



# Tests of $\Lambda$ CDM

*Carlos S. Frenk*  
*Institute for Computational Cosmology,*  
*Durham*

# Using (sub)halos

The new Ogden  
Centre at Durham





# Testing $\Lambda$ CDM with (sub)halos

## I. What do we know about subhalos in $\Lambda$ CDM

- Abundance
- Radial distribution
- Structure

## II. How can we use subhalos to test $\Lambda$ CDM

- In the optical
- In gamma rays
- With gravitational lensing

# Testing $\Lambda$ CDM with (sub)halos

Subhalos are best studied with cosmological simulations

- 
- I. N-body simulations
  - II. Hydrodynamical simulations

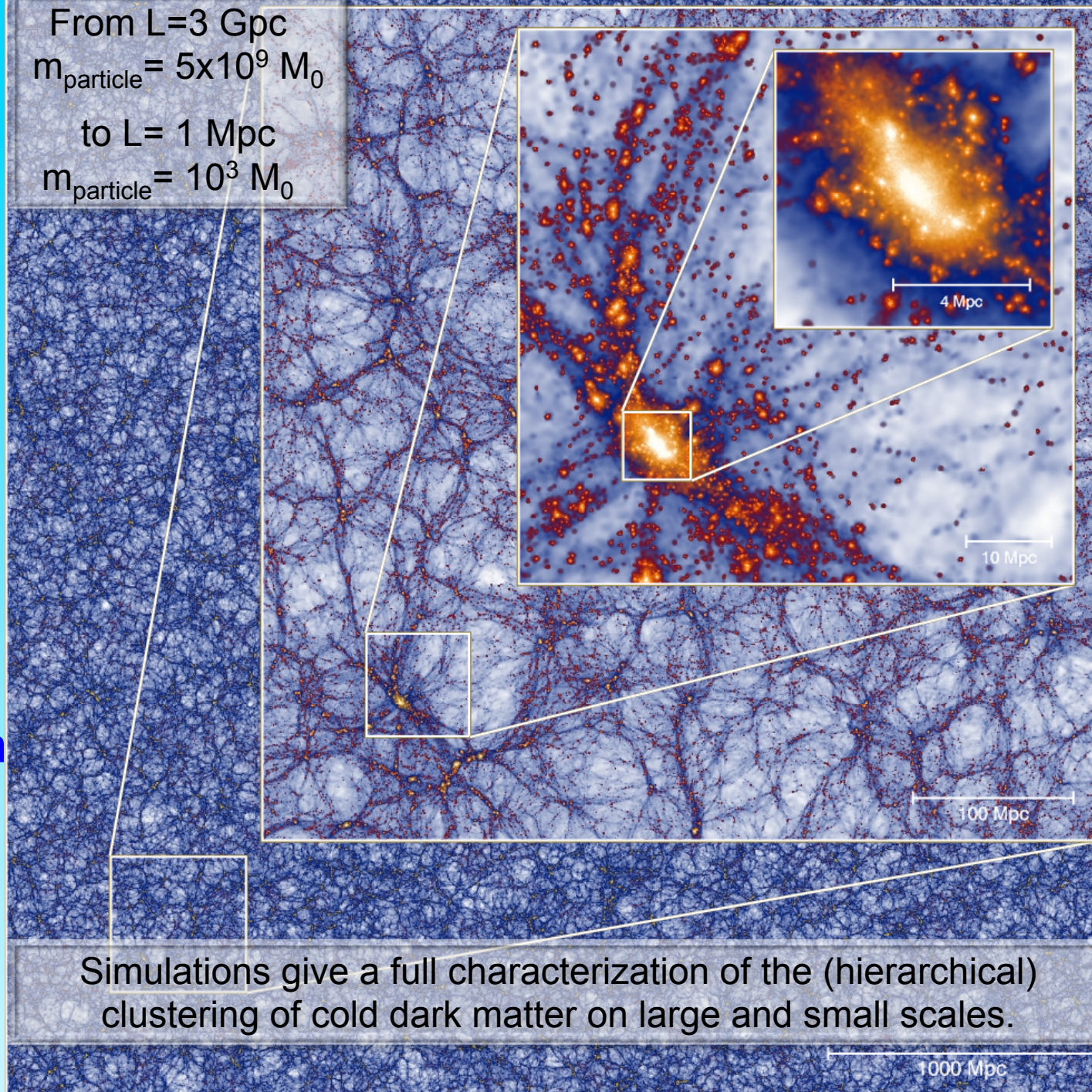


VIRG

N-body  
simulations

The formation,  
evolution,  
abundance,  
clustering &  
structure of dark  
matter halos from  
CDM initial  
conditions is  
(almost) a solved  
problem

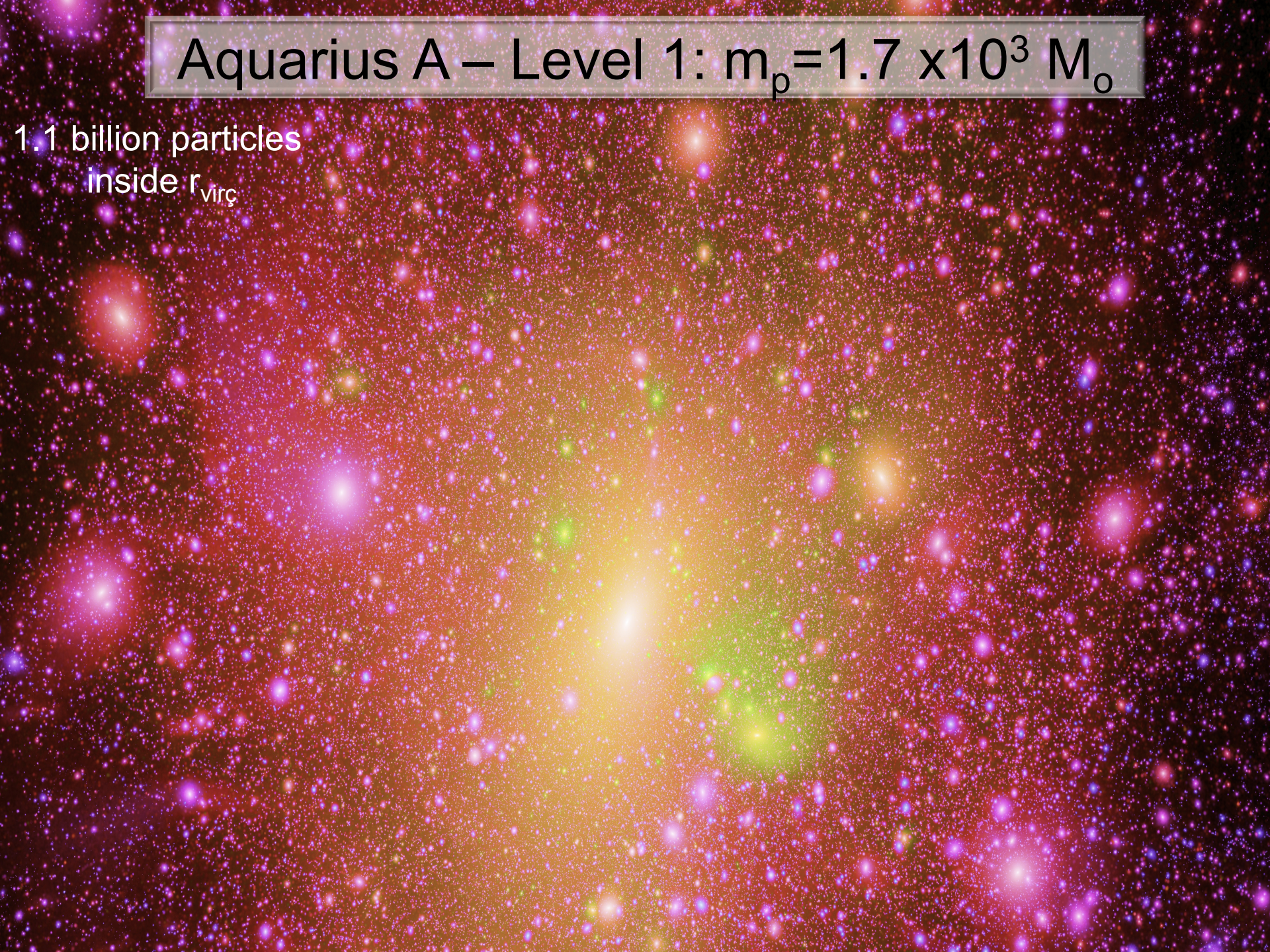
From  $L=3$  Gpc  
 $m_{\text{particle}} = 5 \times 10^9 M_0$   
to  $L=1$  Mpc  
 $m_{\text{particle}} = 10^3 M_0$





# Aquarius A – Level 1: $m_p = 1.7 \times 10^3 M_\odot$

1.1 billion particles  
inside  $r_{\text{vir}}$





# Aquarius A – Level 1: $m_p = 1.7 \times 10^3 M_\odot$

1.1 billion particles  
inside  $r_{\text{vir}}$

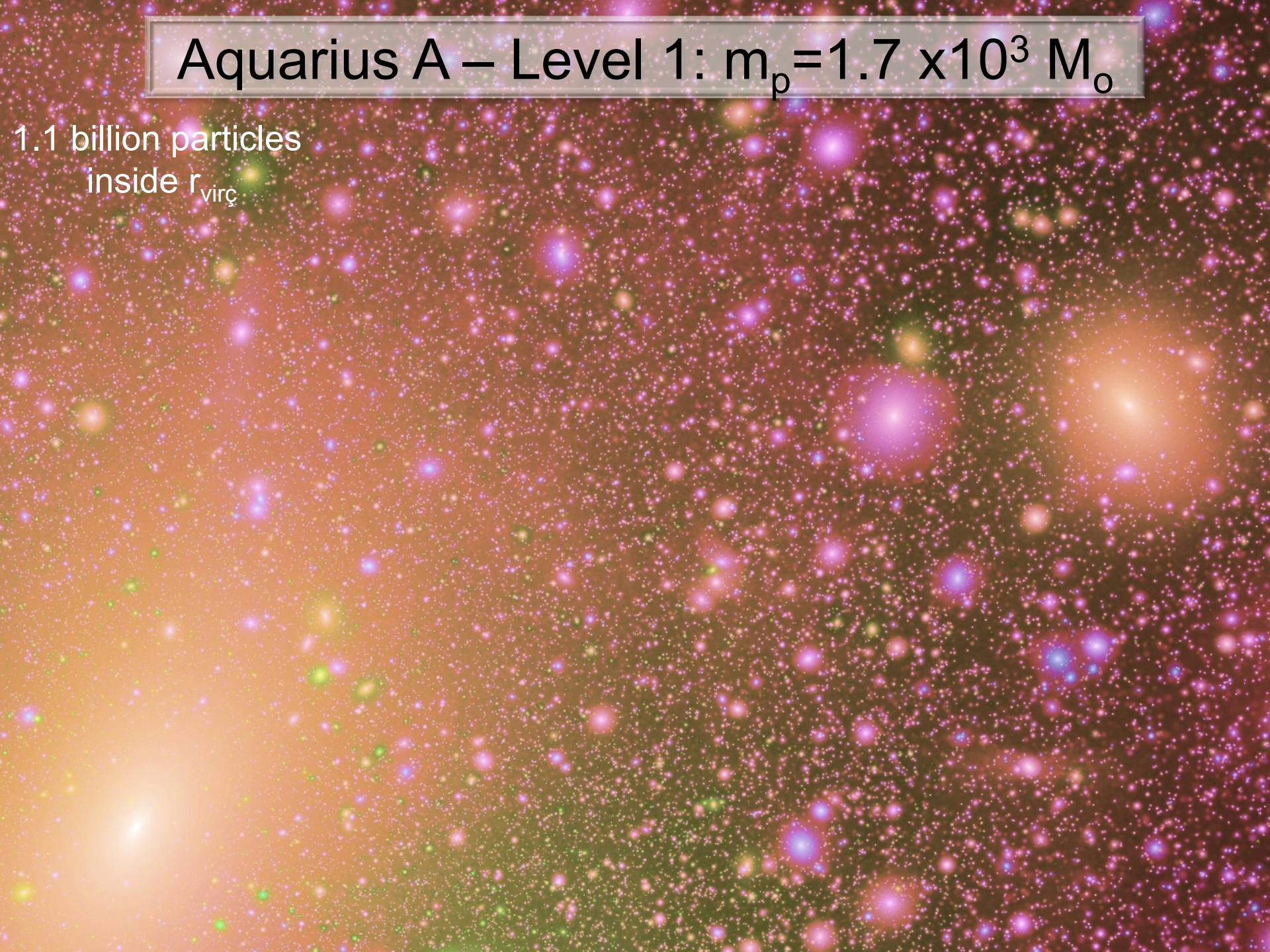


2400<sup>3</sup> run



# Aquarius A – Level 1: $m_p = 1.7 \times 10^3 M_\odot$

1.1 billion particles  
inside  $r_{\text{vir}}$

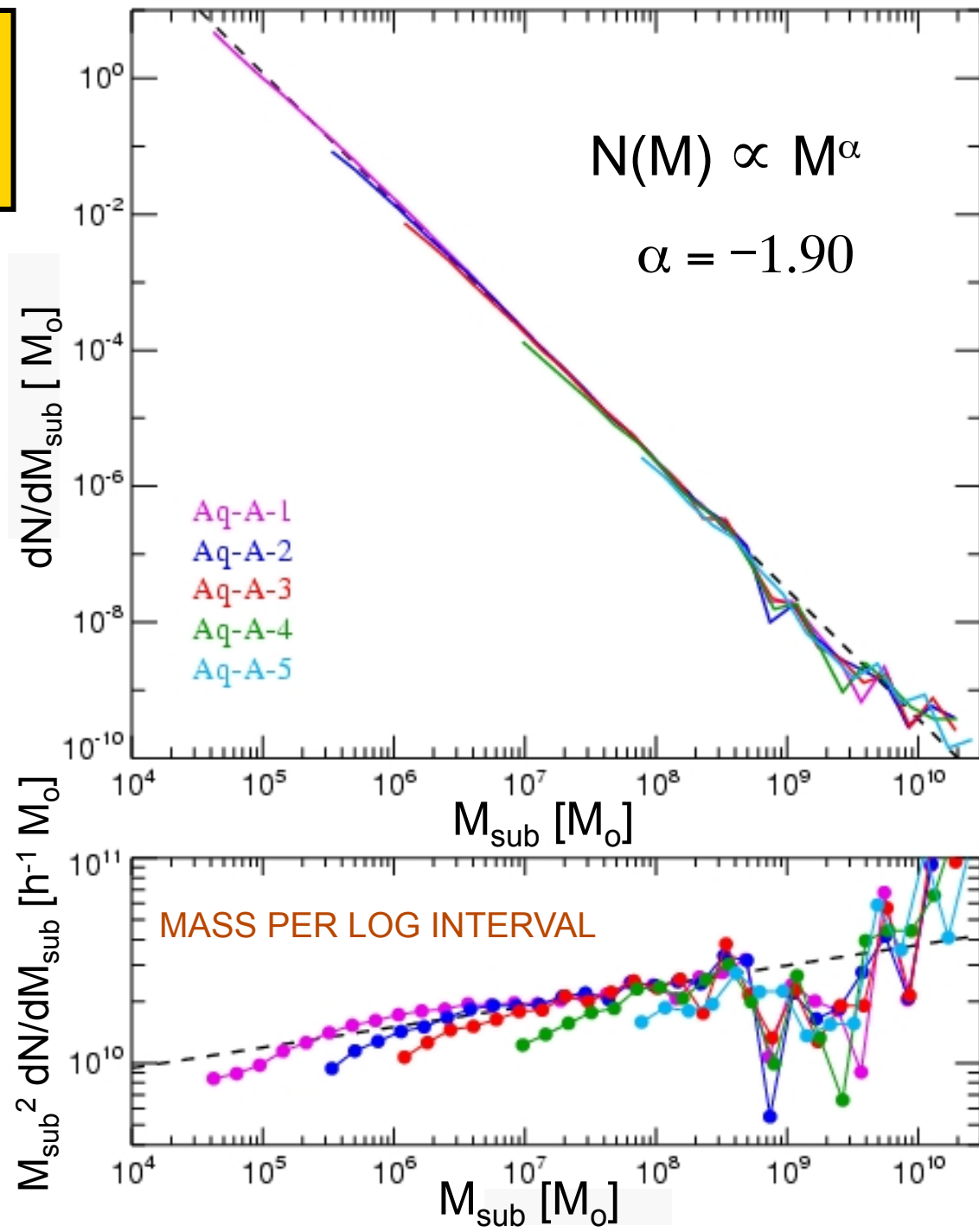




# The mass function of substructures

- The subhalo mass function is **shallower** than  $M^2$
- Subcritical slope  $\rightarrow$  **total mass** in substructures **converges** at faint end
- **Most** of the substructure **mass** is in the few **most massive** halos

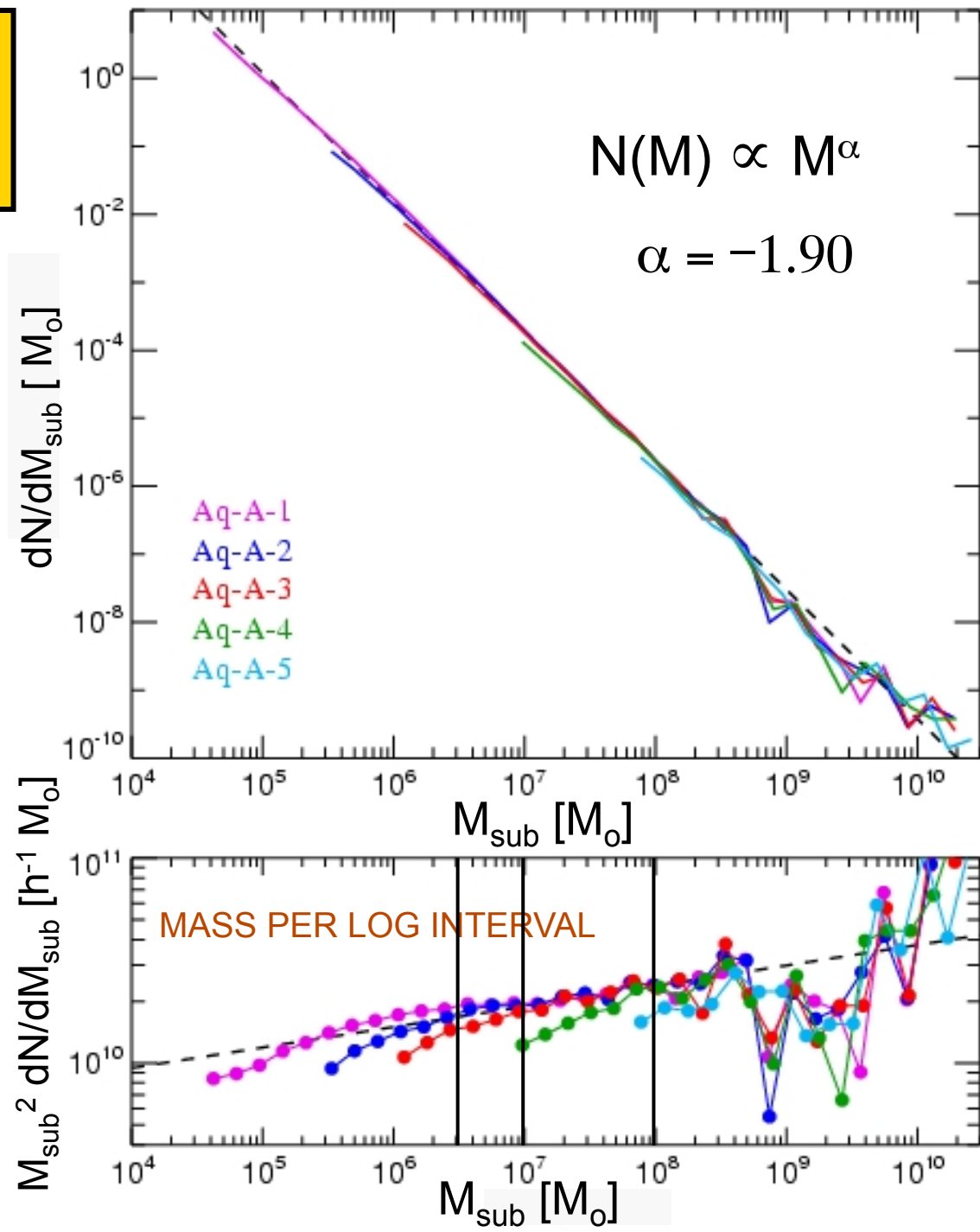
Virgo consortium '08



# The mass function of substructures

The subhalo mass function is **converged** (to better than a **few percent**) for halos of **>200** particles, even for **moderate resolution**, over a factor of 2000 in mass

Virgo consortium '08





# The substructure $V_{\max}$ function

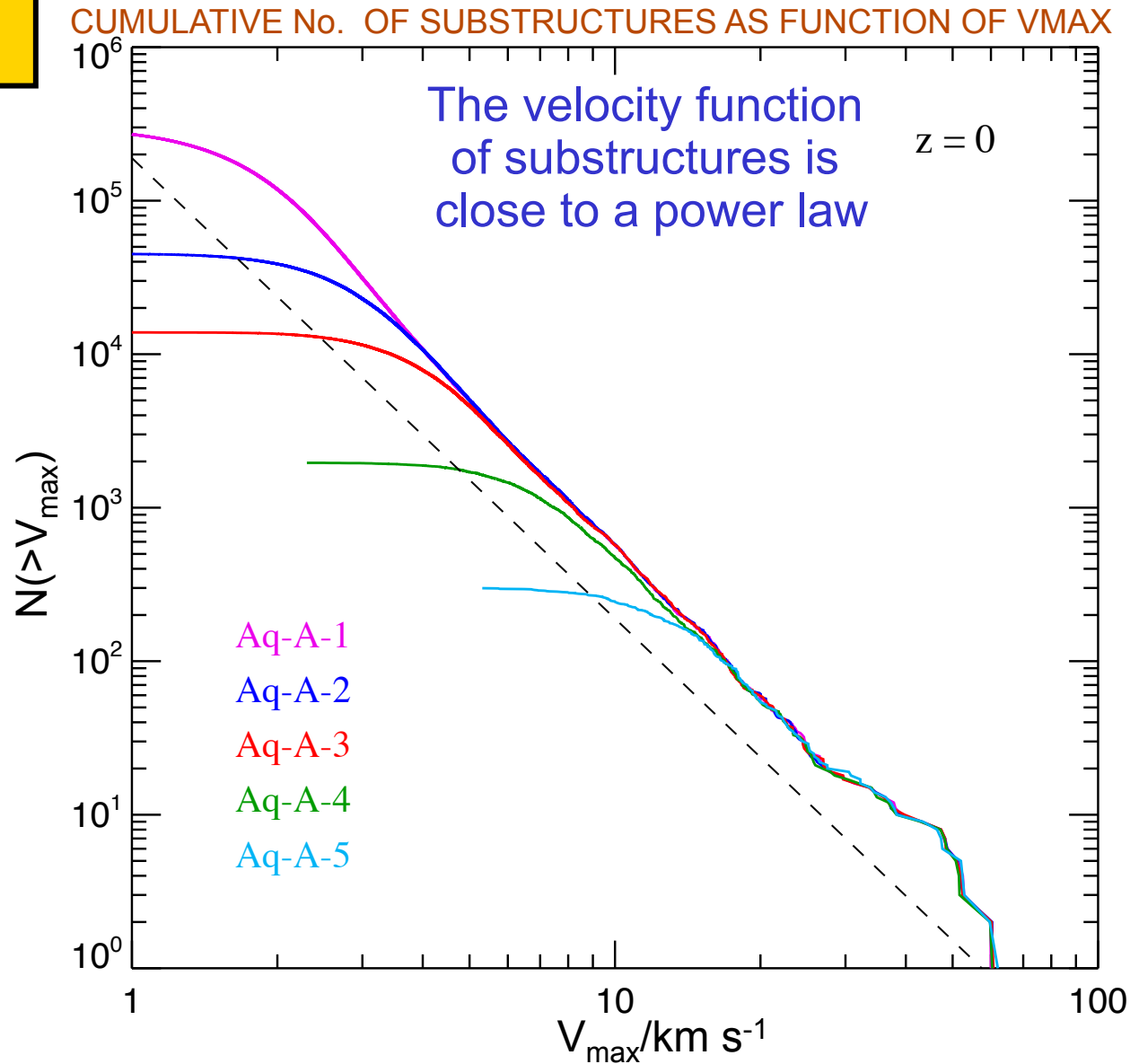
$V_{\max}$  mass function is also well converged for halos of  $>200$  particles

