

A conclusive test of cold dark matter

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1980s



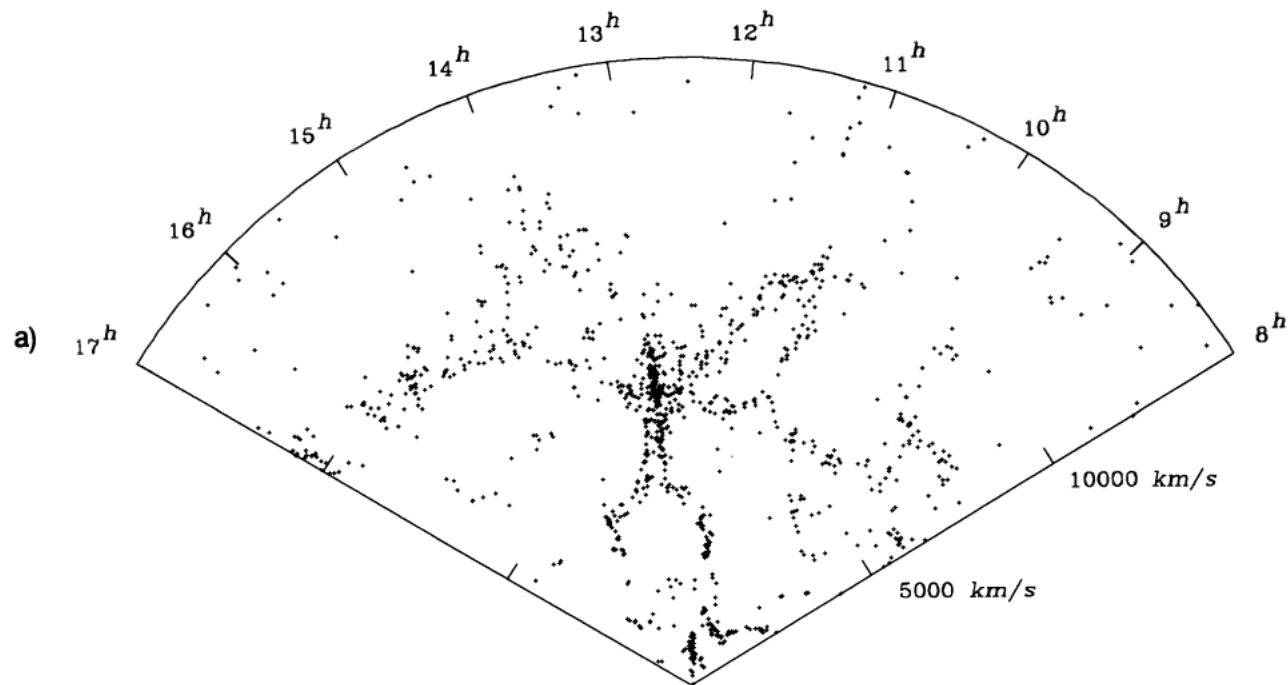
2020s



1980s

DE LAPPARENT, GELLER, AND HUCHRA

Vol. 302



The CfA redshift survey

2020s

Galaxy distribution encodes info about dark matter and dark energy

5 billion yrs

DESI already has > 10 million spectra

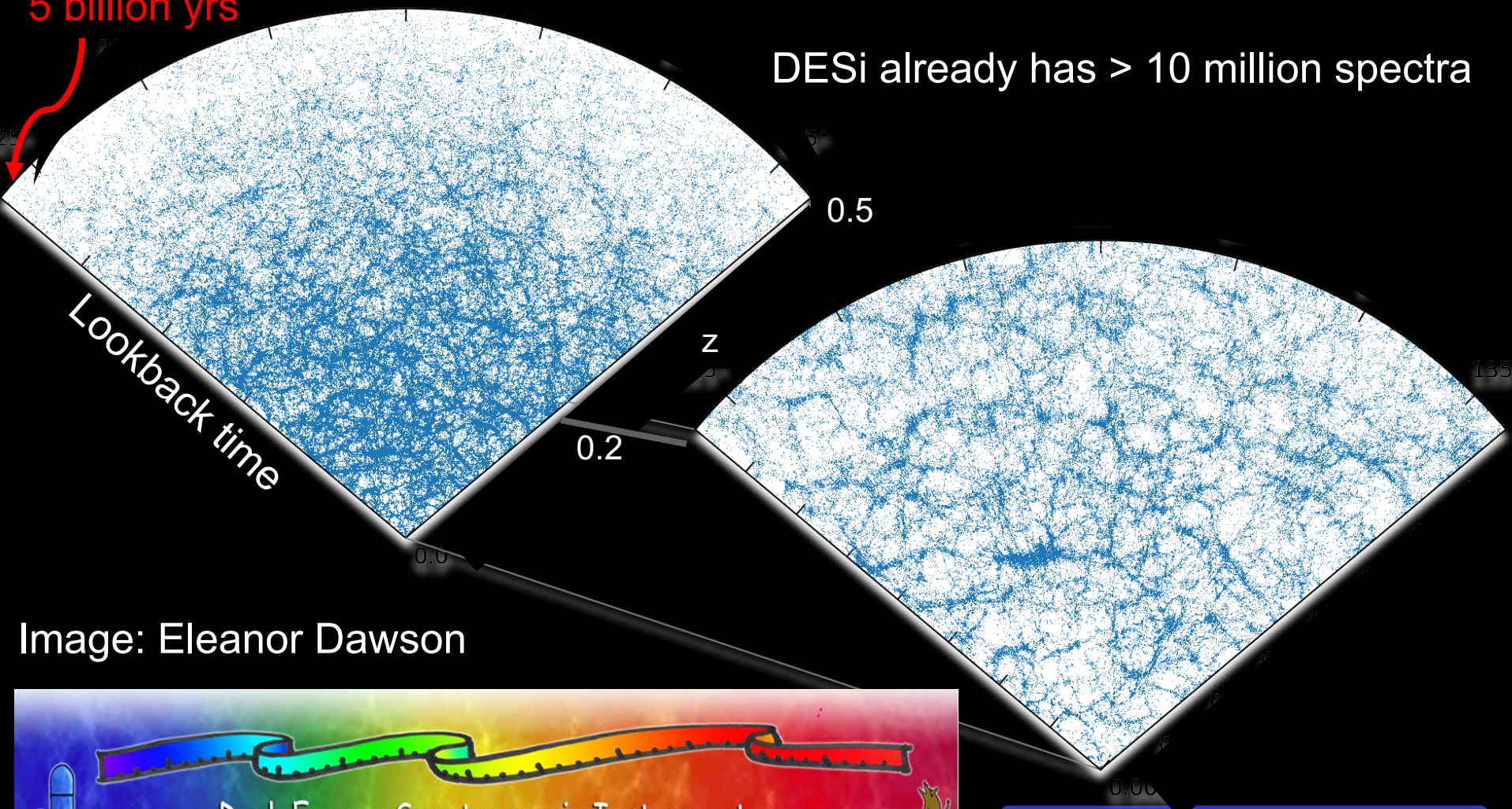
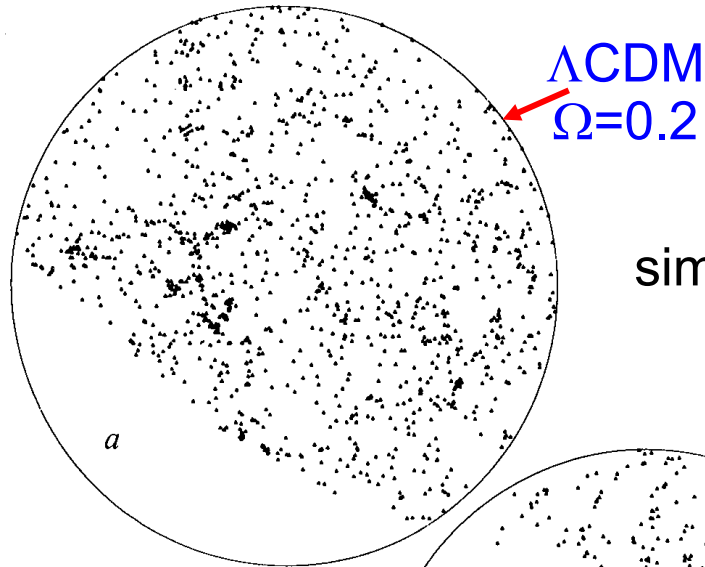


Image: Eleanor Dawson

Dark Energy Spectroscopic Instrument

1980s

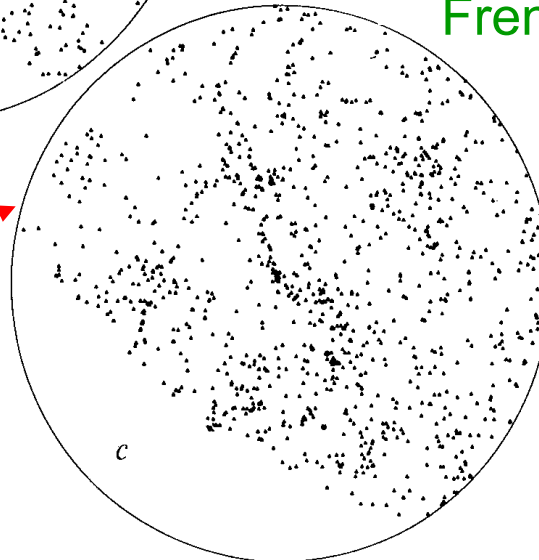
The Λ CDM cosmology



Early Λ CDM N-body
simulations \rightarrow realistic LSS

Davis, Efstathiou,
Frenk & White 1985

CfA redshift
survey



VIRGO

2020s

The properties of the dark matter distribution on all scales
is a solved problem in CDM

125 Mpc/h

31.25 Mpc/h

0.5 Mpc/h

Springel et al '05, '08,
Gao et al '11



STARS

NEUTRINOS

Neutrinos make
up $< 1\%$ of total
dark matter

Can simulate their
distribution with 1%
accuracy

DESI may be able to measure the mass of the neutrino

GAS

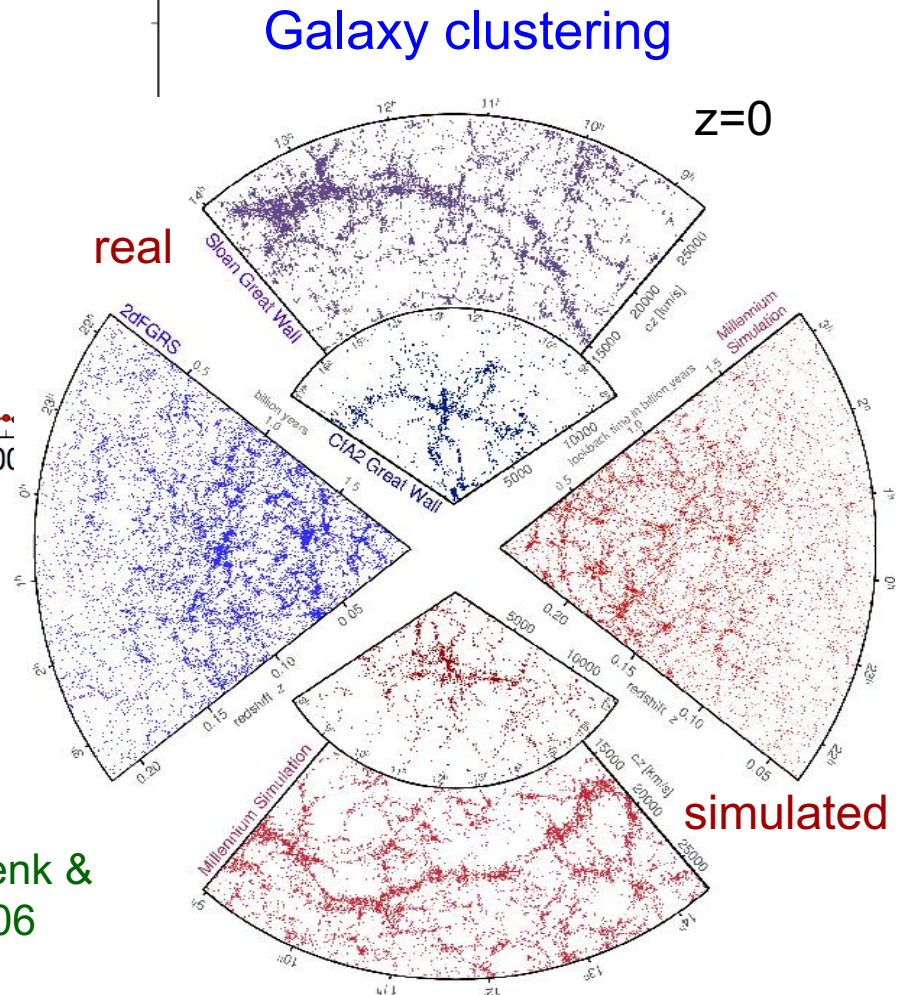
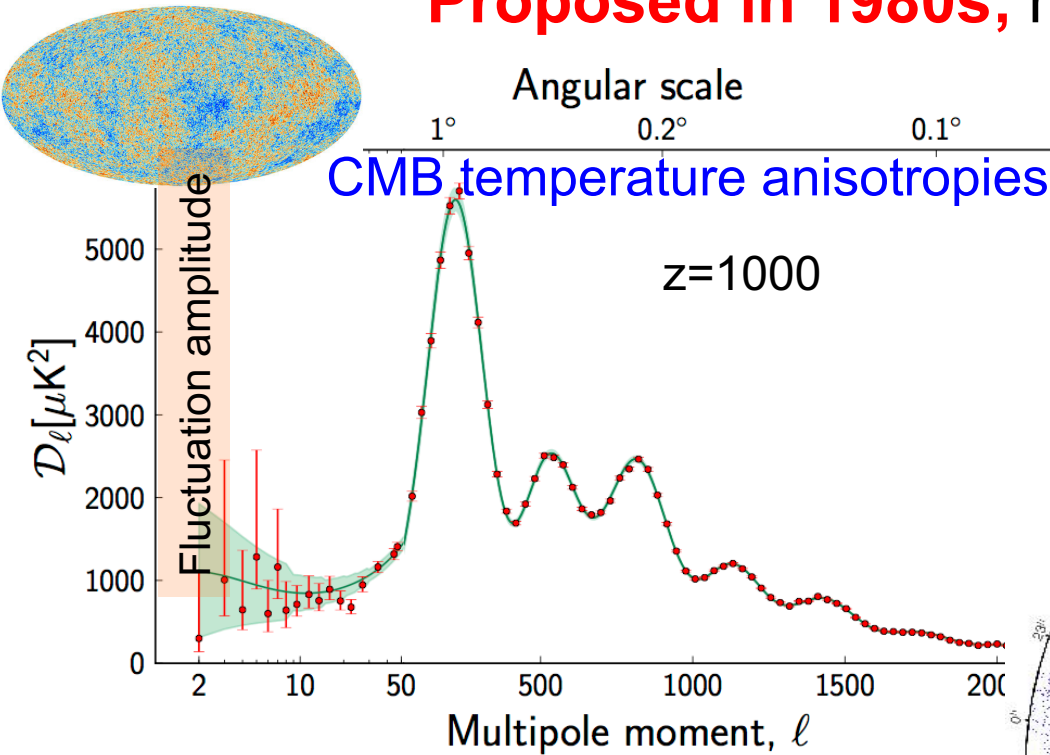
CDM

