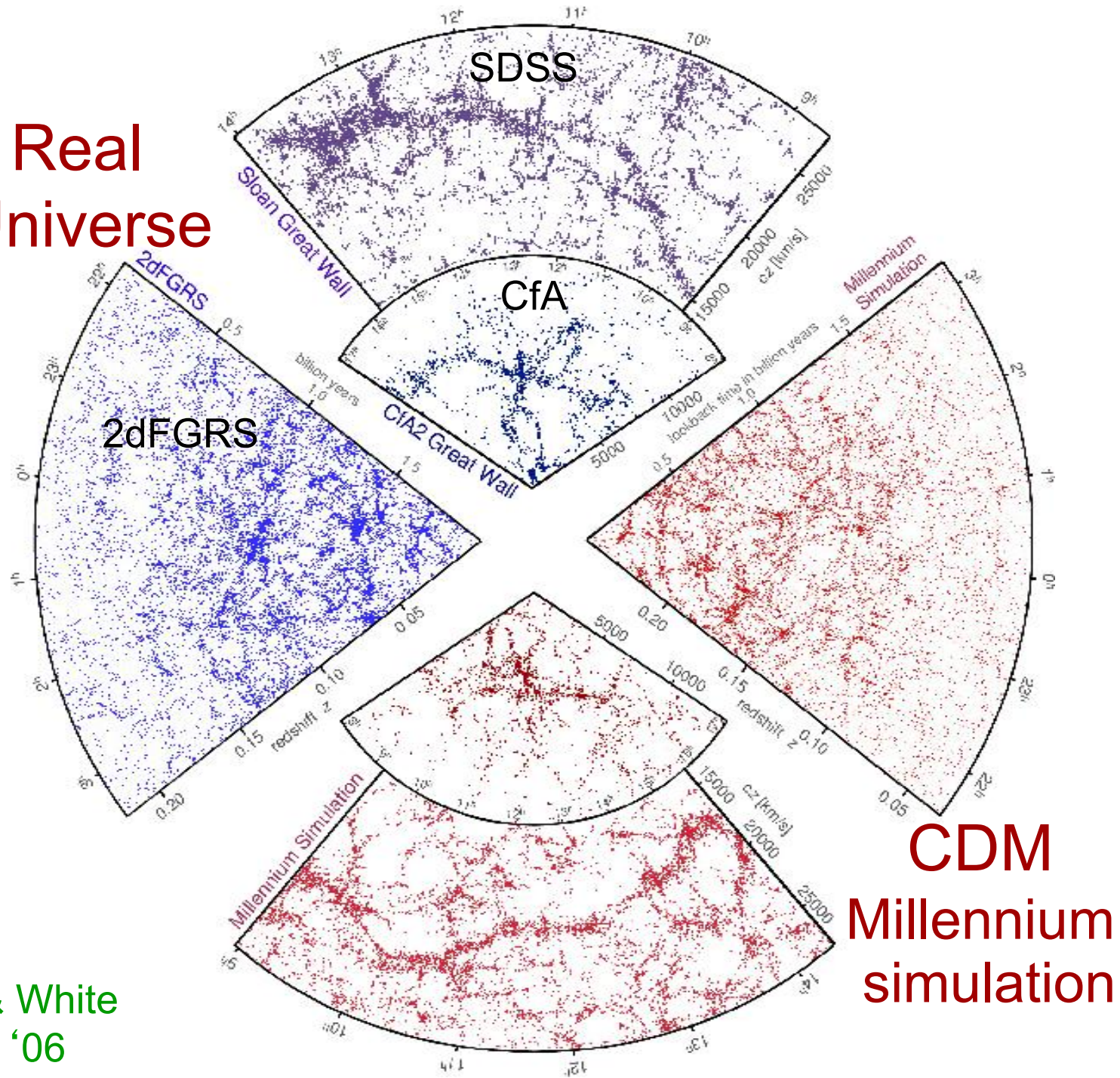
In CDM structure
forms hierarchically



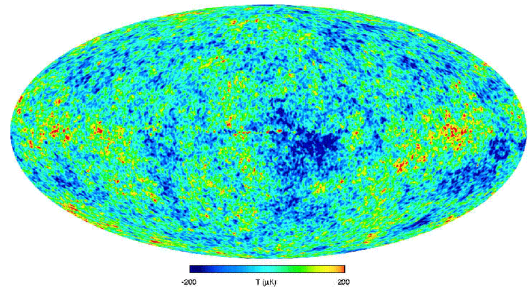
Planck: CMB temperature anisotropies



Real Universe



The cosmic power spectrum: from the CMB to the 2dFGRS

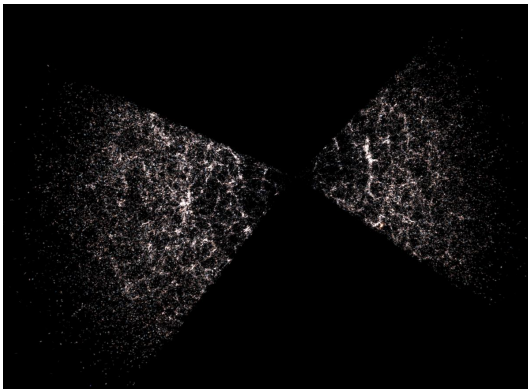


$z \sim 1000$

$\text{Log } k^3 P(k)$

wavelength k^{-1} (comoving h^{-1} Mpc)

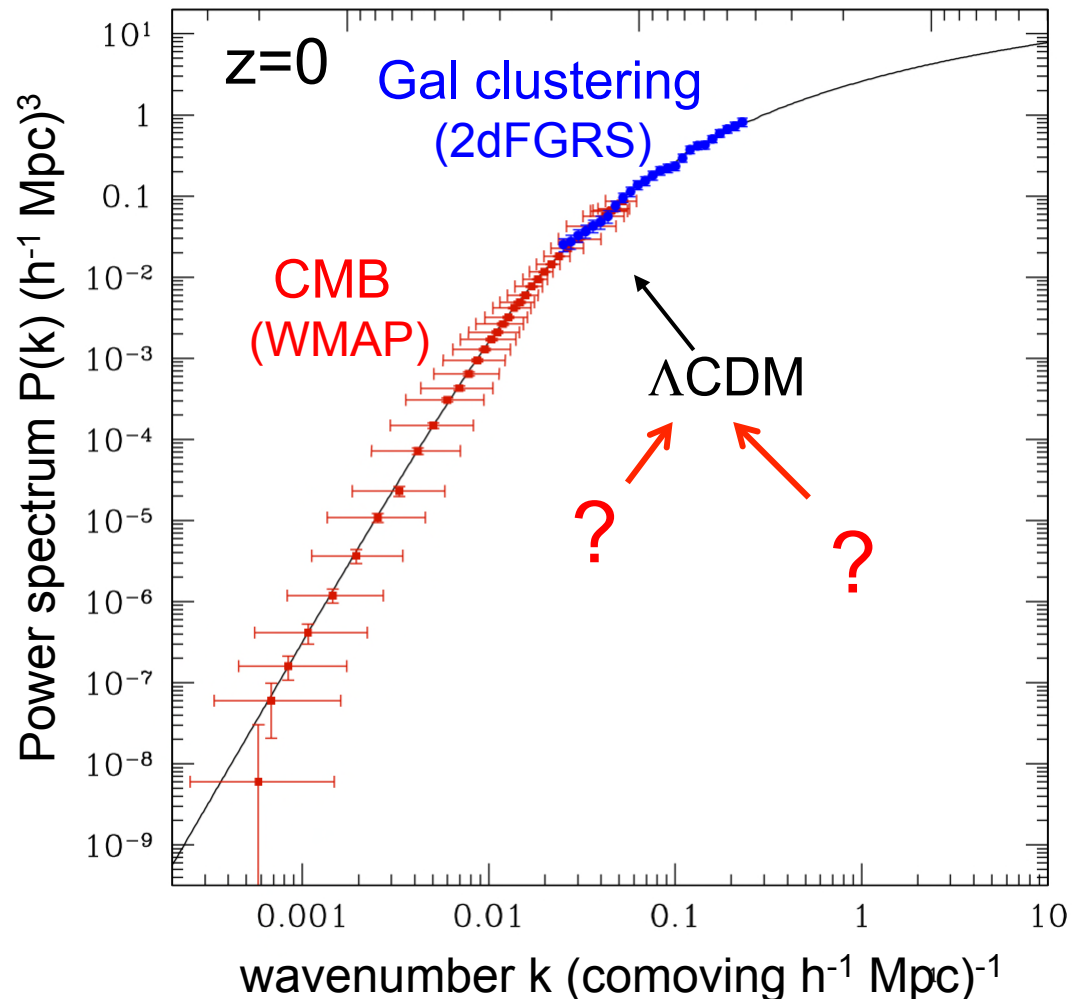
1 000 100 10



$z \sim 0$

⇒ Λ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06



The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming →

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

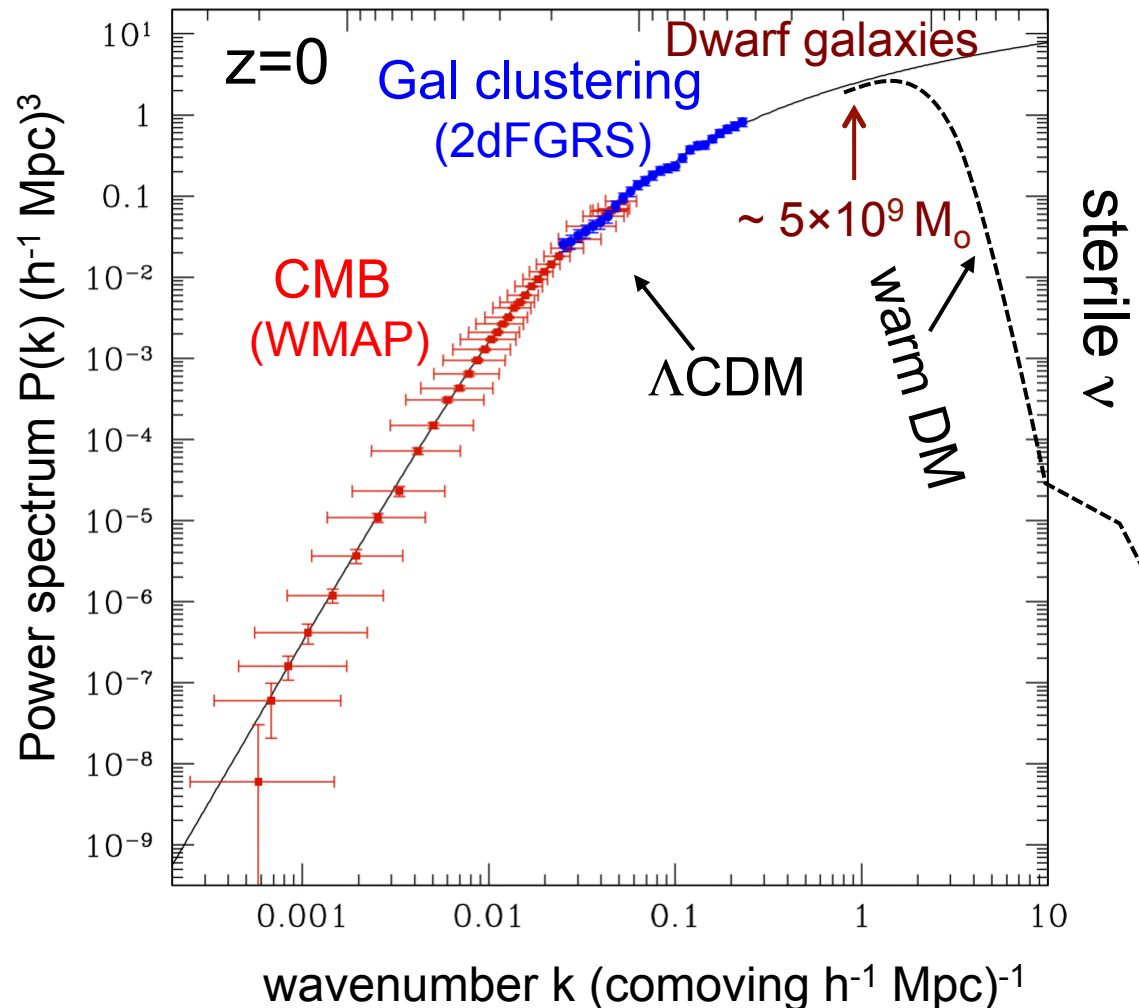
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Log $k^3 P(k)$ wavelength k^{-1} (comoving $h^{-1} \text{ Mpc}$)





Cold Dark Matter

Warm Dark Matter

13.4 billion years ago

cold dark matter

warm dark matter

How can we distinguish between these?

Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,
Boyarski & Ruchayskiy '12

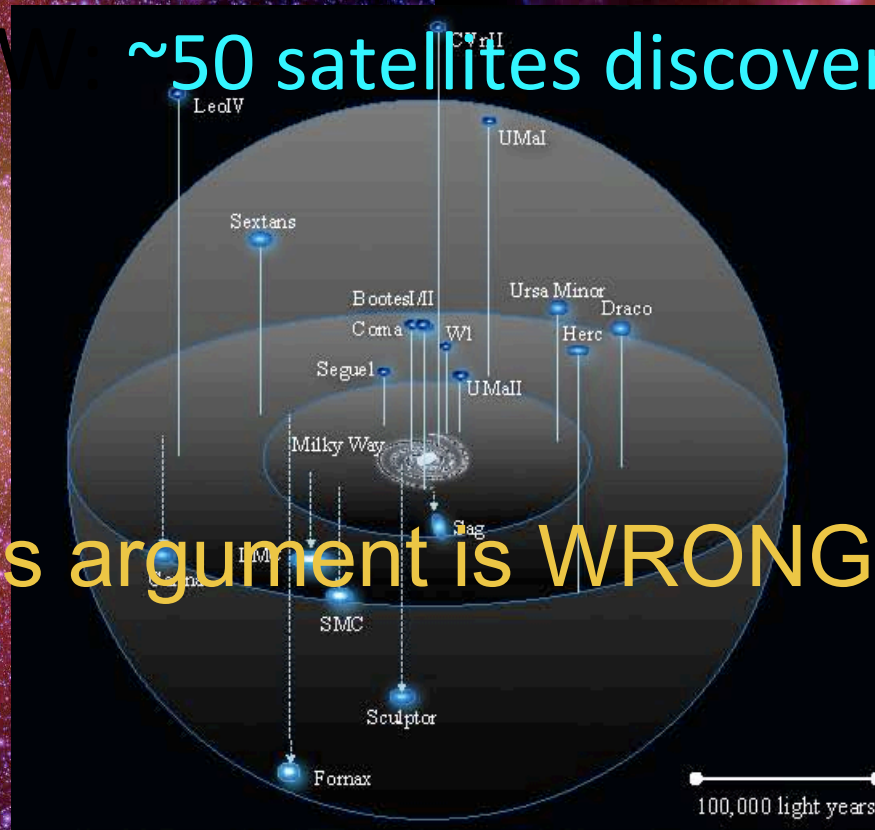
cold dark matter

warm dark matter

Obvious test: count satellites in MW or M31

In the MW ~50 satellites discovered so far

This argument is WRONG!