Level 1 → converged results for

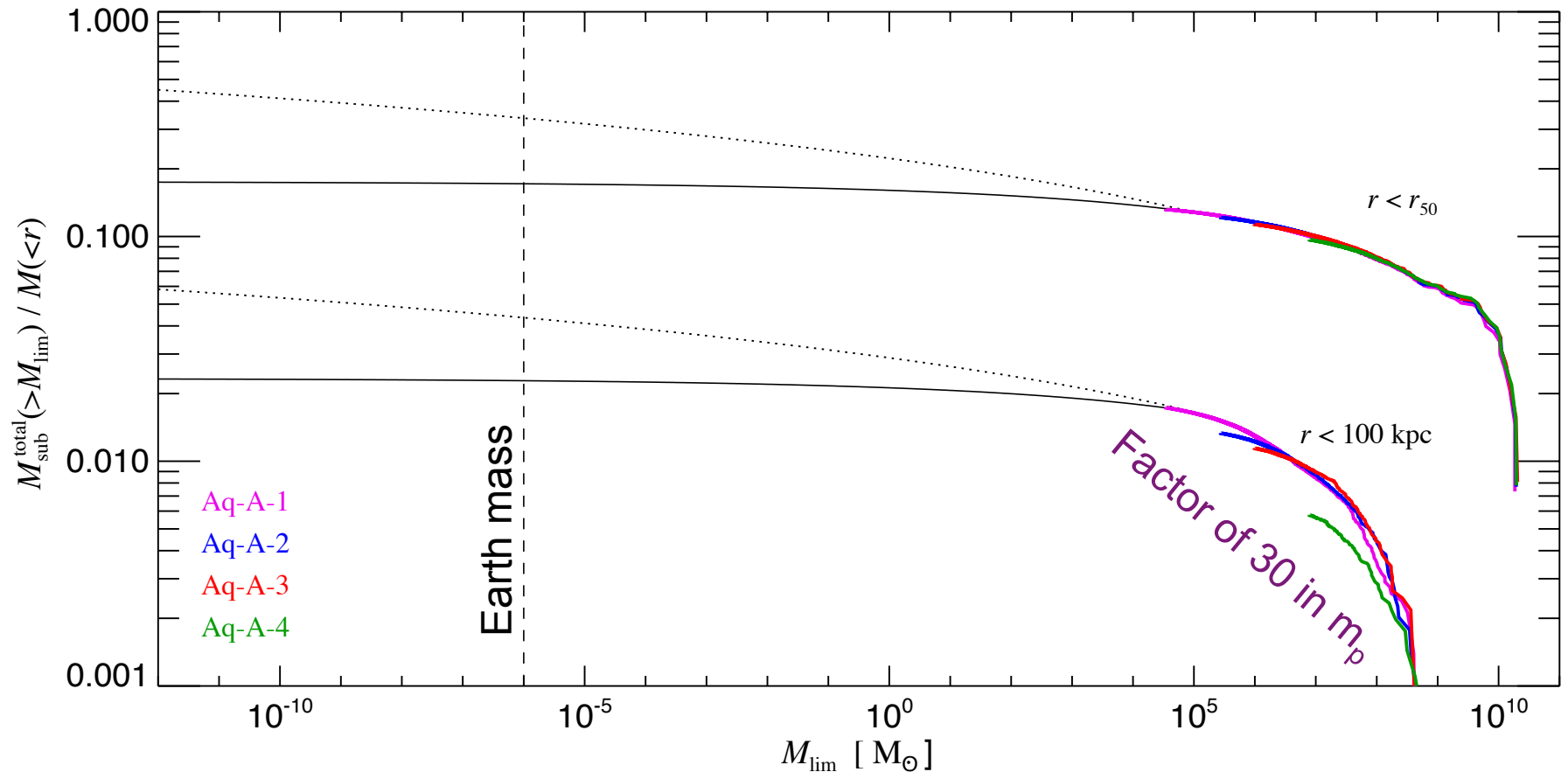
$$V_{\max} > 1.5 \text{ km/s}$$

$$r_{\max} > 165 \text{ pc}$$

Springel et al. '08



# The mass fraction in substructures



The mass fraction in substructure is well converged over a factor of 30 in mass resolution



# Subhalo density profiles

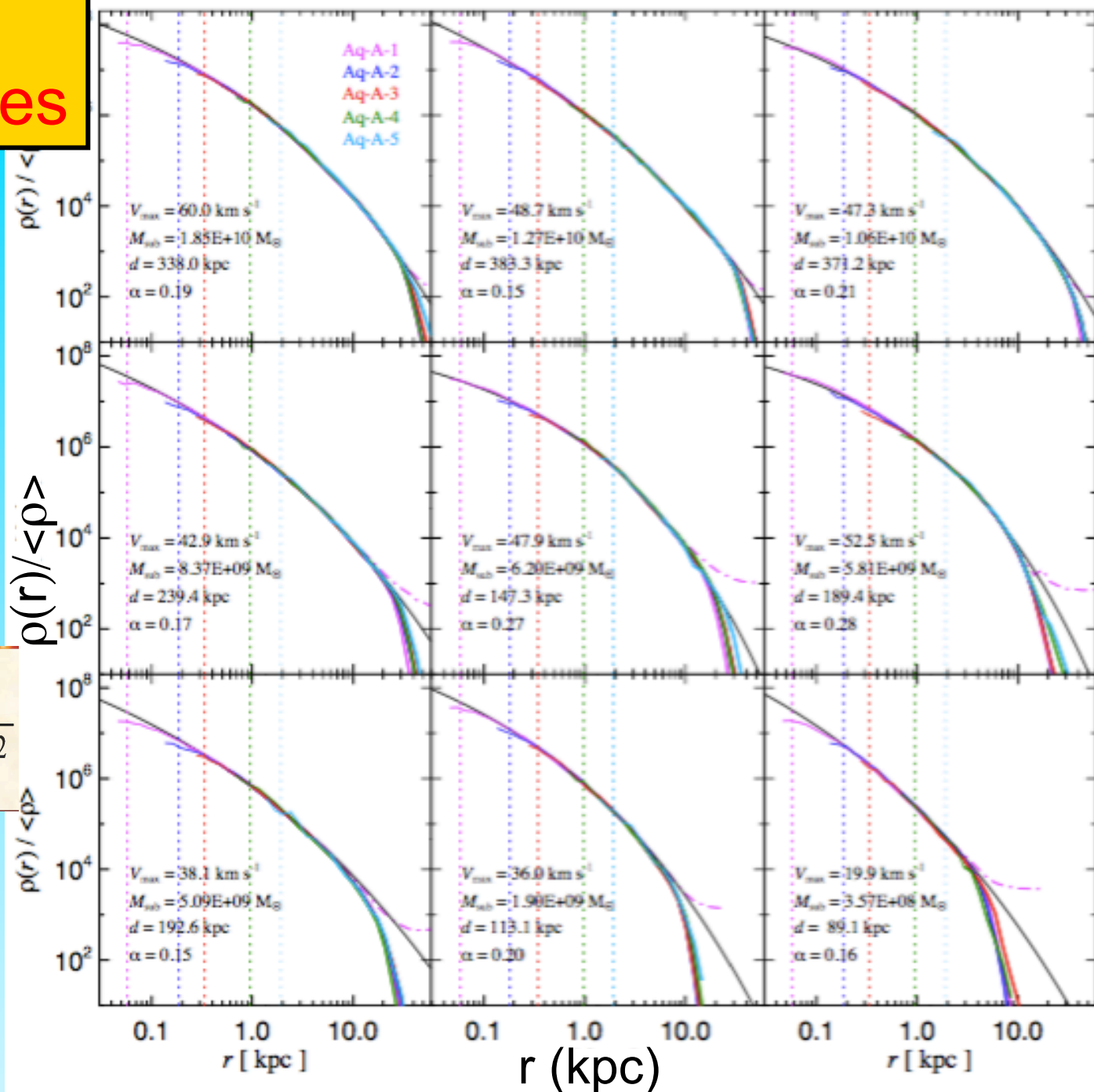
Converged  
beyond Power  
et al radius

Well fit by **NFW**

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

or **Einasto**  
profiles

Springel et al. '08





VIRGO

[icc.dur.ac.uk/Eagle](http://icc.dur.ac.uk/Eagle)

“Evolution and assembly of galaxies and  
their environment”

# THE EAGLE PROJECT

## Virgo Consortium

**Durham:** Richard Bower, Michelle Furlong, Carlos Frenk, Matthieu Schaller, James Trayford, Yelti Rosas-Guevara, Tom Theuns, Yan Qu, John Helly, Adrian Jenkins.

**Leiden:** Rob Crain, Joop Schaye.

**Other:** Claudio Dalla Vecchia, Ian McCarthy, Craig Booth...



# Effects of baryons in subhalos

Baryon effects:

- I. Light up some subhalos by star formation
- II. Change their inner structure slightly
- III. Central galaxy can destroy small subhalos



# The Eagle Simulations

EVOLUTION AND ASSEMBLY OF GALAXIES AND THEIR ENVIRONMENTS

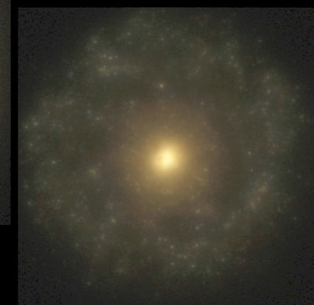
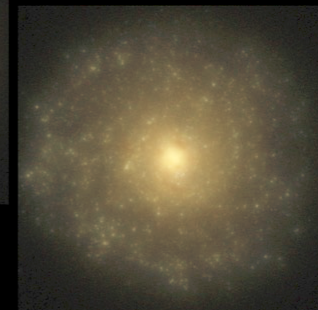
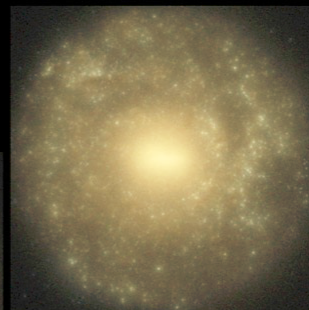
The Hubble Sequence realised in cosmological simulations

E0

E7

S0

SB



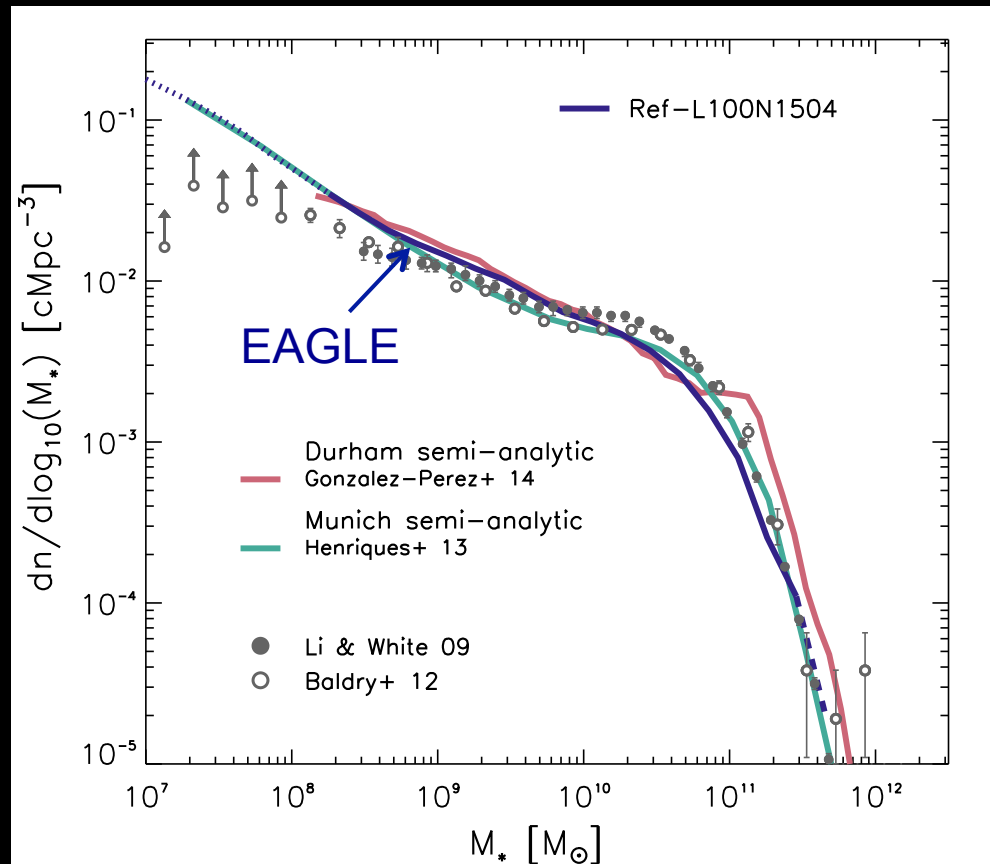
Irr

S

Trayford et al '15

# Galaxy stellar mass function

## Comparison to semi-analytic models





Most subhalos never make a galaxy!

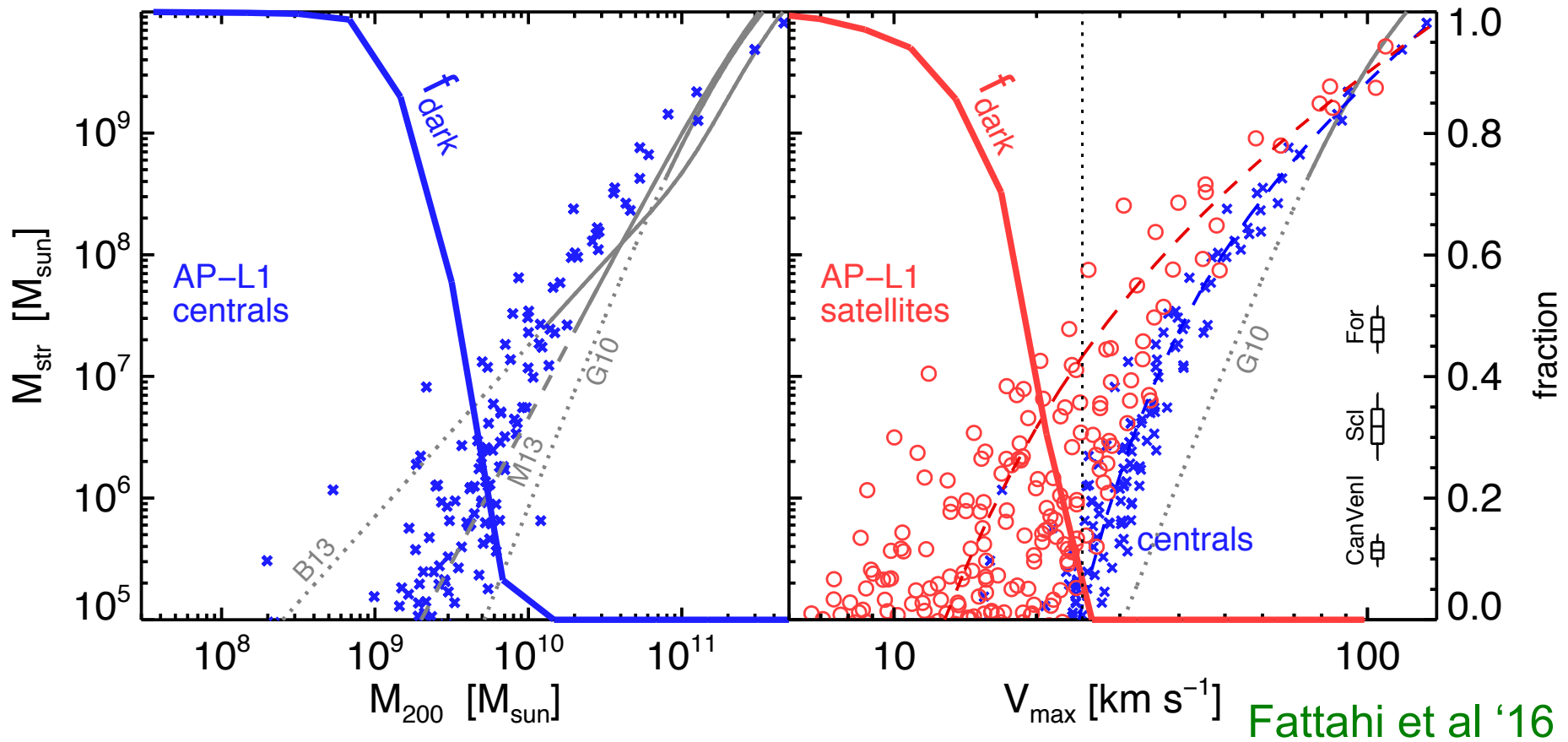
Because:

- Reionization heats gas to  $10^4\text{K}$ , preventing it from cooling and forming stars in small halos ( $T_{\text{vir}} < 10^4\text{K}$ )
- Supernovae feedback expels residual gas in slightly larger halos



# Fraction of dark subhalos

$$V_c = \sqrt{\frac{GM}{r}} \quad V_{\max} = \max V_c$$



Fattahi et al '16

All halos of mass  $< 5 \times 10^8 M_{\odot}$  or  $V_{\max} < 7 \text{ km/s}$  are dark ( $m_* < 10^4 M_{\odot}$ )