200 Mpc

Elbers, Frenk, Jenkins, Li,
Pascoli '23

The Λ CDM model of cosmogony

Proposed in 1980s; now empirically supported by:

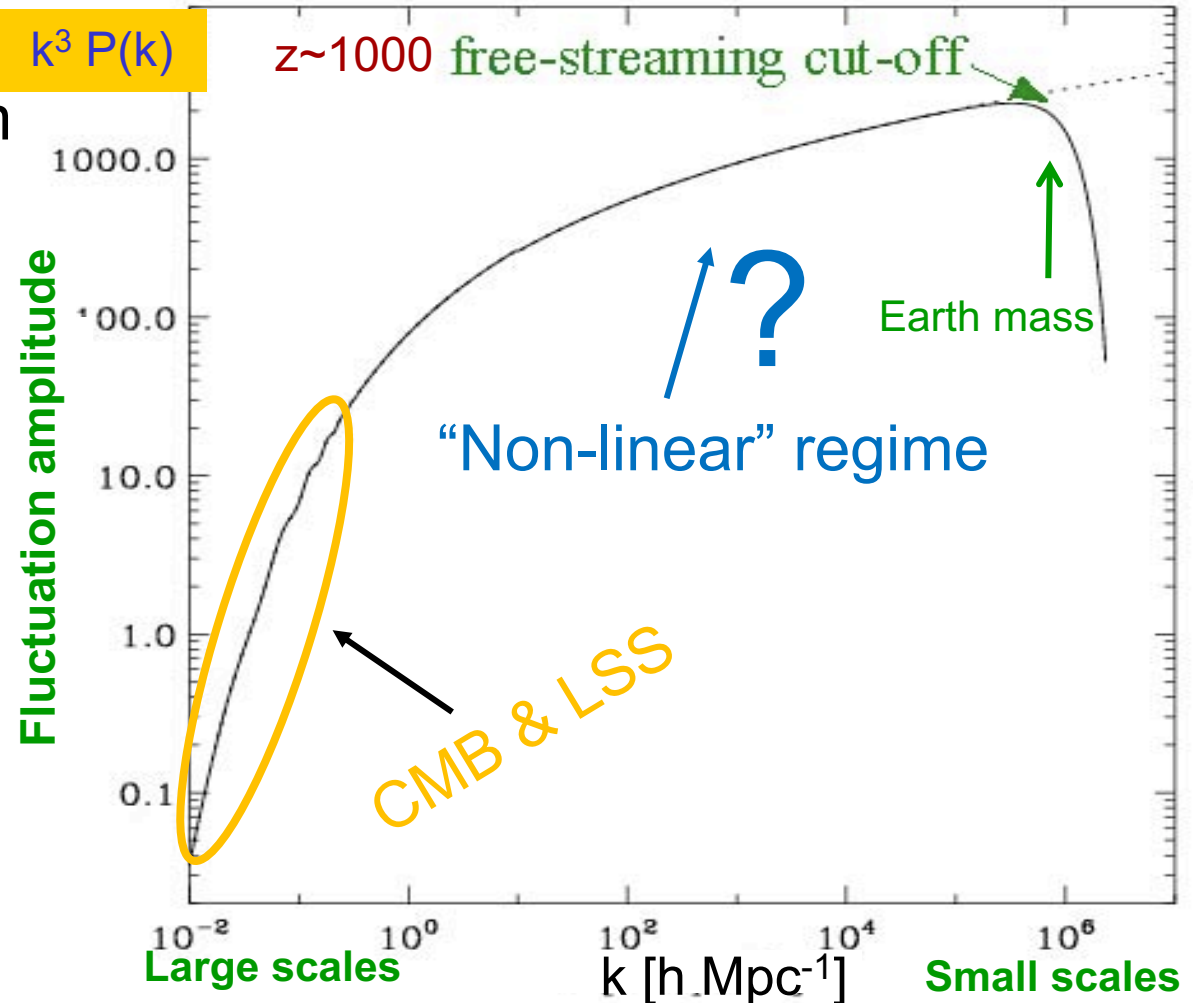


Springel, Frenk &
White 2006

The cold dark matter power spectrum

Linear power spectrum
("power per octave")

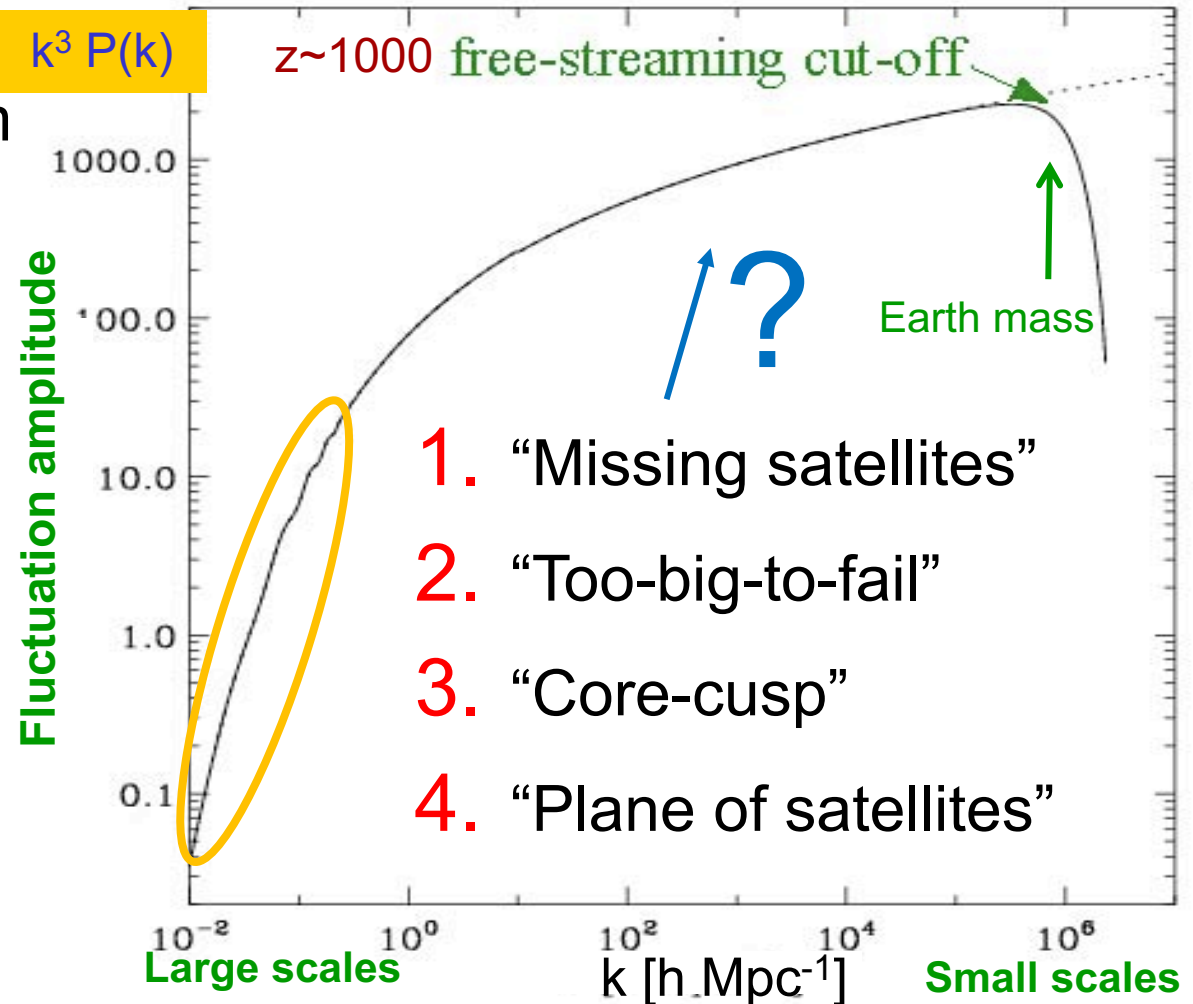
Assumes a 100GeV wimp
Green et al '04



The cold dark matter power spectrum

Linear power spectrum
("power per octave")

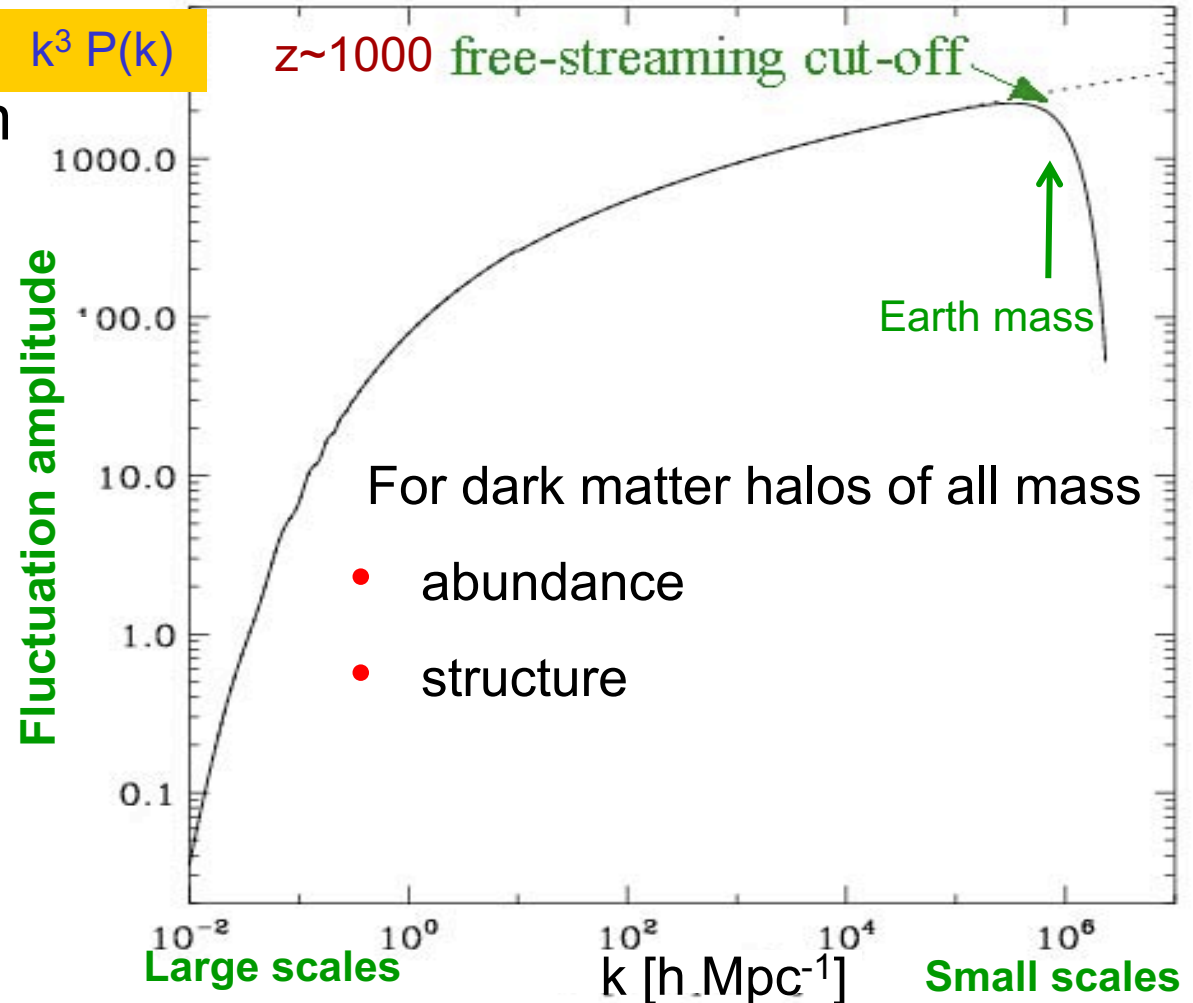
Assumes a 100GeV wimp
Green et al '04



The cold dark matter power spectrum

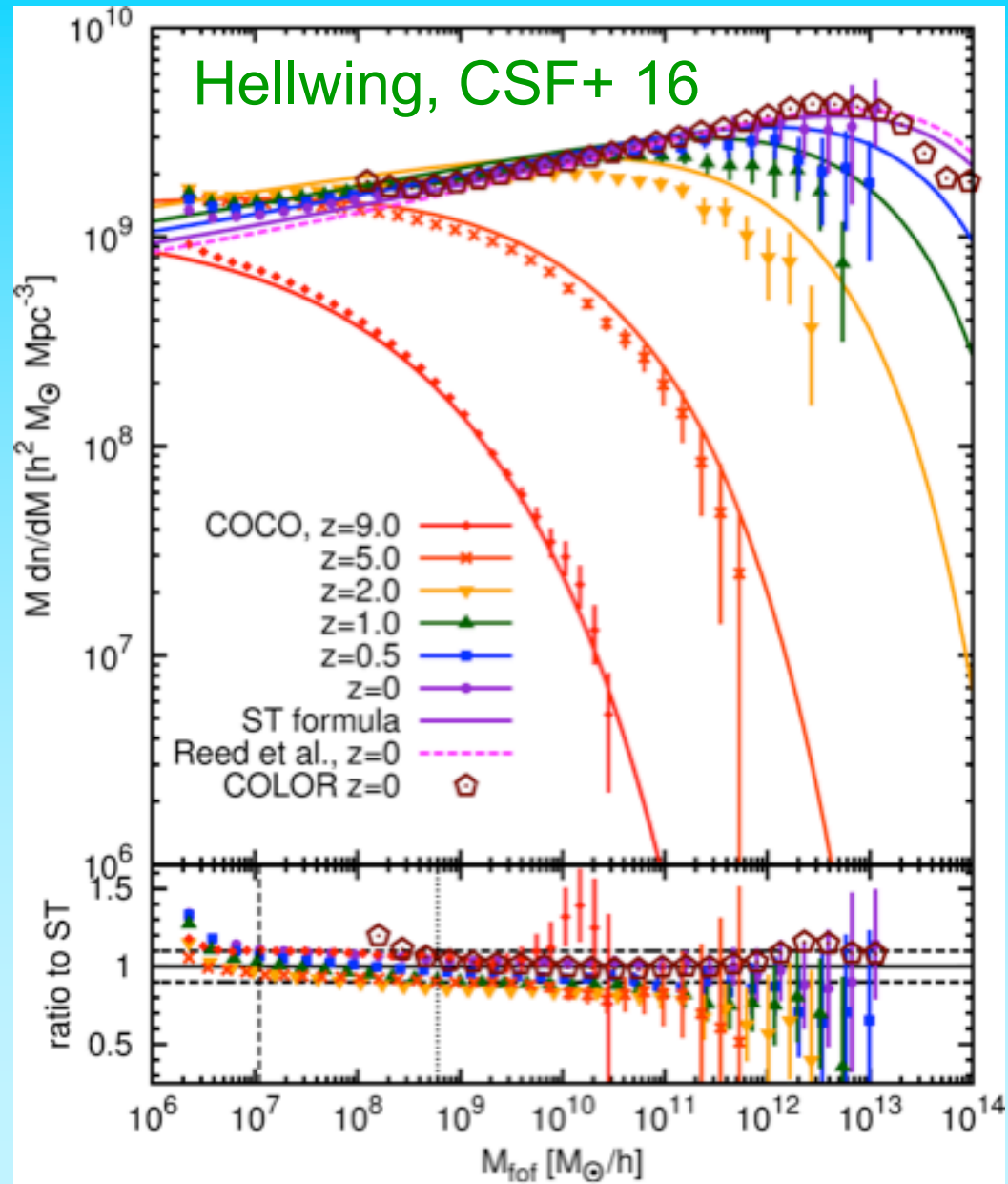
Linear power spectrum
(“power per octave”)