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,
Boyarski & Ruchayskiy '12

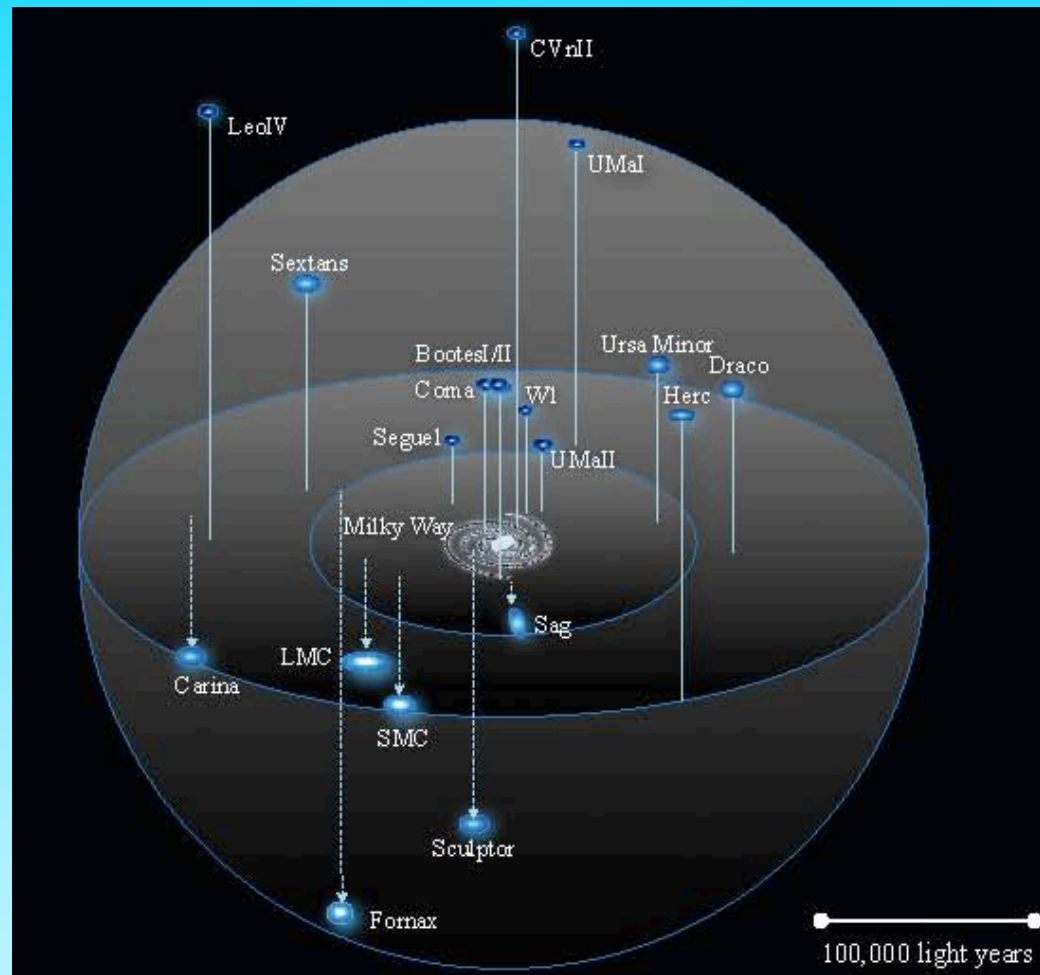
The MW satellite luminosity function

How many satellites are there in the MW?

About **55** satellites known in the MW so far from partial surveys (e.g. SDSS, Pan-STARRS, DES)

Can infer **total** population from survey selection function, assuming a **radial distribution** (from simulations)

(Newton+18, Koposov+08, Tollerud+08, Hargis+14)

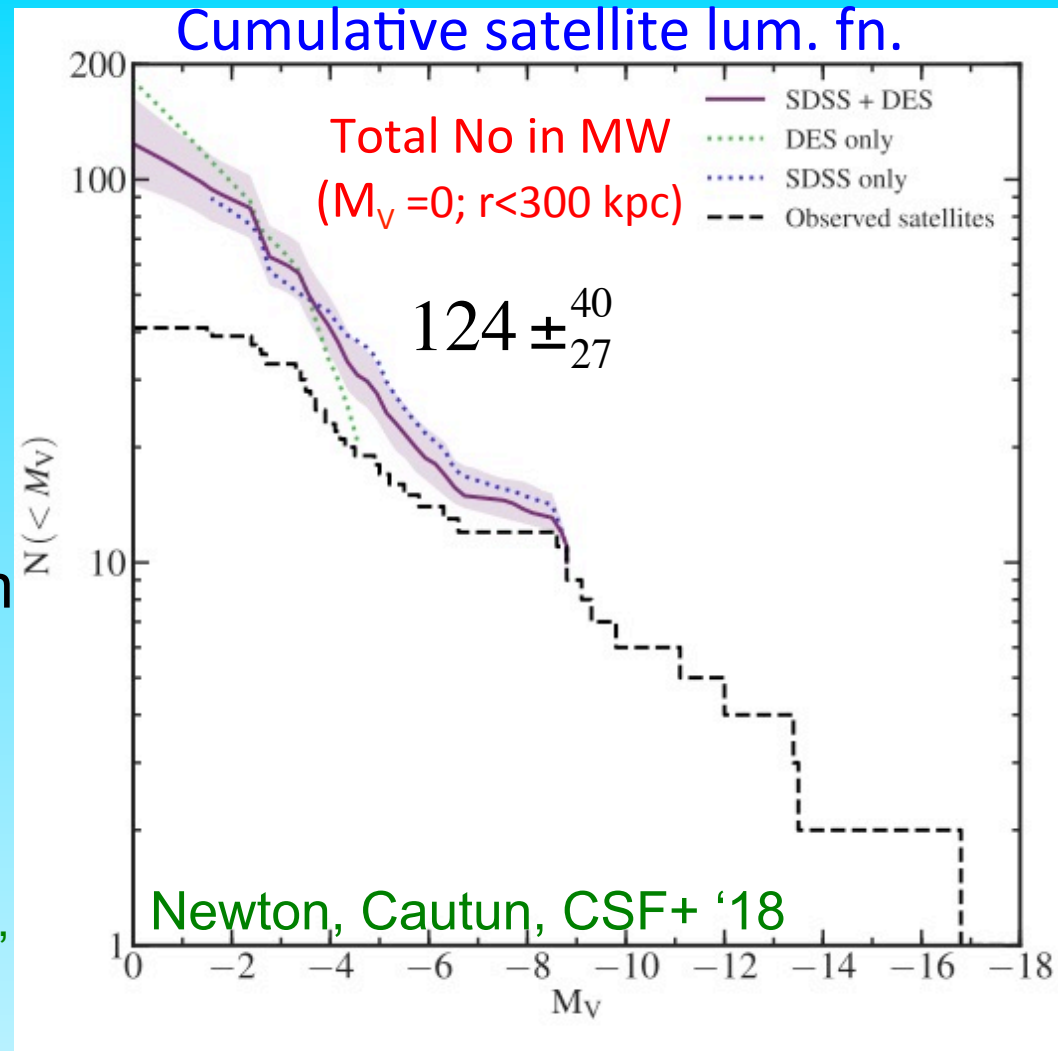


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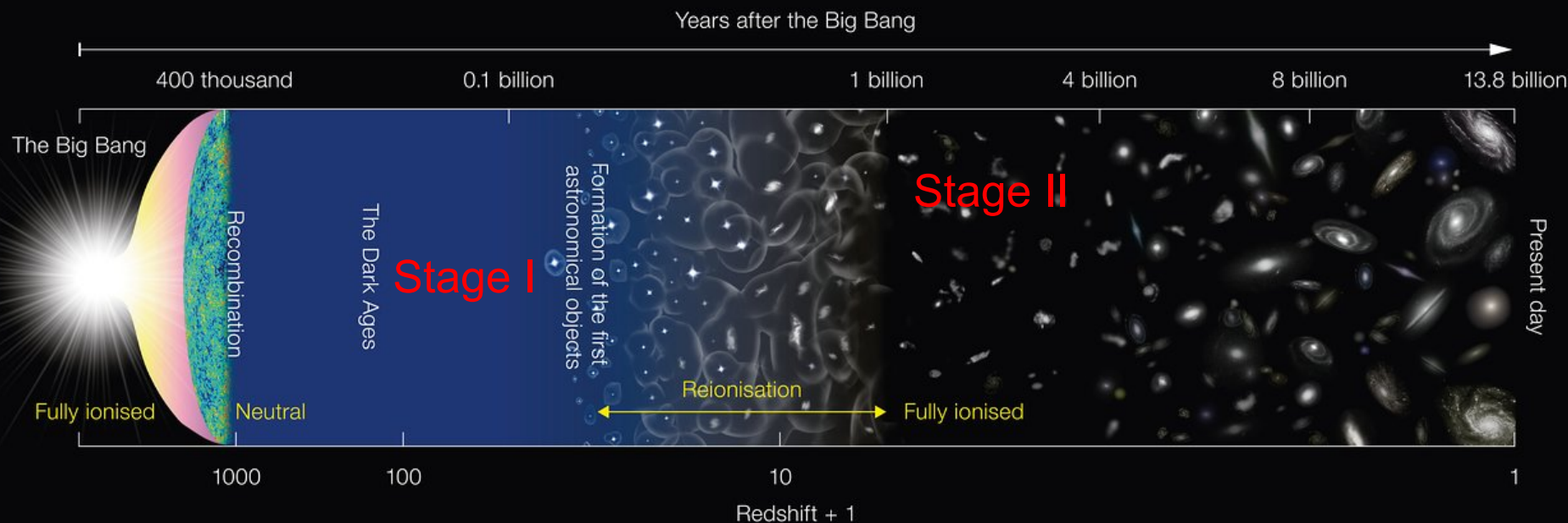
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Most subhalos never make a galaxy!

The two stages of galaxy formation



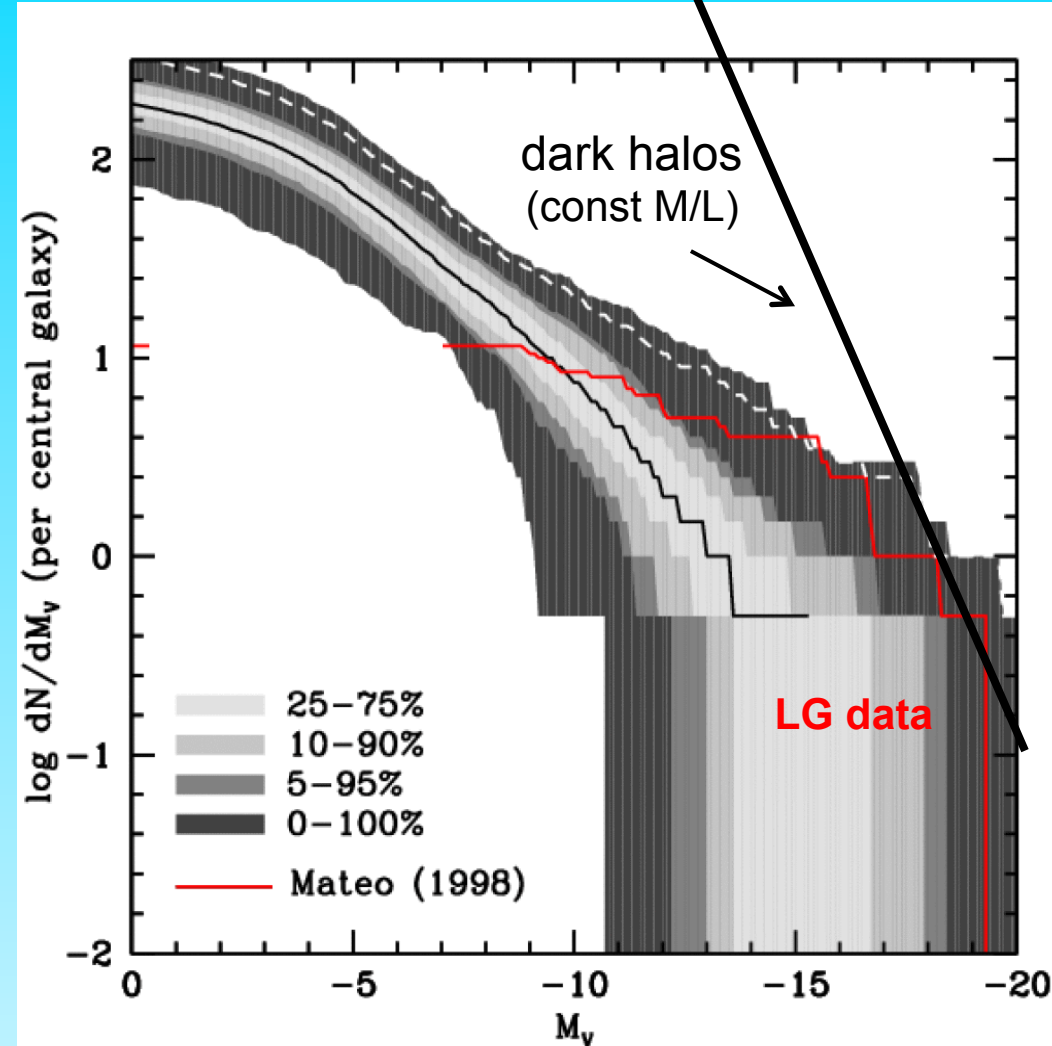
Stage I: Galaxies begin to form during the “dark ages”

First stars reionize H and heat it up to 10^4K → prevents gas from cooling in halos of “ T_{vir} ” $< 10^4\text{K}$ – galaxy formation is interrupted

Stage II: Halos with “ T_{vir} ” $> 10^4\text{K}$ form → galaxy formation resumes

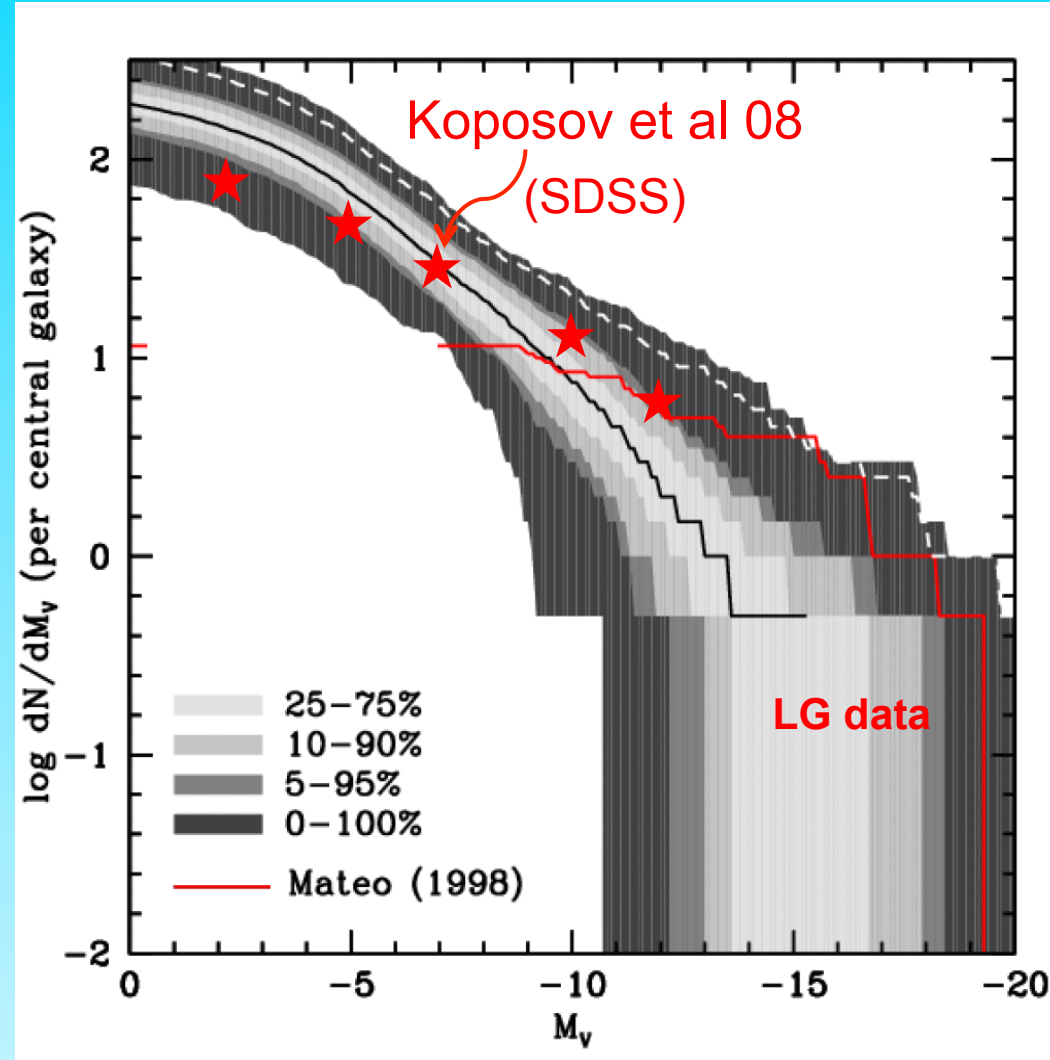
Luminosity Function of Local Group Satellites

- Median model → correct abund. of sats brighter than $M_V = -9$ and $V_{\text{cir}} > 12$ km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare (~10% of cases)