VIRG

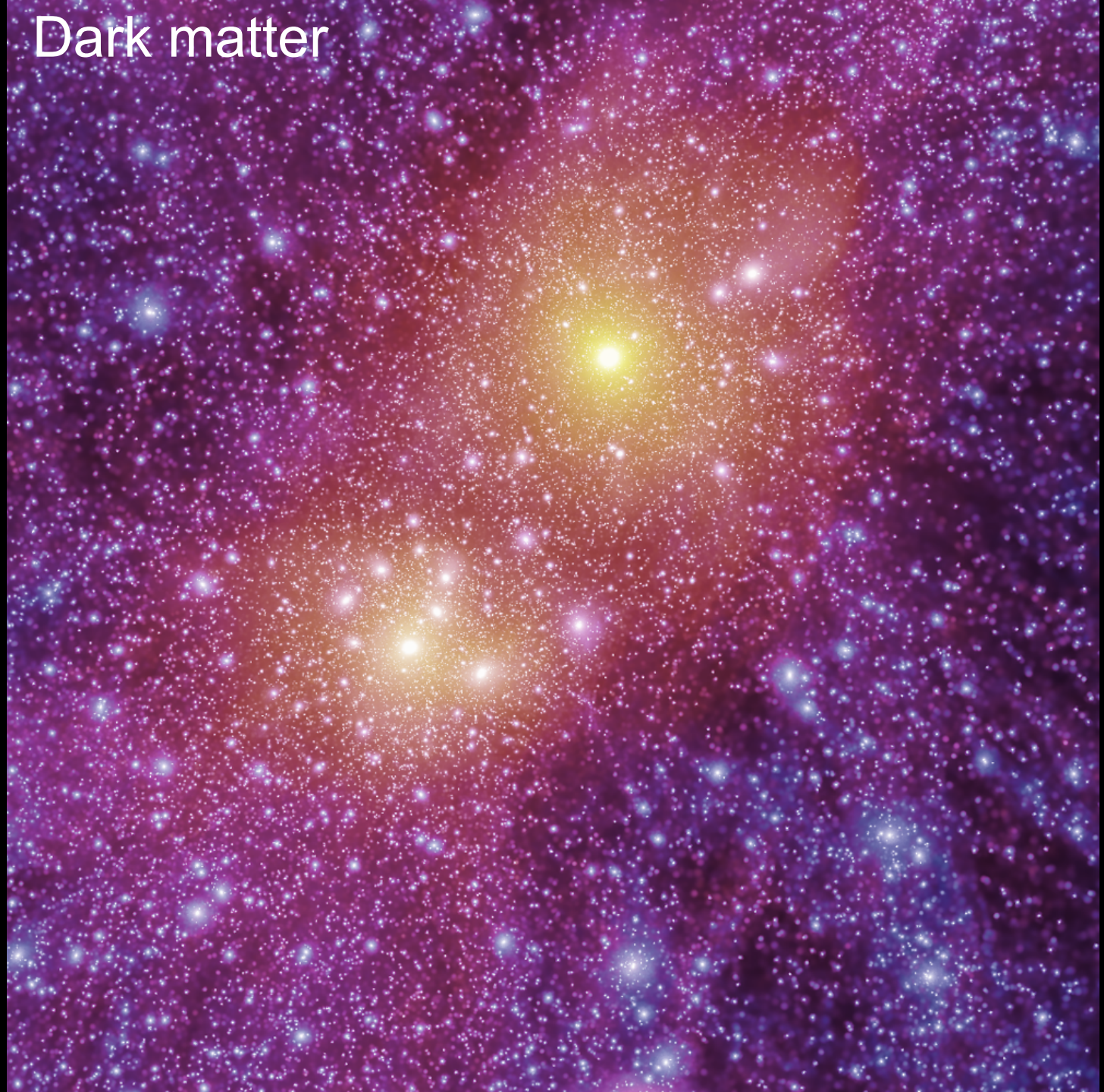
Dark matter

Local Group

APOSTLE  
EAGLE full  
hydro  
simulations

CDM

Sawala et al '16





Stars

VIRG

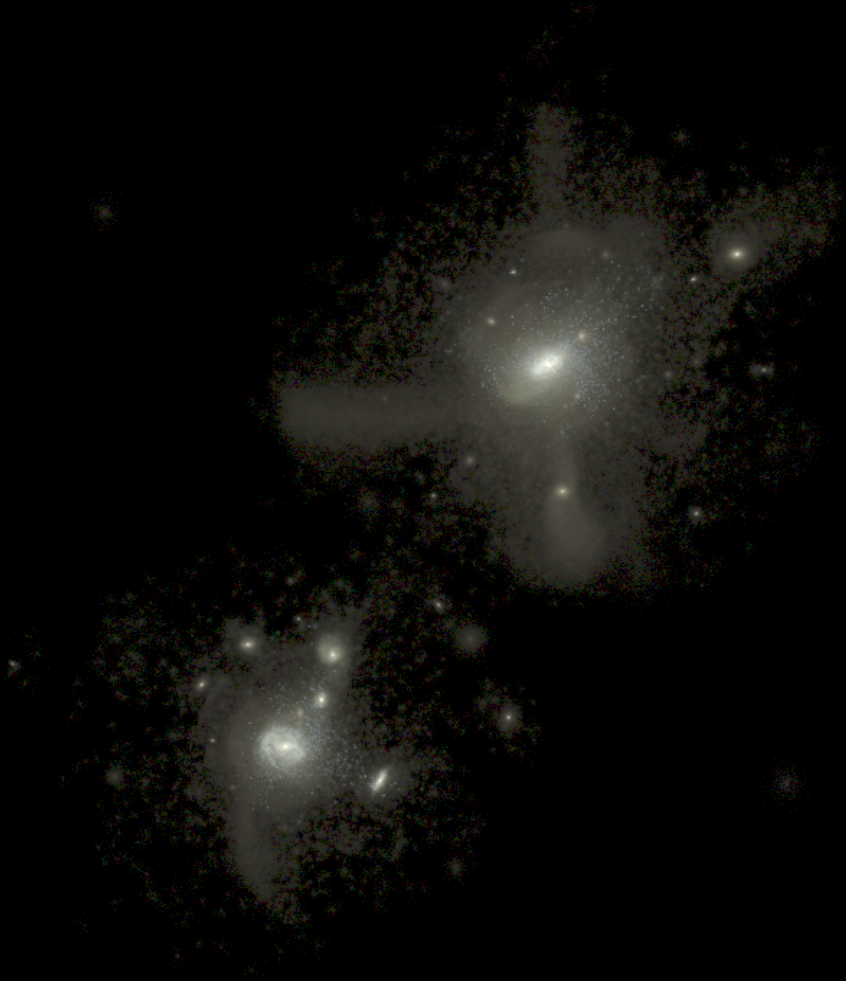
Local Group

APOSTLE  
EAGLE full  
hydro  
simulations

Stars

Far fewer satellite galaxies than CDM halos

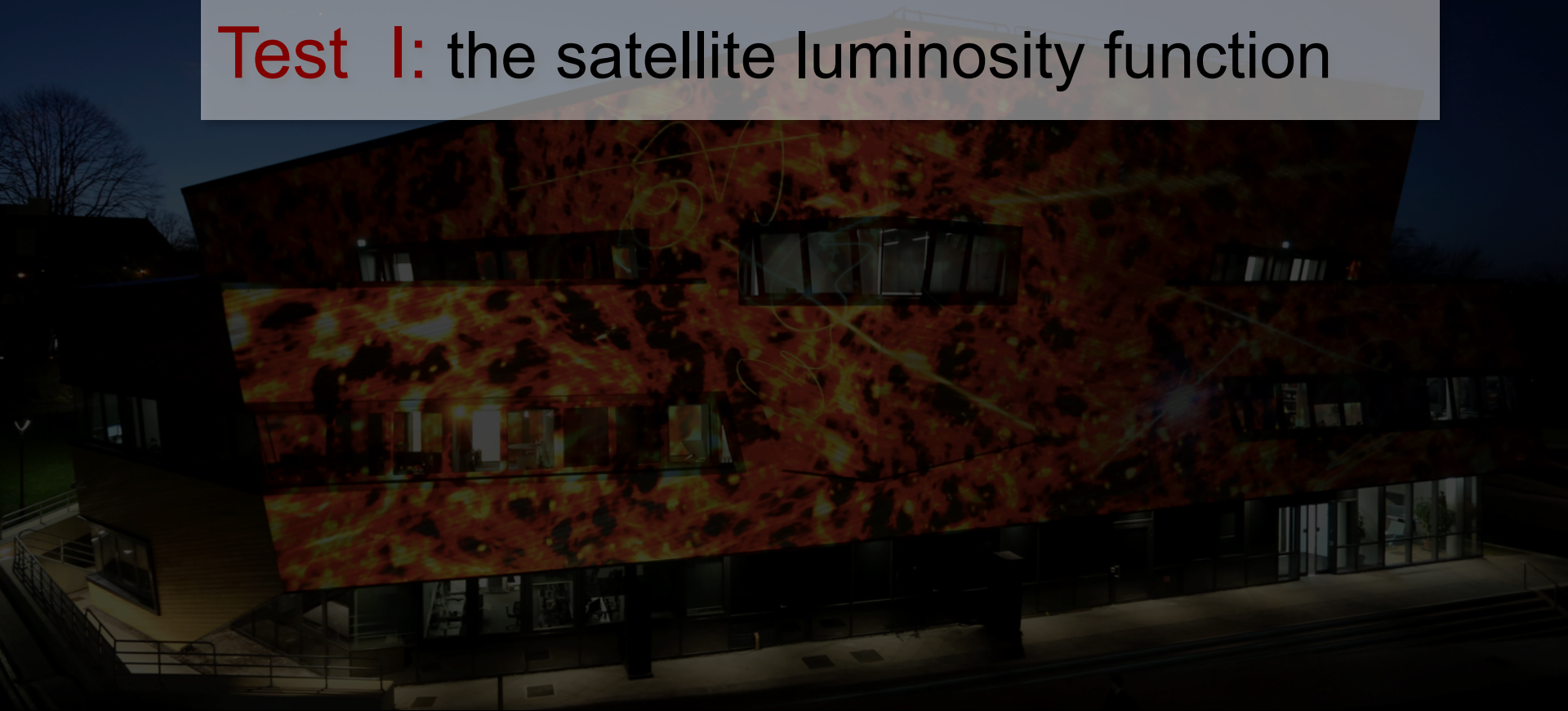
Sawala et al '16





# Tests of $\Lambda$ CDM with subhalos

**Test I:** the satellite luminosity function



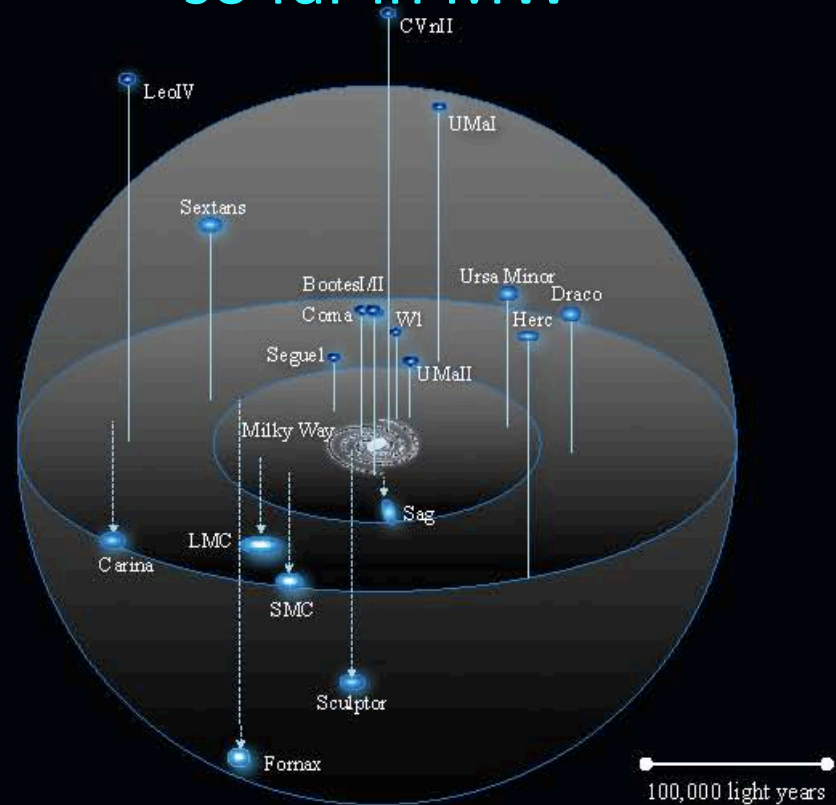


# The satellites of the Milky Way

cold dark matter



~50 satellites discovered  
so far in MW

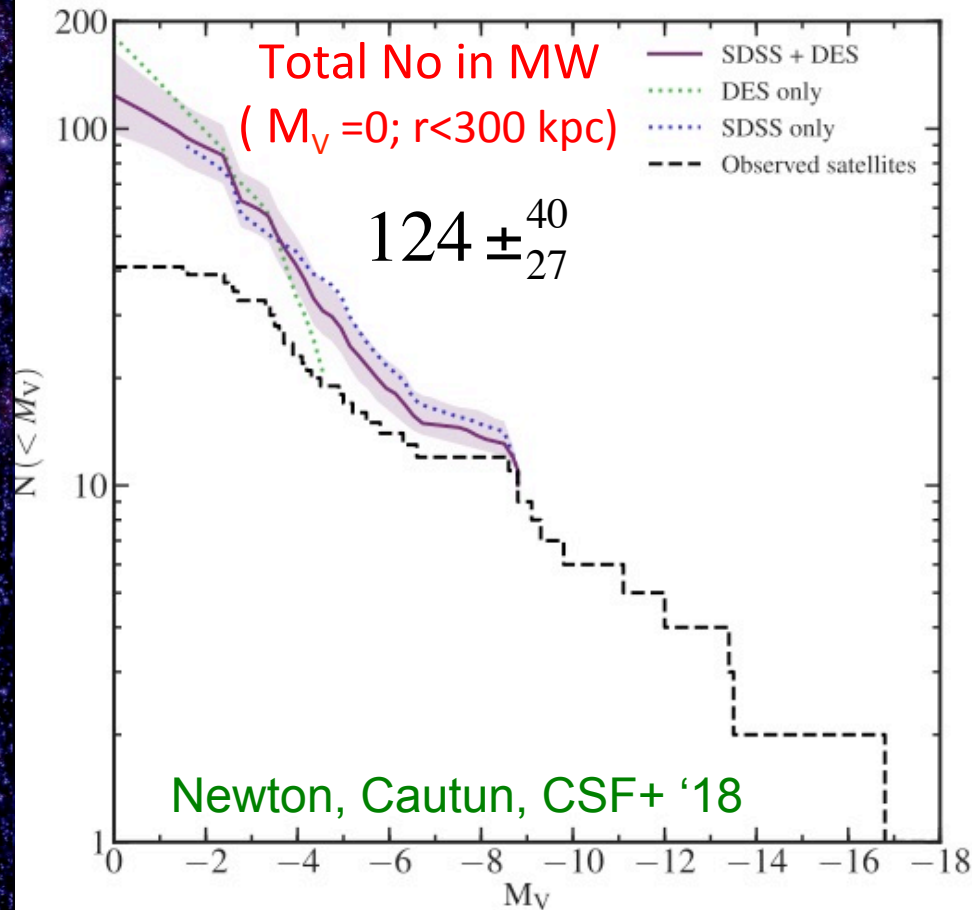




# The satellites of the Milky Way

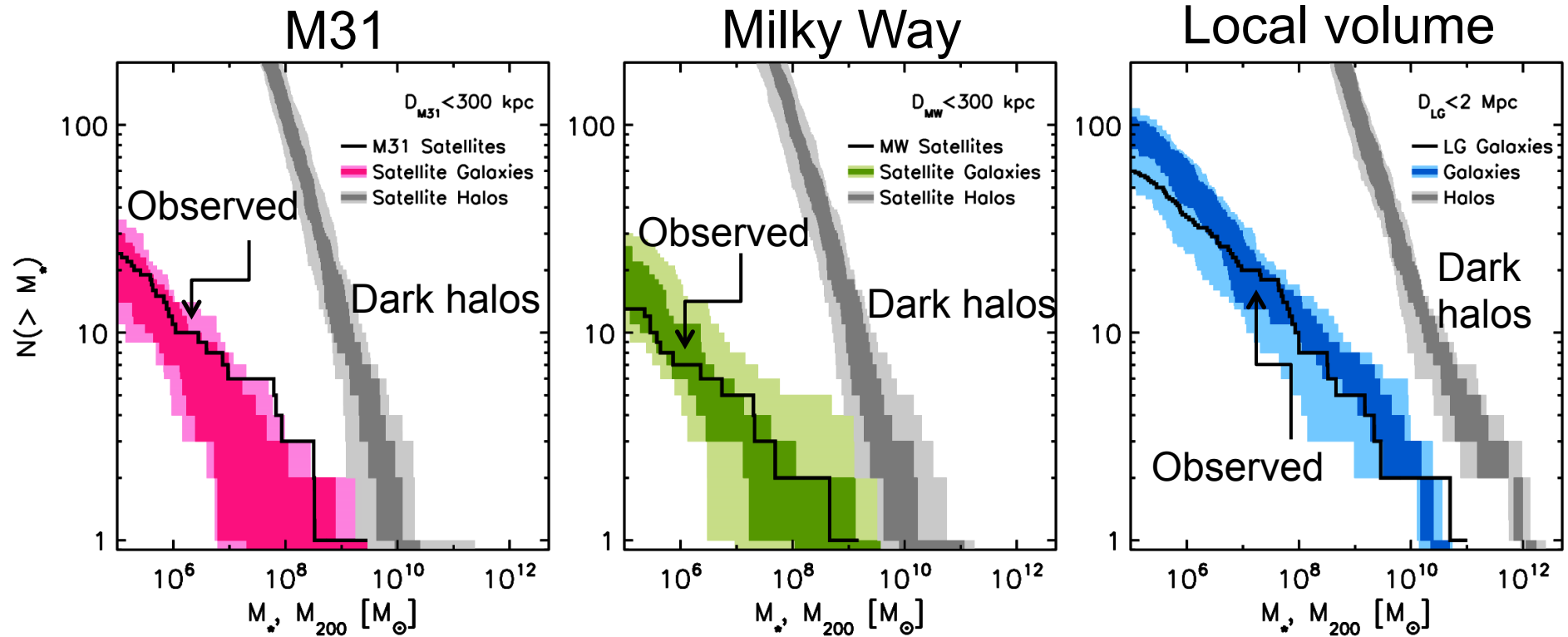
cold dark matter

Total No in MW (to  $M_V = 0$ )  
is:



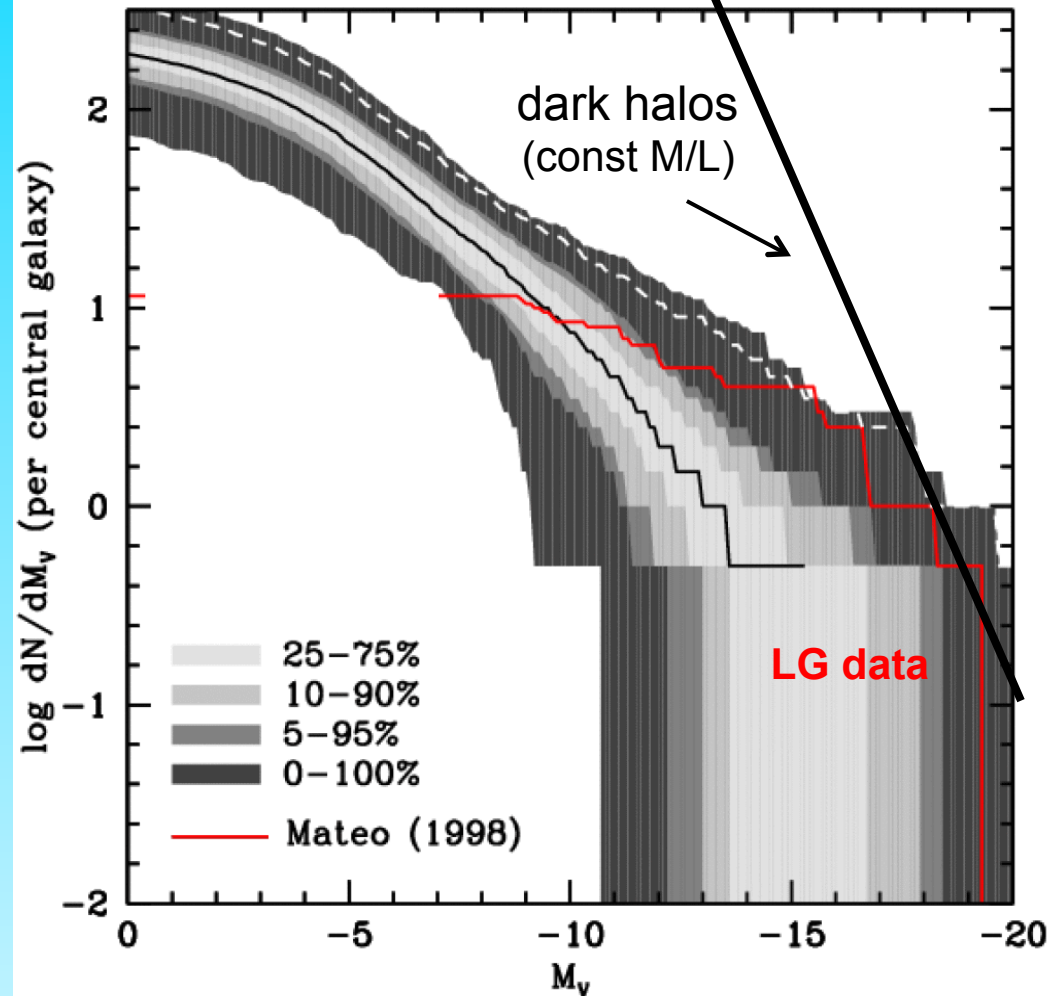


# EAGLE Local Group simulation



# Luminosity Function of Local Group Satellites

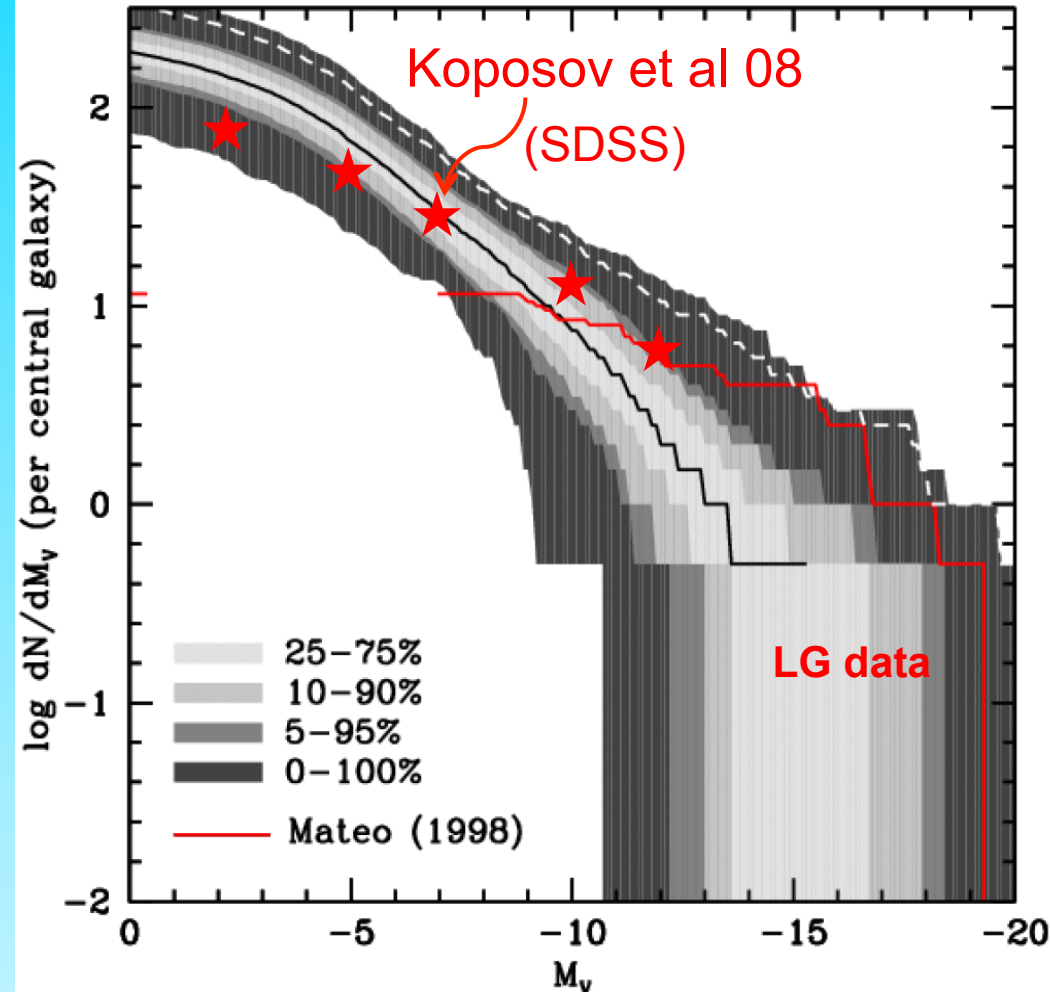
- Median model → correct abund. of sats brighter than  $M_V = -9$  and  $V_{\text{cir}} > 12$  km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare (~10% of cases)



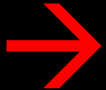


# Luminosity Function of Local Group Satellites

- Median model → correct abund. of sats brighter than  $M_V = -9$  and  $V_{\text{cir}} > 12$  km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare (~10% of cases)



Observed abundance of satellites  
is compatible with CDM

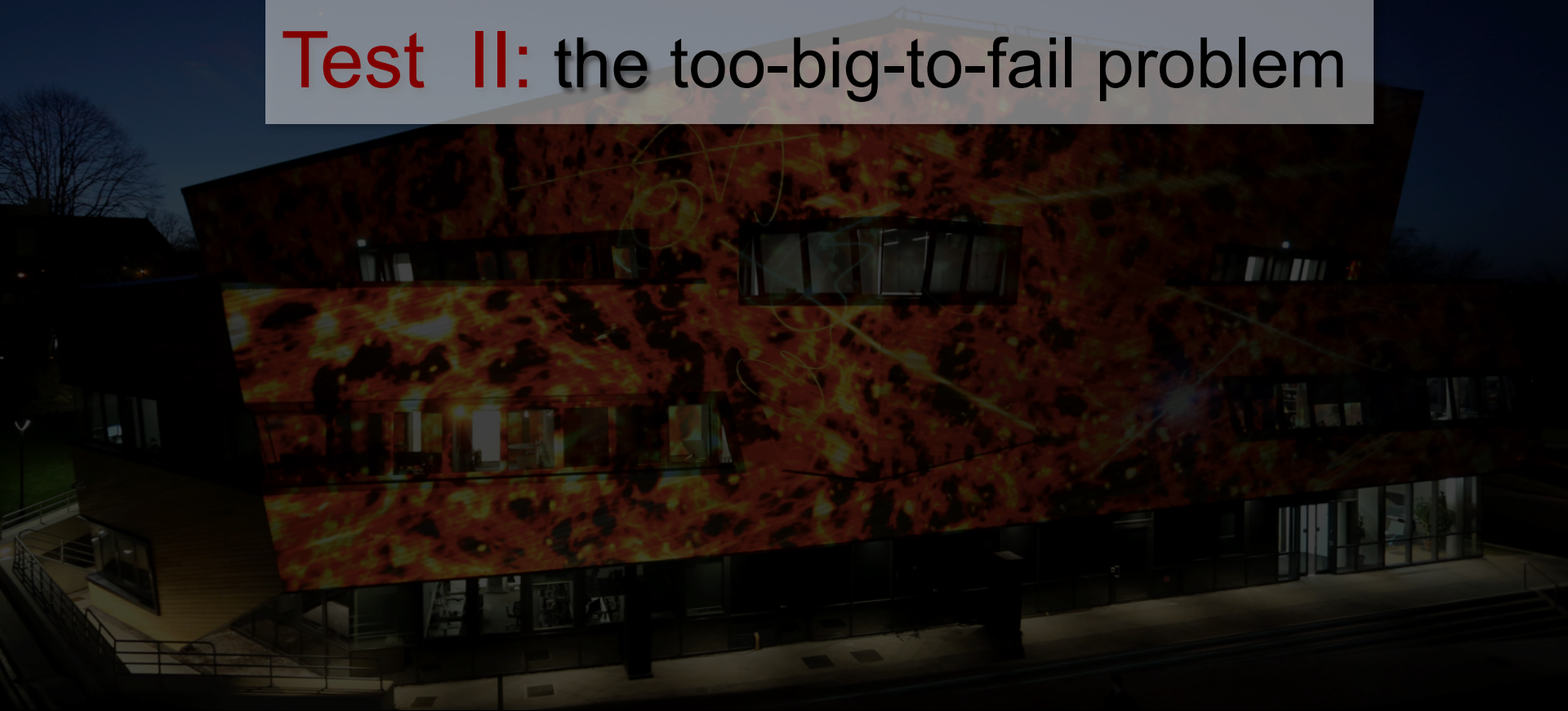


There is **no** such thing as the  
“satellite problem” in CDM!