Assumes a 100GeV wimp
Green et al '04

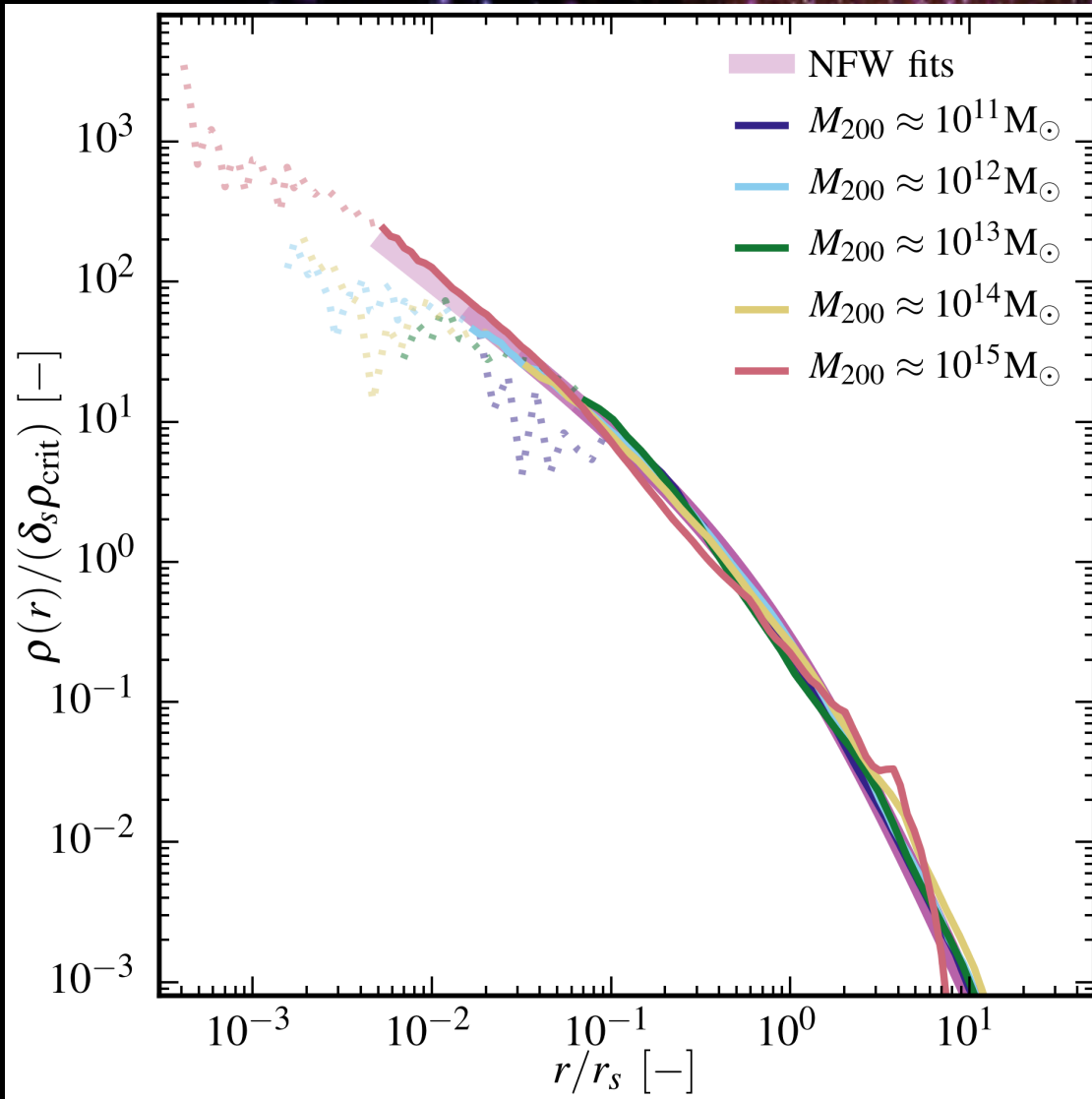


The halo mass function

Until recently, halo mass function known from
 $10^6 - 10^{15} M_{\odot}$
 from hi-z to $z=0$



The density profile of cold dark matter halos



Shape of halo profiles
~independent of halo mass &
cosmological parameters

Density profiles are “cuspy” –
no ‘core’ near the centre

Fitted by simple formula:

$$\frac{\rho(r)}{\rho_{\text{crit}}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

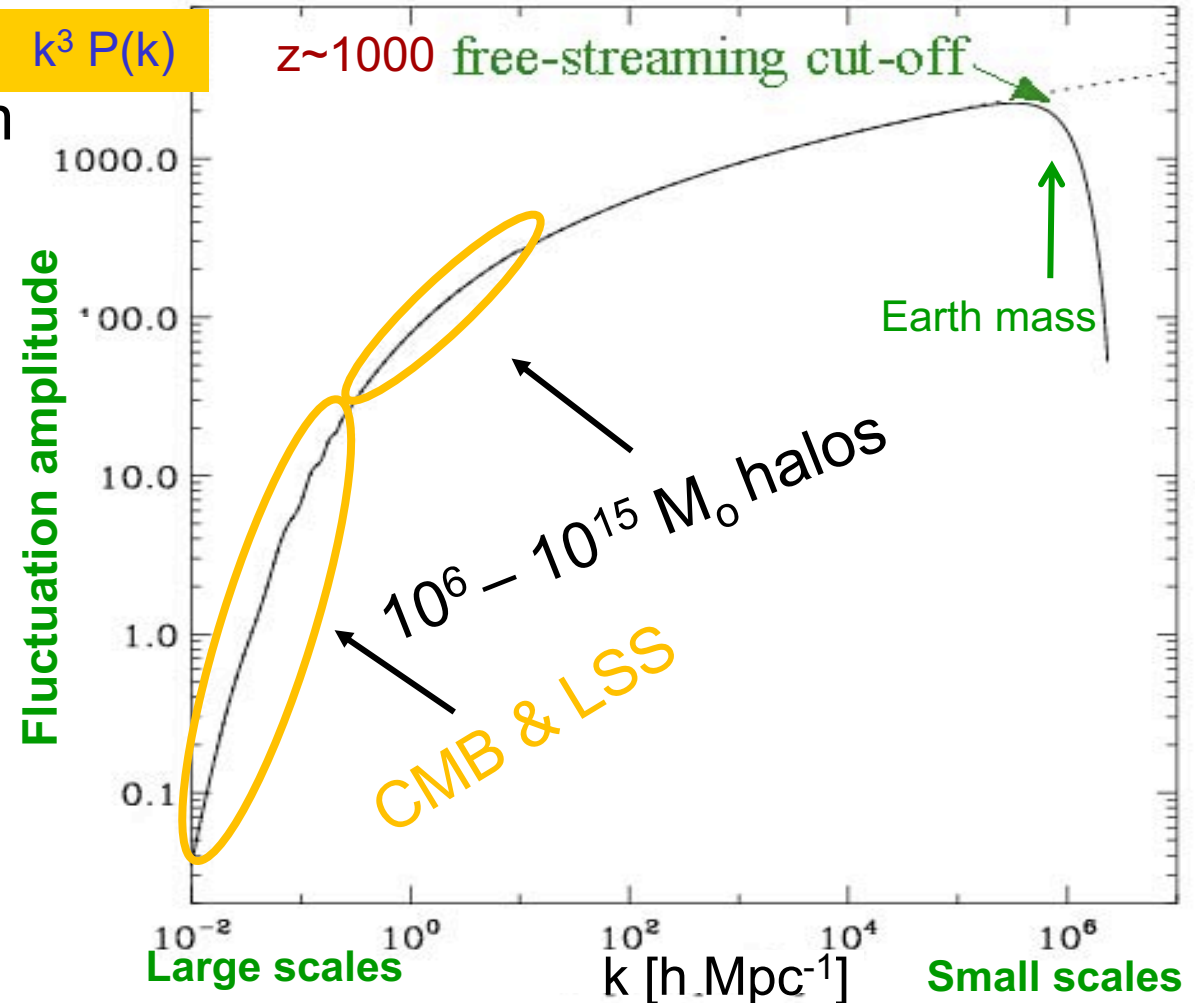
(Navarro, Frenk & White '97)

More massive halos and
halos that form earlier have
higher densities (bigger δ)

The cold dark matter power spectrum

Linear power spectrum
("power per octave")

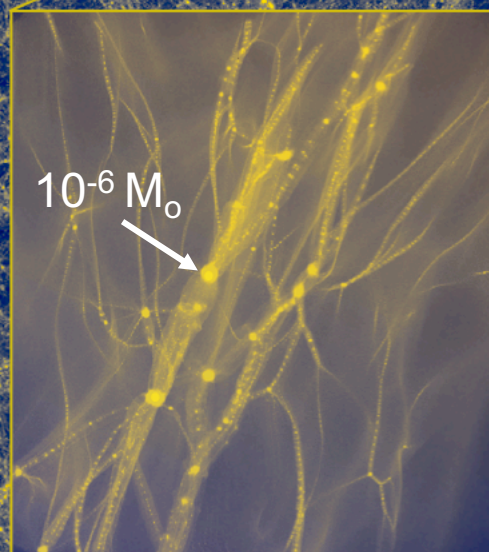
Assumes a 100GeV wimp
Green et al '04





The number of
dark matter
halos from
Earth mass to
clusters

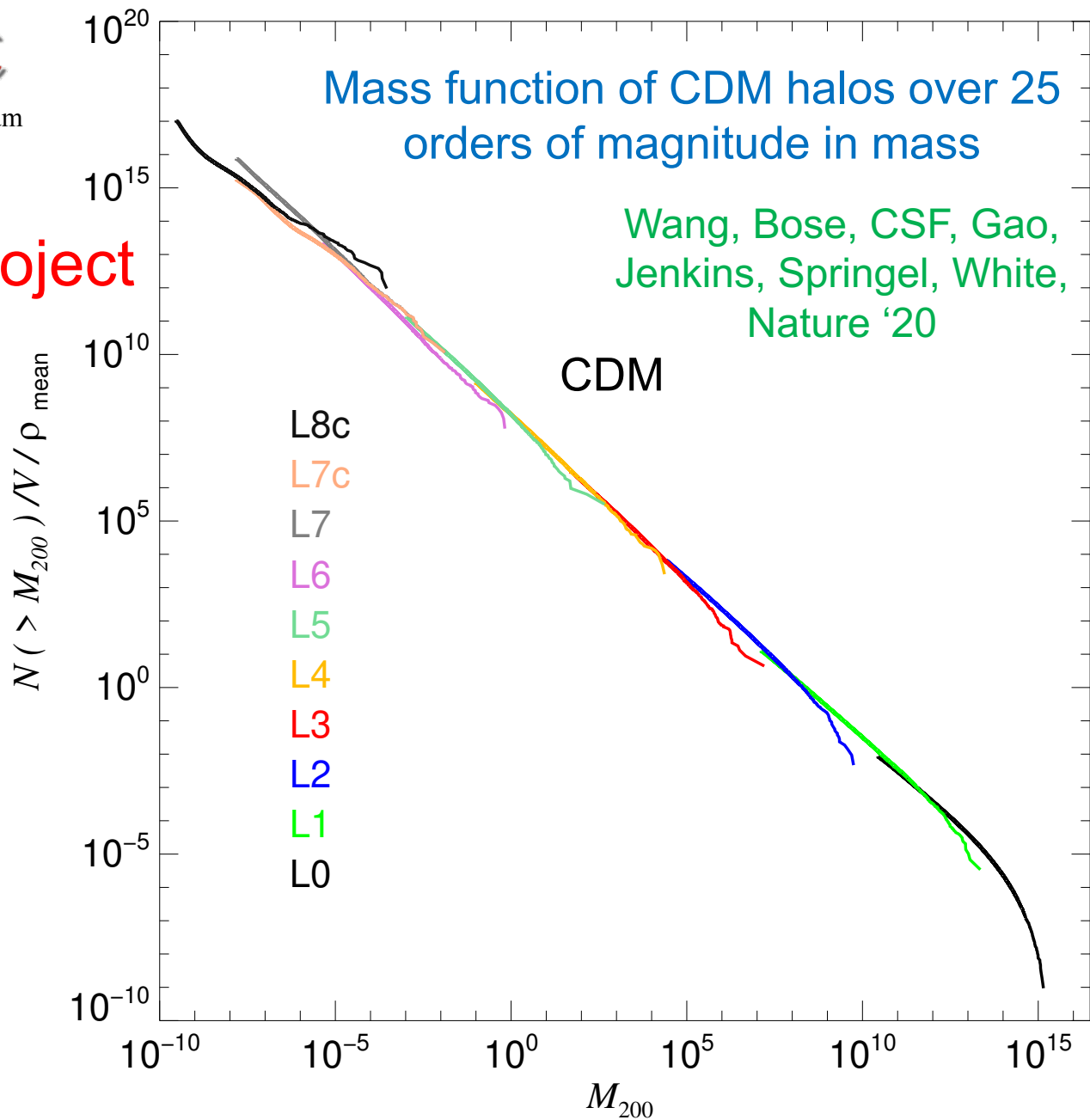
Successive
resimulations of
“void” regions at
increasing
resolution