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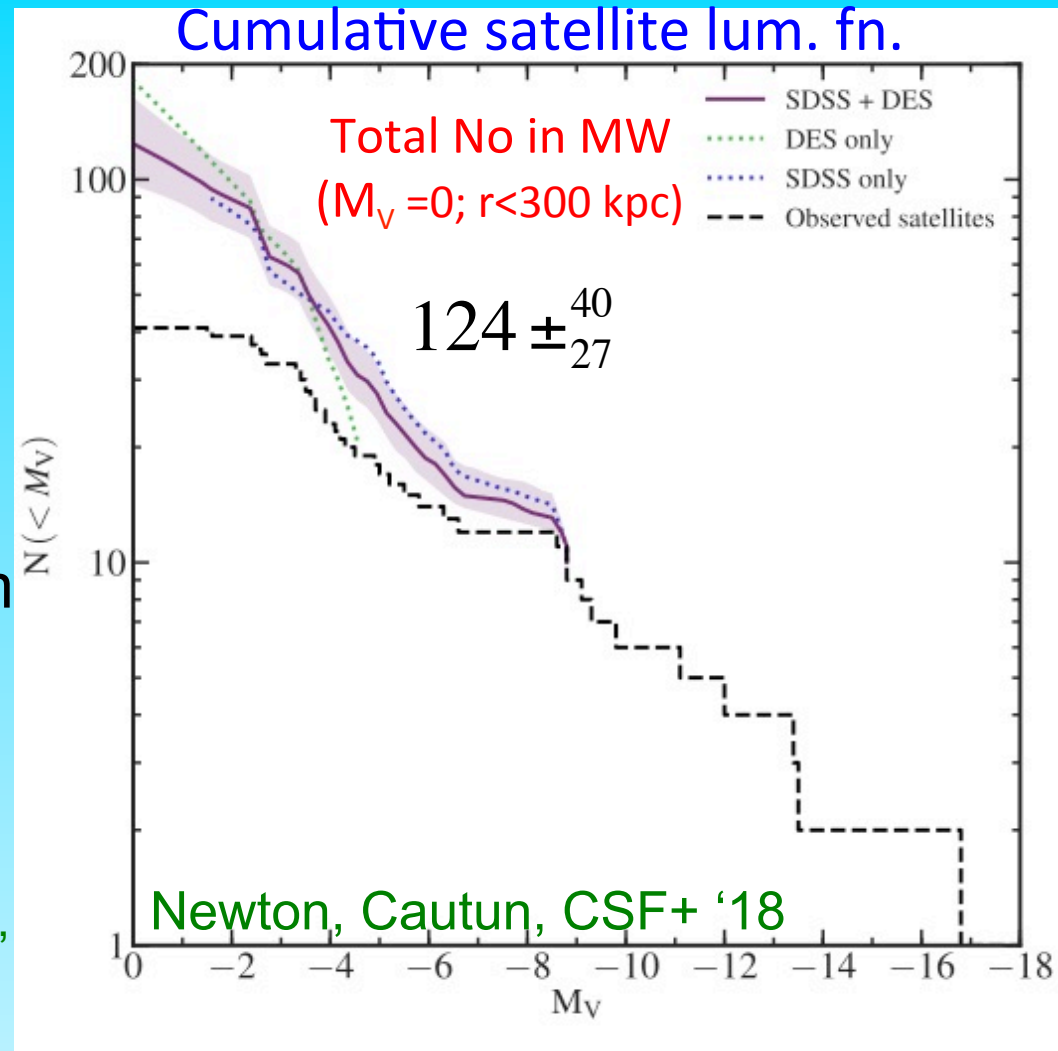


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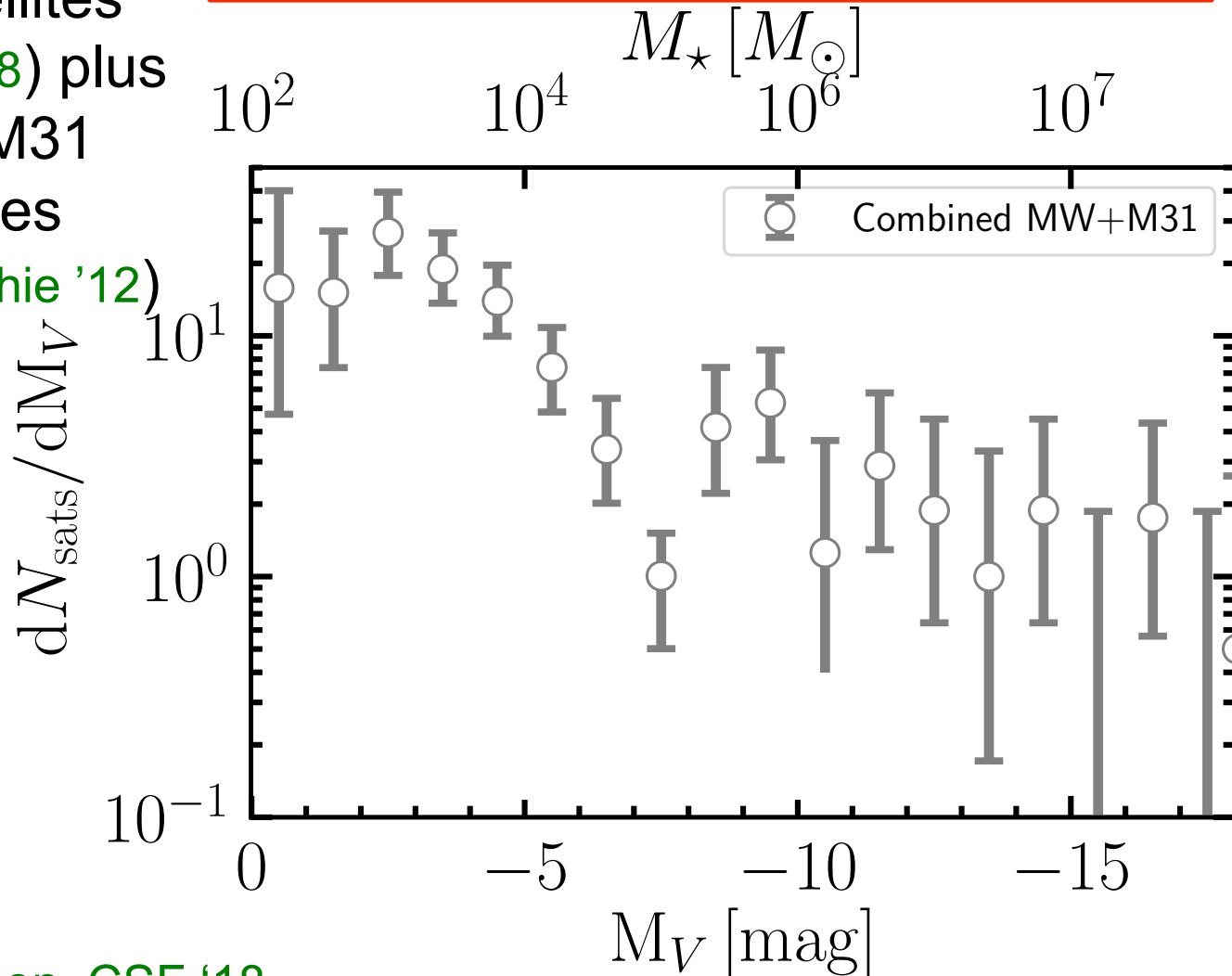
(Newton+18, Koposov+08, Tollerud+08, Hargis+14)



The MW/M31 sat. luminosity function

MW satellites
(Newton+ '18) plus
 $M_V < -8$ M31
satellites
(Mcconnachie '12)

Differential satellite luminosity function



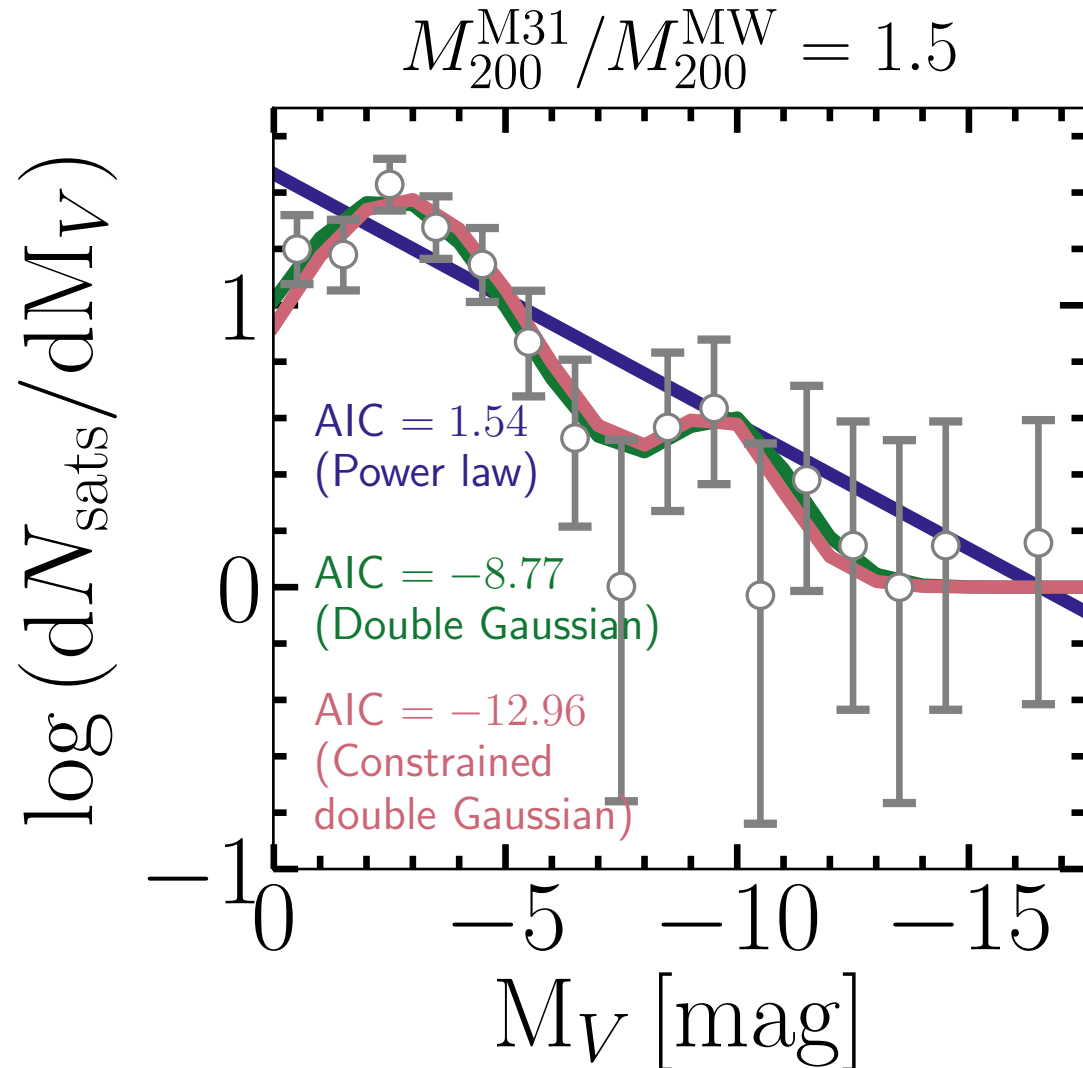
The 2 populations of galactic satellites

Fit 3 models and
compare using
**Akaike Information
Criterion (AIC)**

Model	AIC
Power law	-1.5
Double Gaussian	-8.8
Constrained DG*	-13.0

*Assumes $V_{\text{cut}} = 30$ km/s

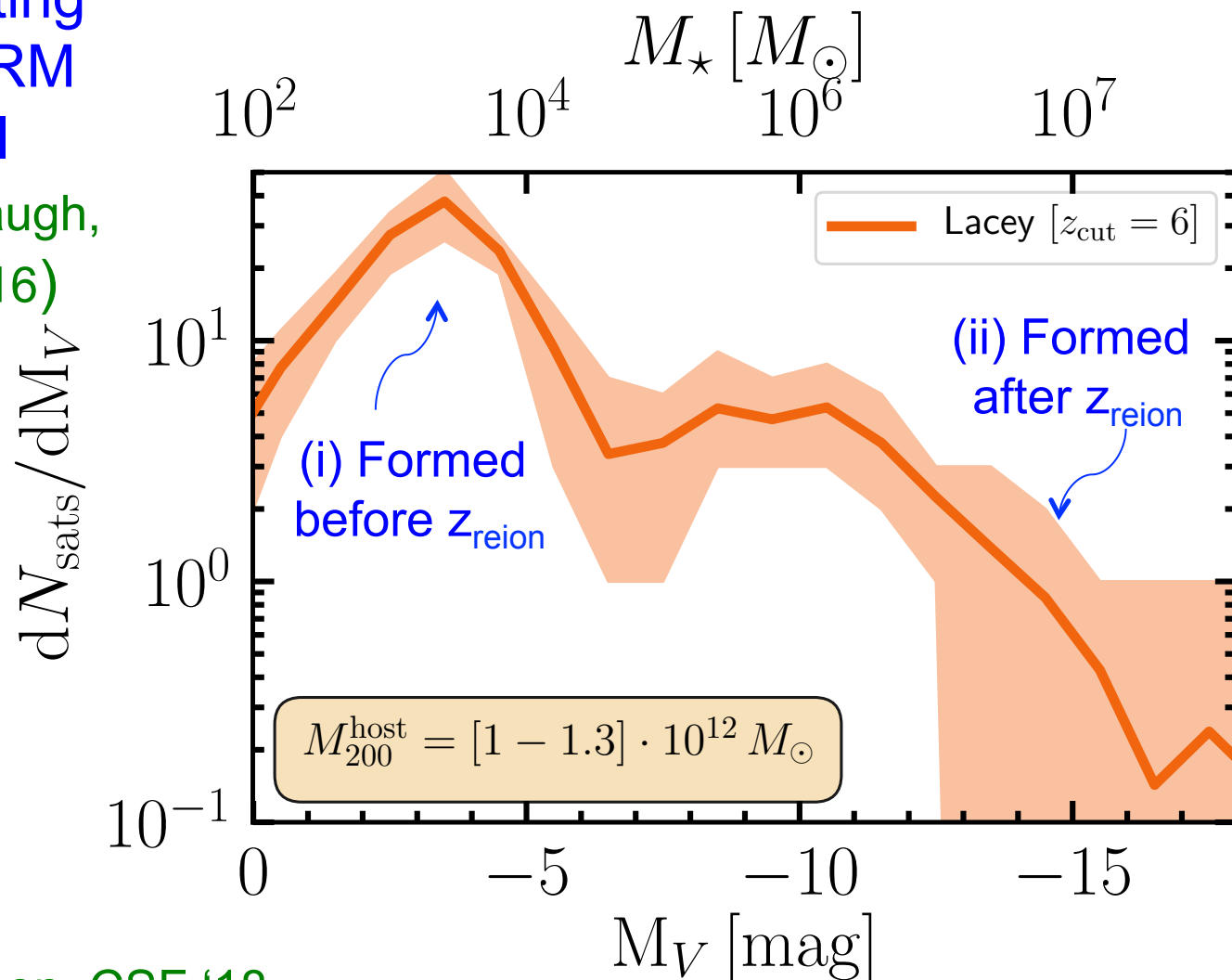
Bose, Deason, CSF '18



Theory vs data

Pre-existing
GALFORM
model

(Lacey, Baugh,
CSF + '16)