# Tests of $\Lambda$ CDM with subhalos

**Test II:** the too-big-to-fail problem

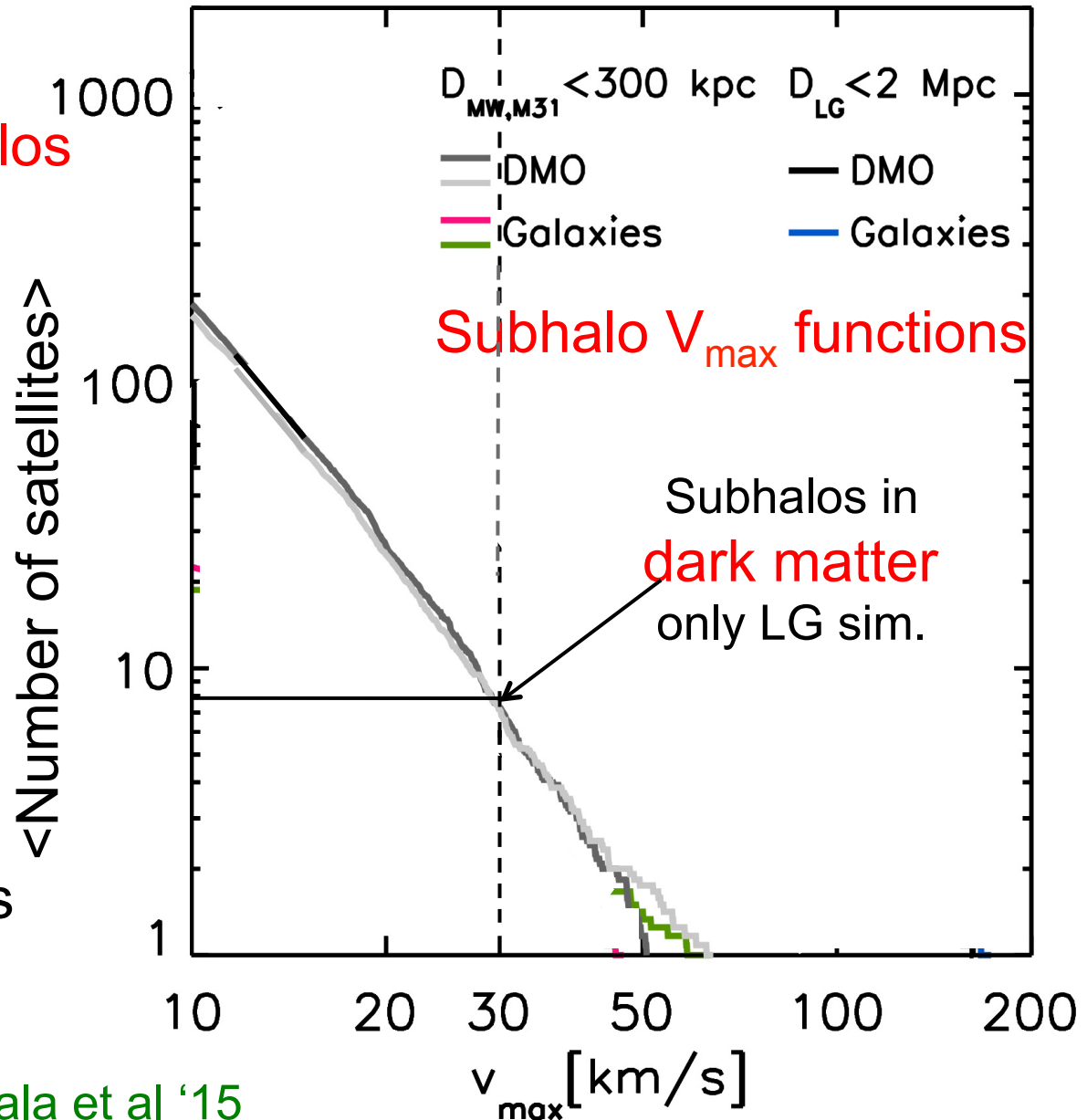


# Too-big-to-fail: the baryon bailout

DM only sims  $\rightarrow$   **$\sim 10$  halos**  
with  $V_{\max} > 30$  km/s



But **MW** has only **3**:  
LMC, SMC, Sagittarius



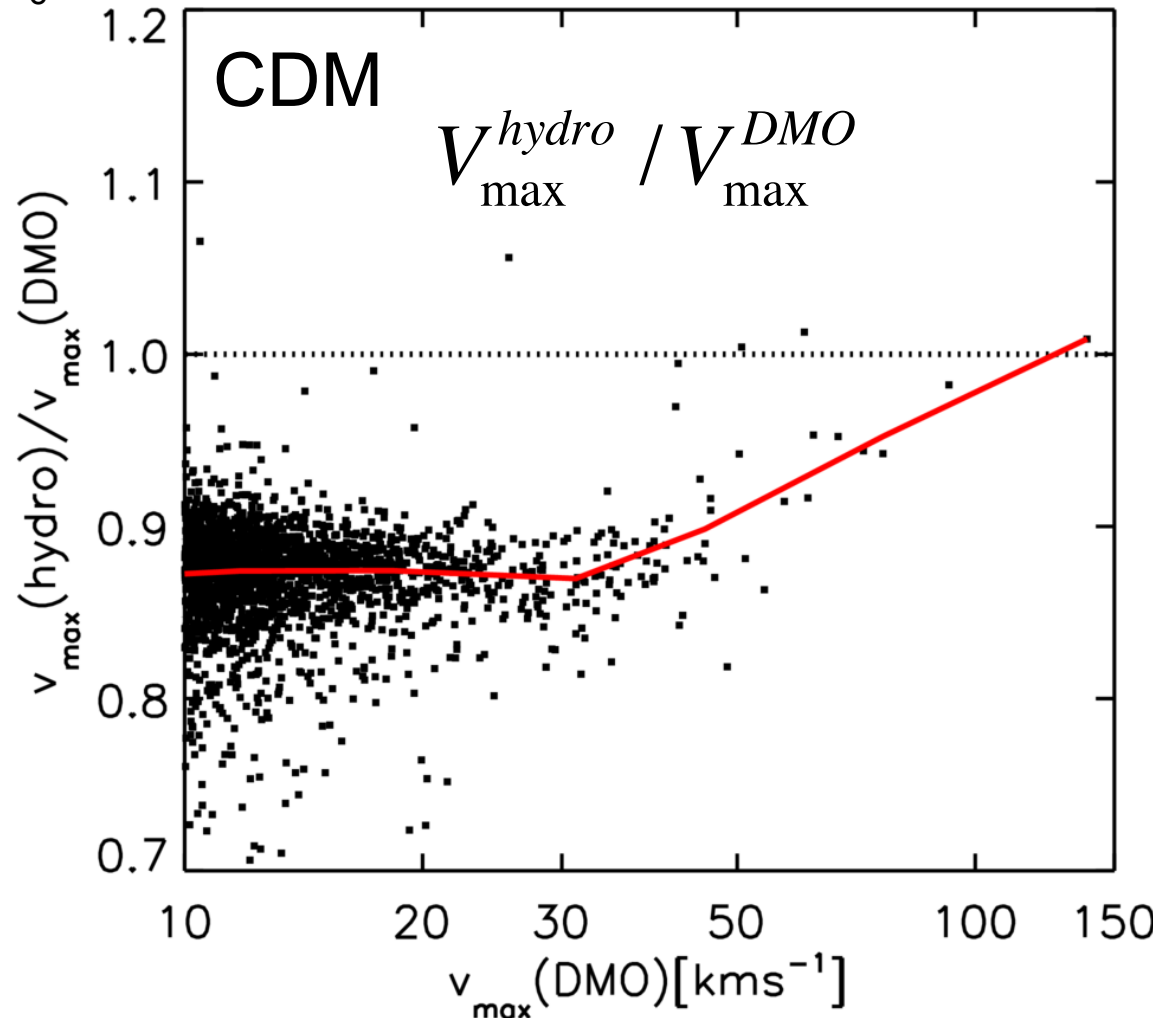
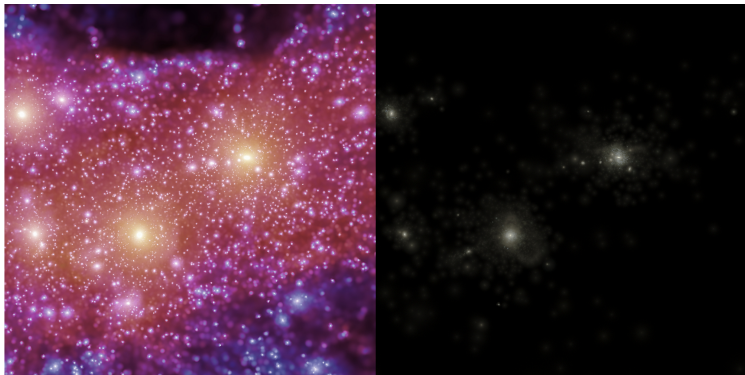


# Baryon effects on halo structure

$$V_c = \sqrt{\frac{GM}{r}} \quad V_{\max} = \max V_c$$

Reduction in  $V_{\max}$  due to  
SN feedback:

→ Lowers halo mass &  
thus halo growth rate

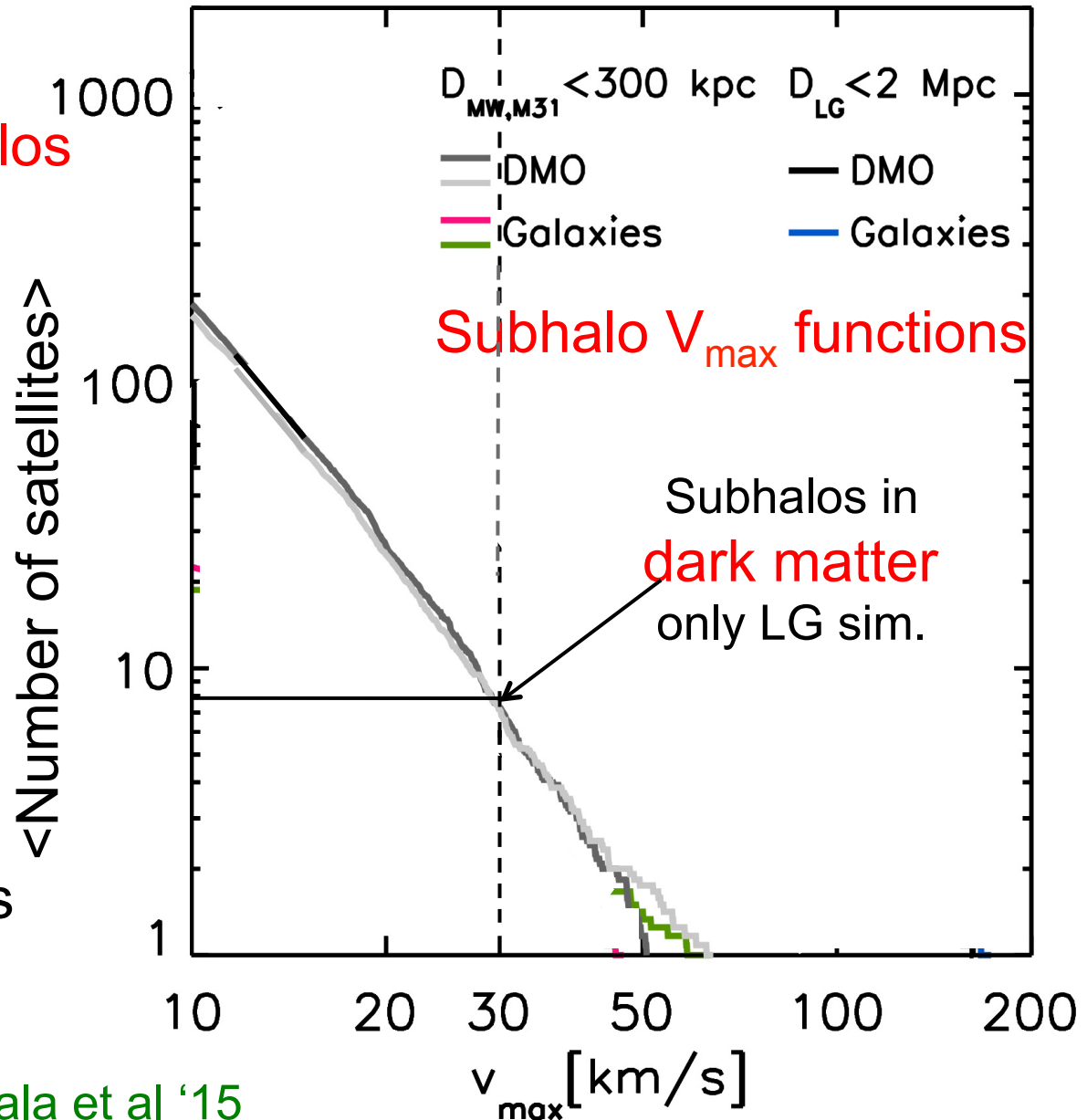


# Too-big-to-fail: the baryon bailout

DM only sims  $\rightarrow$   **$\sim 10$  halos**  
with  $V_{\max} > 30$  km/s



But **MW** has only **3**:  
LMC, SMC, Sagittarius



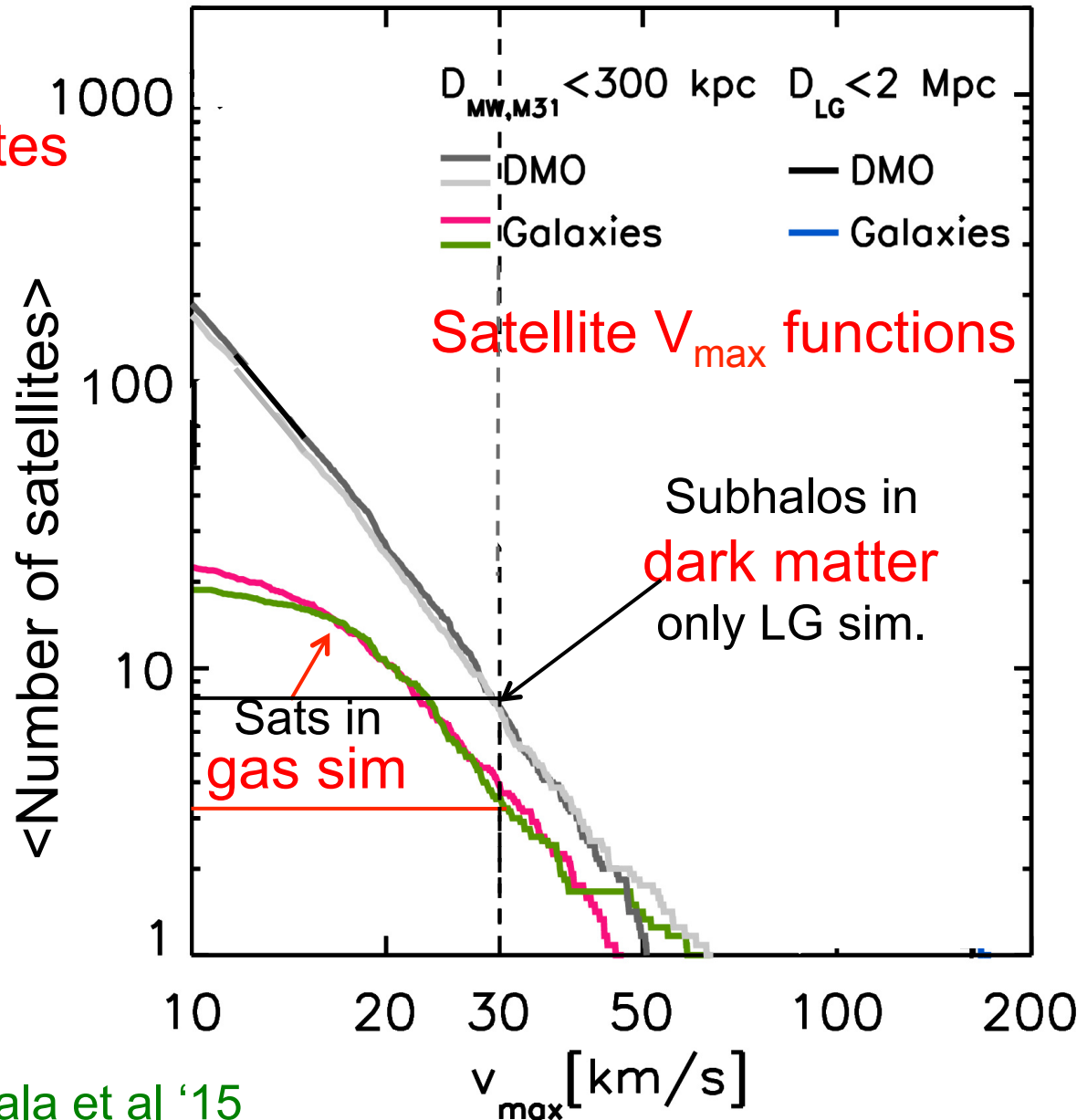


# Too-big-to-fail: the baryon bailout

Hydro sims  $\rightarrow$  **~3 satellites**  
with  $V_{\max} > 30$  km/s

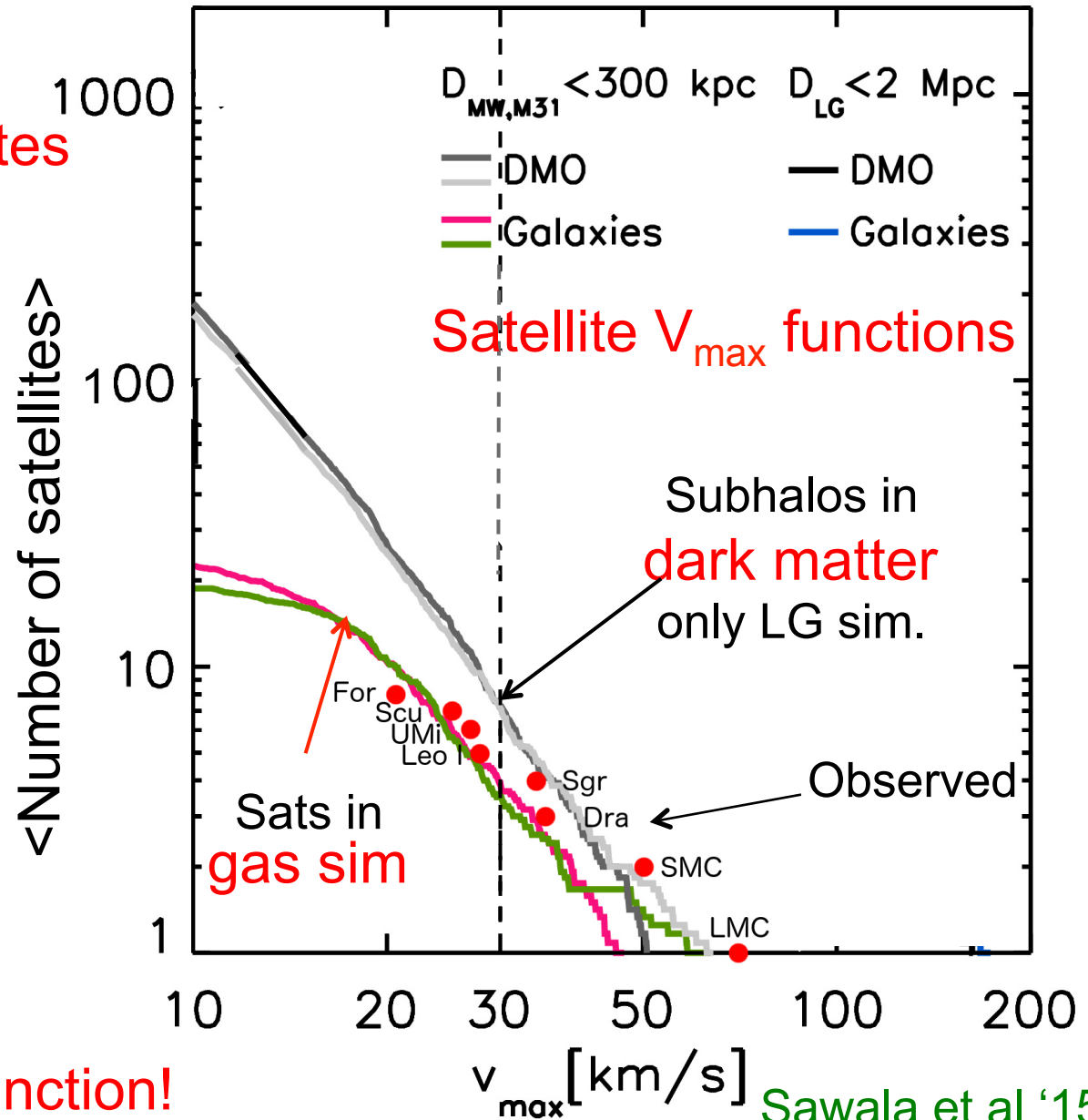


Sawala et al '15



# Too-big-to-fail: the baryon bailout

Hydro sims  $\rightarrow$  **~3 satellites**  
with  $V_{\max} > 30$  km/s



. and with correct  $V_{\max}$  function!



# Tests of $\Lambda$ CDM with subhalos

Test III: inner density profile (core/cusp problem)



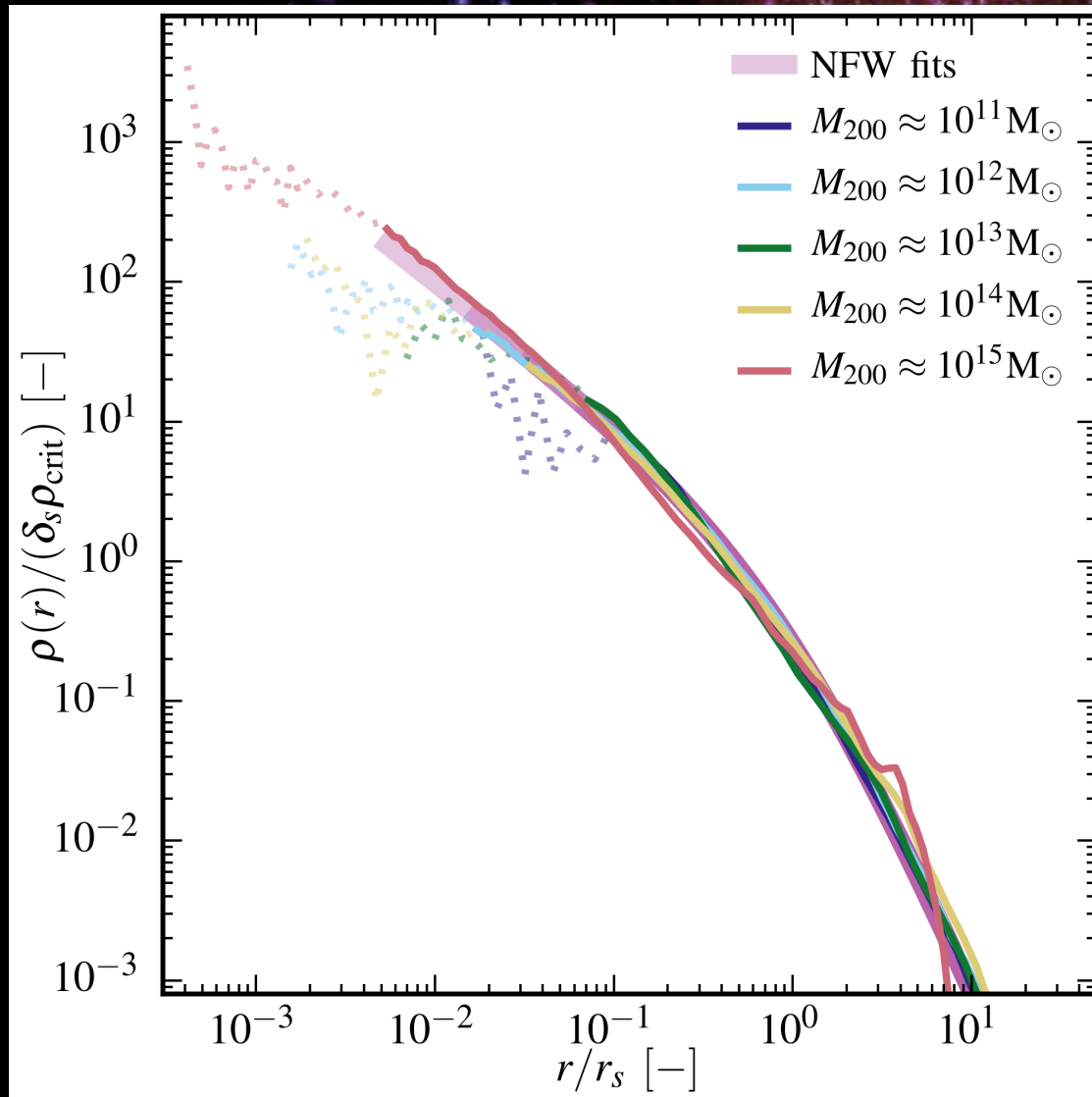
# Dark matter halos: cores or cusps?