200 pc

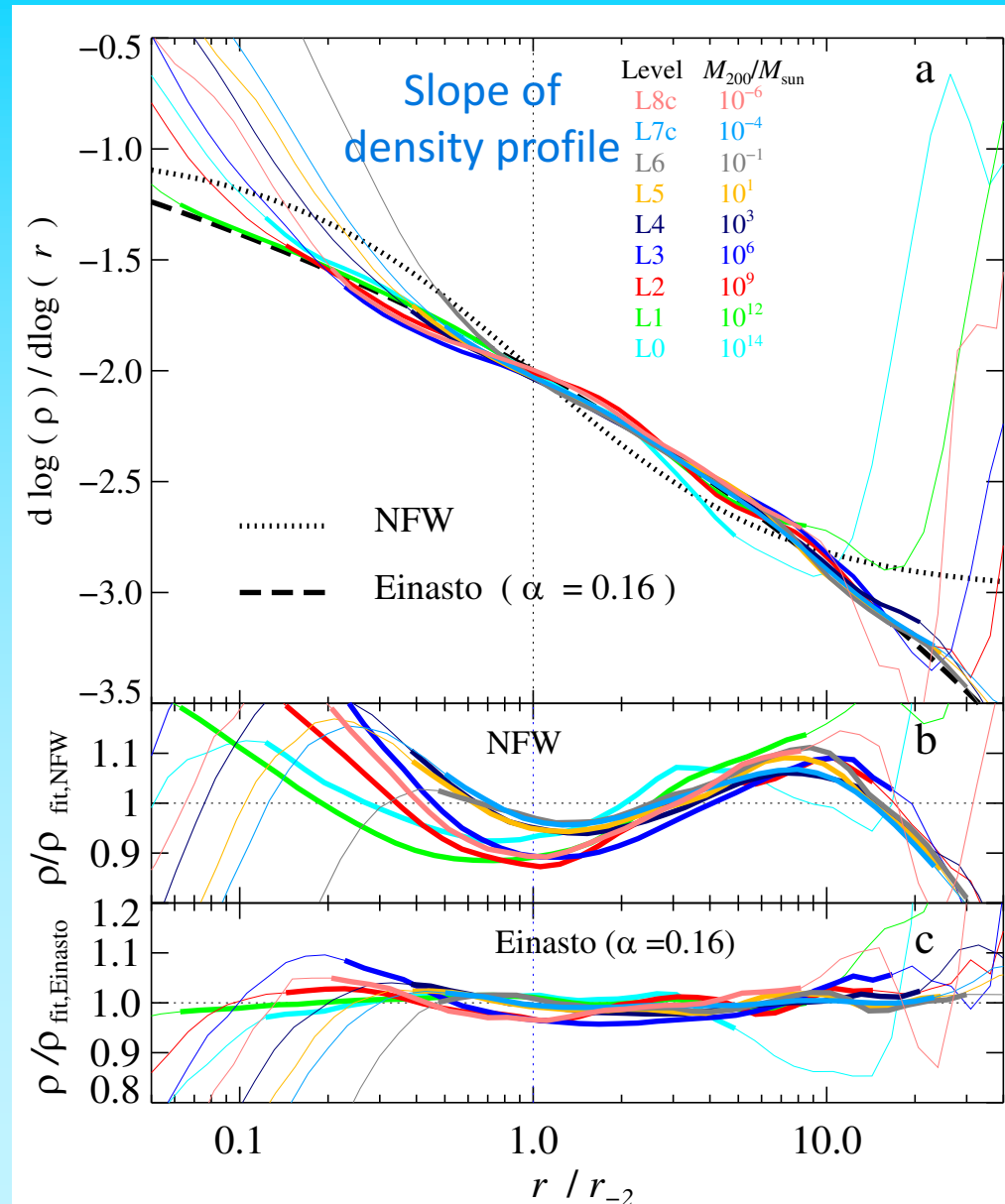
Wang, Bose, CSF,
Gao, Jenkins,
Springel, White,
Nature '20

The VVV project



Density profile shapes

Over **20 orders** of magnitude in halo **mass** and 4 orders of magnitude in density, the mean density **profiles** of halos are **fit** by **NFW** to within **20%** and by **Einasto** ($\alpha = 0.16$) to within **7%**





We know abundance & structure of halos of ALL masses
How many make a galaxy?



Flammarion 1888: tete des etoiles

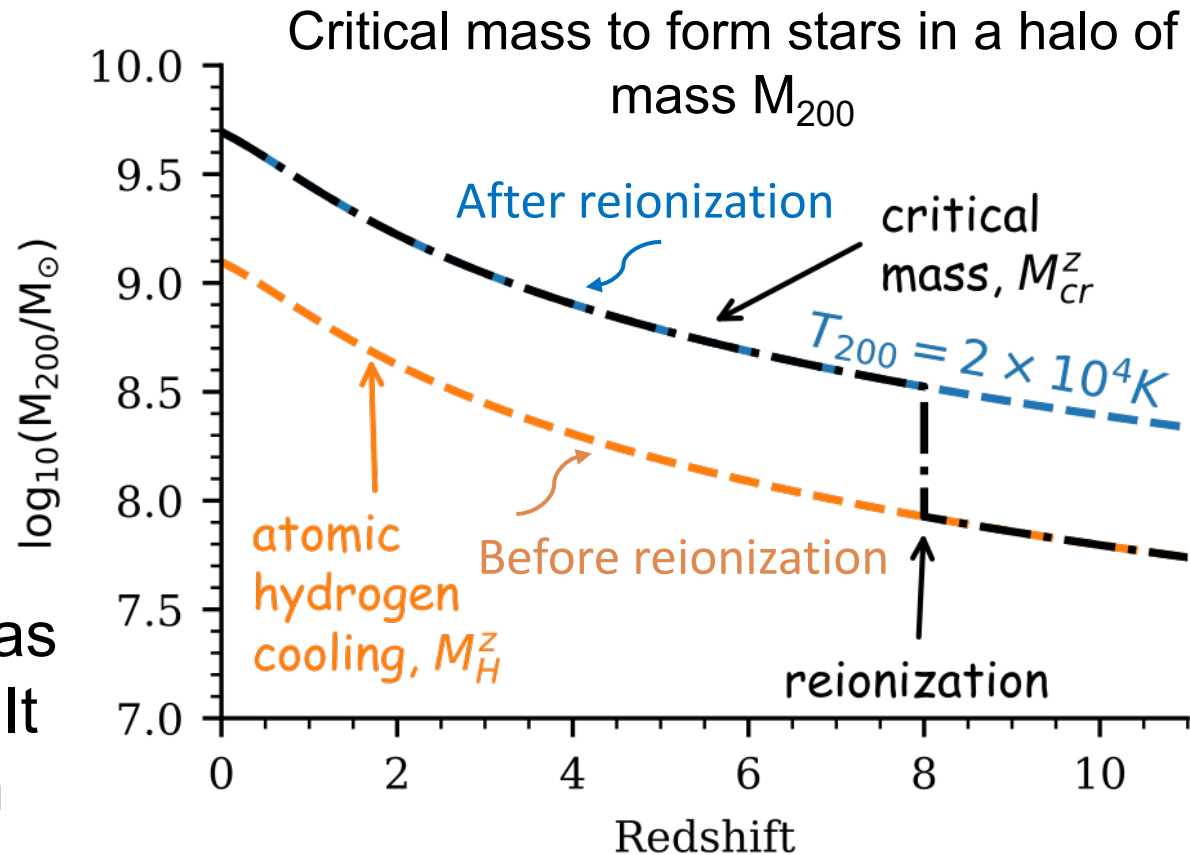
A galaxy formation primer

1. Before reionization, stars can only form if atomic H cooling is effective: $\rightarrow T > 7000 \text{ K}$

$$M_H^z \sim (4 \times 10^7 M_\odot) \left(\frac{1+z}{11} \right)^{-3/2}$$

2. After H reionization, gas is heated to $T = 2 \times 10^4 \text{ K}$. It can only cool and form stars in halos with:

$$T_{\text{vir}} > T_{\text{IGM}} = 2 \times 10^4 \text{ K}$$

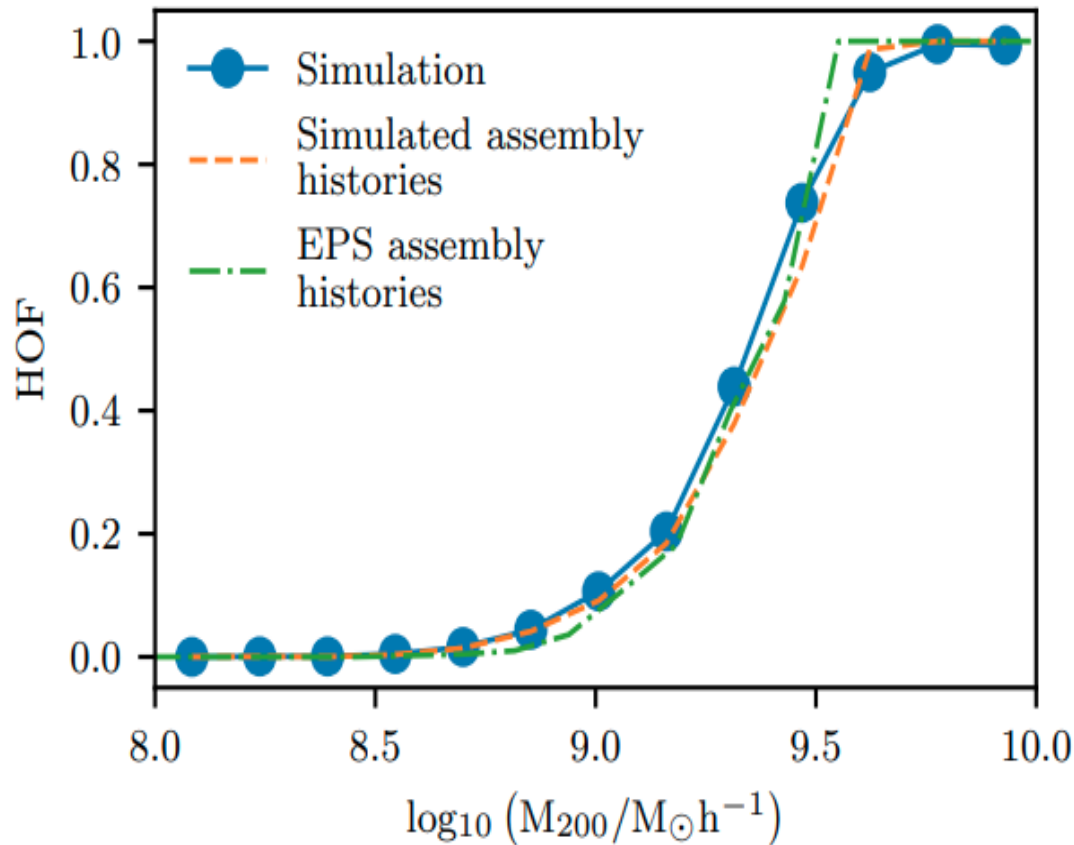


Benitez-Llambay & CSF '20

A galaxy formation primer

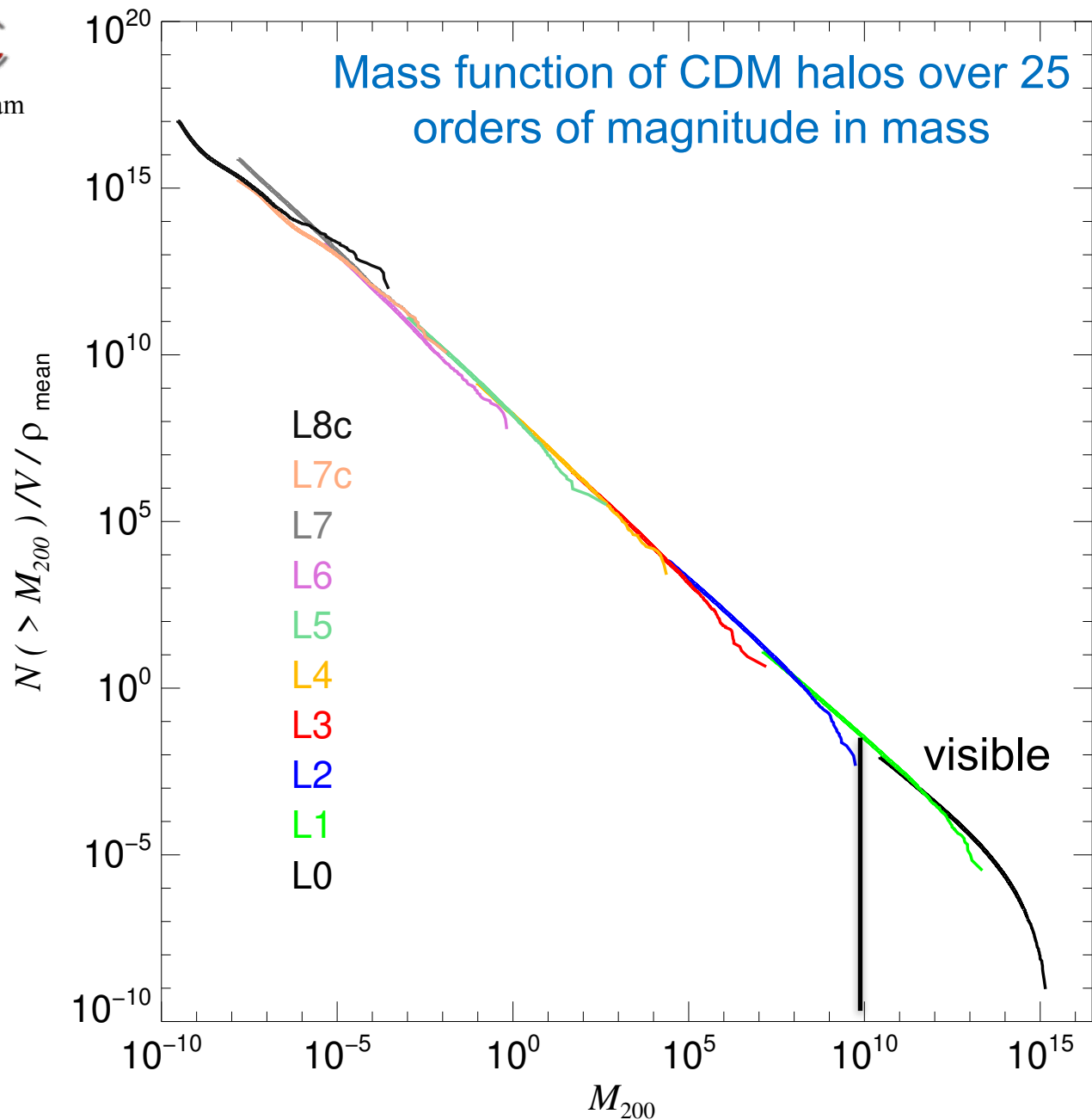
Halo Occupation Fraction (HOF): fraction of halos of a given mass today that host a galaxy

fraction of halos that host a galaxy



$M < 3 \times 10^8 M_{\odot}$
 \rightarrow dark

$M > 3 \times 10^9 M_{\odot}$
 \rightarrow visible



The small-scale “crisis” of CDM

1. “Missing satellites”
2. “Too-big-to-fail”
3. “Core-cusp”
4. “Plane of satellites”



CDM

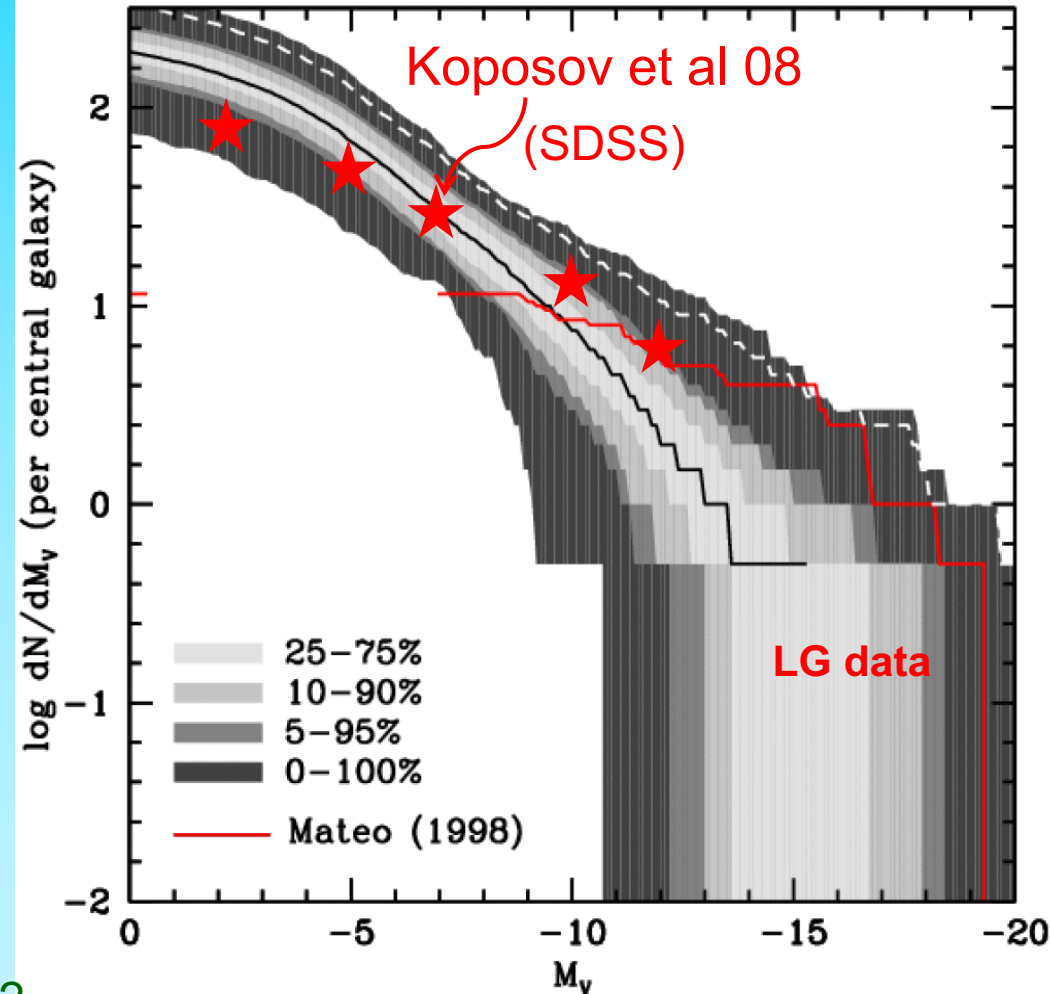
DM-only CDM simulations predict many more subhalos in the Milky Way than there are observed satellites

“Missing satellites” problem

Most subhalos never make a galaxy!