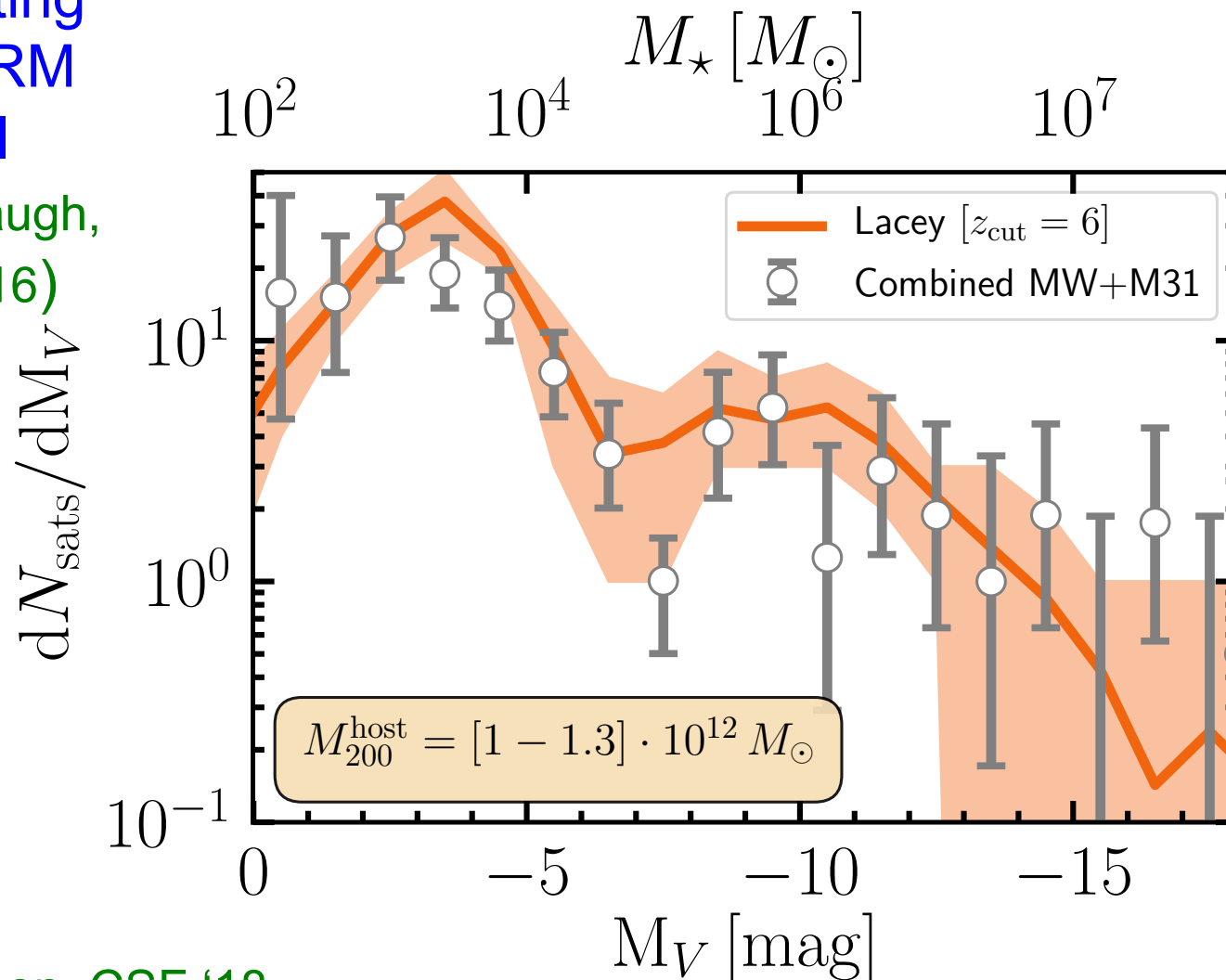


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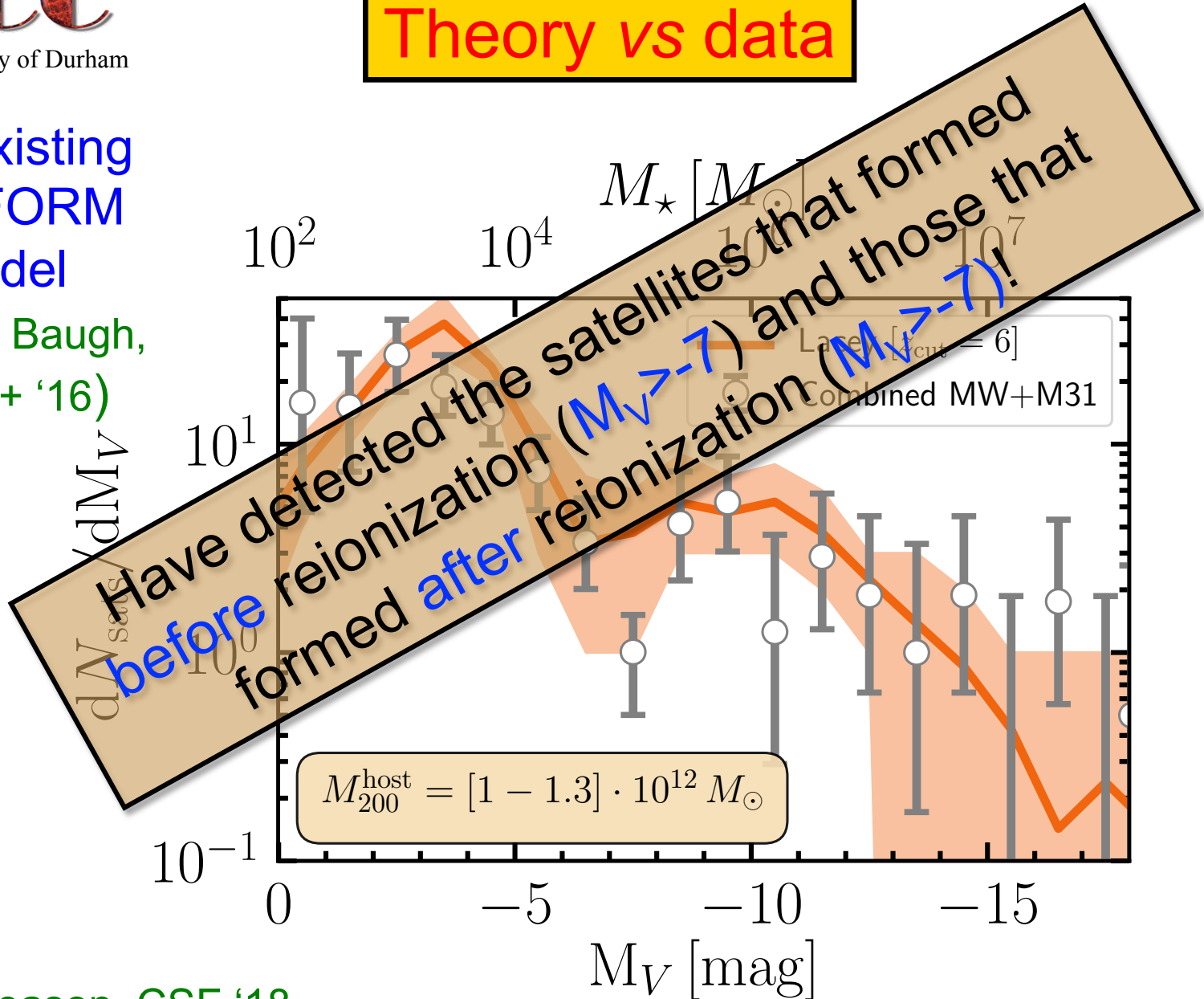


Bose, Deason, CSF '18

Theory vs data

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Bose, Deason, CSF '18



VIRGO

icc.dur.ac.uk/Eagle

“Evolution and assembly of galaxies and
their environment”

THE EAGLE PROJECT

Virgo Consortium

Durham: Richard Bower, Michelle Furlong, Carlos Frenk, Matthieu Schaller, James Trayford, Yelti Rosas-Guevara, Tom Theuns, Yan Qu, John Helly, Adrian Jenkins.

Leiden: Rob Crain, Joop Schaye.

Other: Claudio Dalla Vecchia, Ian McCarthy, Craig Booth...

The Eagle Simulations

EVOLUTION AND ASSEMBLY OF GALAXIES AND THEIR ENVIRONMENTS

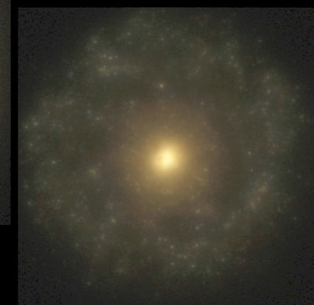
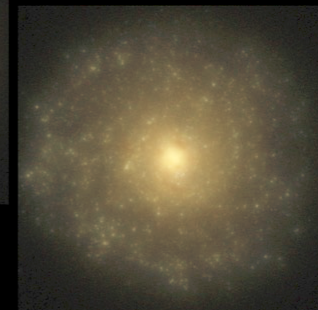
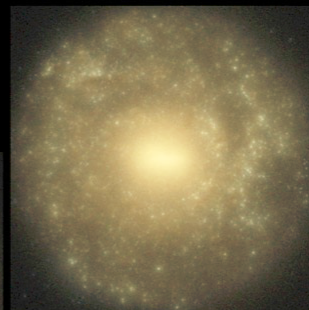
The Hubble Sequence realised in cosmological simulations

E0

E7

S0

SB



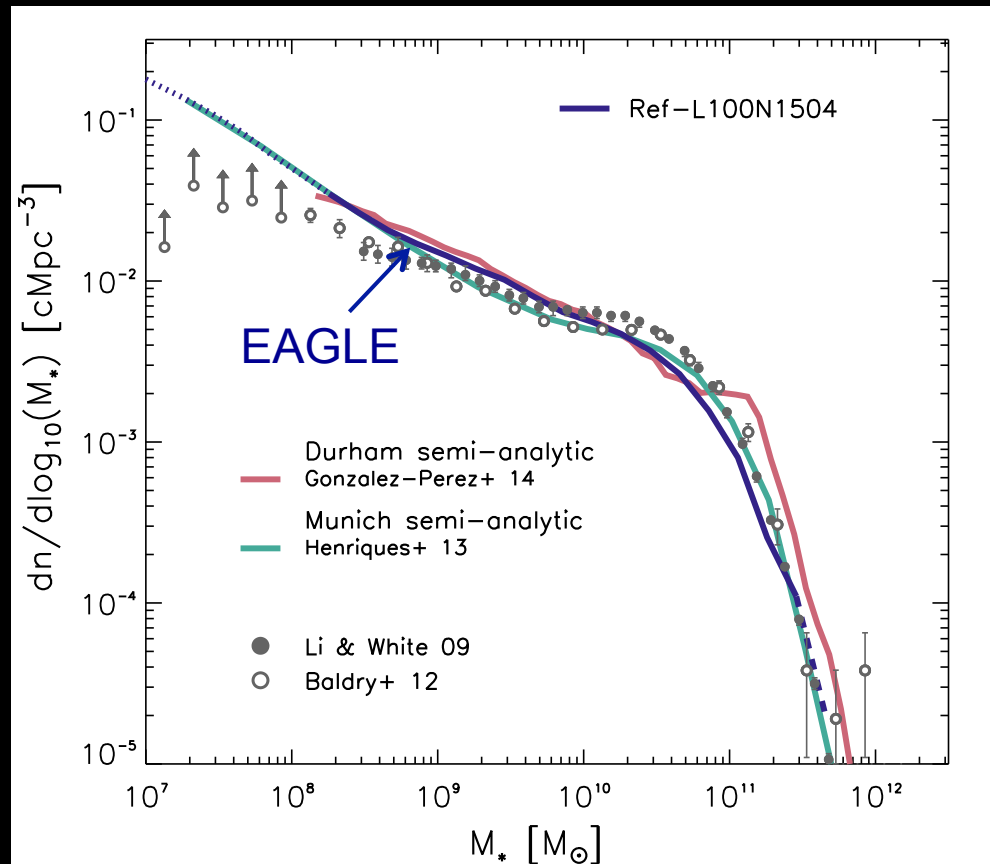
Irr

S

Trayford et al '15

Galaxy stellar mass function

Comparison to semi-analytic models



VIRG

Dark matter

APOSTLE
EAGLE full
hydro
simulations

Local Group

CDM

Sawala et al '16



Stars

VIRGO

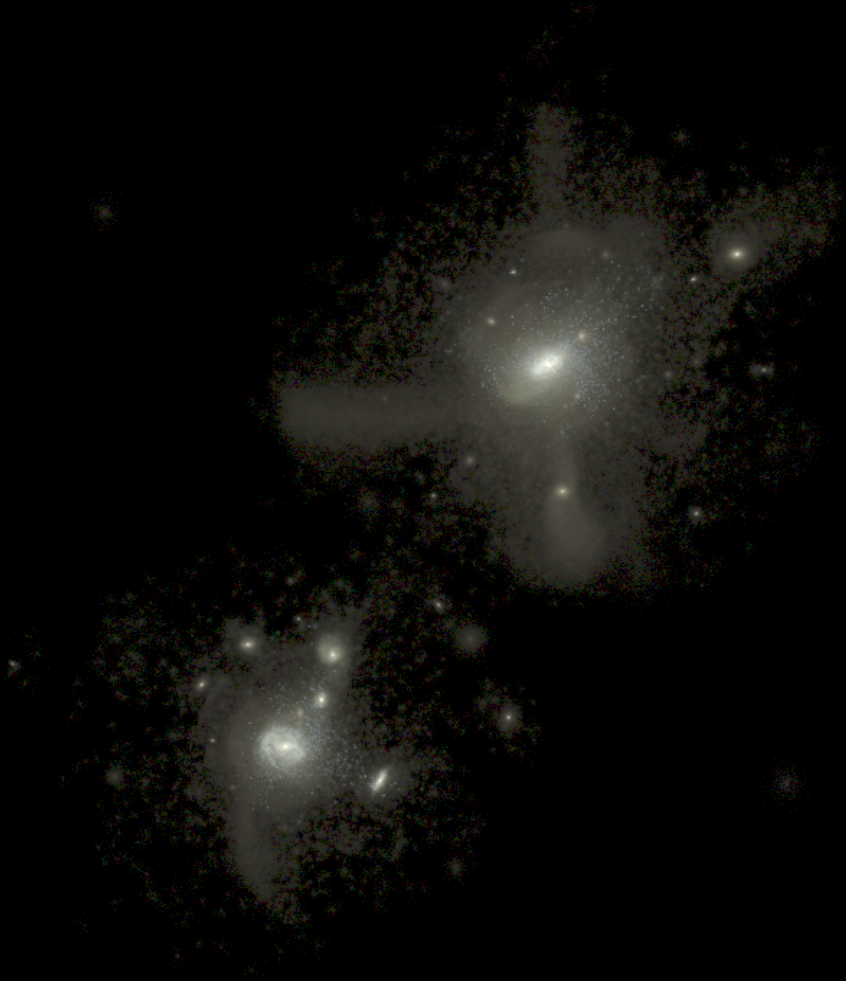
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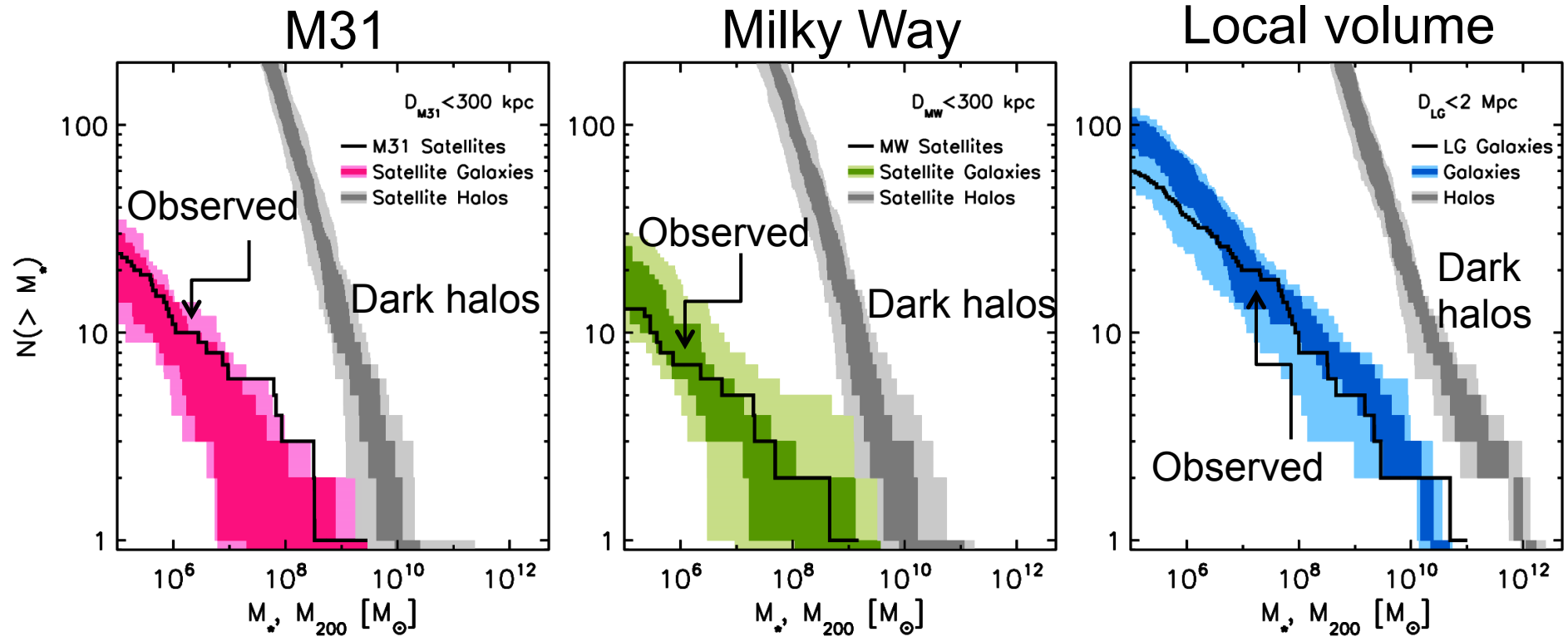
Stars