## Two myths

- The DM halos of observed dwarfs have central cores
- Hydro simulations of dwarfs produce cores if they have bursty star formation



# The Density Profile of Cold Dark Matter Halos



Shape of halo profiles  
~independent of halo mass &  
cosmological parameters

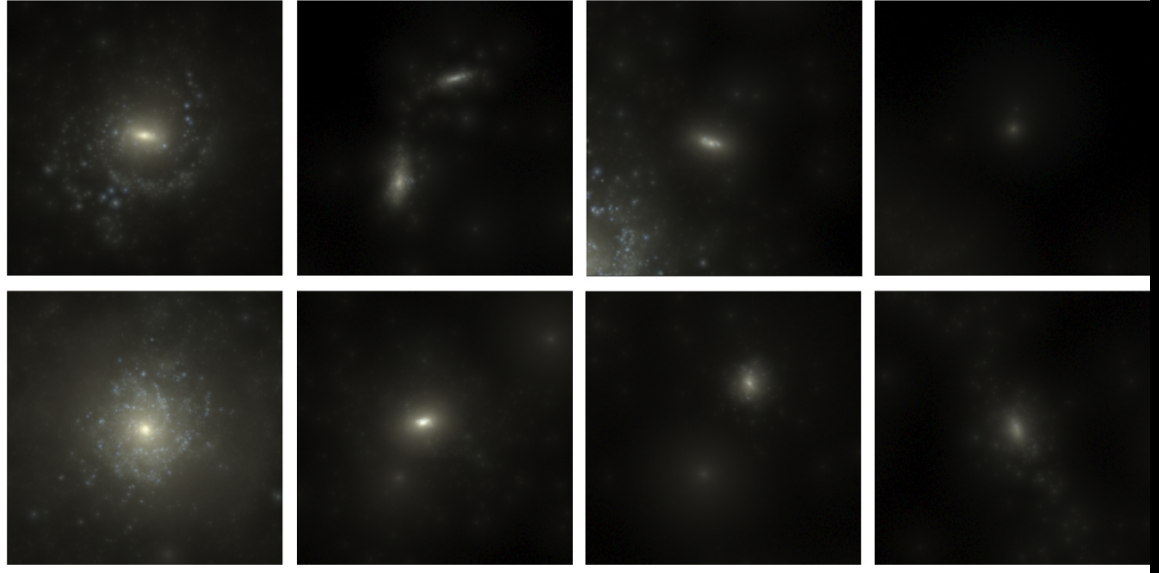
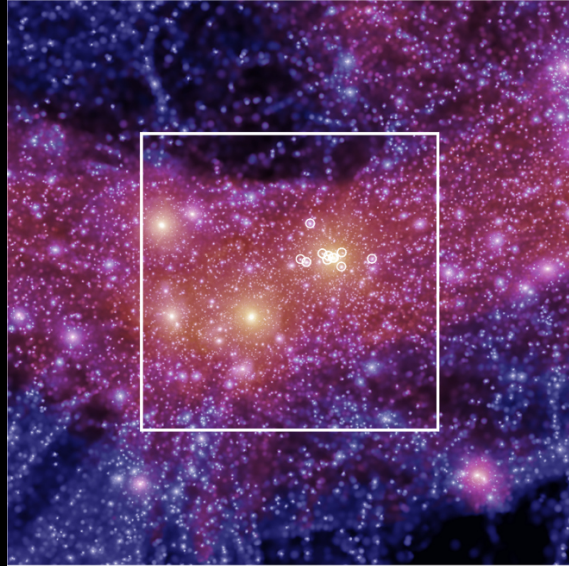
Density profiles are “cuspy” -  
no ‘core’ near the centre

Fitted by simple formula:

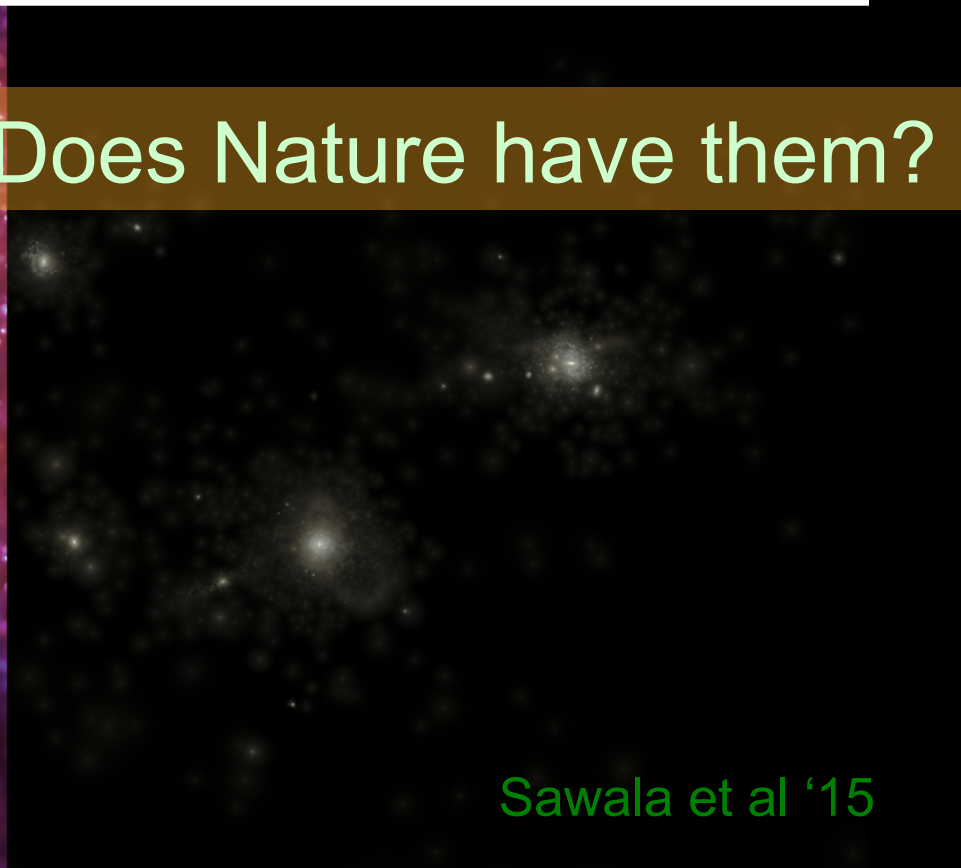
$$\frac{\rho(r)}{\rho_{\text{crit}}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

(Navarro, Frenk & White '97)

More massive halos and  
halos that form earlier have  
higher densities (bigger  $\delta$ )



Does Nature have them?



Sawala et al '15





# The density profile of halos/subhalos

Two main approaches:

- I. Stellar dynamics
- II. Gas rotation curves

# The DM halo of the Sculptor dwarf

Sculptor has two stellar pops:

(i) centrally concentrated, high [Fe/H]

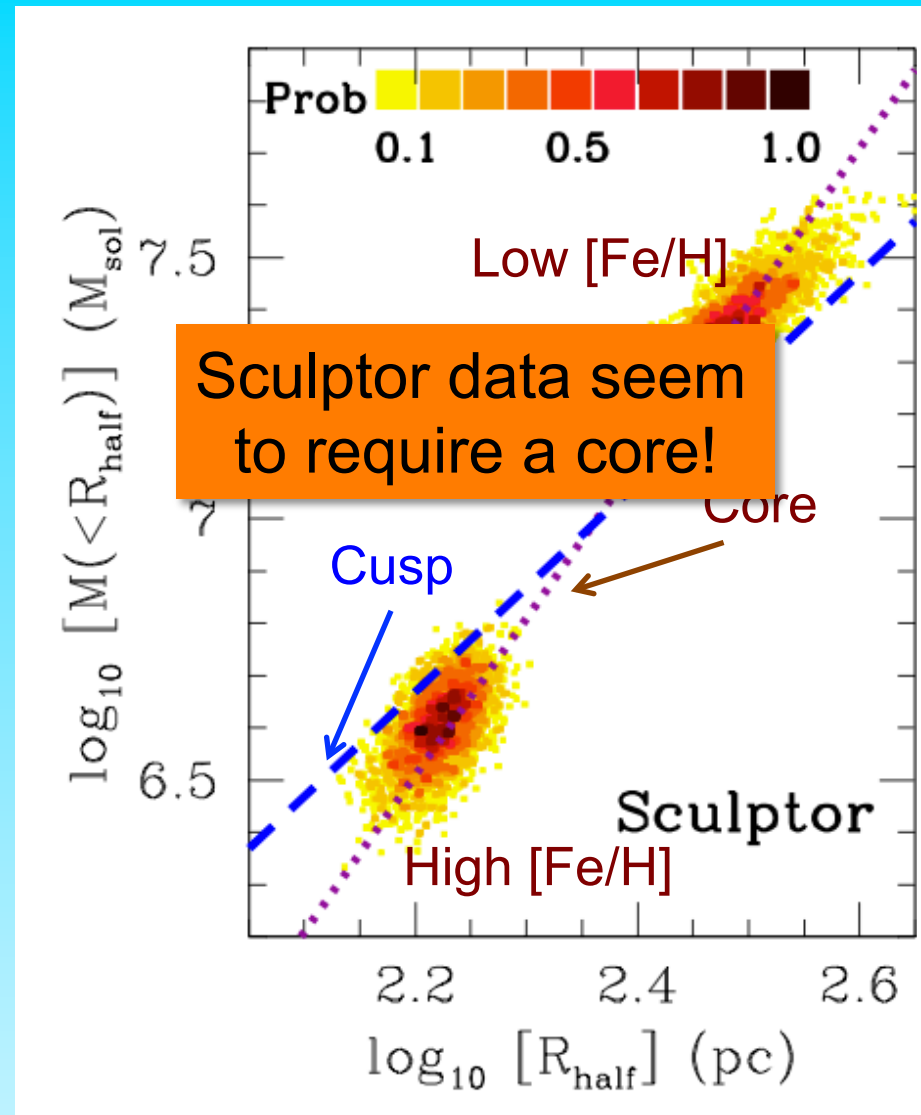
(ii) extended, low [Fe/H]

$$M(< r) = \mu \frac{r < \sigma_{los}^2 >}{G}$$

$r = r_{1/2}$

Walker '10; Wolf et al '10 →

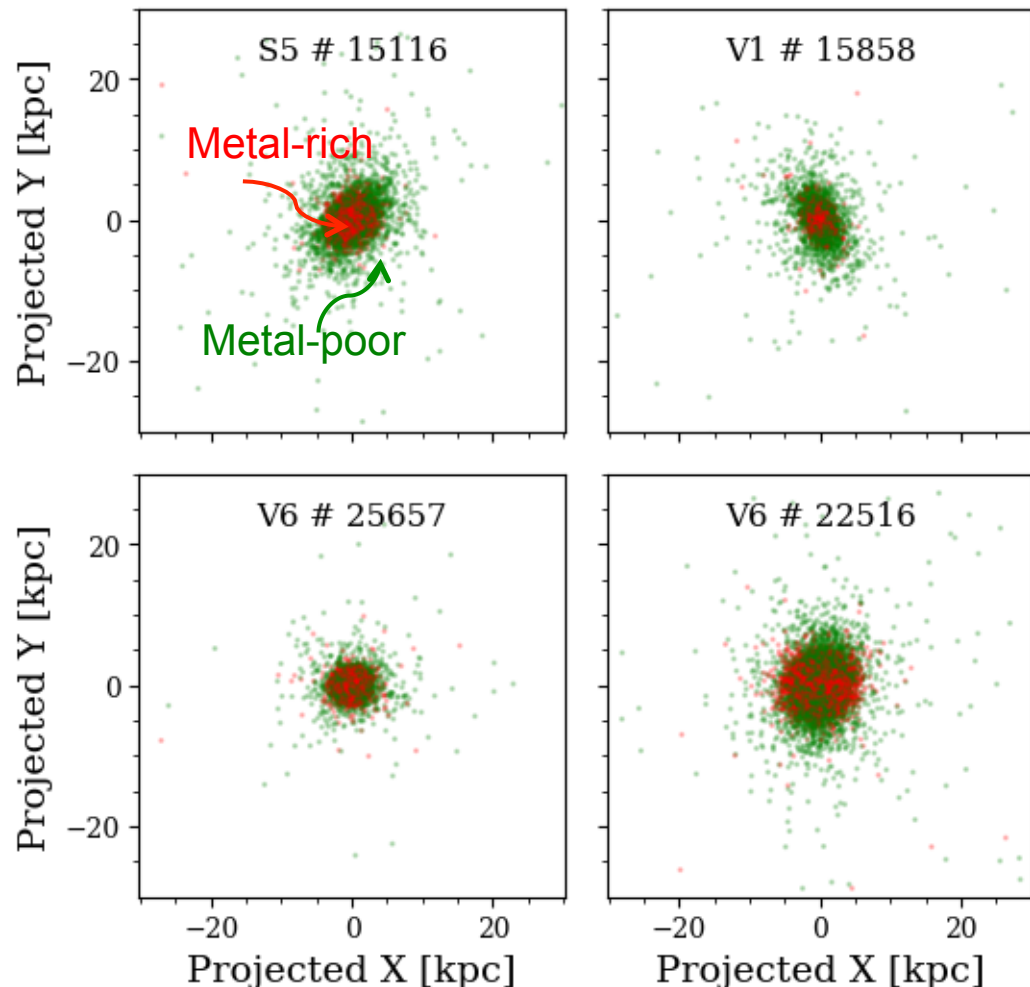
if  $r = r_{1/2}$ ,  $\mu = 2.5$ , independently of model assumptions!



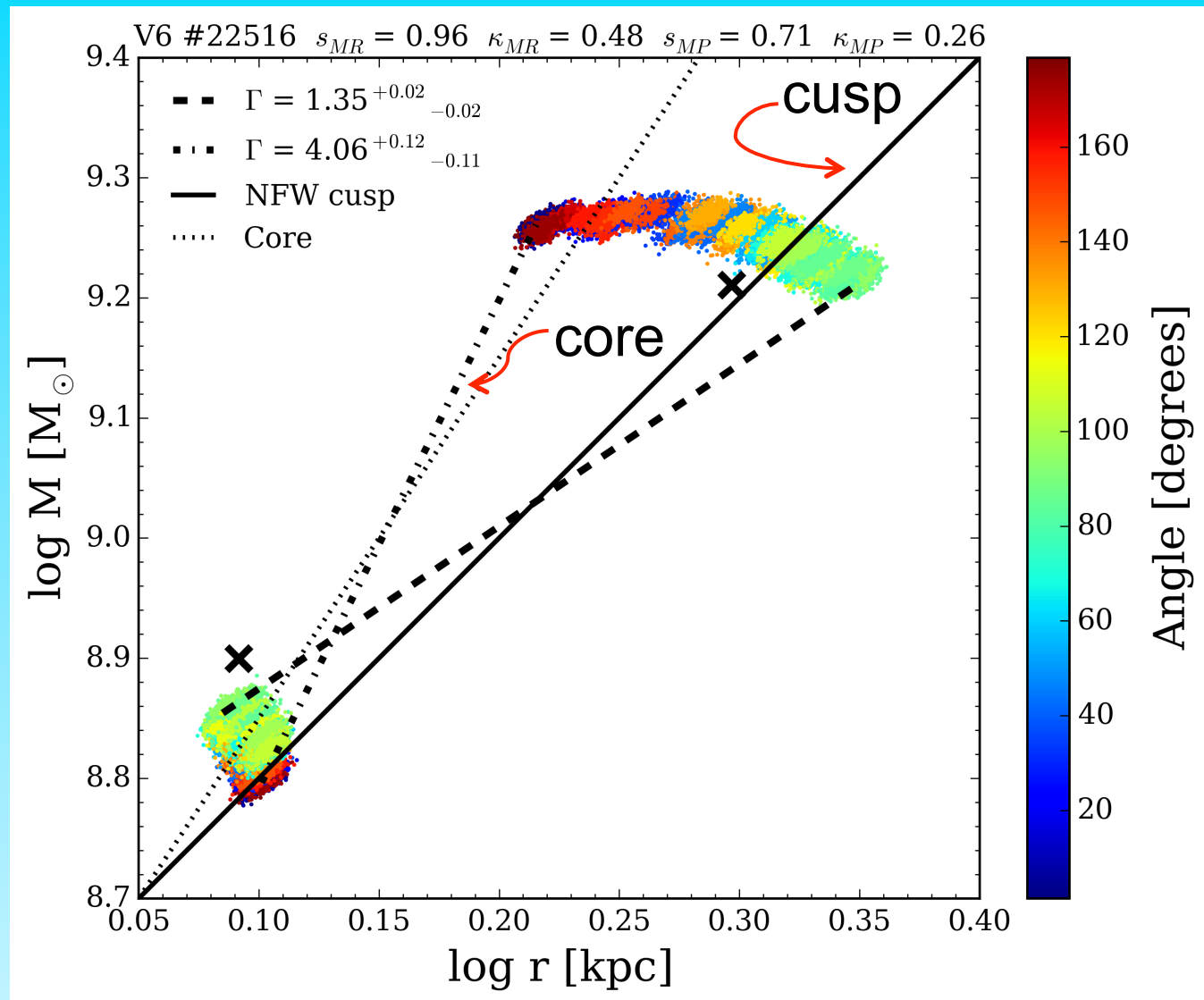


Wolf/Walker mass estimator assumes equilibrium and spherical symmetry

The stellar populations are not spherical and the shapes of the two can be different



The inferred slope  
(core or cusp)  
depends on the  
viewing angle!





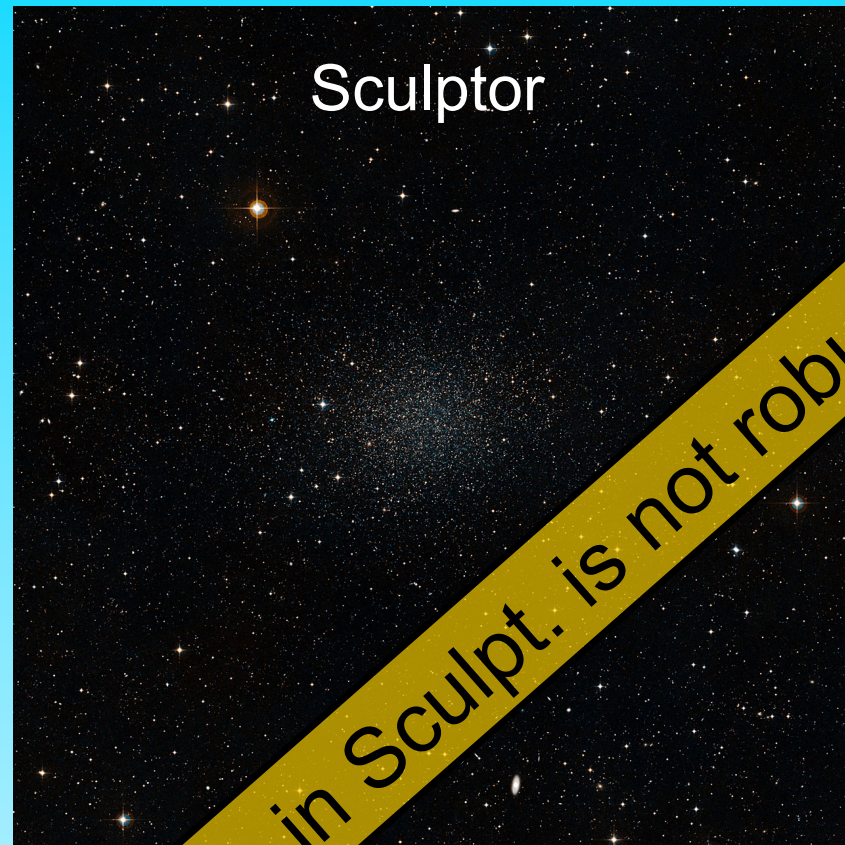
# The DM halo of the Sculptor dwarf

$$M(< r) = \mu \frac{r \langle \sigma_{los}^2 \rangle}{G}$$

Key assumption of mass estimator:

spherical symmetry

Is Sculptor spherical?



WP11 core in Sculpt. is not robust

Genina, CSF et al '17



Many nearby galaxies now have hi-res 2D HI velocity fields → ideal for inferring potential

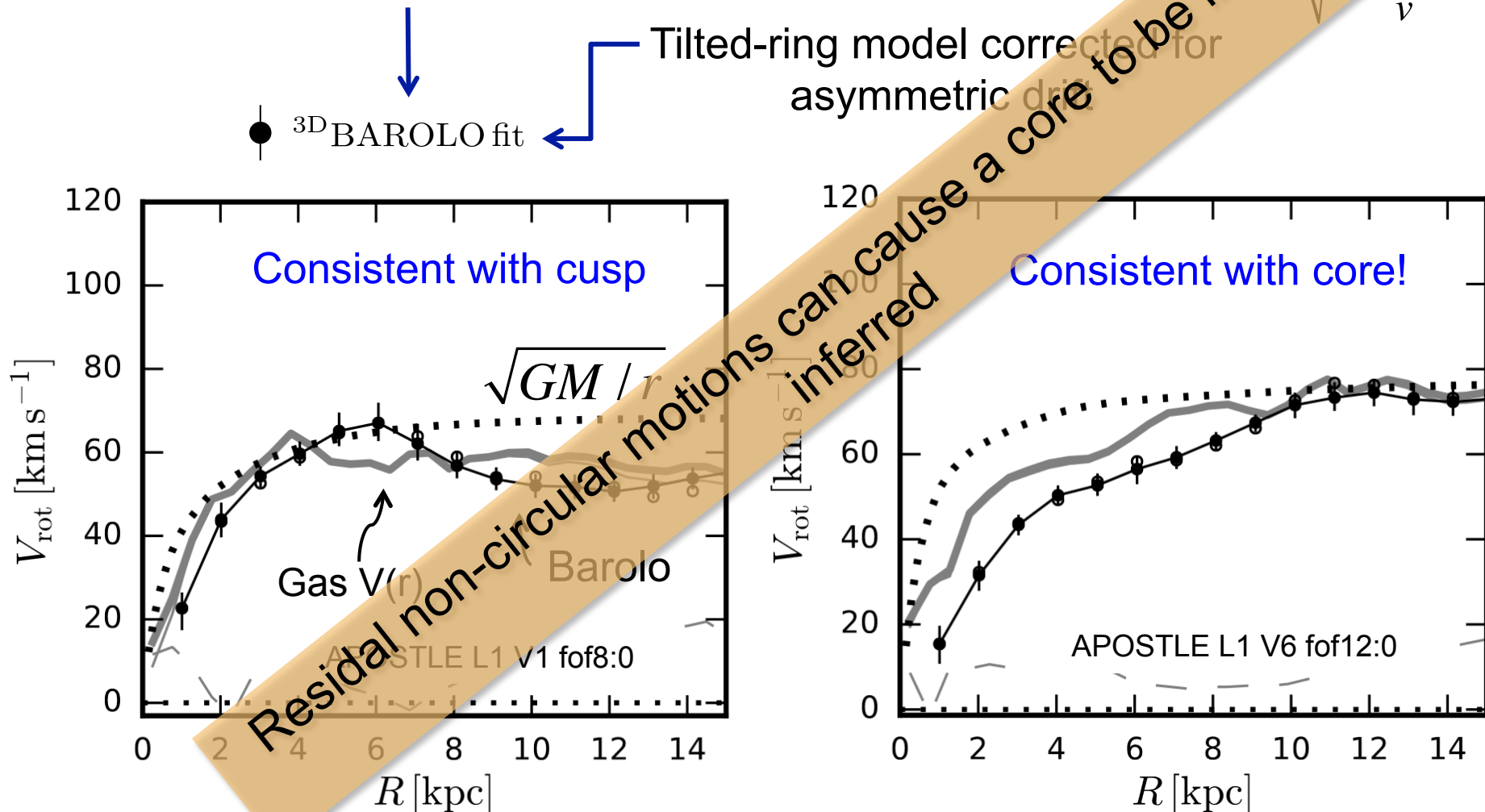
Assume: gas is in centrifugal equilibrium on approximately circular orbits



# Rotation curves of 2 APOSTLE dwarfs

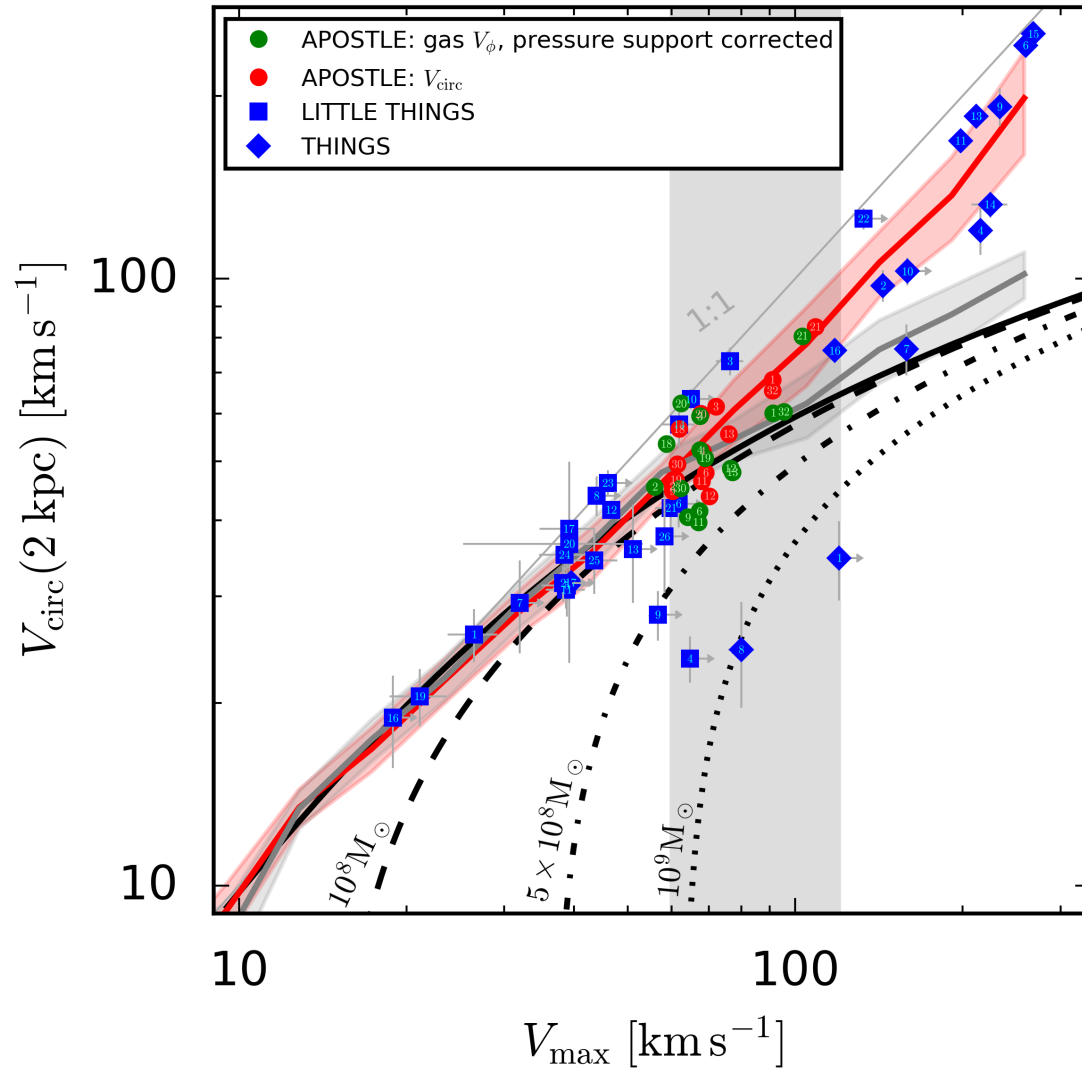
APOSTLE galaxies all have NFW cusps

2D velocity field  $\rightarrow V_c(r)$  (rotn curve); in dynamical equilibrium:  $v_c = \sqrt{\frac{GM(<r)}{v}}$