Luminosity Function of Local Group Satellites

- Median model → correct abund. of sats brighter than $M_V = -9$ and $V_{\text{cir}} > 12$ km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare (~2% of cases)



Benson, Frenk, Lacey, Baugh & Cole '02
(see also Kauffman et al '93, Bullock et al '01)



$$V_c = \sqrt{\frac{GM}{r}}$$

$$V_{\max} = \max V_c$$

The satellites of the MW



CDM has ~ 10 subhalos with $V_{\text{max}} > 30$ km/s

MW has only 3 satellites
with $V_{\text{max}} > 30$ km/s
(LMC, SMC, Sgr)

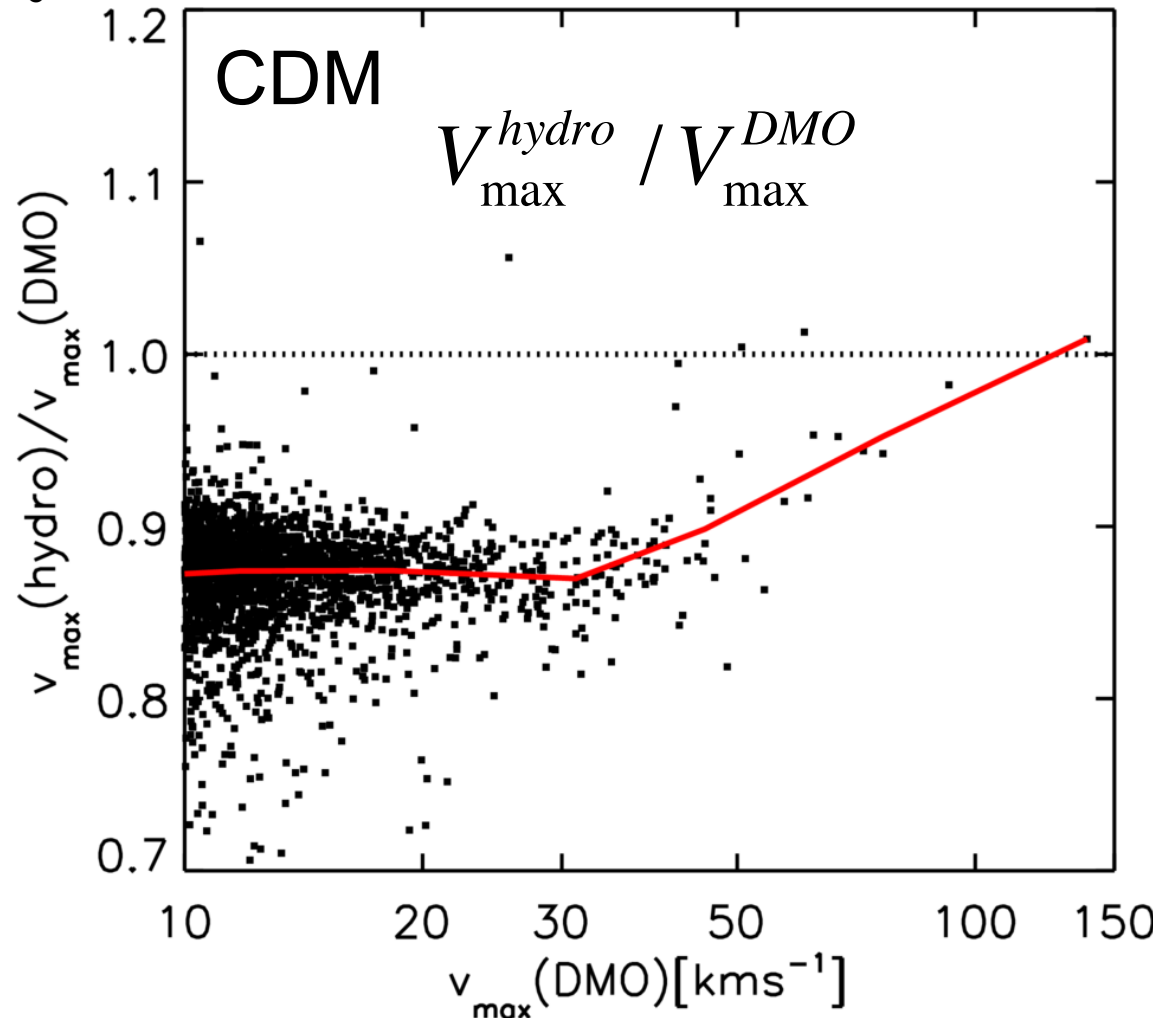
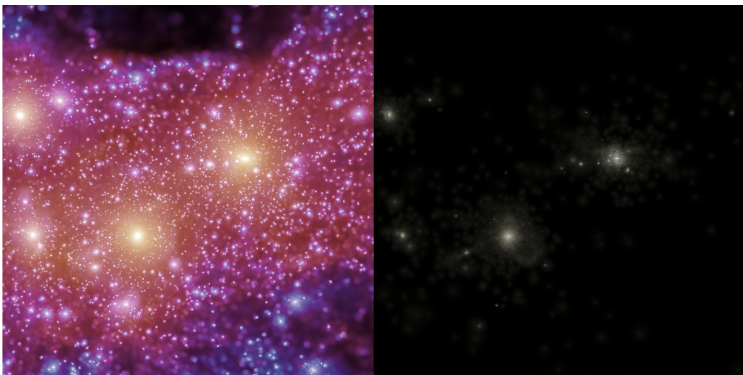
Why did these not make a galaxy?

Too-big-to-fail in CDM: baryon effects

$$V_c = \sqrt{\frac{GM}{r}} \quad V_{\max} = \max V_c$$

Reduction in V_{\max} due to
SN feedback:

→ Lowers halo mass &
thus halo growth rate



Sawala, CSF et al. '13, '15

The core/cusp “problem”

DMO simulations predict
NFW profiles

But some galaxies are
inferred to have cores

The core/cusp “problem”

DMO simulations predict
NFW profiles

Cusps → cores

Perturb central halo region
by growing a galaxy
adiabatically and removing
it suddenly (Navarro, Eke
& Frenk '96)

Cores may also form by
repeated fluctuations in central
potential (e.g. by SN
explosions) (Read & Gilmore
'05; Pontzen & Governato
'12, '14; Bullock & Boylan-
Kolchin '17)

Navarro, Eke & Frenk (1996)

The cores of dwarf galaxy haloes L75

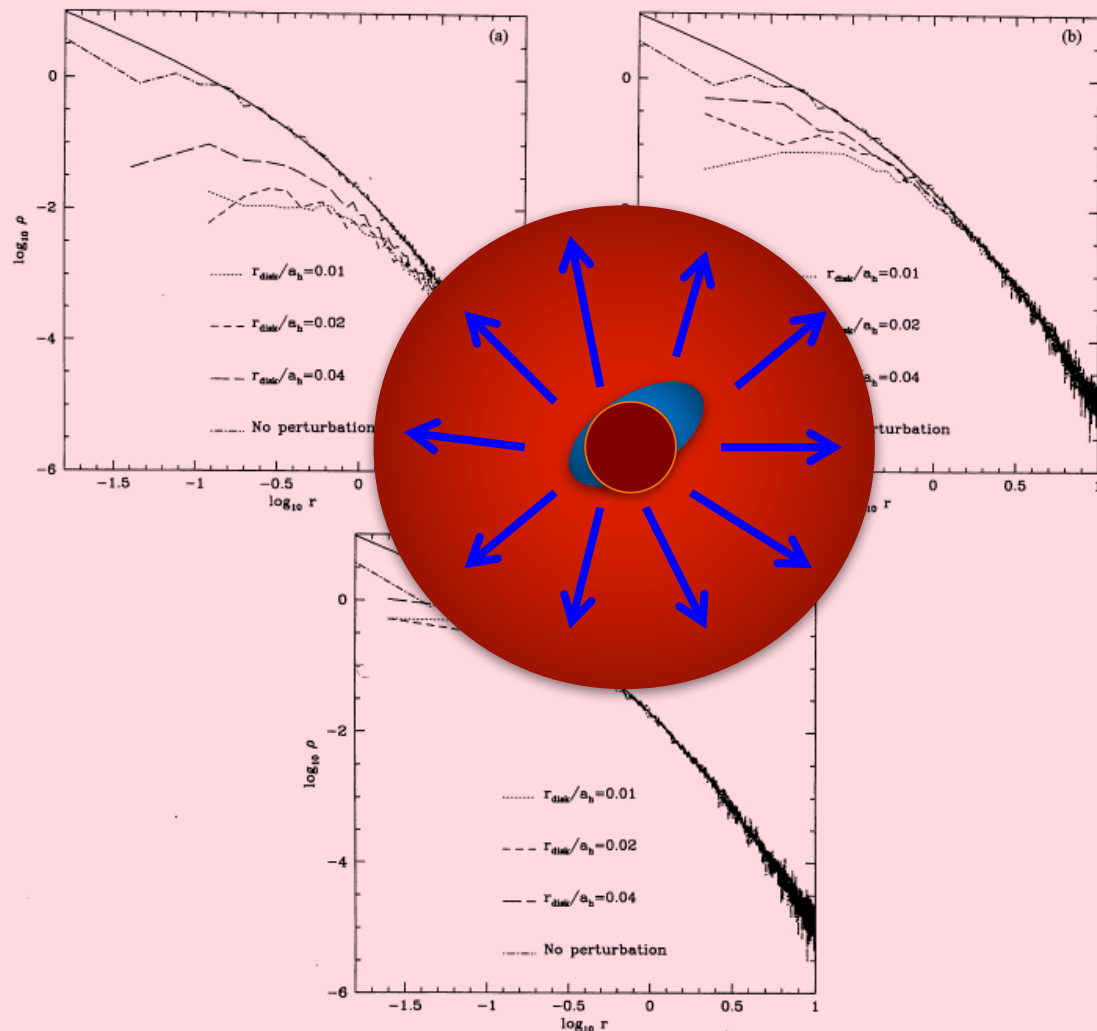
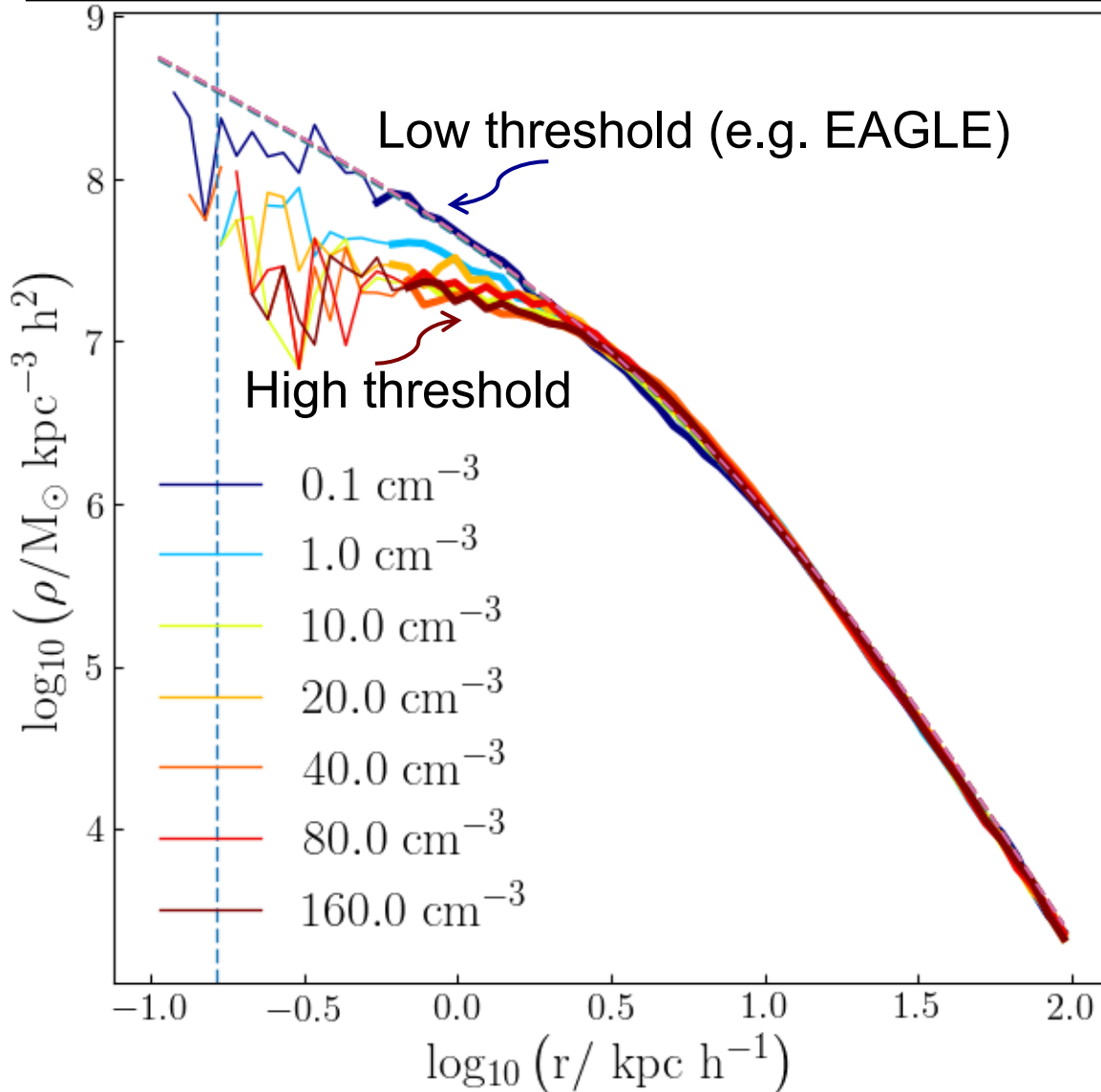


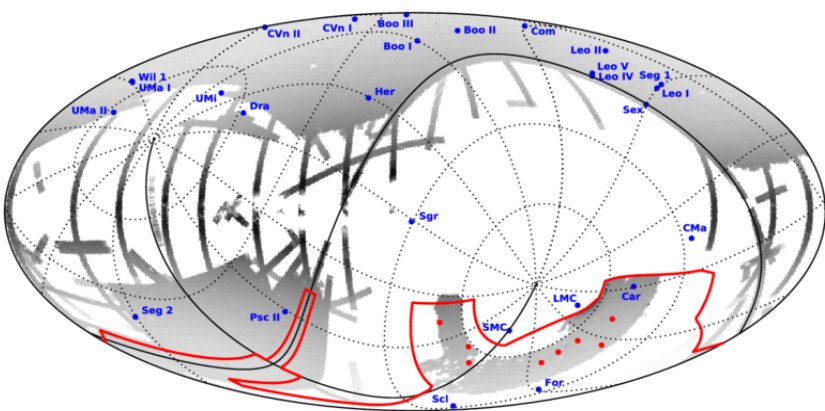
Figure 3. Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10,000-particle realization of the Hernquist model run in isolation at $t=200$. (a) $M_{\text{disc}}=0.2$. (b) $M_{\text{disc}}=0.1$. (c) $M_{\text{disc}}=0.05$.