Far fewer satellite galaxies than CDM halos

Sawala et al '16



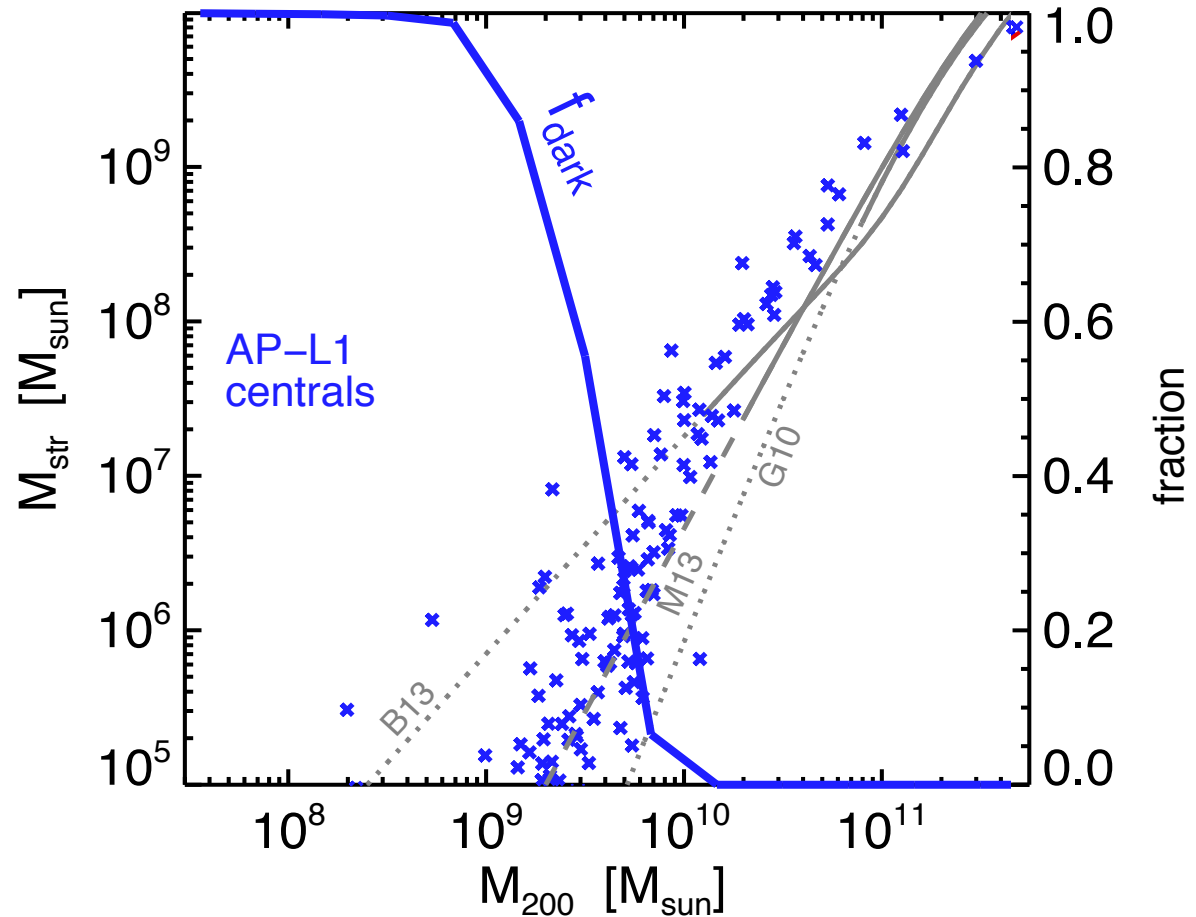
EAGLE Local Group simulation



Fraction of dark subhalos

$$V_c = \sqrt{\frac{GM}{r}}$$

$$V_{\max} = \max V_c$$



All halos of mass $< 5 \times 10^8 M_\odot$ or $V_{\max} < 7 \text{ km/s}$ are dark ($m_* < 10^4 M_\odot$)

There is **no** such thing as the
“**satellite problem**” in CDM!

CDM theory **predicts 2** populations of gal.
satellites, formed (i) before and (ii) after
reionization



Seem to be **present** in the **data**

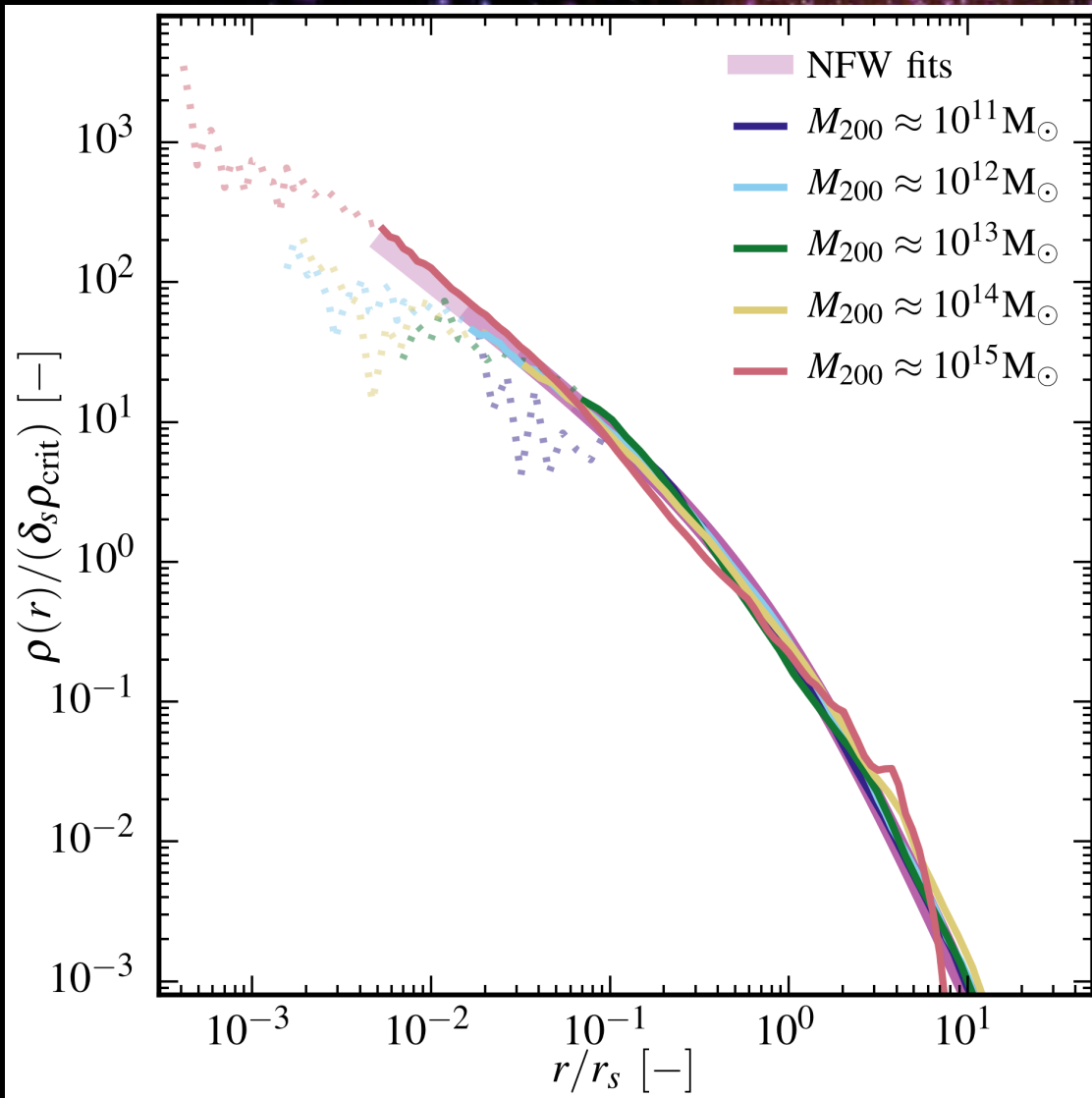


The MW satellite lum fn is
compatible with CDM

Can the inner
structure of satellites
provide a test?



The Density Profile of Cold Dark Matter Halos



Shape of halo profiles
~independent of halo mass &
cosmological parameters

Density profiles are “cuspy” -
no ‘core’ near the centre

Fitted by simple formula:

$$\frac{\rho(r)}{\rho_{\text{crit}}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

(Navarro, Frenk & White '97)

More massive halos and
halos that form earlier have
higher densities (bigger δ)



The core-cusp problem

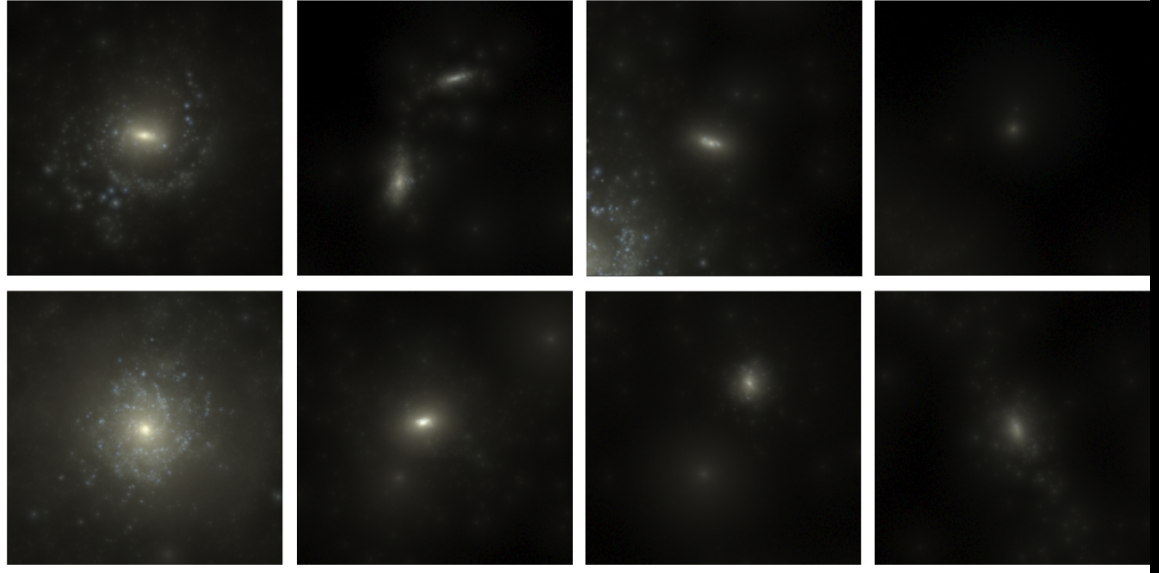
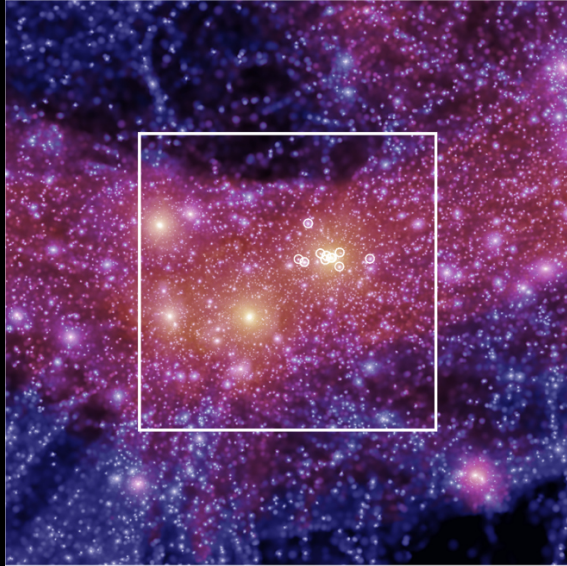
cold dark matter

warm dark matter

Halos and subhalos in CDM & WDM have
cuspy NFW profiles

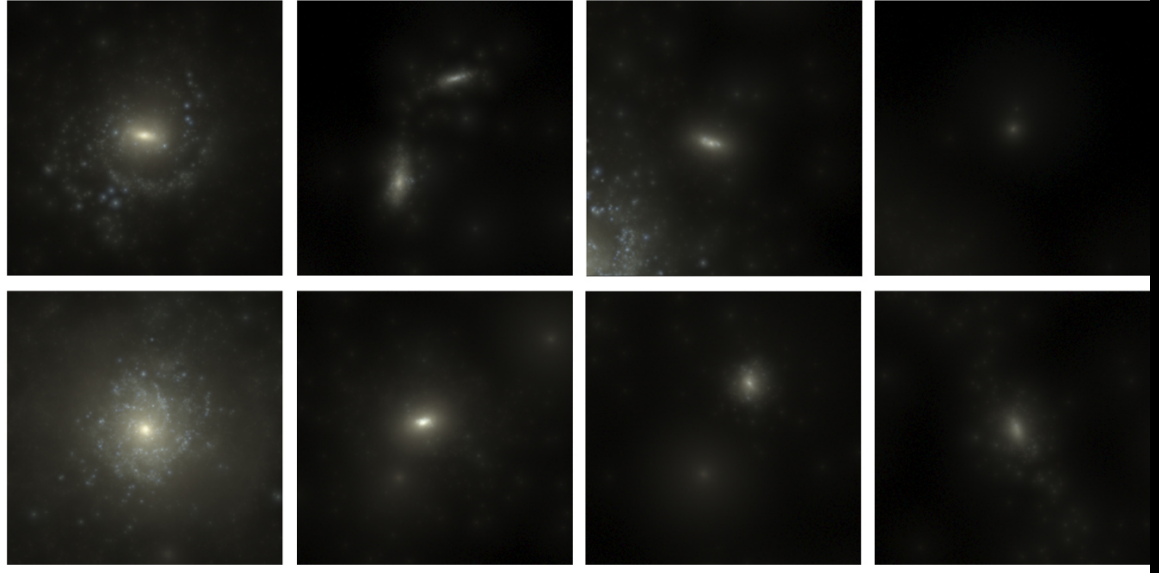
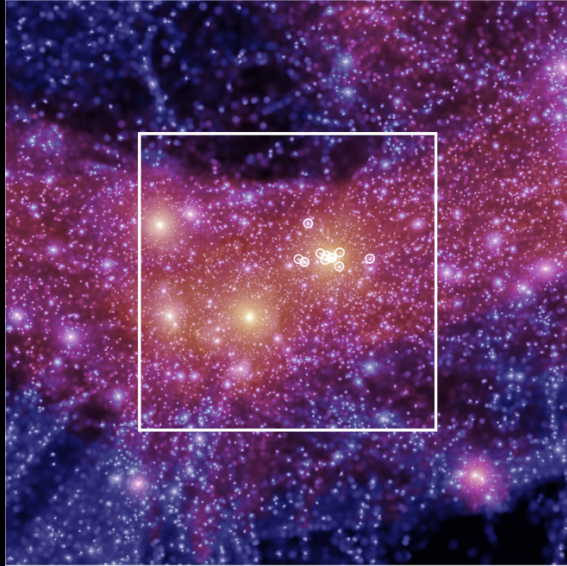
$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r / r_s)(1 + r / r_s)^2}$$

Lovell, Eke, Frenk, Gao, Jenkins, Theuns '12



EAGLE/Apostle/
Auriga galaxies have
NFW cusps

Sawala et al '15



Does Nature have them?



Sawala et al '15



There is **NO** evidence for
cores in dwarf galaxies

(Existing data are consistent
with either cusps or cores)

(e.g Strigari+ 15, Genina +18,
Oman+ 18)



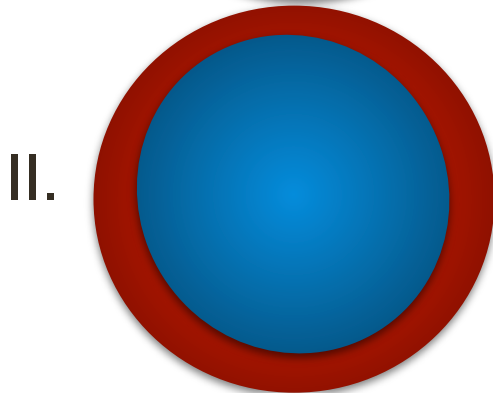
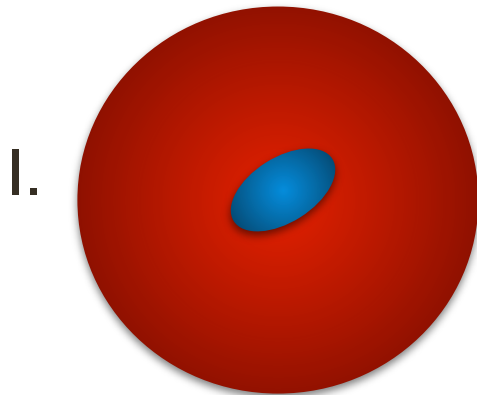


But if cores were found in halos, would this rule out CDM (and WDM)?