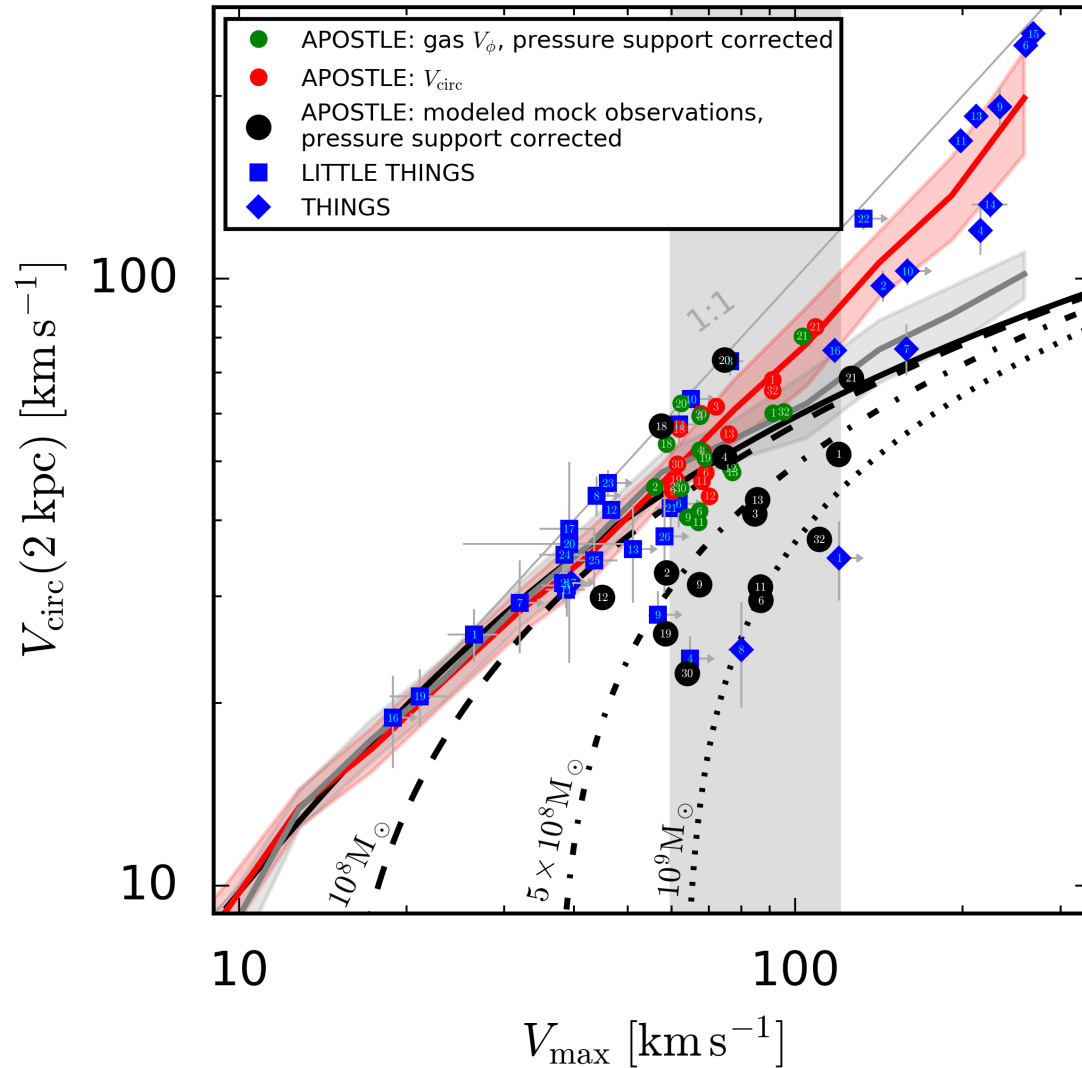
Oman et al '18; Marasco et al '18

# The diversity of rotation curves





# The diversity of rotation curves





But, if cores were found in galaxies would  
that rule out CDM and WDM?



# The physics of core formation

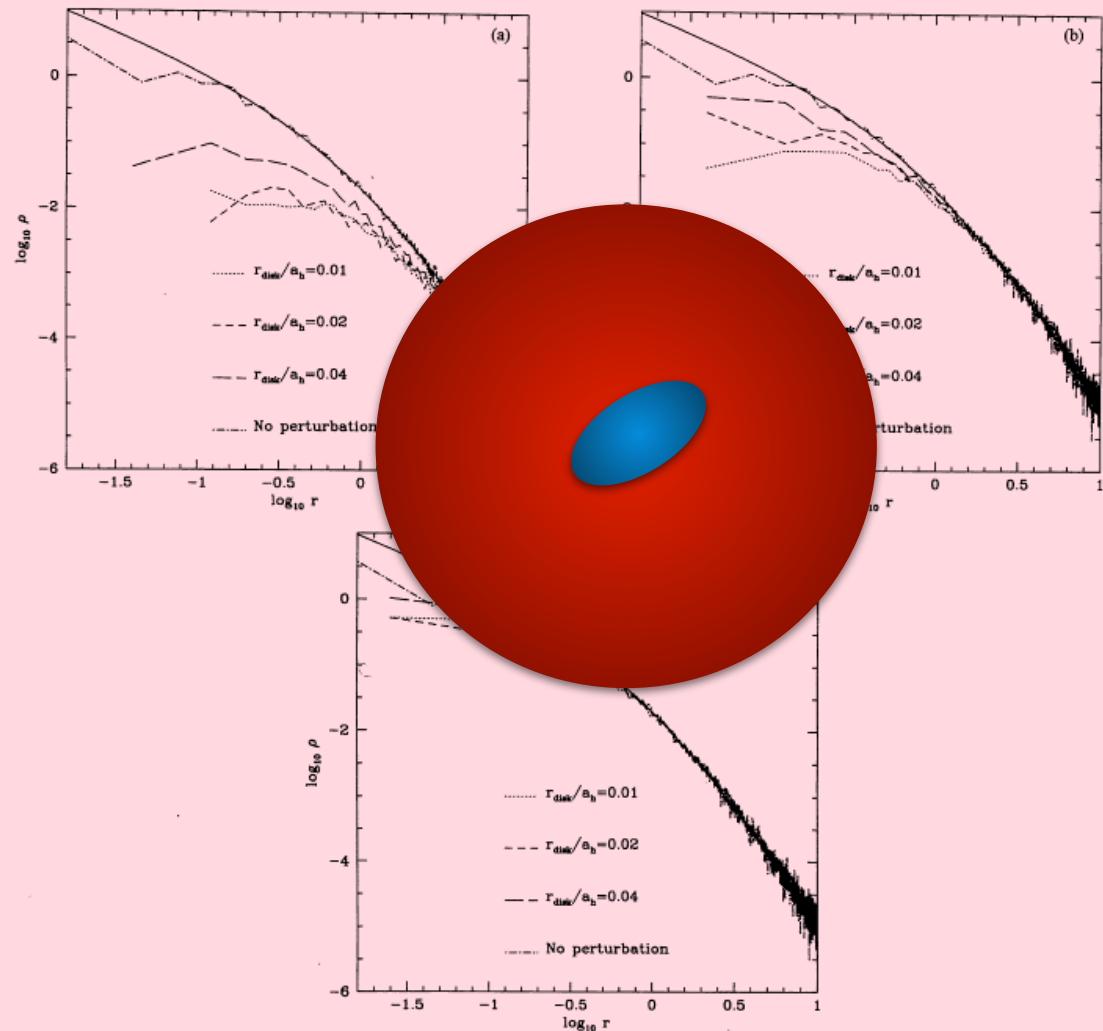
Cusps → cores

Perturb central halo region  
by growing a galaxy  
adiabatically and removing  
it suddenly (Navarro, Eke  
& Frenk '96)

Cores may also form by  
repeated fluctuations in  
central potential (e.g. by  
SN explosions) (Read &  
Gilmore '05; Pontzen &  
Governato '12,'14; Bullock &  
Boylan-Kolchin '17)

Navarro, Eke & Frenk (1996)

The cores of dwarf galaxy haloes L75

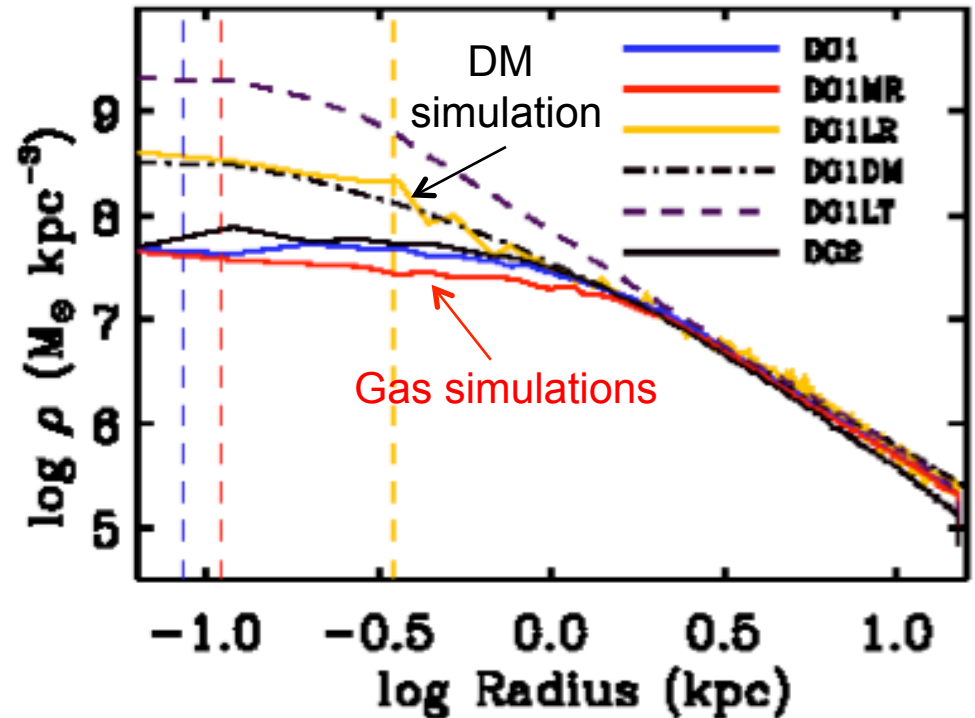


**Figure 3.** Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10 000-particle realization of the Hernquist model run in isolation at  $t = 200$ . (a)  $M_{\text{disc}} = 0.2$ . (b)  $M_{\text{disc}} = 0.1$ . (c)  $M_{\text{disc}} = 0.05$ .

# Cores in dwarf galaxy simulations

Governato et al. assume  
high density threshold for  
star formation

- High threshold allows large gas mass to accumulate in centre
- Sudden repeated removal of gas transfers binding energy



Governato et al. '12

Pontzen et al. '12

# Cores or cusps in simulations?

Depends on details of how star formation is modelled  
(subgrid physics)

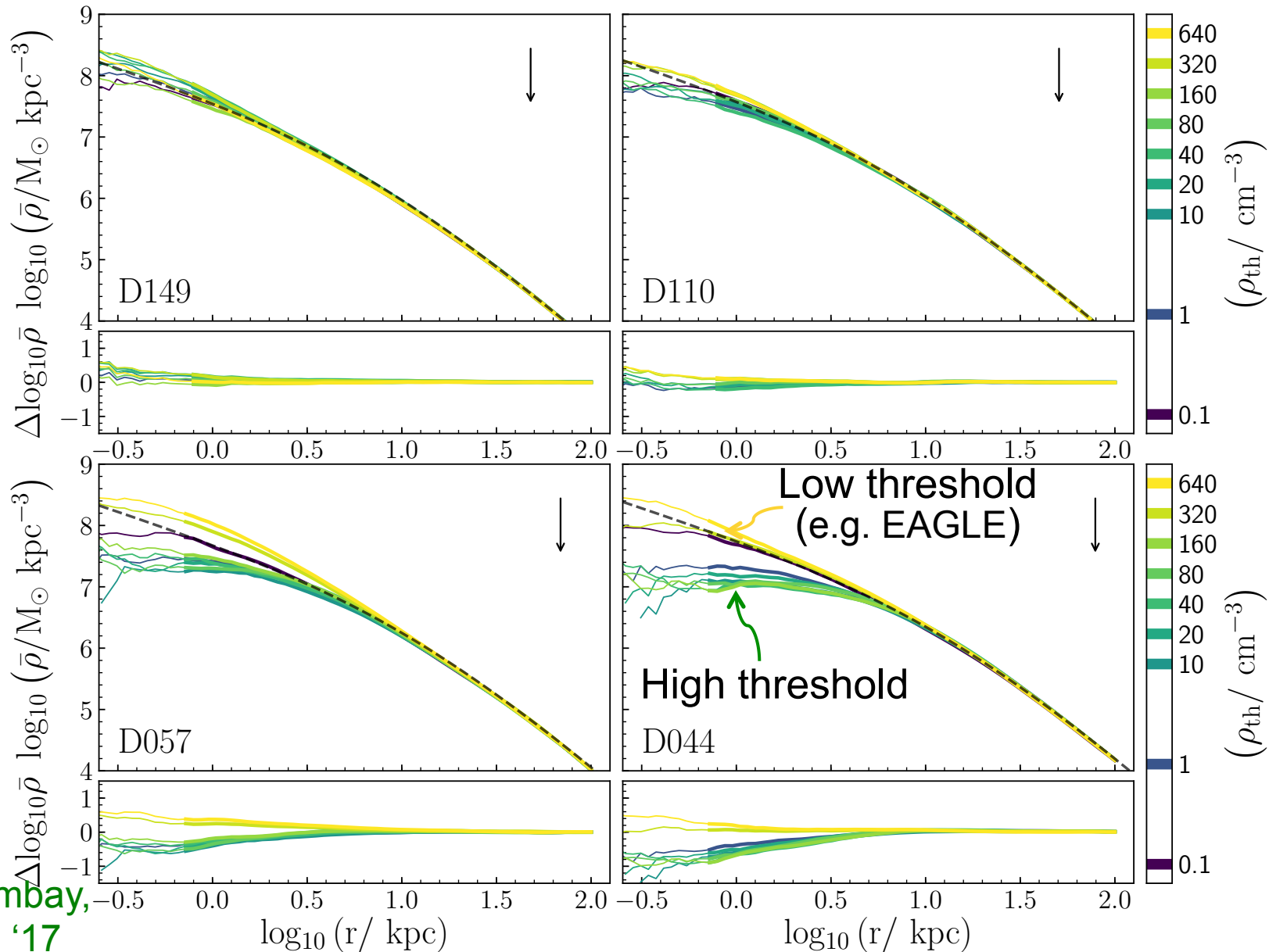
**Key parameter:** gas density threshold for star formation

High density → NEF mechanism

Low density → not enough central gas density to perturb DM



# Cores or cusps in simulations?





There is **NO** strong evidence  
for cores in dwarf galaxies

(Existing data are consistent  
with either cusps or cores)

But in any case cores  
can be easily created  
by baryon effects



# Tests of $\Lambda$ CDM with subhalos

## I. What do we know about subhalos in $\Lambda$ CDM (and $\Lambda$ WDM)

- Abundance
- Radial distribution
- Structure

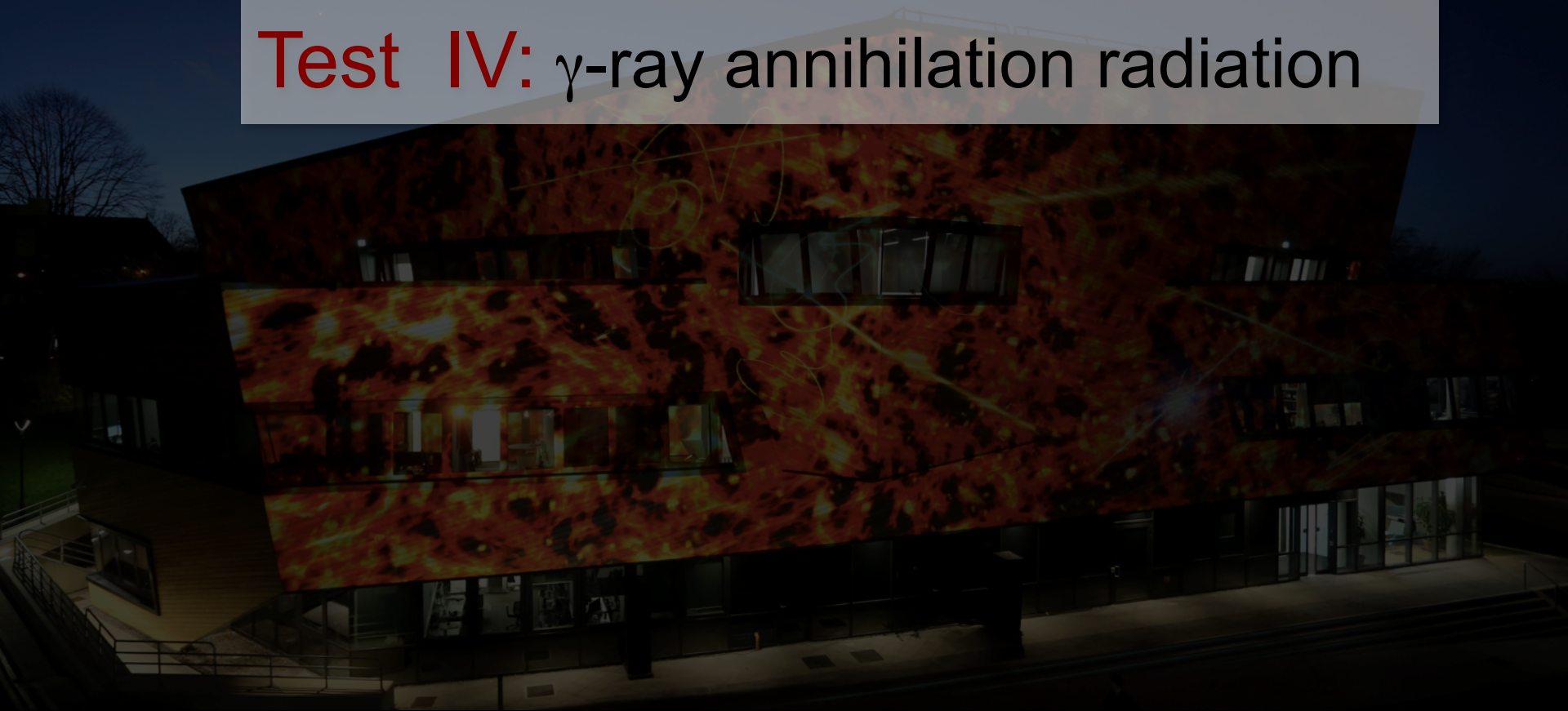
## II. How can we use subhalos to test $\Lambda$ CDM

- In the optical
- In gamma rays
- With gravitational lensing



# Tests of $\Lambda$ CDM with subhalos

Test IV:  $\gamma$ -ray annihilation radiation



# A blueprint for detecting CDM

Supersymmetric particles **annihilate** and lead to production of  **$\gamma$ -rays** which may be **observable** by **FERMI**

Intensity of annihilation radiation at  $\mathbf{x}$  depends on:

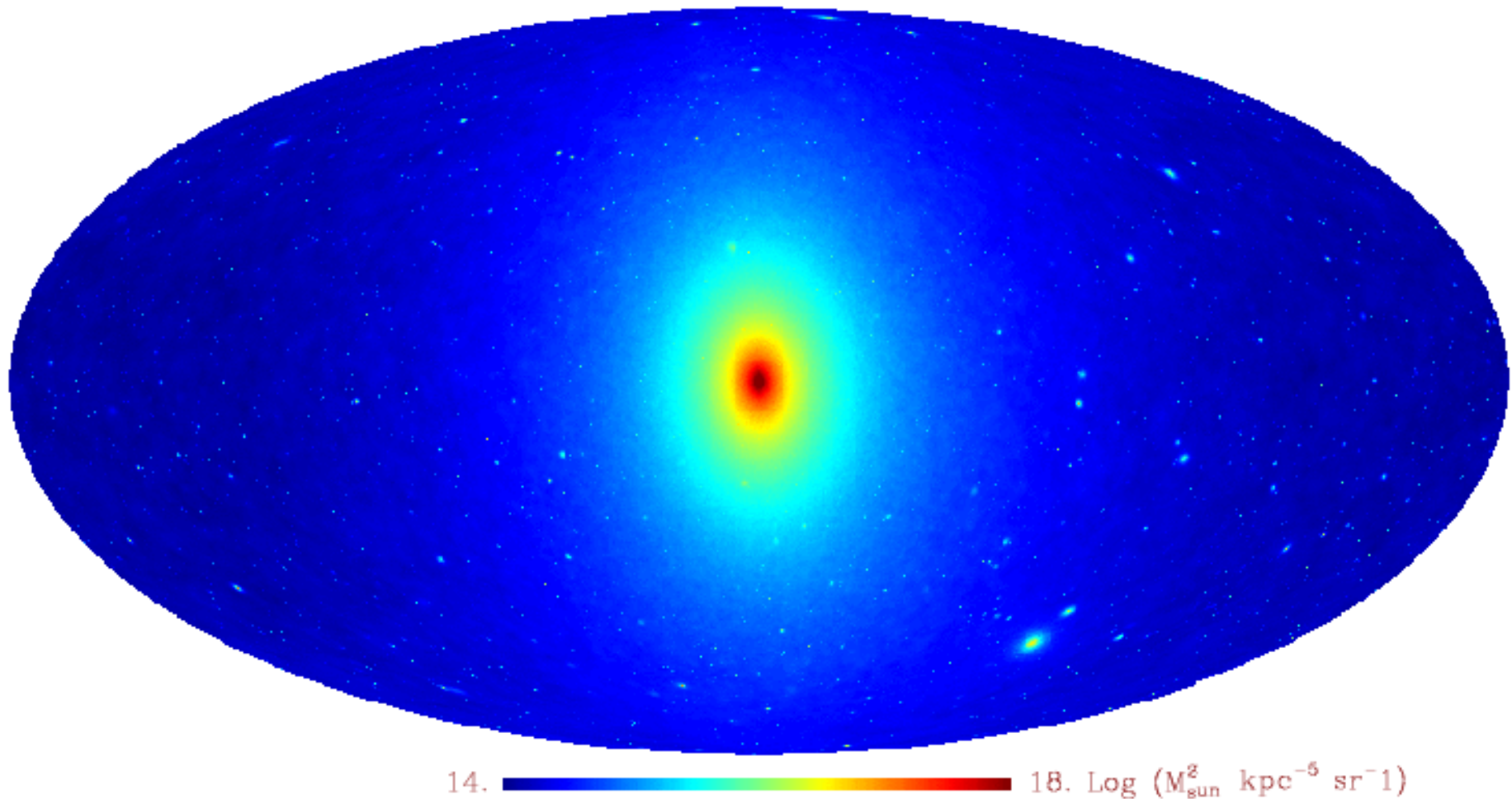
$$\int \rho^2(\mathbf{x}) \langle \sigma v \rangle dV$$

halo density at  $\mathbf{x}$        $\uparrow$        $\uparrow$  cross-section

For a smooth NFW profile: 
$$L \propto \frac{V_{\max}^4}{r_{\max}}$$

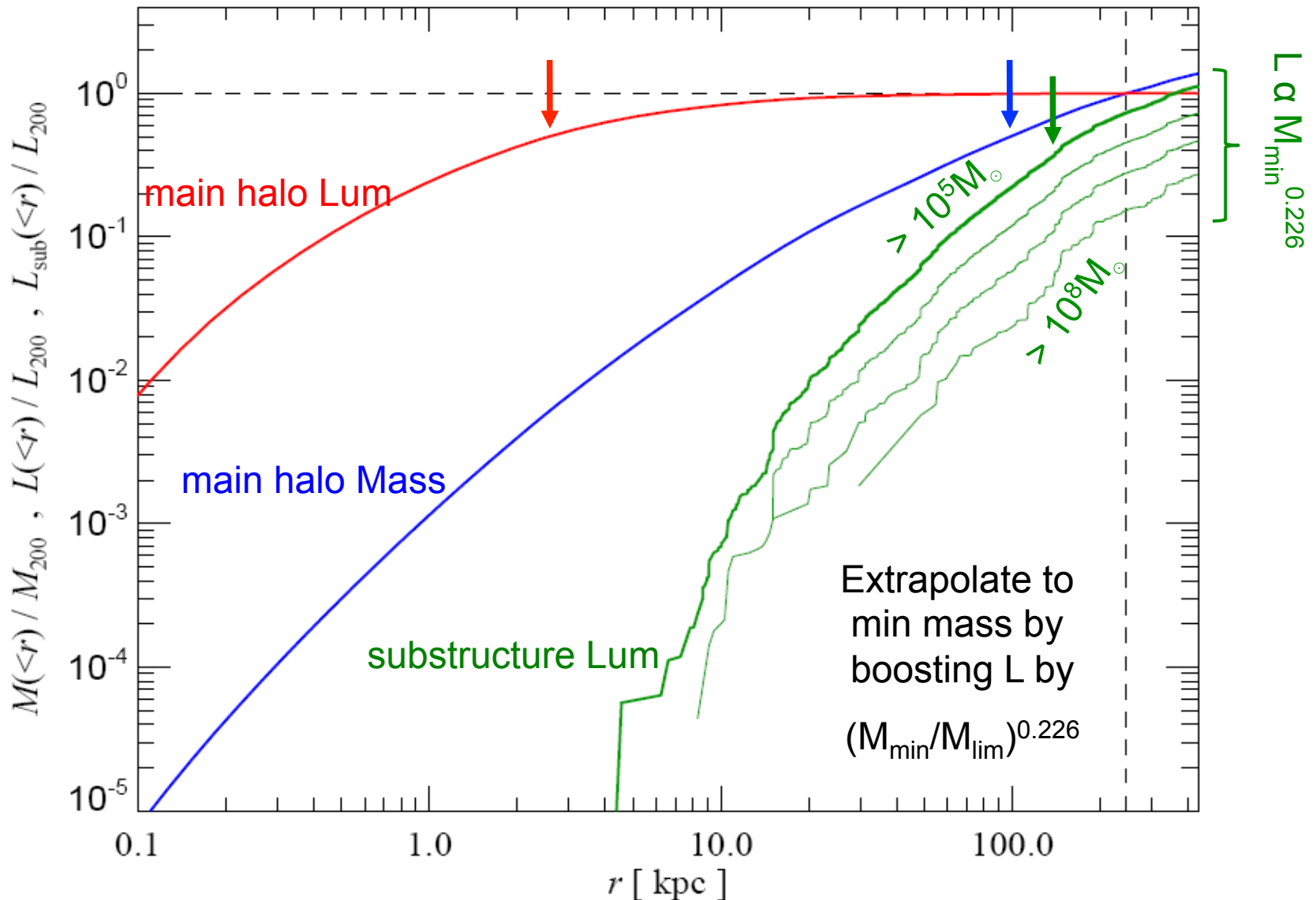
# Milky Way halo seen in DM annihilation radiation