Cores or cusps in simulations?

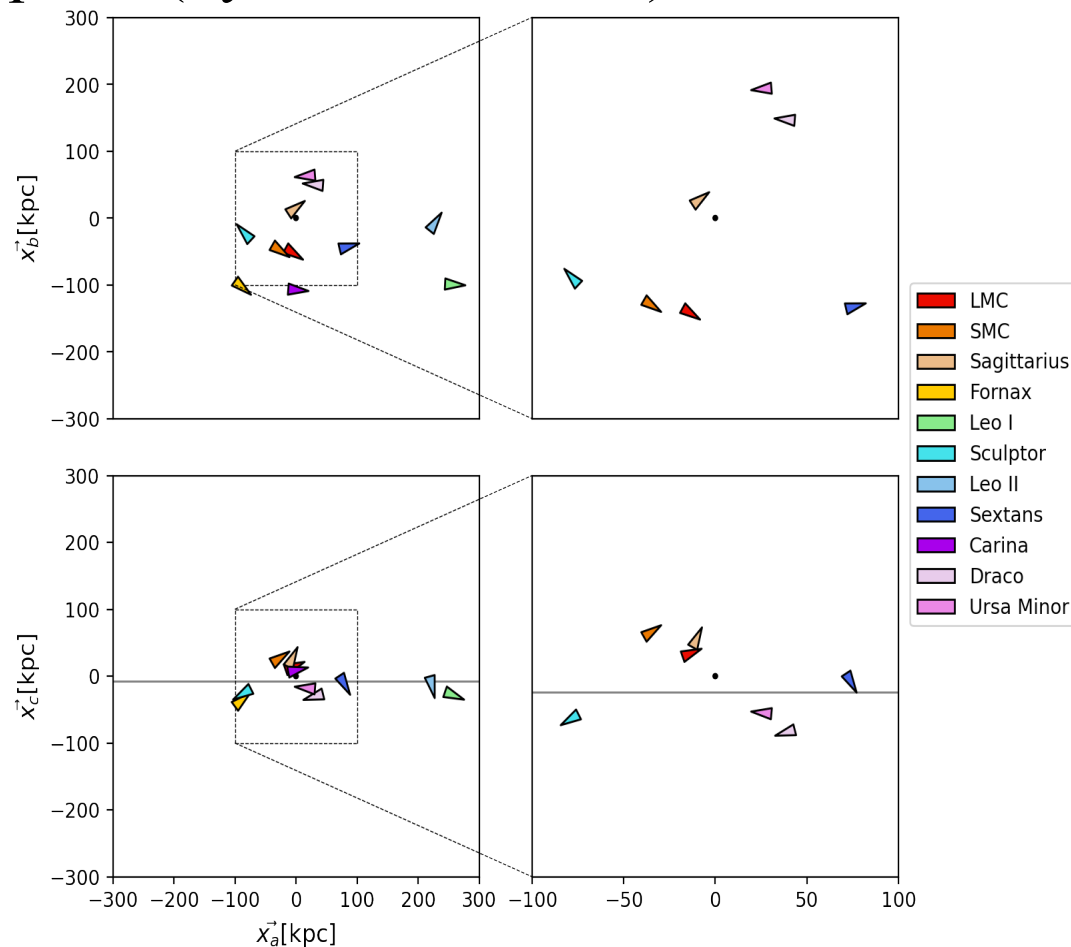


The plane of satellites in the MW

Problem: the 11 “classical” Milky Way satellites are in a thin, possibly rotating plane (Lynden-Bell 1976)



Bechtol+ 2015



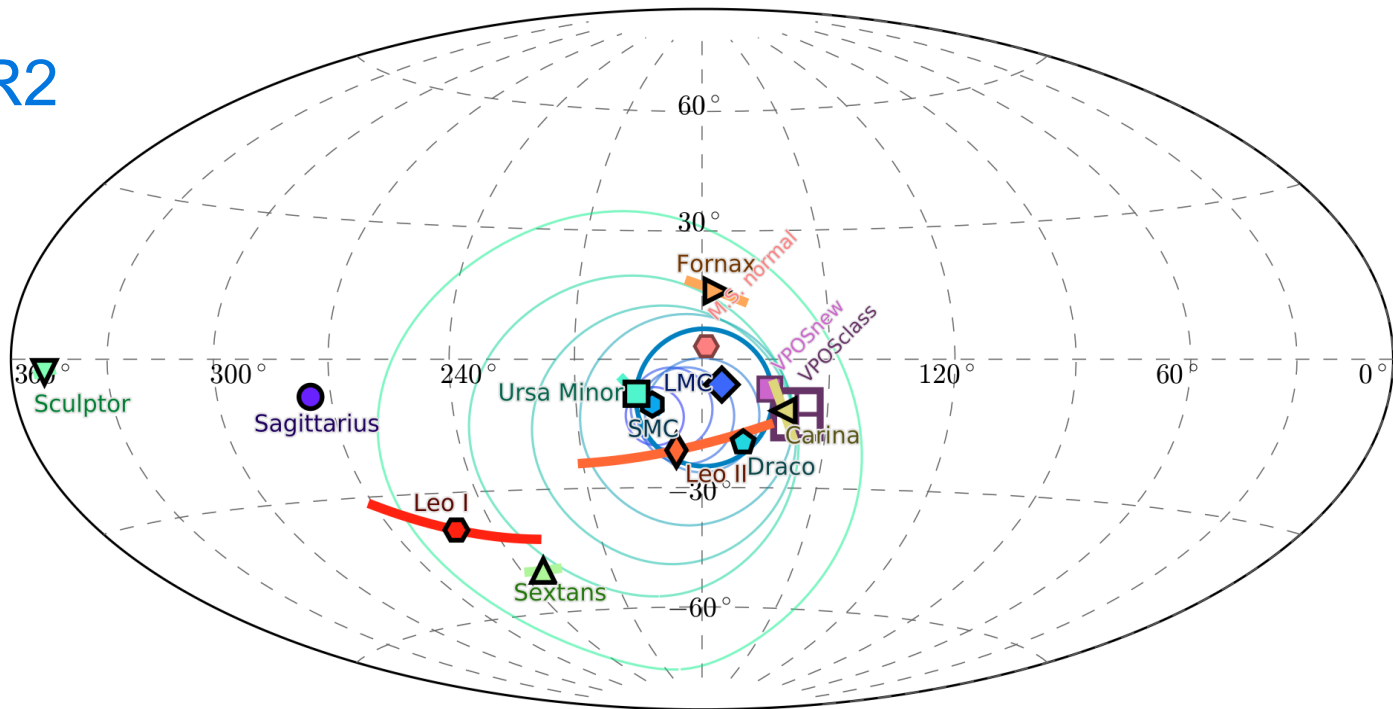
Sawala, Cautun, CSF et al '22

The plane of satellites in the MW

The plane could be a spinning disk

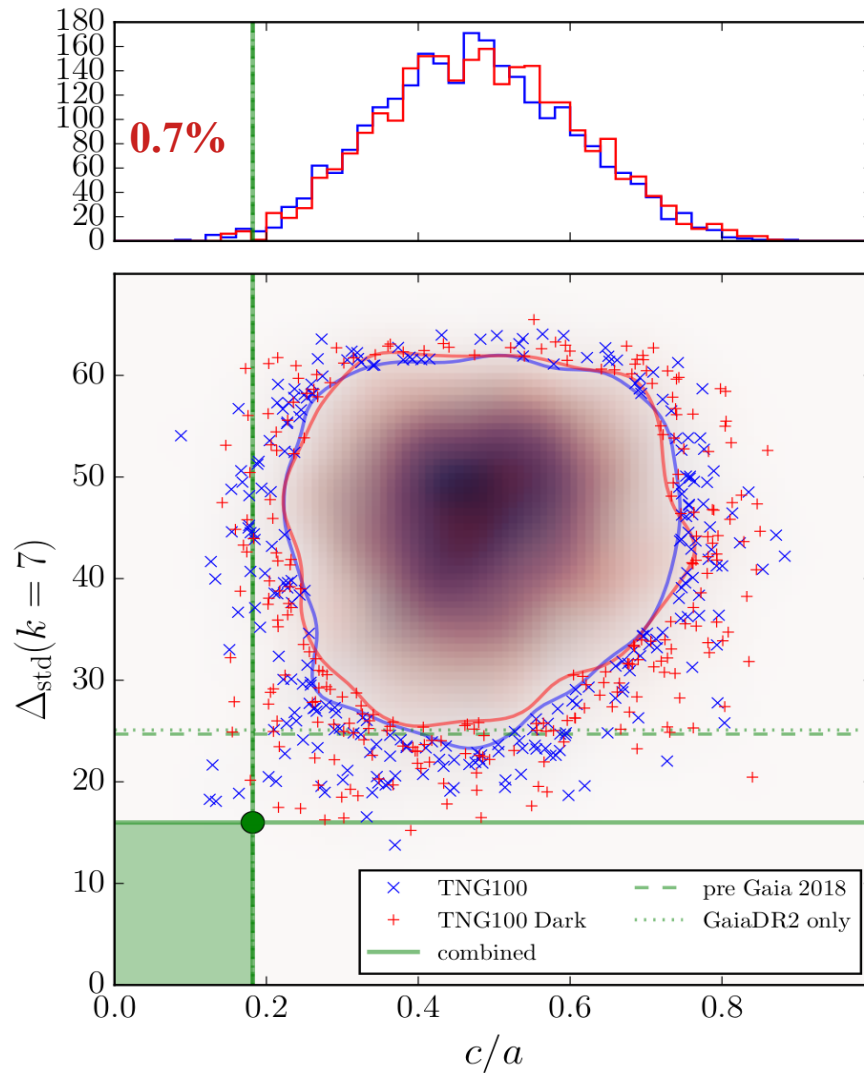
The orbital poles of 7 of the 11 satellites are clustered

GAIA DR2



Pawlowski & Kroupa (2020)

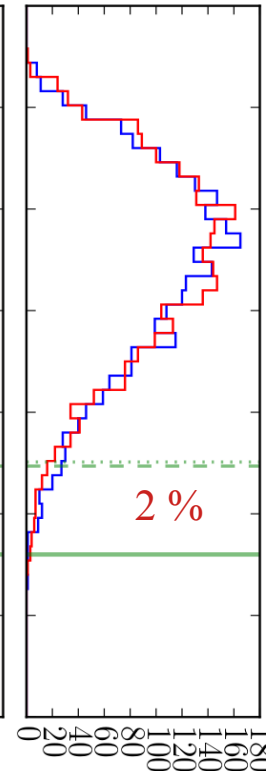
The plane of satellites in the MW



How rare is it?

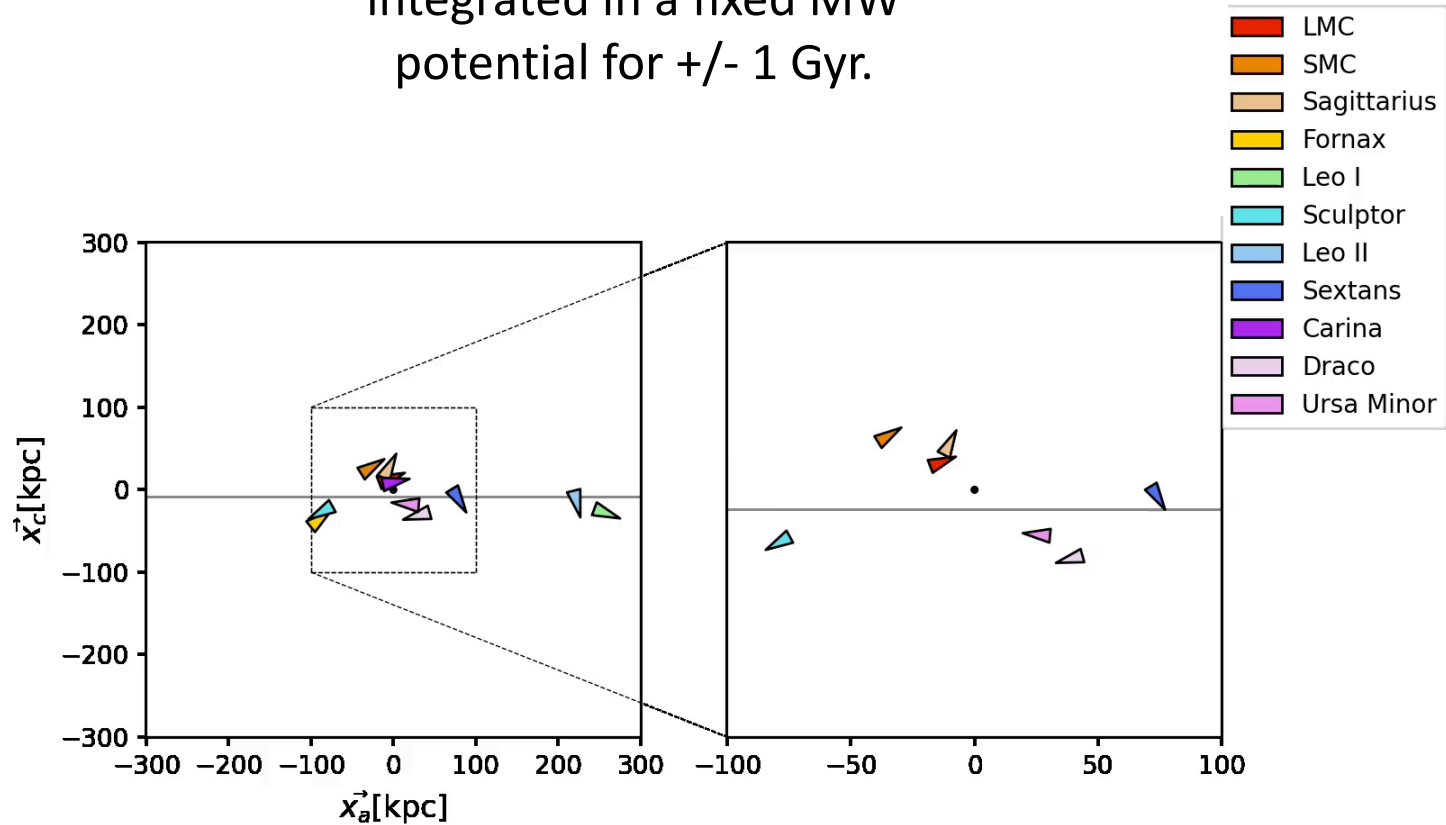
No strong correlation –
 $< 1 : 100,000$ chance?