The physics of core formation

Cusps \rightarrow cores

Perturb central halo region
by growing a galaxy
adiabatically and removing
it suddenly (Navarro, Eke
& Frenk '96)



Navarro, Eke & Frenk (1996)

The cores of dwarf galaxy haloes L75

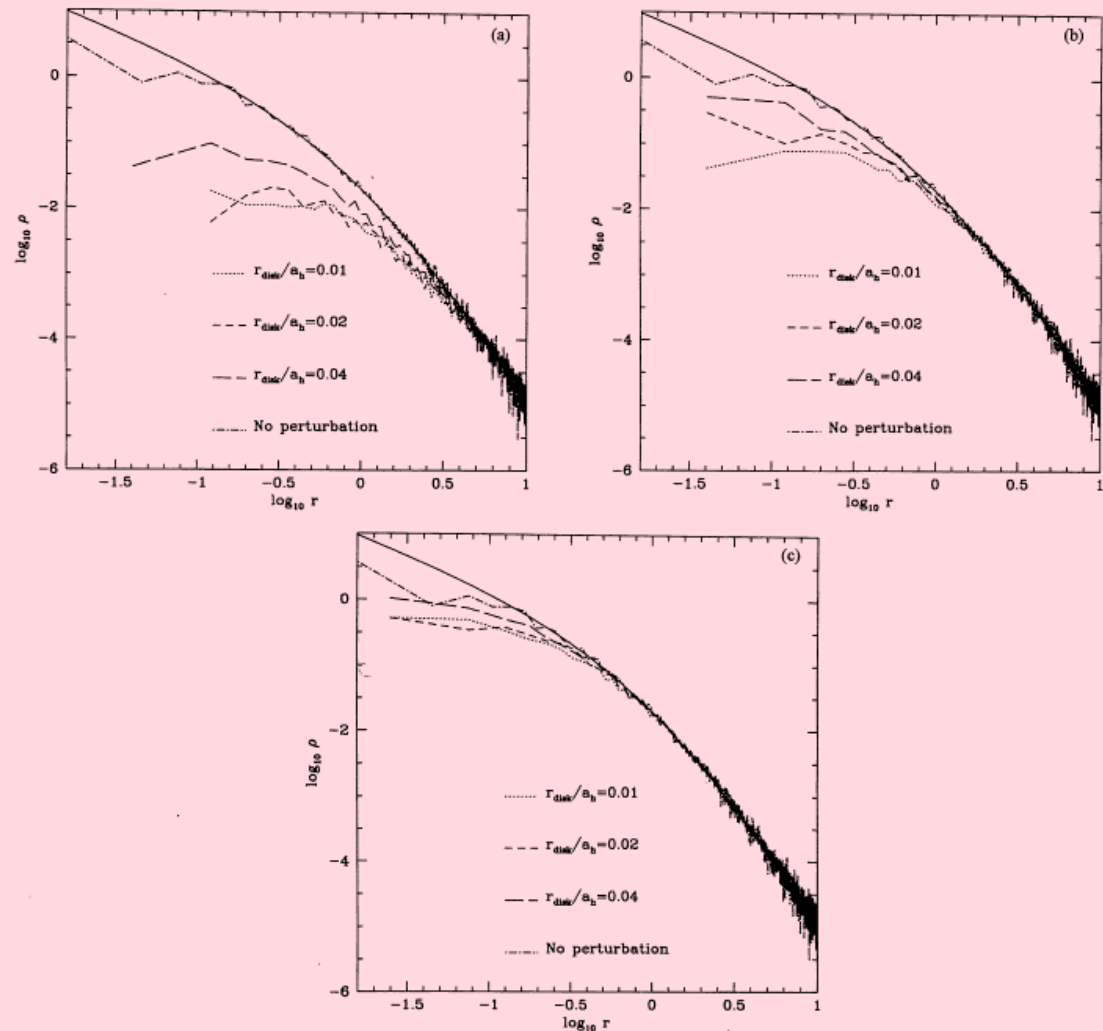


Figure 3. Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10 000-particle realization of the Hernquist model run in isolation at $t=200$. (a) $M_{\text{disc}}=0.2$. (b) $M_{\text{disc}}=0.1$. (c) $M_{\text{disc}}=0.05$.

The physics of core formation

Cusps \rightarrow cores

Perturb central halo region
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Cores may also form by
repeated fluctuations in
central potential (e.g. by
SN explosions) (Read &
Gilmore '05; Pontzen &
Governato '12,'14; Bullock &
Boylan-Kolchin '17)

Navarro, Eke & Frenk (1996)

The cores of dwarf galaxy haloes L75

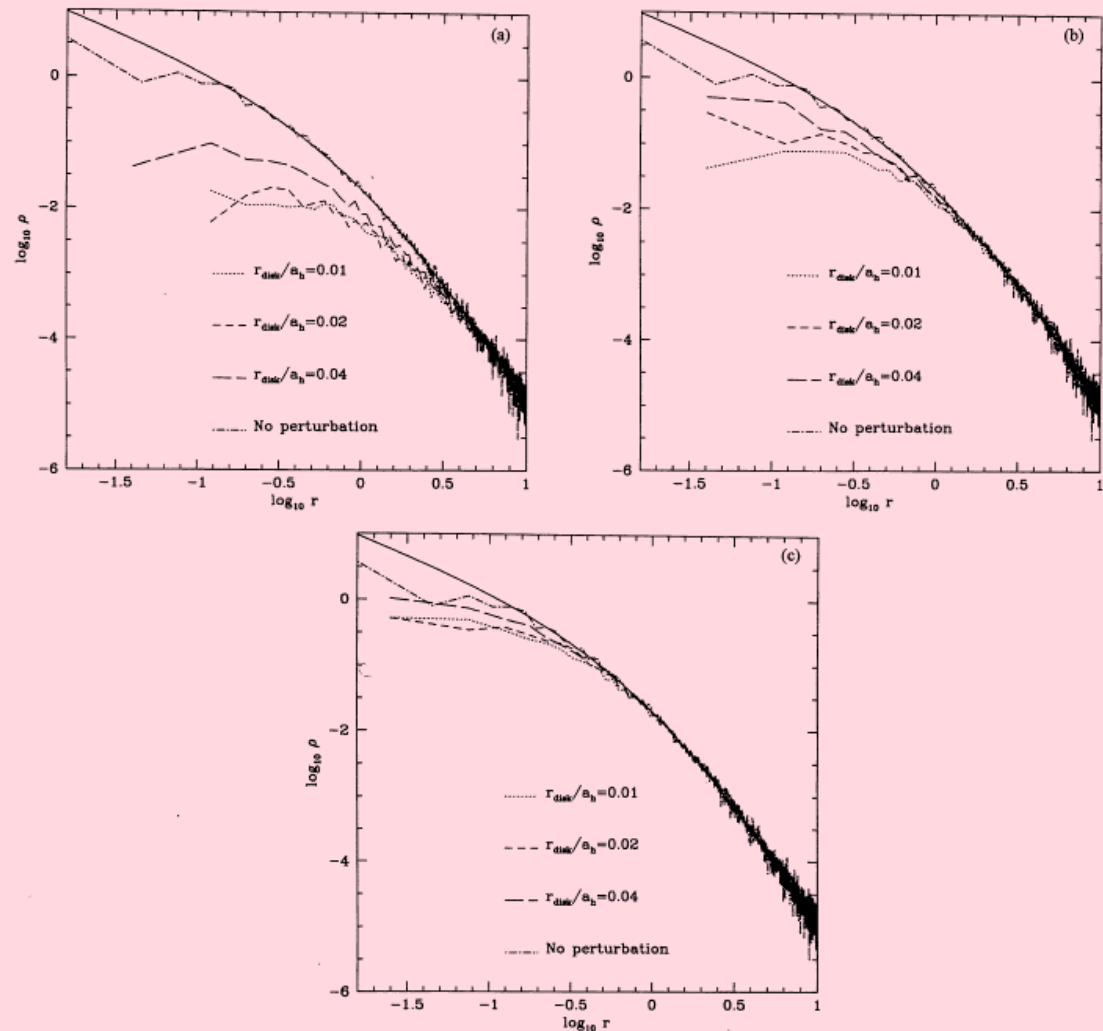


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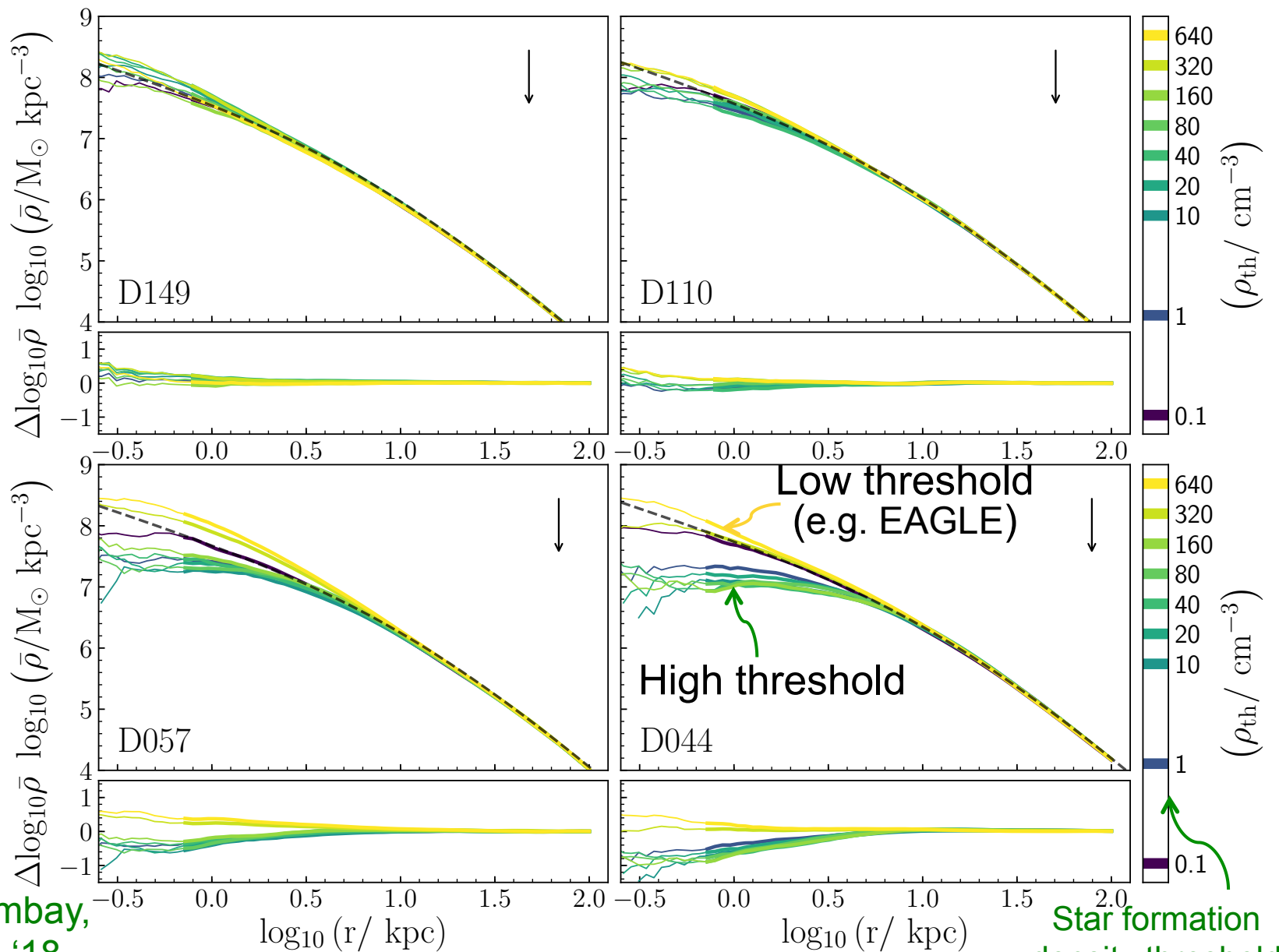
Cores or cusps in simulations?

Key parameter: gas density threshold for star formation

High density → NEF mechanism

Low density → not enough central gas density to perturb DM

Cores or cusps in simulations?





There is **NO** strong evidence
for cores in dwarf galaxies

(Existing data are consistent
with either cusps or cores)

But in any case cores
can be easily created
by baryon effects





Is there any way we can
distinguish CDM from
WDM?

There is no need for
despair: there is a way
to distinguish them





Can we distinguish CDM/WDM?

cold dark matter

warm dark matter

Rather than counting faint galaxies,
count the number of dark halos



Can we distinguish CDM/WDM?

cold dark matter

warm dark matter

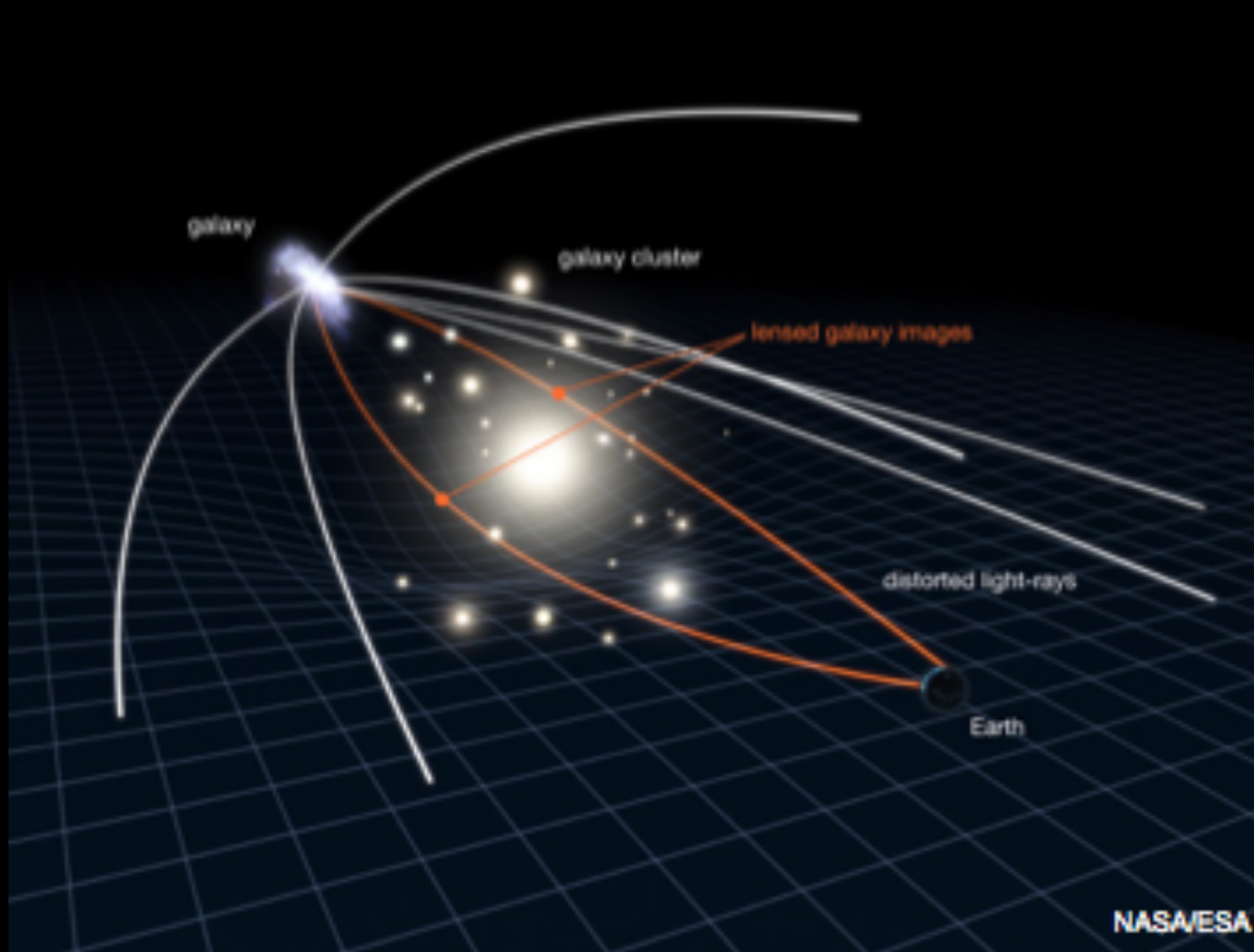
Dark halos can be detected through
gravitational lensing