## Aquarius simulation





# Mass and annihilation radiation profiles of a MW halo

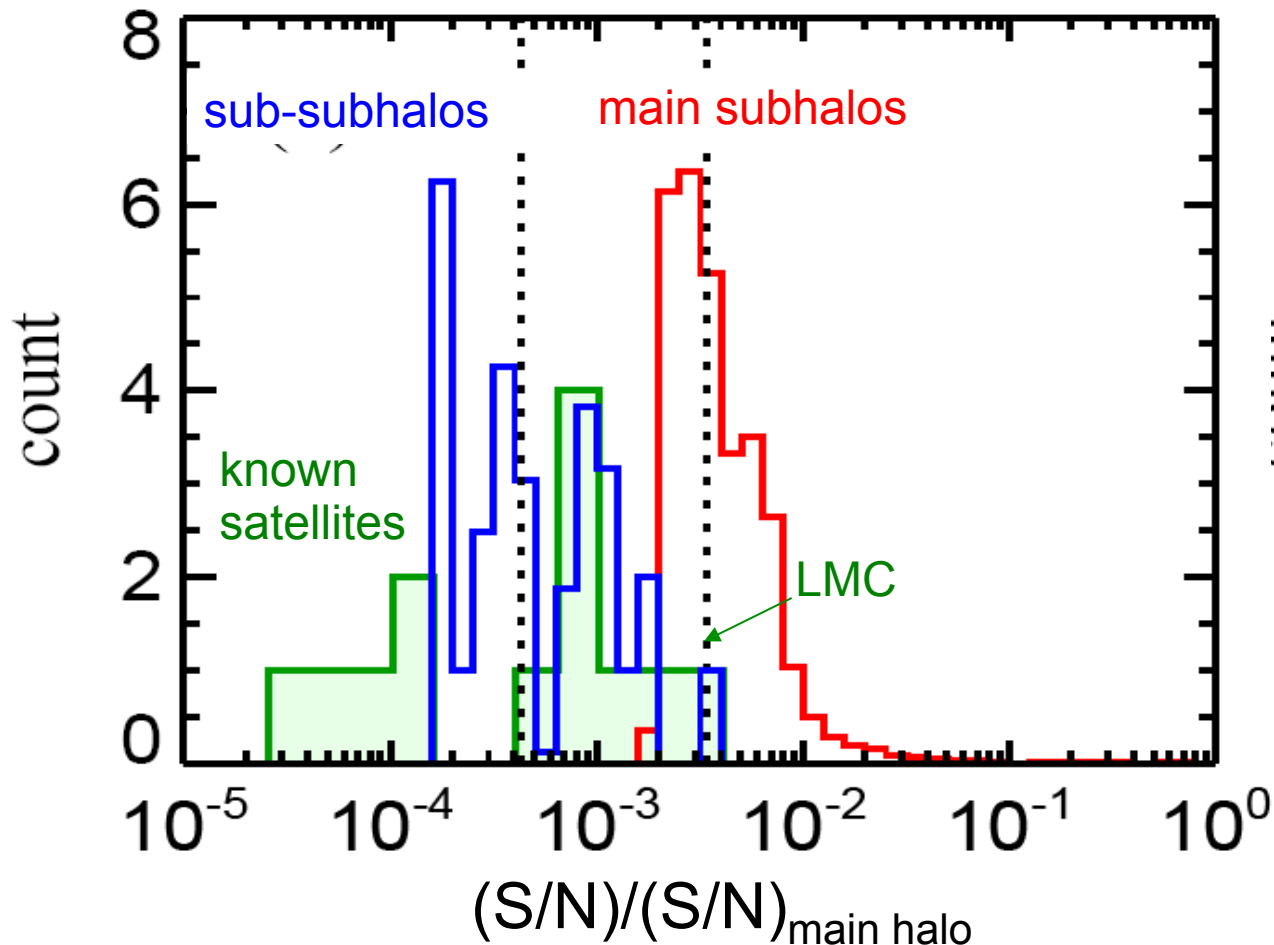


# A blueprint for detecting halo CDM

Springel + '08b

S/N for detecting  
subhalos in units of  
that for detecting the  
main halo

30 highest S/N  
objects, assuming  
use of optimal filters



- Highest S/N subhalos have 1% of S/N of main halo
- Highest S/N subhalos have 10 times S/N of known satellites
- Substructure of subhalos has no influence on detectability



Can CDM be ruled out?

Yes !





# Tests of $\Lambda$ CDM with subhalos

## I. What do we know about subhalos in $\Lambda$ CDM (and $\Lambda$ WDM)

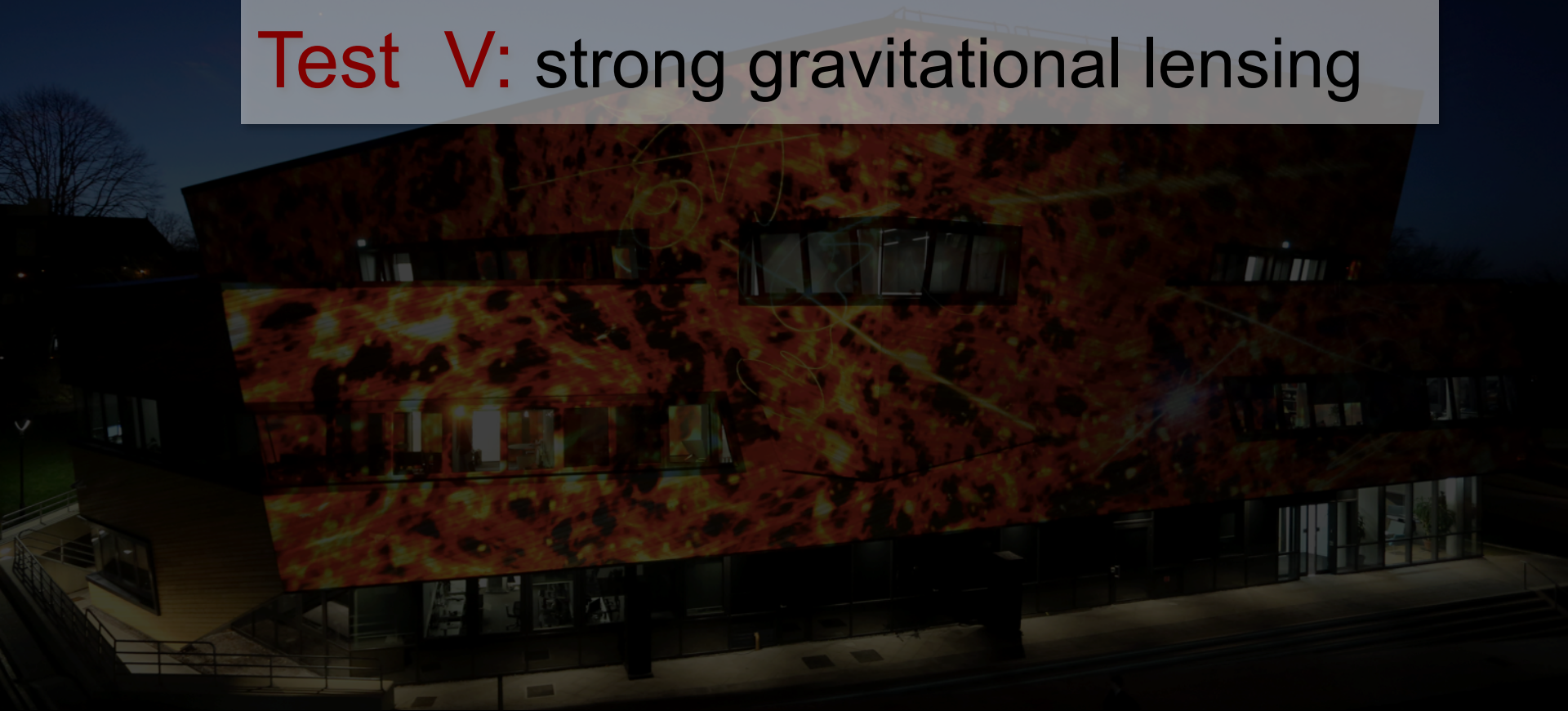
- Abundance
- Radial distribution
- Structure

## II. How can we use subhalos to test $\Lambda$ CDM

- In the optical
- In gamma rays
- With gravitational lensing

# Tests of $\Lambda$ CDM with subhalos

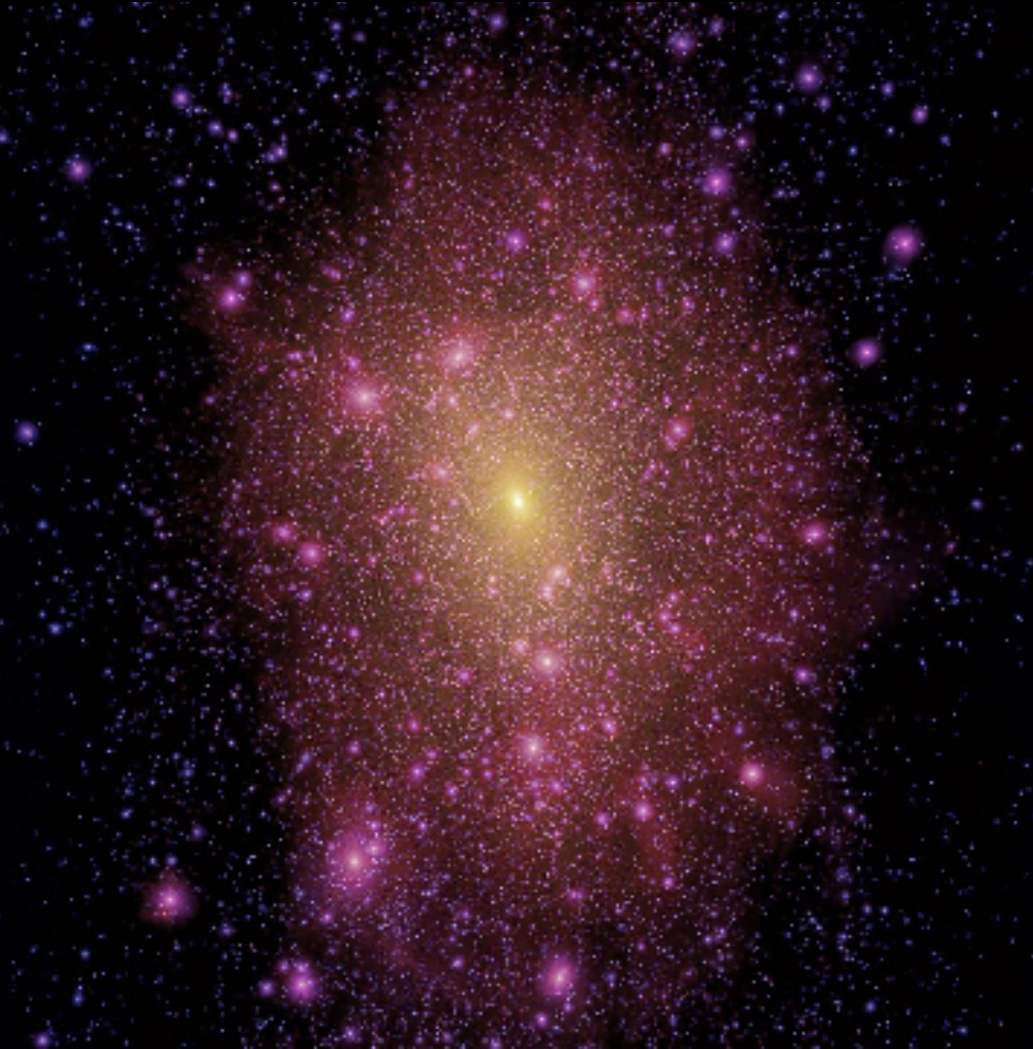
Test V: strong gravitational lensing





# The satellites of the Milky Way

cold dark matter



The **key** prediction of CDM is that there should be a very large number of **small dark matter** halos, too small to have made a galaxy.



cold dark matter

warm dark matter

How can we test these?

Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
Boyarski & Ruchayskiy '12

# The subhalo mass function

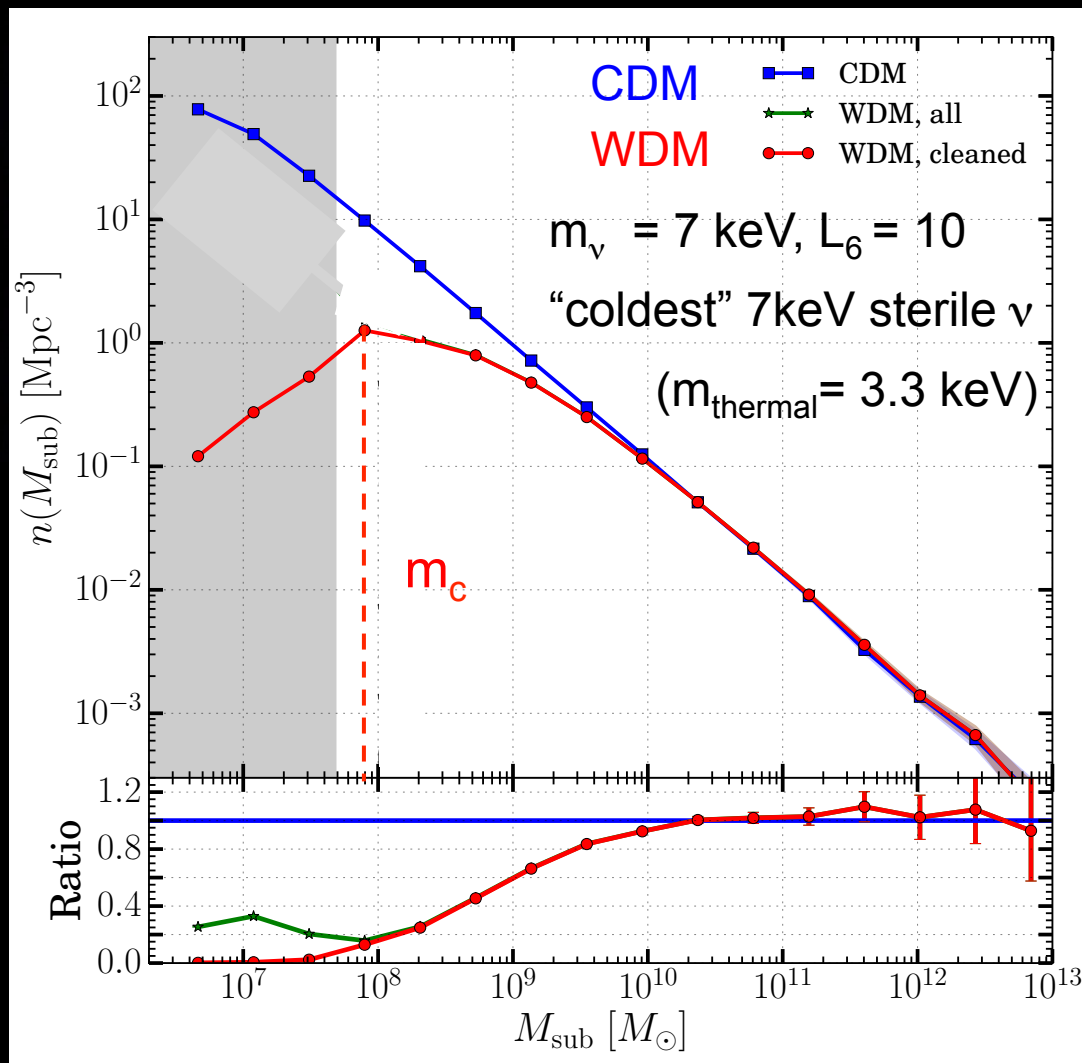


CDM

WDM

3 x fewer WDM subhalos at  $3 \times 10^9 M_\odot$

10 x fewer at  $10^8 M_\odot$







# Can we distinguish CDM/WDM?

cold dark matter

warm dark matter

Dark halos can be detected through  
gravitational lensing

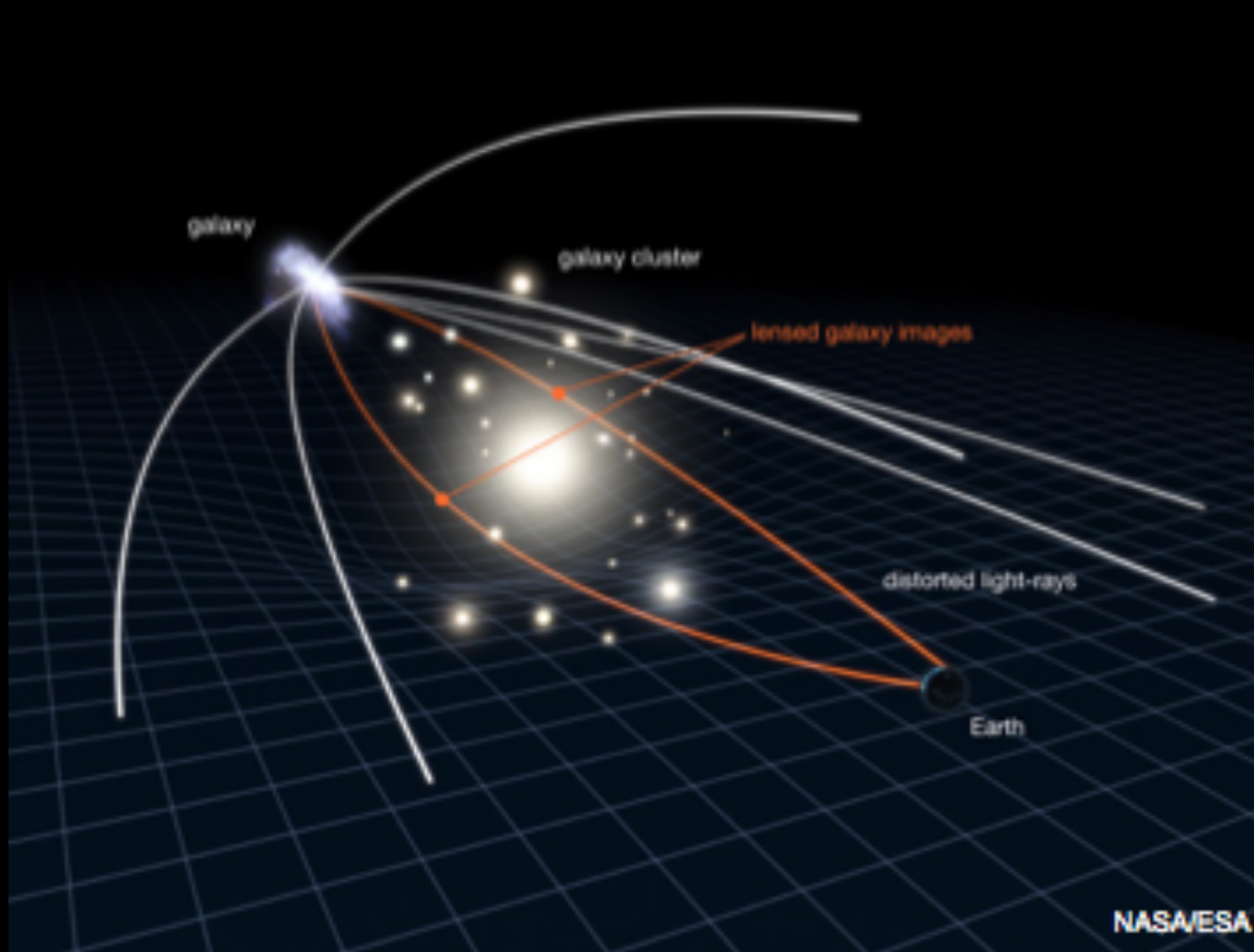




# Gravitational lensing: Einstein rings

How to rule out CDM

# Gravitational lensing: Einstein rings



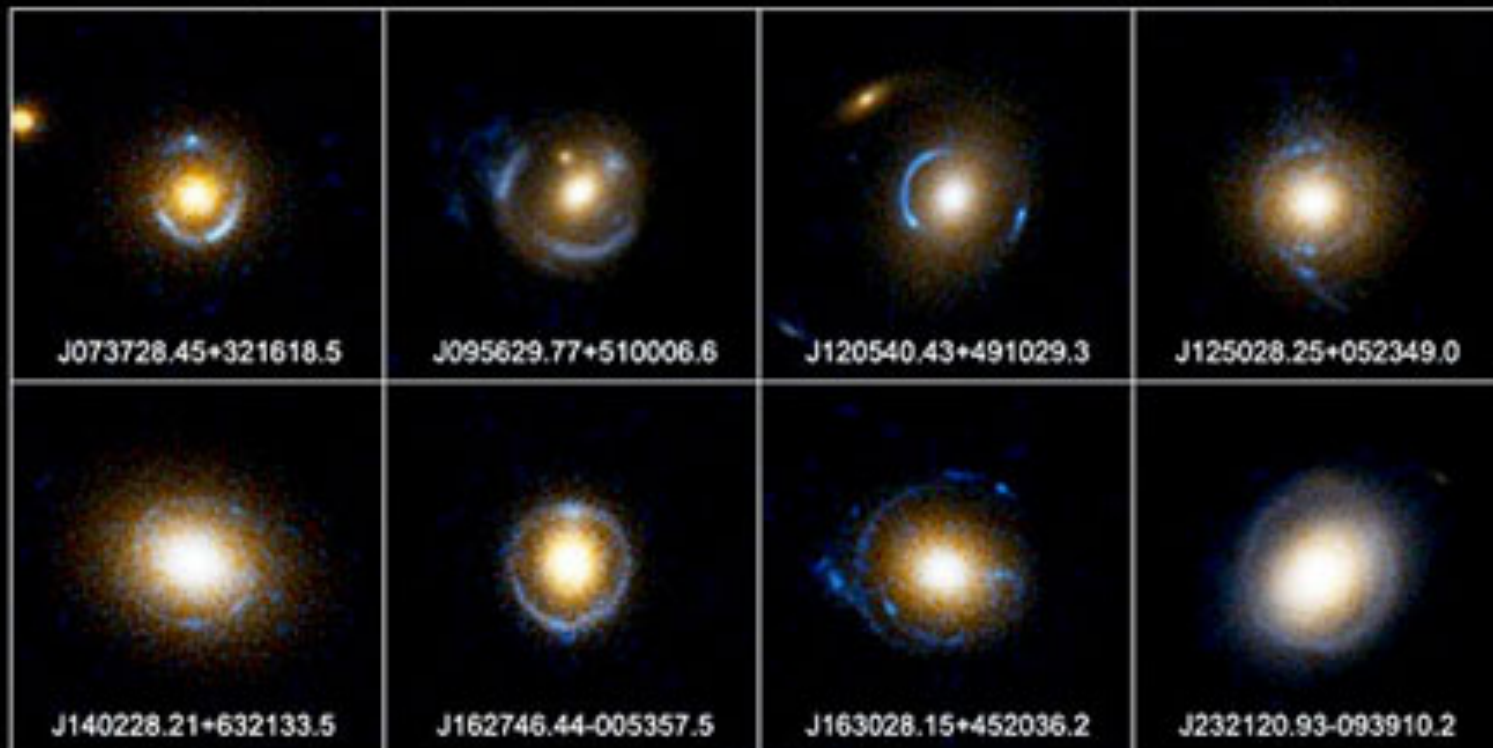
When the source and the lens are well aligned → strong arc or an Einstein ring