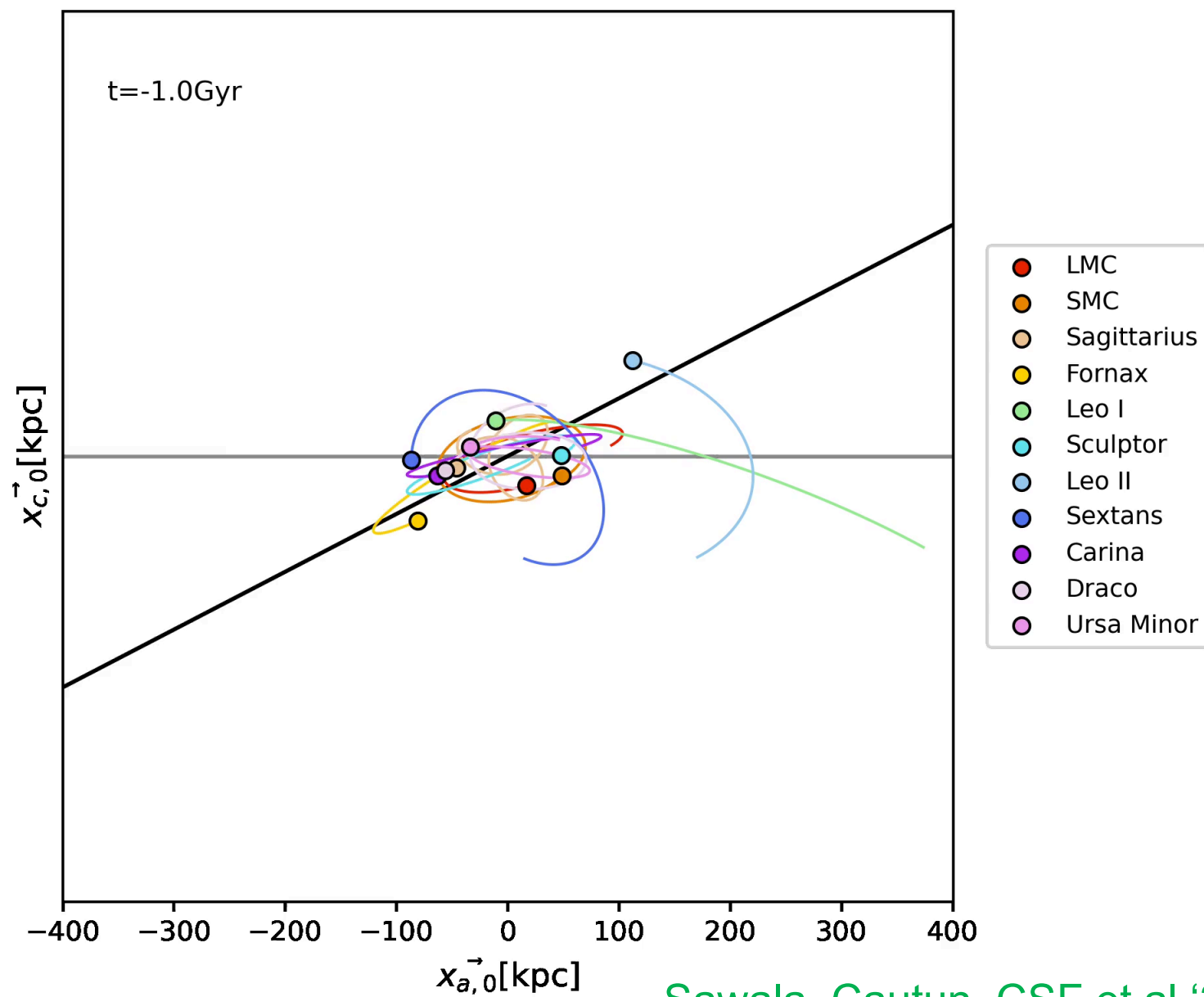
Eigenvalues
of inertia
tensor
 $a > b > c$



Pawlowski & Kroupa (2020)

Gaia EDR3 proper motions,
integrated in a fixed MW
potential for +/- 1 Gyr.





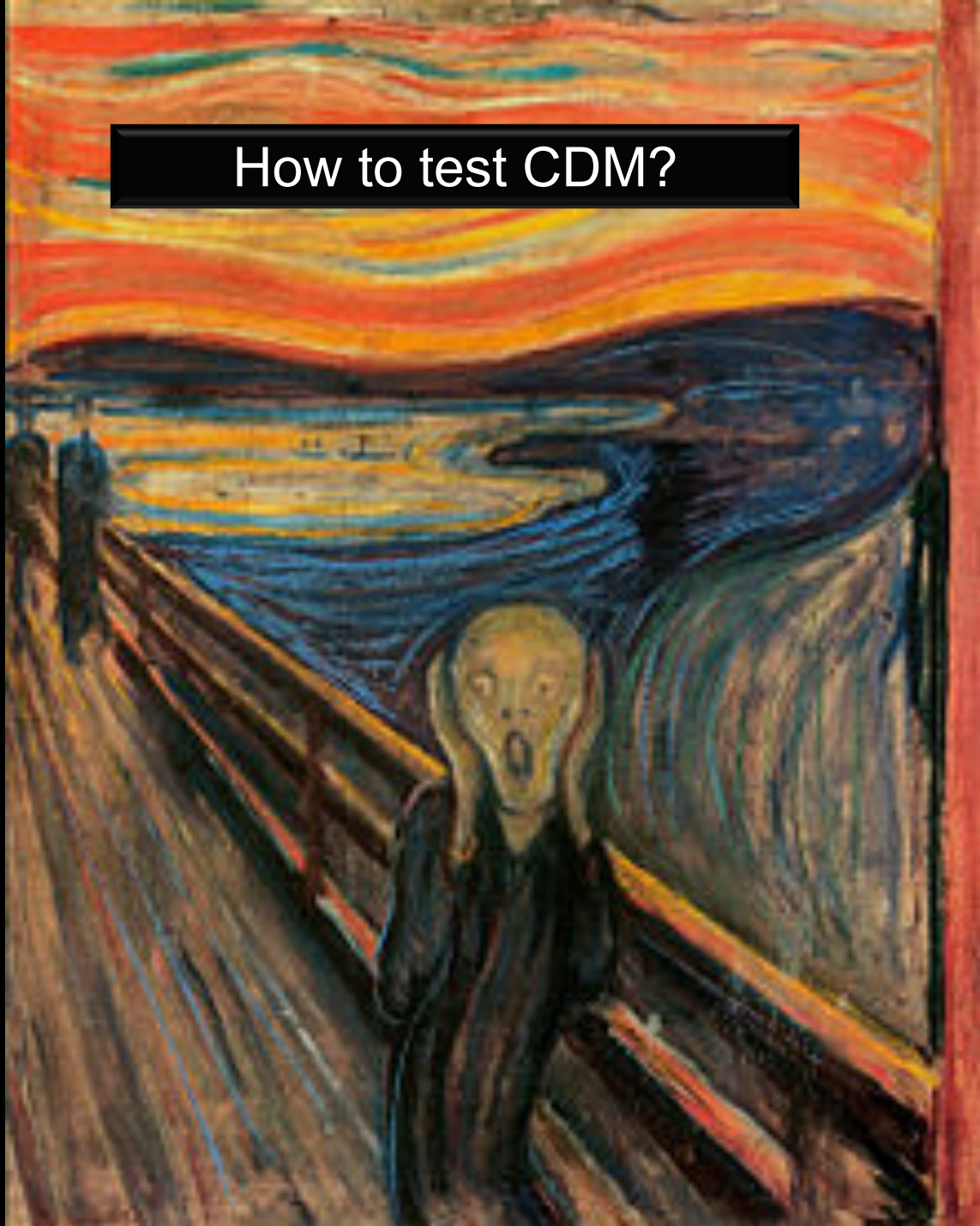
The rotating plane of satellites

200 Λ CDM N-body
simulations of Local Group
analogues: $m_p = 1 \times 10^6 M_\odot$

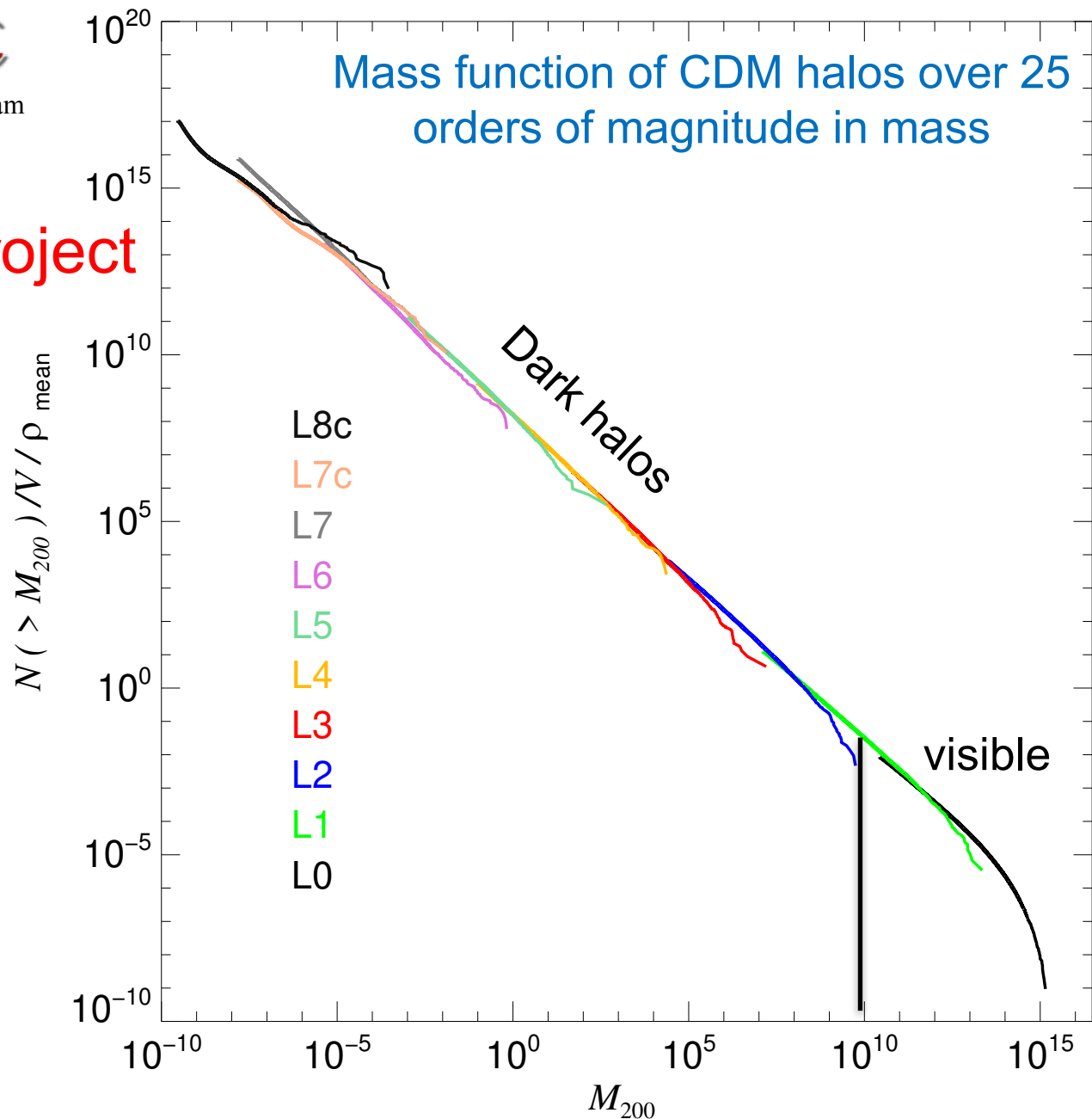
We have 5/200 (2.5%) more clustered than the MW (compared to 0.04%)
Still rare, but *not astronomically unlikely*.



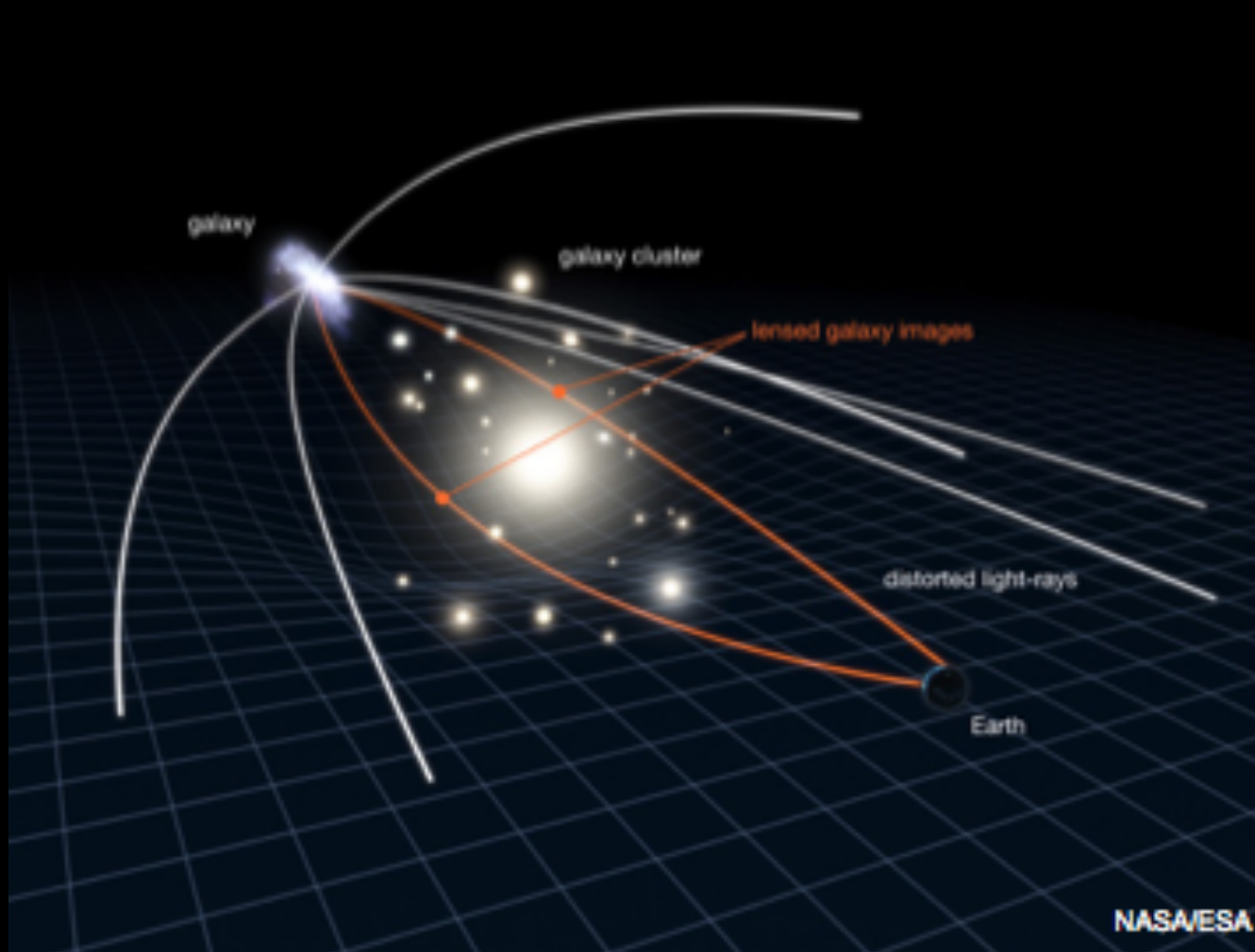
How to test CDM?