Gravitational lensing: Einstein rings

How to rule out CDM

Gravitational lensing: Einstein rings



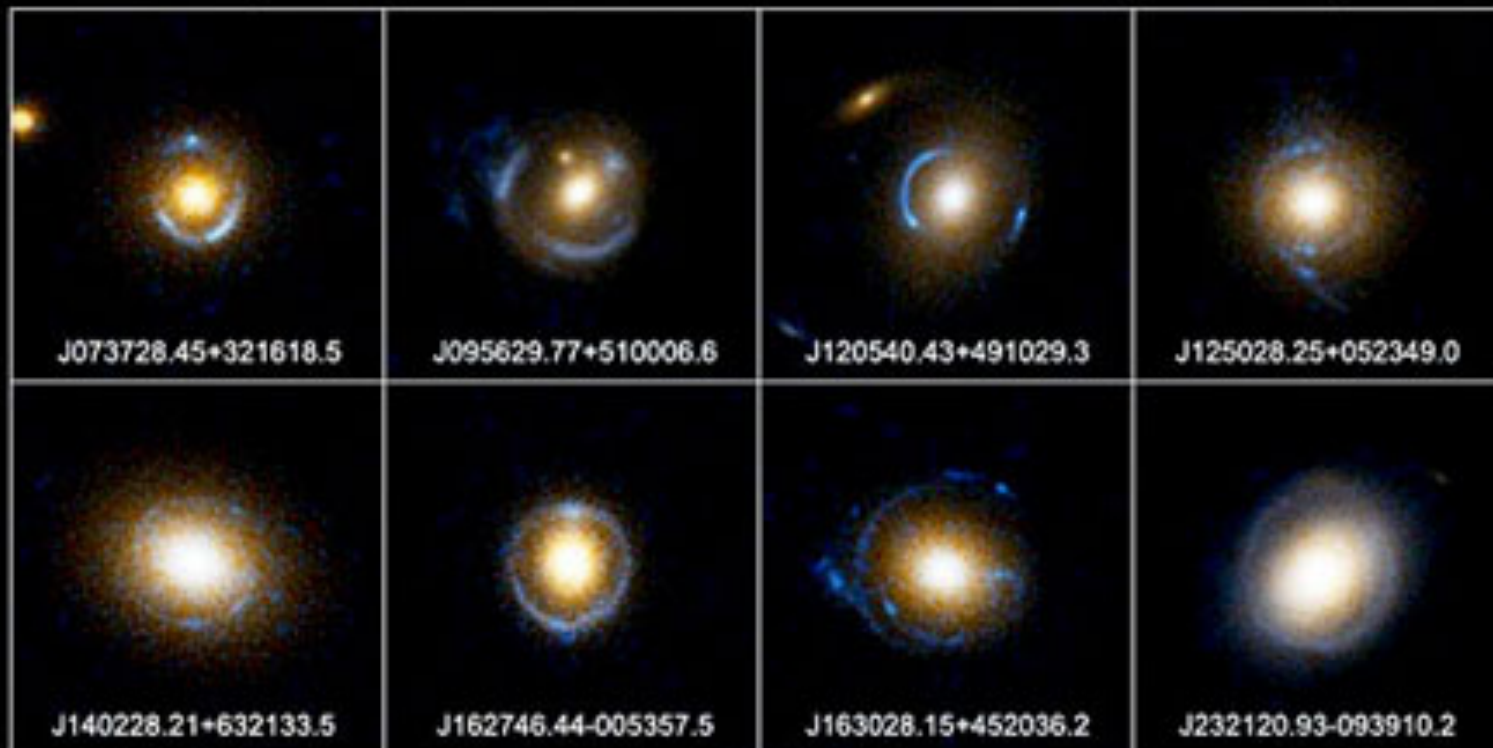
When the source and the lens are well aligned → strong arc or an Einstein ring



SLAC sample of strong lenses

Einstein Ring Gravitational Lenses

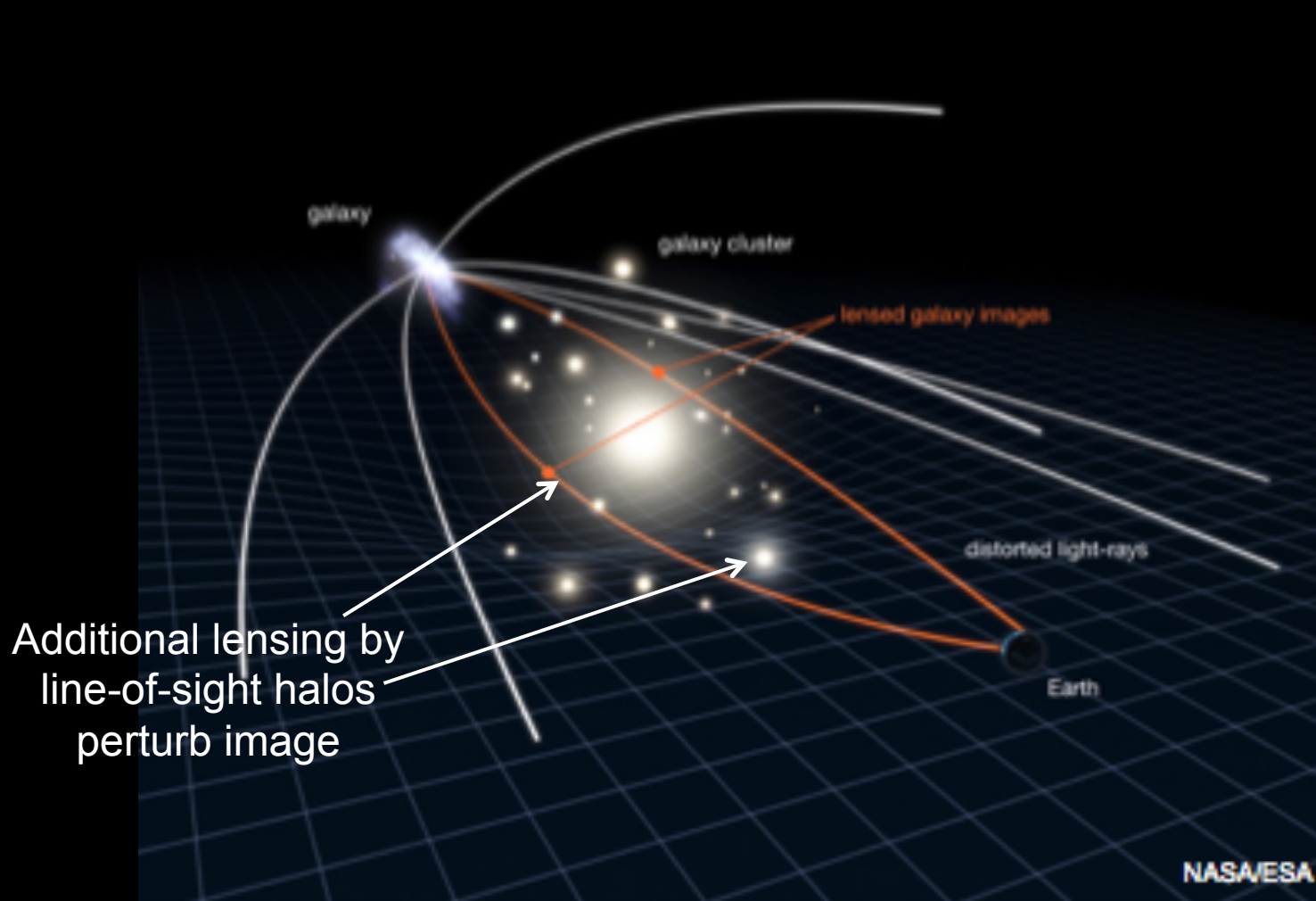
Hubble Space Telescope • ACS



NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

STScI-PRC05-32

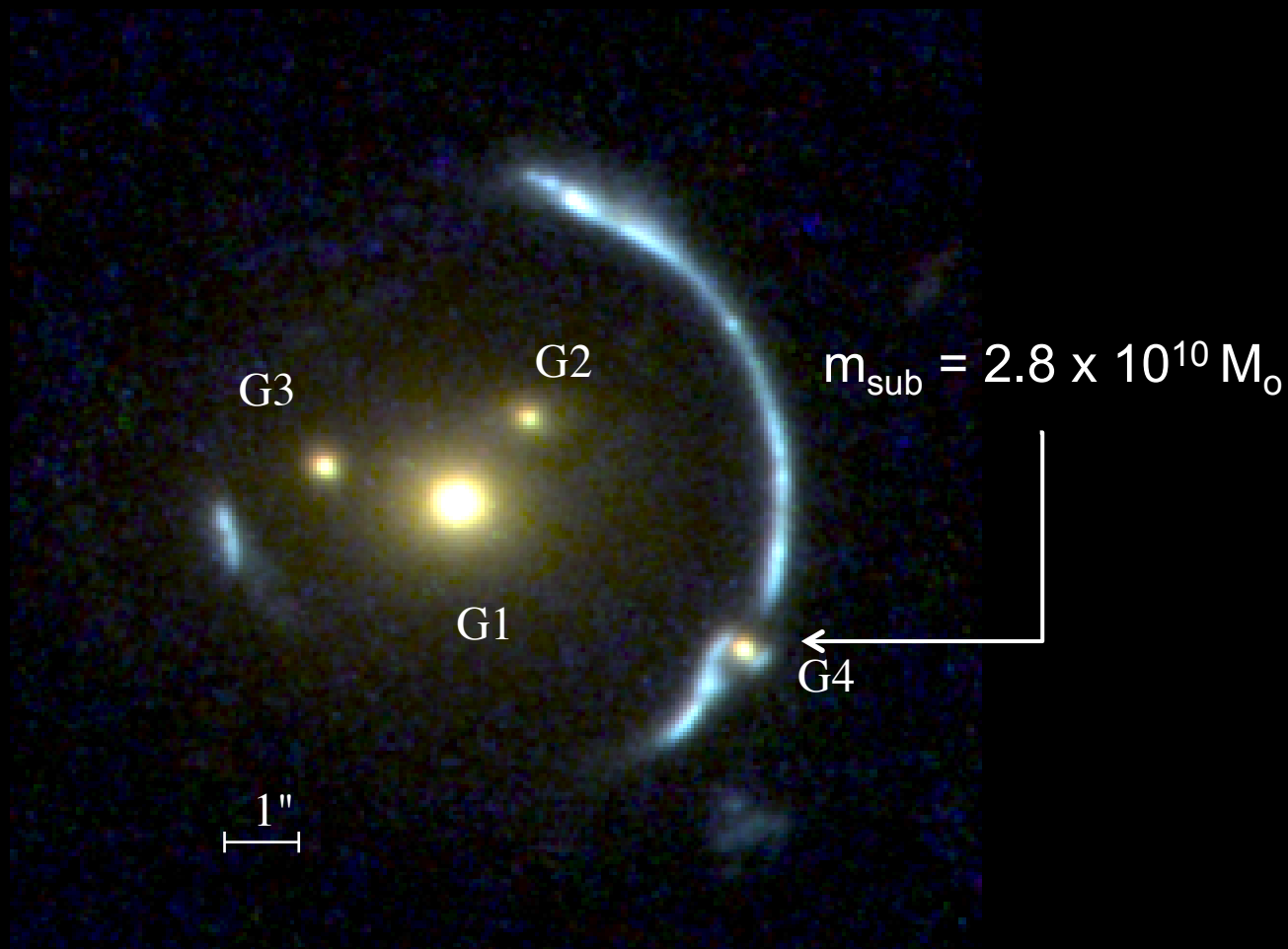
Gravitational lensing: Einstein rings



When the source and the lens are well aligned → strong arc or an Einstein ring

Gravitational lensing: Einstein rings

Halos projected onto an Einstein ring distort the image





Gravitational lensing: Einstein rings

Halos projected onto an Einstein ring distort the image



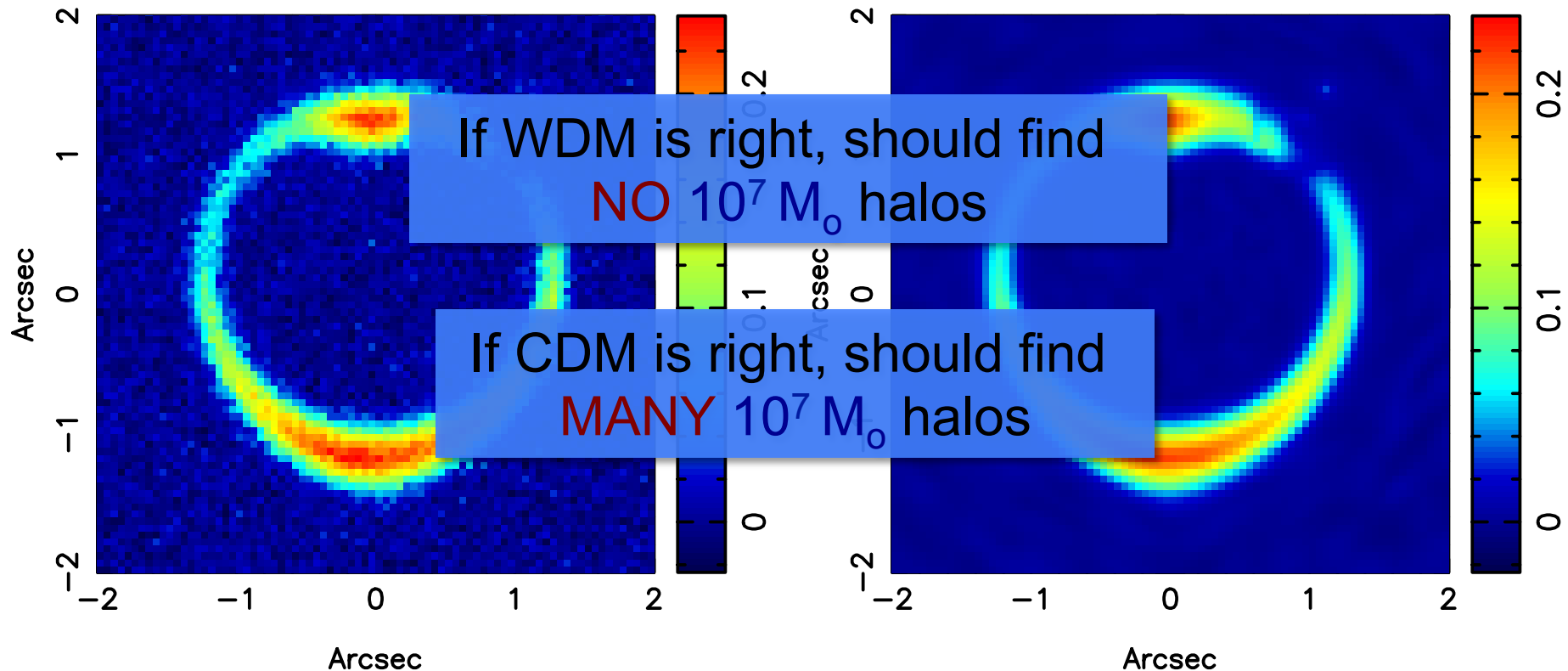
Vegetti & Koopmans '09

Detecting substructures with strong lensing

Can detect subhalos as small as $10^7 - 10^8 M_\odot$

Data

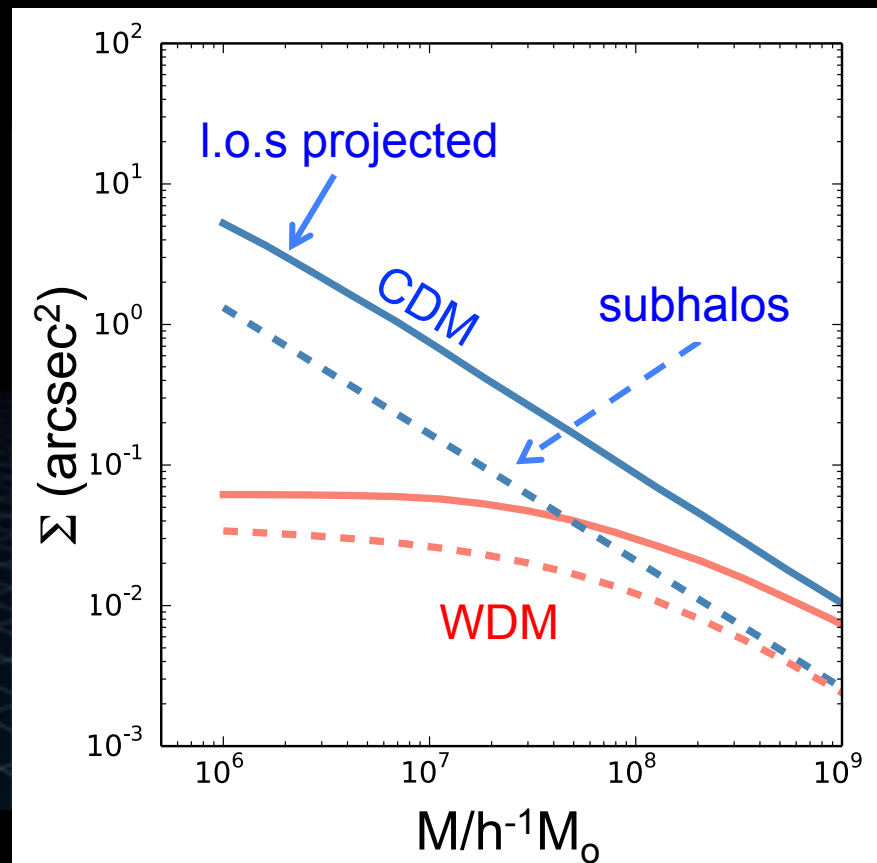
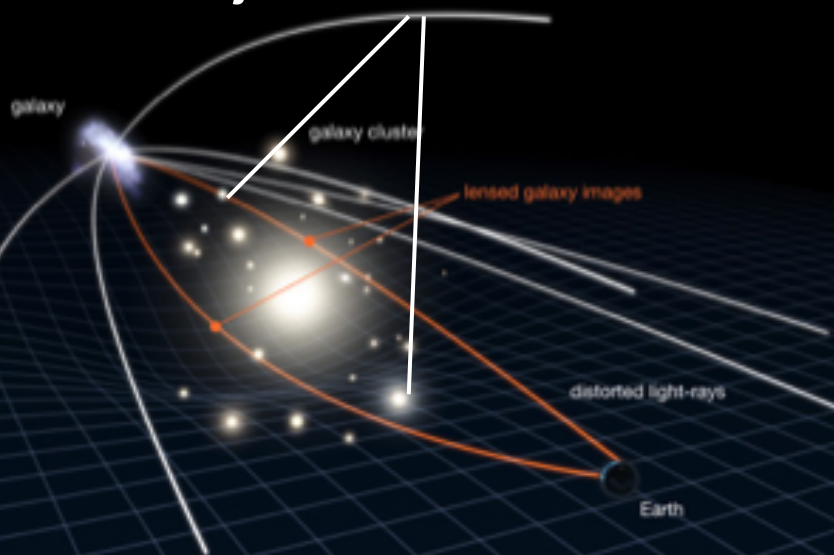
Model



Substructures vs interlopers

Subhalos & halos projected along the l.o.s both lens: who wins?