# SLAC sample of strong lenses

**Einstein Ring Gravitational Lenses**

*Hubble Space Telescope • ACS*

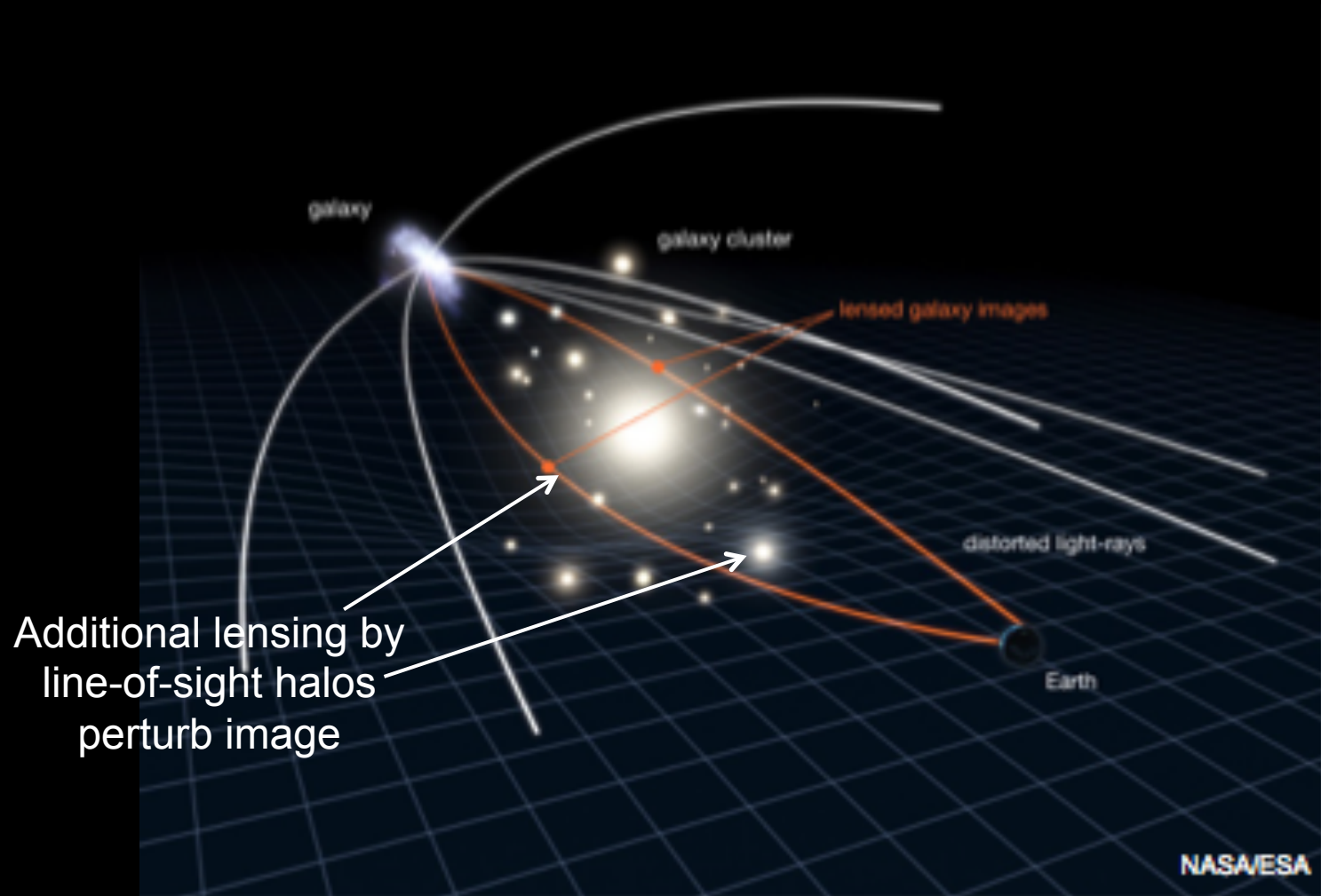


NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

STScI-PRC05-32



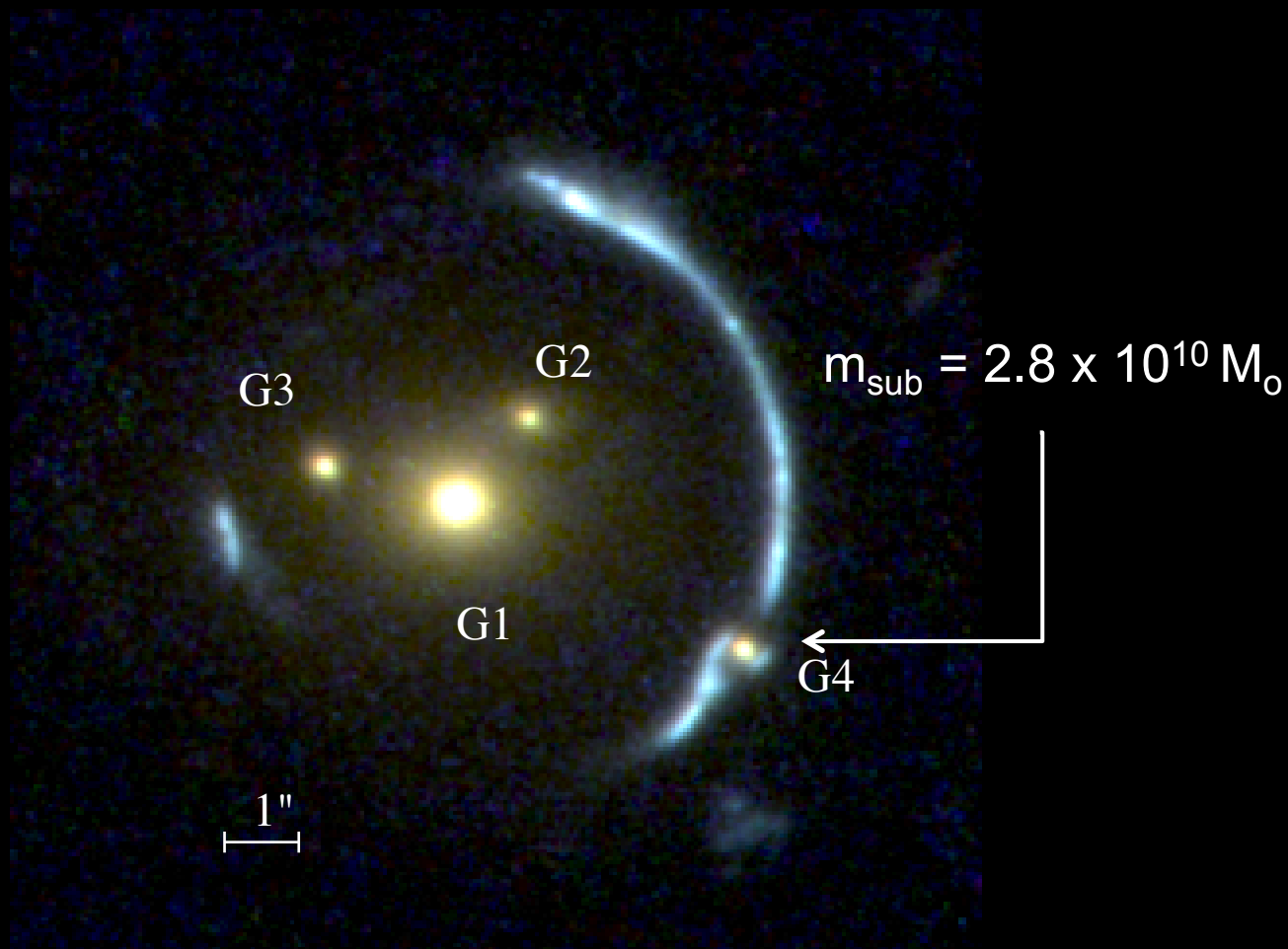
# Gravitational lensing: Einstein rings



When the source and the lens are well aligned → strong arc or an Einstein ring

# Gravitational lensing: Einstein rings

Halos projected onto an Einstein ring distort the image





# Gravitational lensing: Einstein rings

Halos projected onto an Einstein ring distort the image

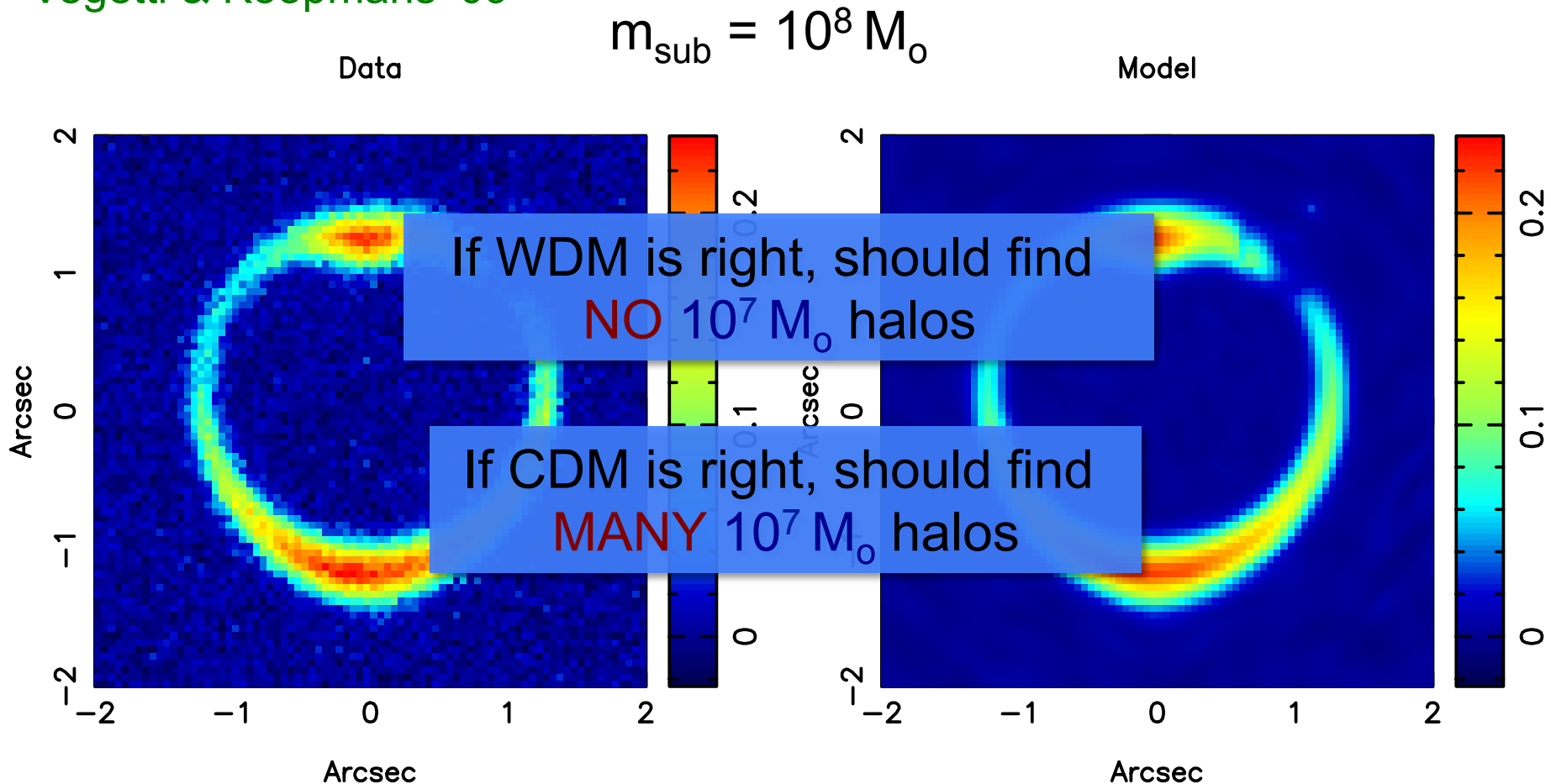


Vegetti & Koopmans '09



# Detecting substructures with strong lensing

Vegetti & Koopmans '09

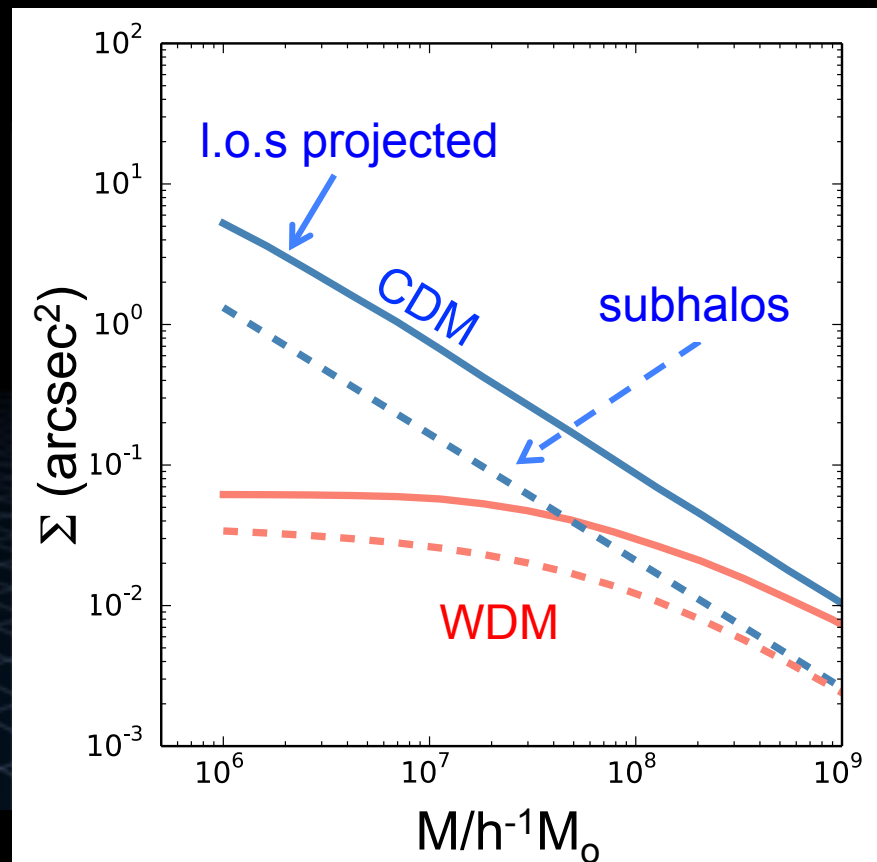
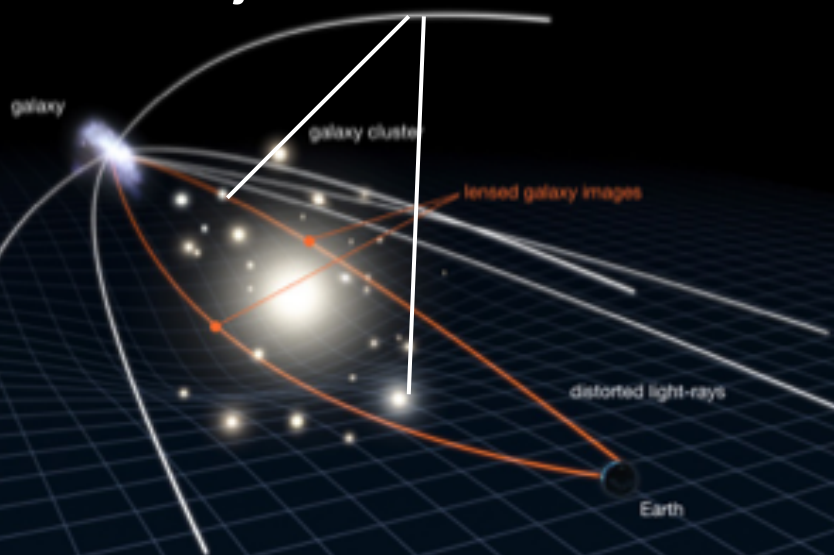


Can detect subhalos as small as  $10^7 M_{\odot}$

# Substructures vs interlopers

Subhalos & halos projected along the l.o.s both lens: who wins?

Projected l.o.s halos

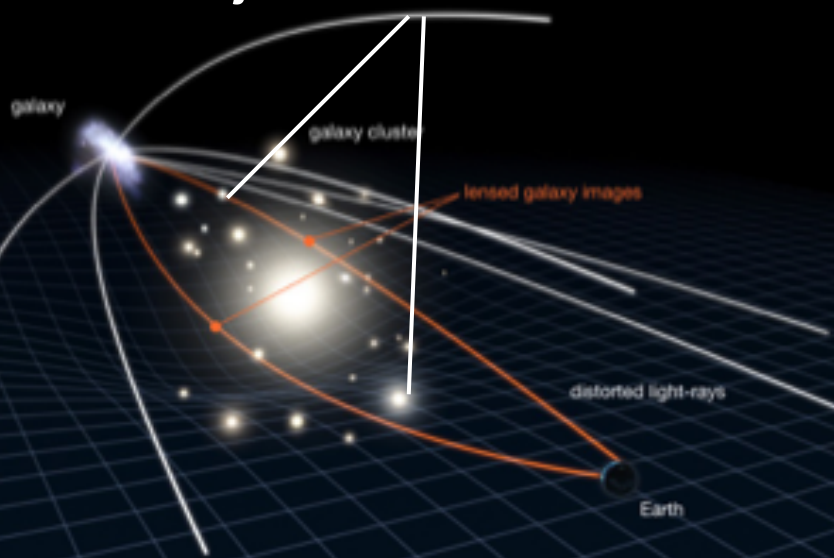


The number of line-of-sight haloes is larger than that of subhaloes

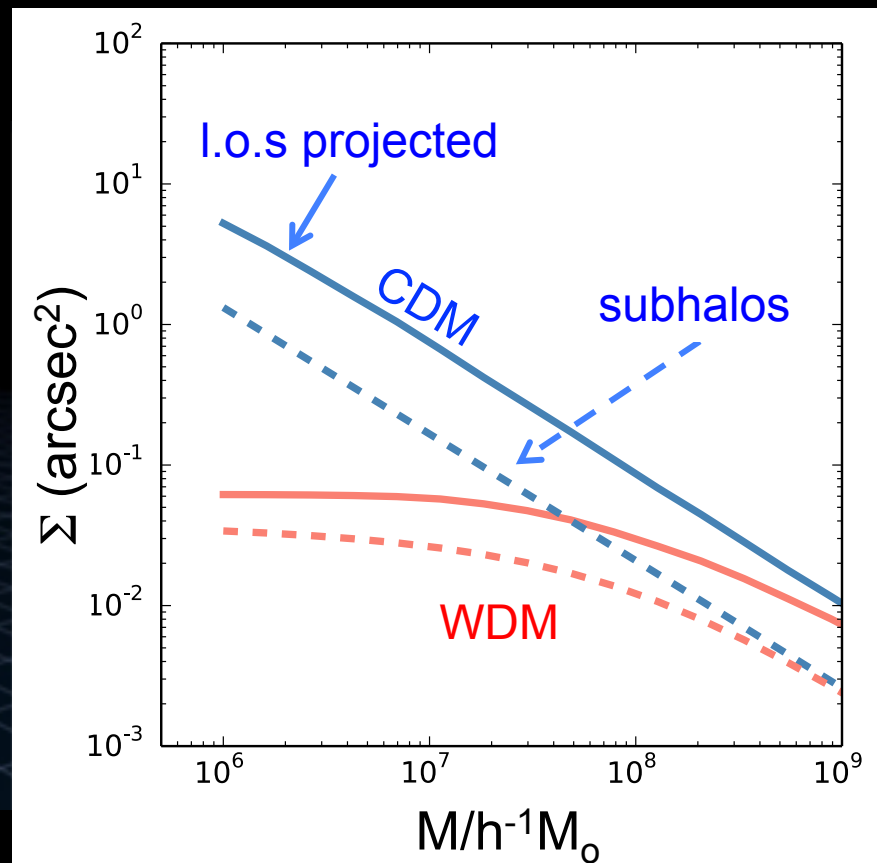
# Substructures vs interlopers

Subhalos & halos projected along the l.o.s both lens: who wins?

Projected l.o.s halos



Li, CSF et al. '16



→ This is the **cleanest** possible **test**: it depends **ONLY** on the **small-mass** end of the “**field**” halo mass function which we know how to calculate and is **unaffected by baryons**



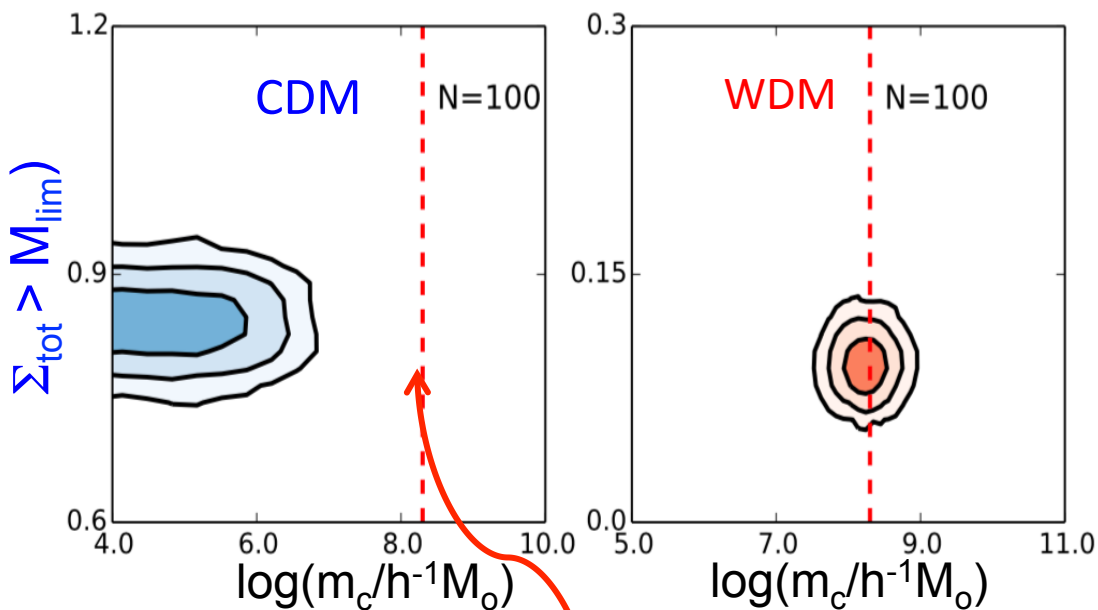
# Detecting substructures with strong lensing

$\Sigma_{\text{tot}}$  = projected halo number density within Einstein ring

$m_c$  = halo cutoff mass

100 Einstein ring systems and detection limit:  $m_{\text{low}} = 10^7 h^{-1} M_\odot$

Detection limit =  $10^7 h^{-1} M_\odot$



$m_c$  = halo cutoff mass

$m_c = 1.3 \times 10^8 h^{-1} M_\odot$  for coldest 7 keV sterile neutrino

- If DM is 7 keV sterile  $\nu \rightarrow$  **exclude** CDM at  $\gg \sigma$ !
- If DM is CDM  $\rightarrow$  **exclude** 7 keV sterile  $\nu$  at  $\gg \sigma$



# Conclusions

Five tests of  $\Lambda$ CDM using subhalos

... of which **only one** is **conclusive** and **possible**

1. The satellite luminosity function: **OK for CDM & WDM**
2. Too-big-to-fail: **OK for CDM & WDM**
3. Core/cusp: no evidence for cores but can be produced by baryon effects: **OK for CDM & WDM**
4.  $\gamma$ -ray annihilation radiation: **potentially conclusive**
5. Distortions of strong gravitational lenses: **conclusive & possible**, but involves **l.o.s halos**, not subhalos