The VVV project



Gravitational lensing: Einstein rings

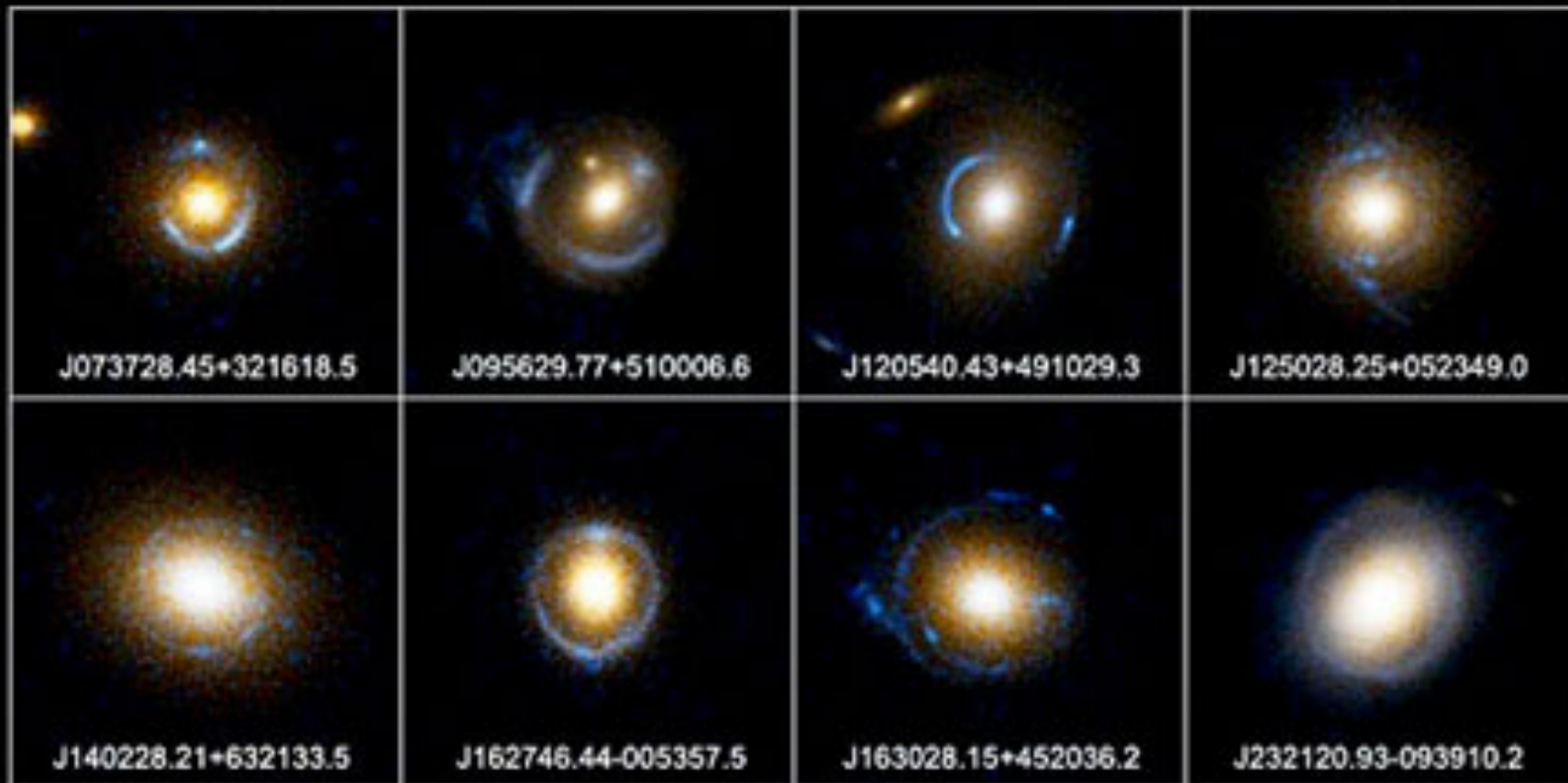


When the source and the lens are well aligned → strong arc or an Einstein ring

SLAC sample of strong lenses

Einstein Ring Gravitational Lenses

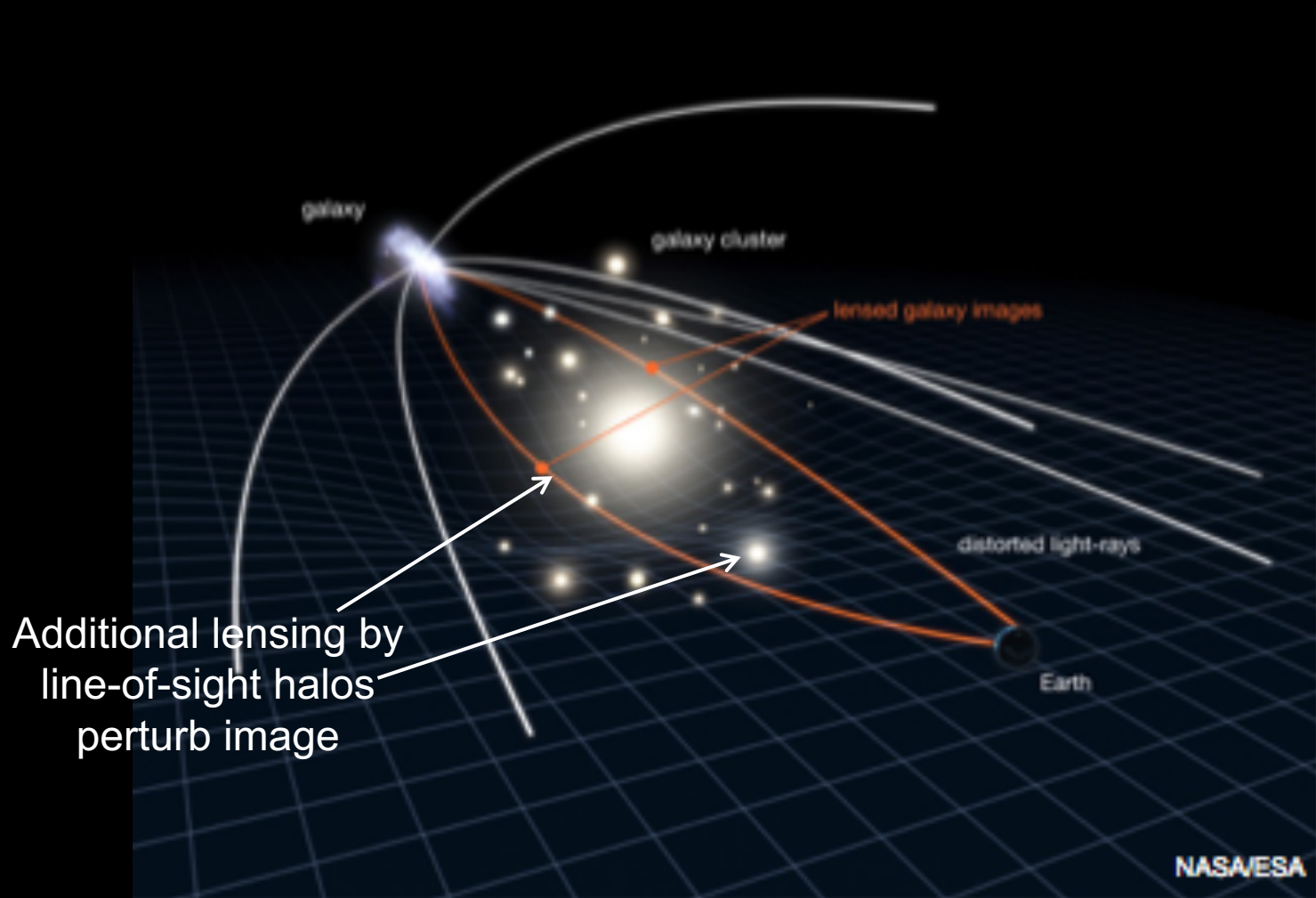
Hubble Space Telescope • ACS



NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

STScI-PRC05-32

Gravitational lensing: Einstein rings



When the source and the lens are well aligned → strong arc or an Einstein ring

Searched for substructure in 55 lenses with good HST imaging

→ 2 detections:  G3

SLACS0946+1006 → $\text{Log } M_{\text{sub}} = 11.59^{+0.18}_{-0.34}$

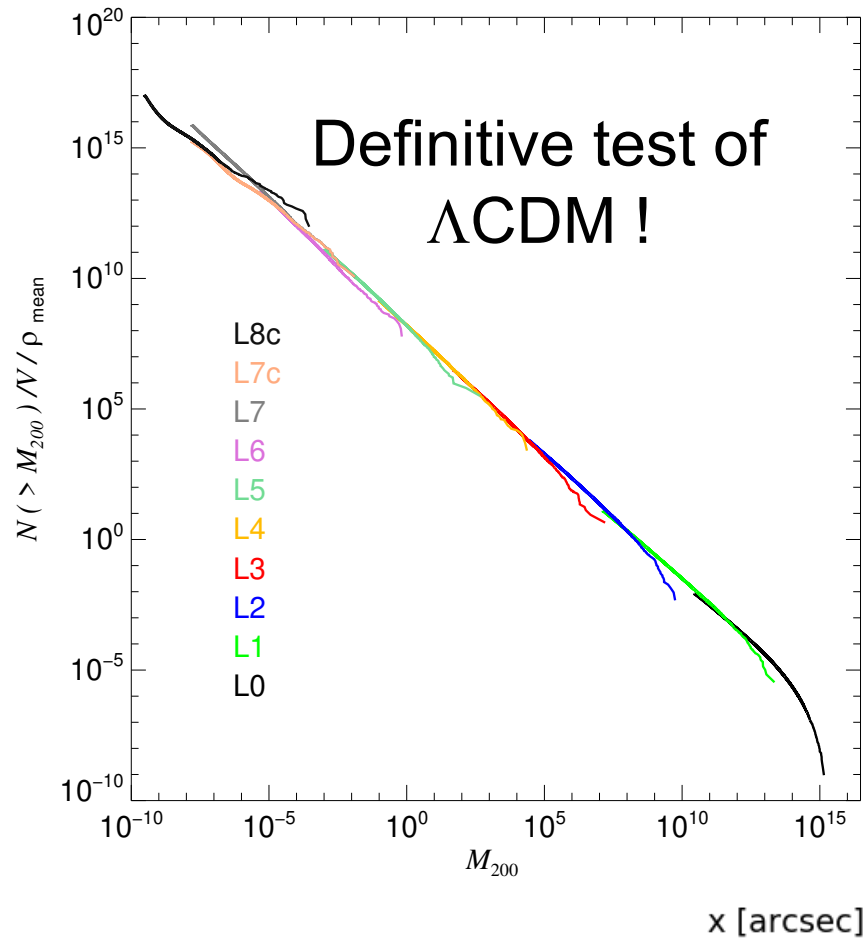
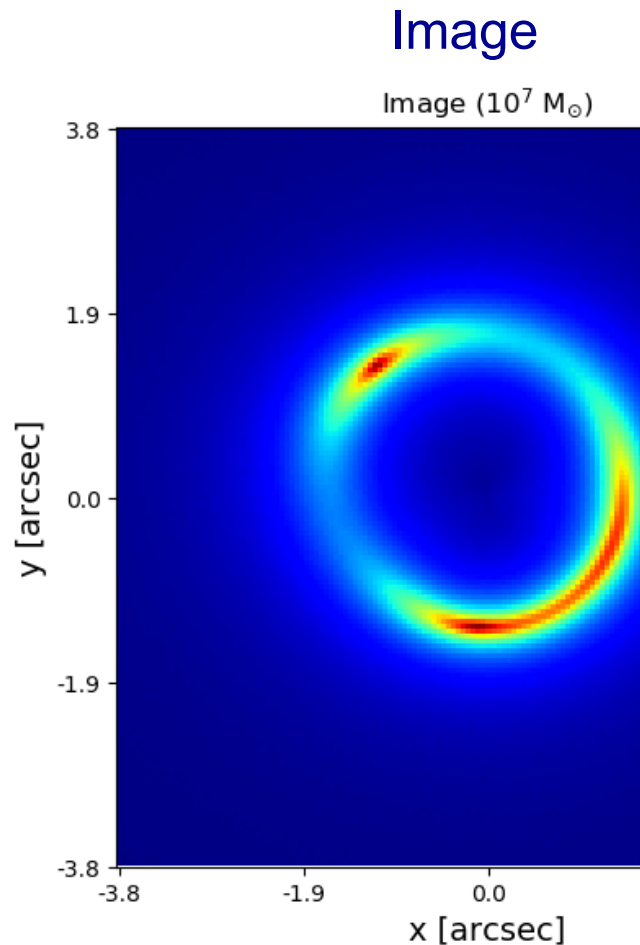
BELLS1226+5457 → $\text{Log } M_{\text{sub}} = 11.80^{+0.16}_{-0.30}$

1"

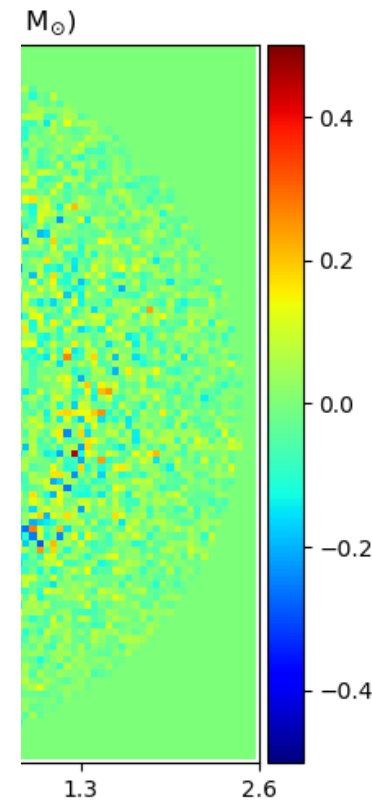
Nightingale, Massey, CSF+ '22

Strong lensing: detecting small halos

HST “data”: $z_{\text{source}}=1$; $z_{\text{lens}}=0.2$ $10^7 M_{\odot}$ halo – **NOT** so easy to spot



nooth model)





Conclusions

- Can test Λ CDM in non-linear regime
- Halo abundance, structure, clustering known from $10^{-6} - 10^{15} M_{\odot}$
- Missing satellites
 - Too-big-to-fail
 - Core/cusp→ “Solved” by baryon effects
- Plane of satellites
 - Plane is transient
 - MW plane not rare
- Definitive test of Λ CDM → dark subhalos → strong lensing



HAPPY BIRTHDAY celebration !