Projected l.o.s halos



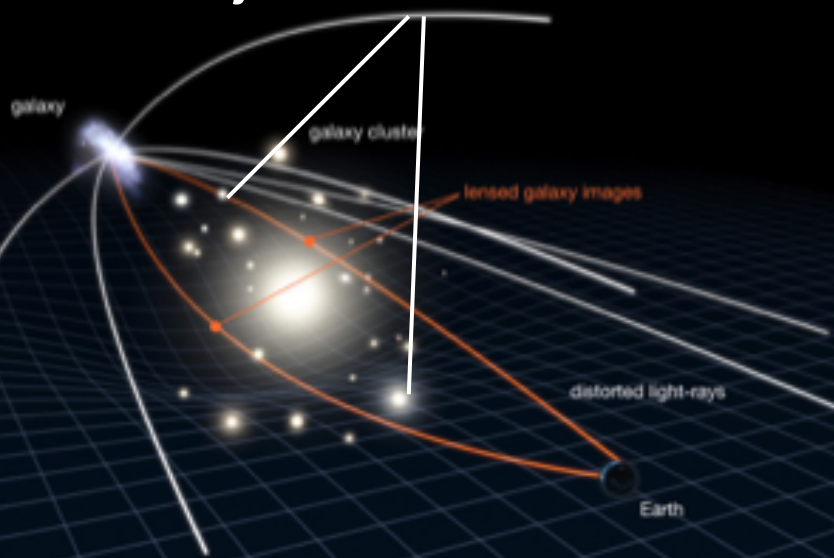
The number of line-of-sight haloes is larger than that of subhaloes



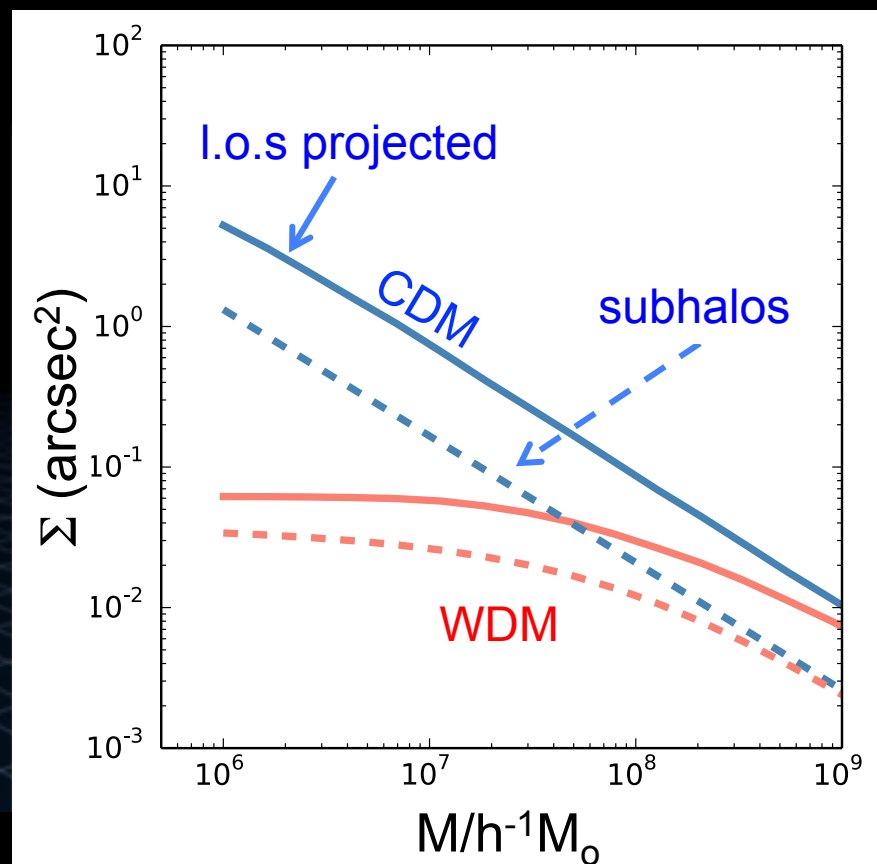
Substructures vs interlopers

Subhalos & halos projected along the l.o.s both lens: who wins?

Projected l.o.s halos



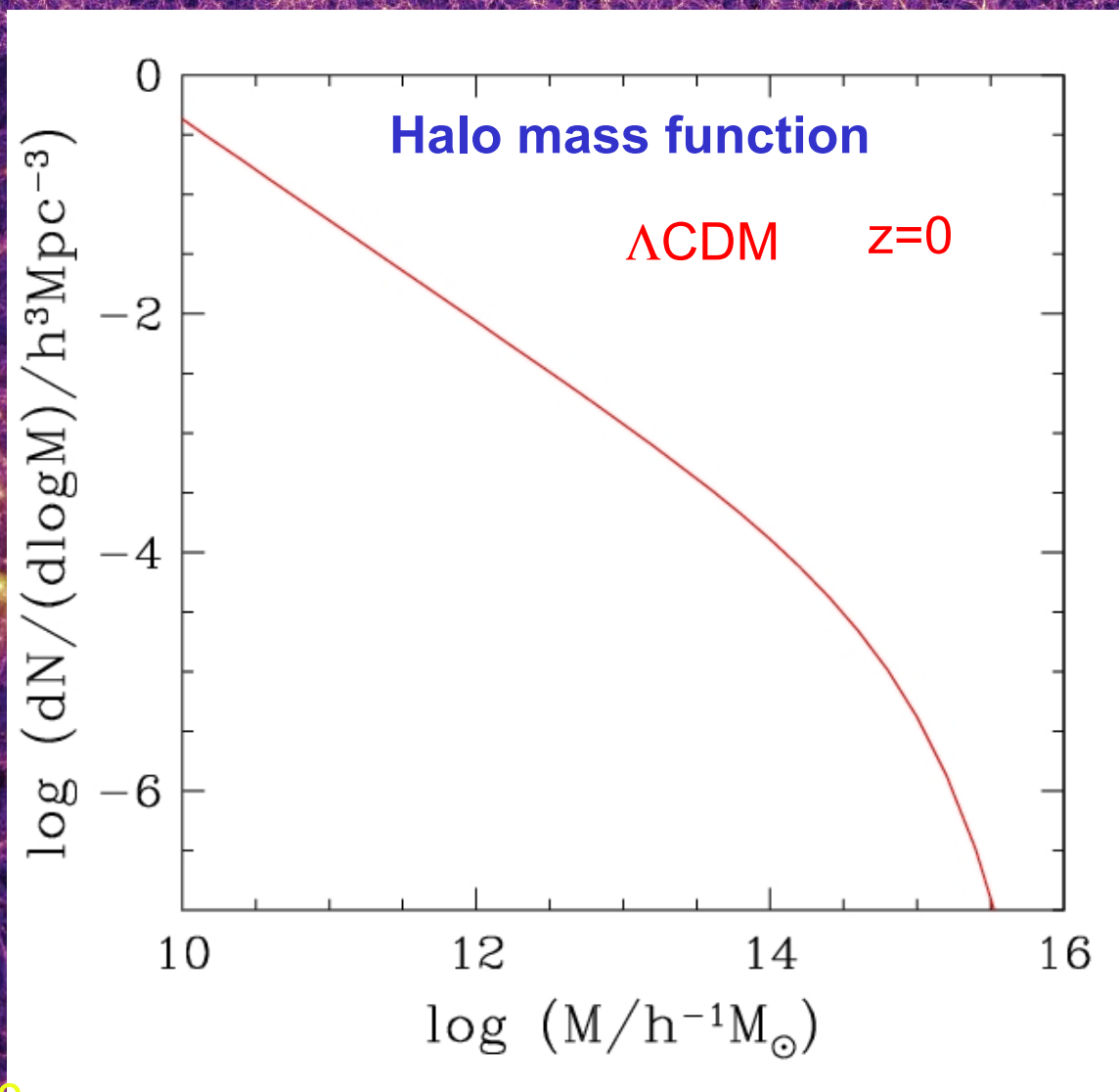
Li, CSF et al. '16



→ This is the **cleanest** possible **test**: it depends **ONLY** on the **small-mass** end of the “**field**” halo mass function which we know how to calculate and is **unaffected by baryons**

VIRGO

The Millennium/Aquarius/Phoenix simulation series



Springel et al '05, '08,
Gao et al '11

The subhalo mass function

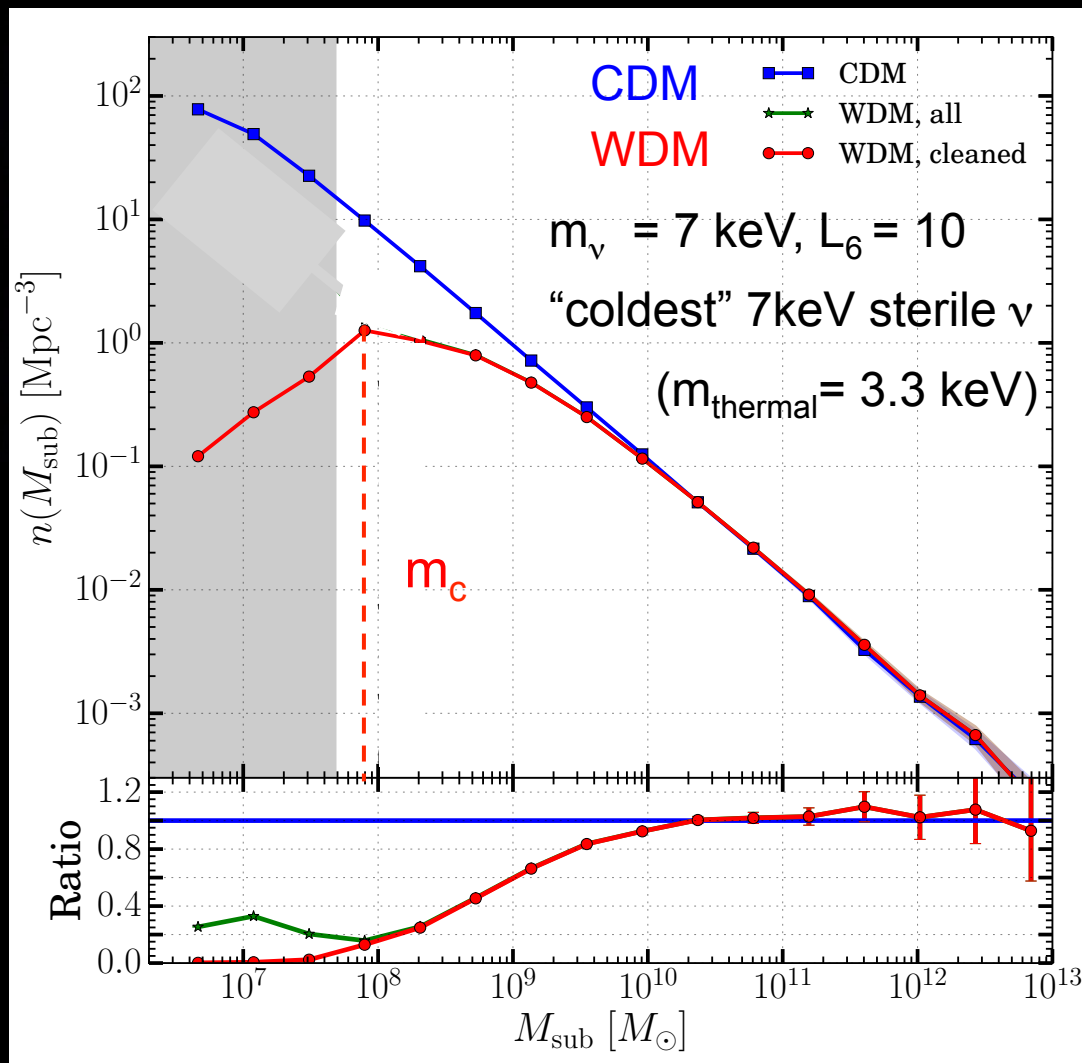


CDM

WDM

3 x fewer WDM subhalos at $3 \times 10^9 M_\odot$

10 x fewer at $10^8 M_\odot$



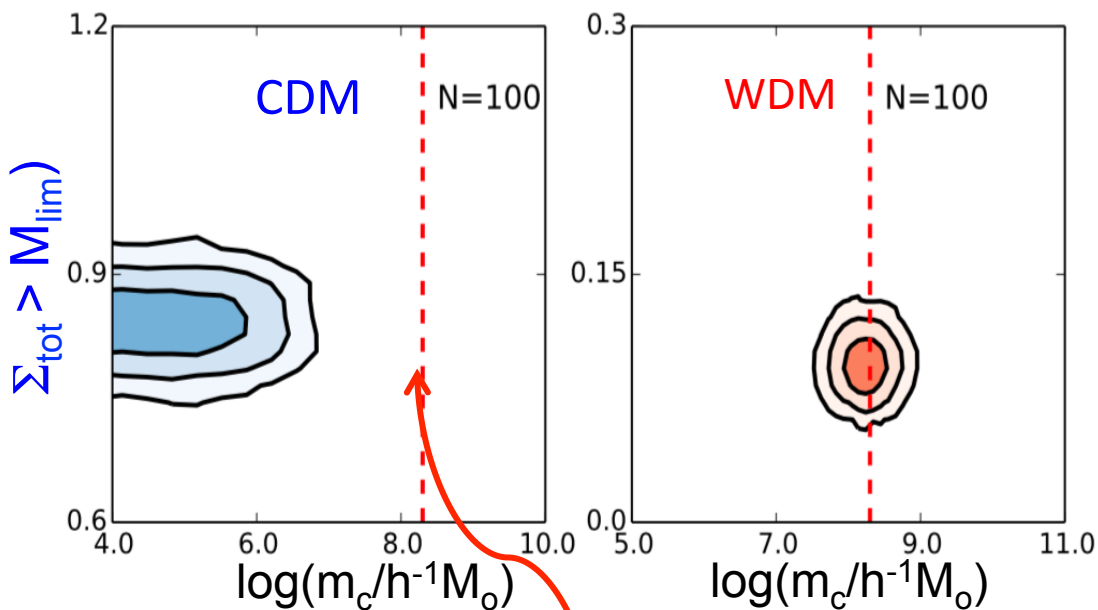
Detecting substructures with strong lensing

Σ_{tot} = projected halo number density within Einstein ring

m_c = halo cutoff mass

100 Einstein ring systems and detection limit: $m_{\text{low}} = 10^7 h^{-1} M_\odot$

Detection limit = $10^7 h^{-1} M_\odot$



m_c = halo cutoff mass

$m_c = 1.3 \times 10^8 h^{-1} M_\odot$ for coldest 7 keV sterile neutrino

- If DM is 7 keV sterile $\nu \rightarrow$ **exclude** CDM at $\gg \sigma$!
- If DM is CDM \rightarrow **exclude** 7 keV sterile ν at $\gg \sigma$



Conclusions

- Λ CDM: great **success** on scales $> 1\text{Mpc}$: CMB, LSS, gal evolution
 - But on these scales **Λ CDM** cannot be distinguished from **WDM**
 - The **identity** of the DM makes a big difference on **small scales**
1. The MW sat lum fn agrees with (**pre-existing**) CDM **predictions** \rightarrow **NO satellite problem** in CDM. Have detected sats formed **before** and **after** recombination.
 2. Halos $< \sim 5 \cdot 10^8 M_0$ are **dark**; halos $> 10^{10} M_0$ are **bright**
 3. No evidence for **cores**; **baryon effects** can make them
 4. Distortions of **strong** gravitational **lenses** offer a **clean test** of CDM vs WDM \rightarrow **and can potentially rule out CDM!**