

# A conclusive test of the cold dark matter model

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*Institute for Computational Cosmology,*  
*Durham*



# The standard model of cosmology

The new Ogden  
Centre at Durham





# The $\Lambda$ CDM model of cosmogony

Cosmological constant      Cold dark matter



- Proposed in 1980s, it is an *ab initio*, **fully specified** model of **cosmic evolution** and the formation of cosmic structure
- Has strong **predictive** power and can, in principle, be **ruled out**
- Has made a number of **predictions** that were subsequently **verified** empirically (e.g. CMB, LSS, galaxy formation)

Three Nobel Prizes in Physics since 2006

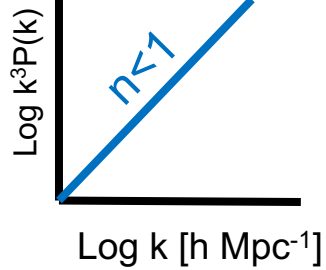
# The big Bang



The cosmic microwave background is emitted  
( $t \sim 350,000$  yrs)

Production of particle dark matter  
( $t \sim 10^{-10}$  s)

Cosmic inflation  
(initial conditions)  
( $t \sim 10^{-35}$  s)



The first light in our Universe

$t = 13.7$  billion yrs

- radiation
- particles
- $W^+$  heavy particles carrying the weak force
- $W^-$
- quark
- anti-quark
- electron
- positron (anti-proton)
- neutron
- meson
- hydrogen
- deuterium
- helium
- lithium

15 thousand million years

300 tho

3 minutes

$10^{-43}$  s

$10^{32}$  deg

$10^{-35}$  degrees

$10^{15}$  degr

degrees

18 degrees

3 degrees K



# Non-baryonic dark matter candidates

From the early 1980s:

Type	example	mass
hot	neutrino	few tens of eV
warm	sterile $\nu$	keV-MeV
cold	axion neutralino	$10^{-5}\text{eV} - 100 \text{ GeV}$

# The dark matter power spectrum

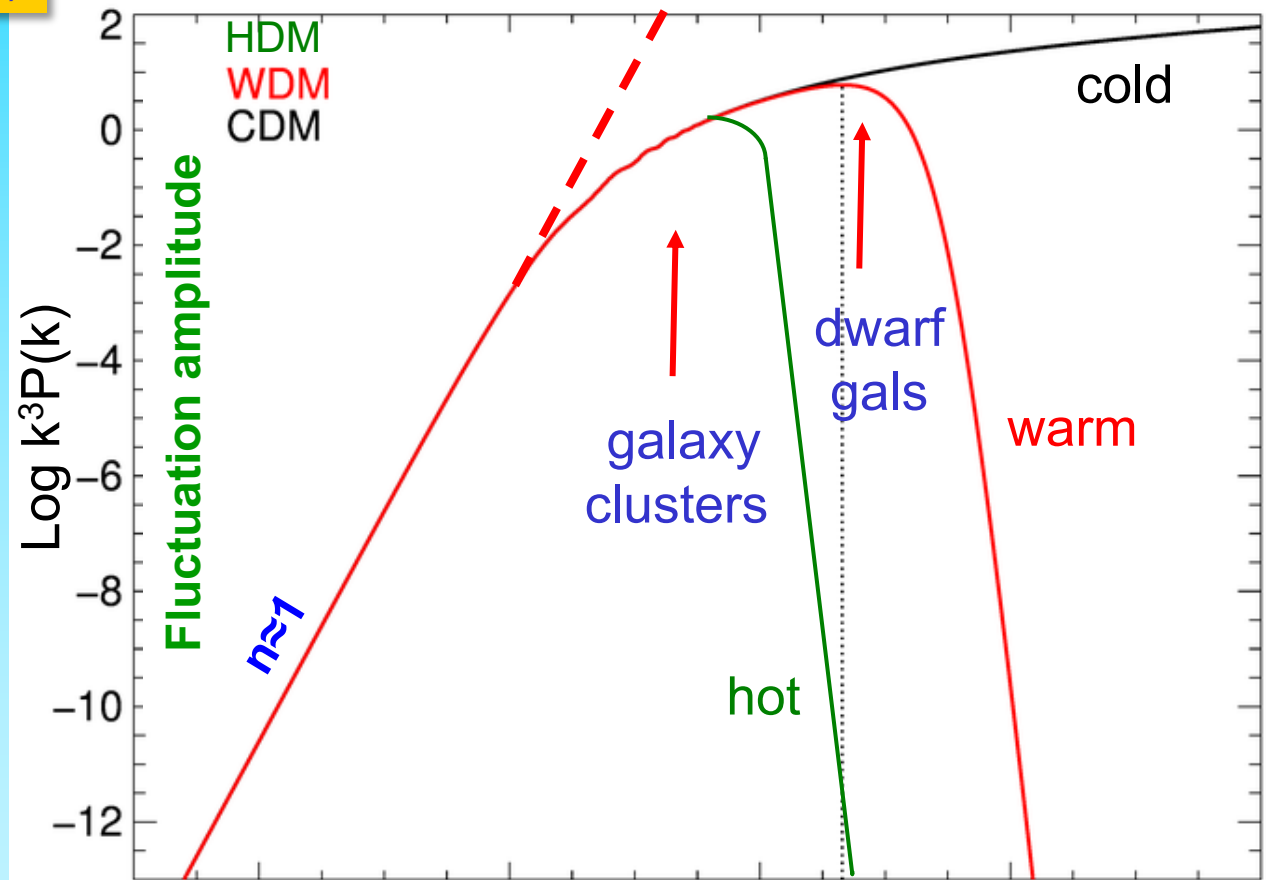
$k^3 P(k)$

The linear power spectrum (“power per octave”)

Free streaming →

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

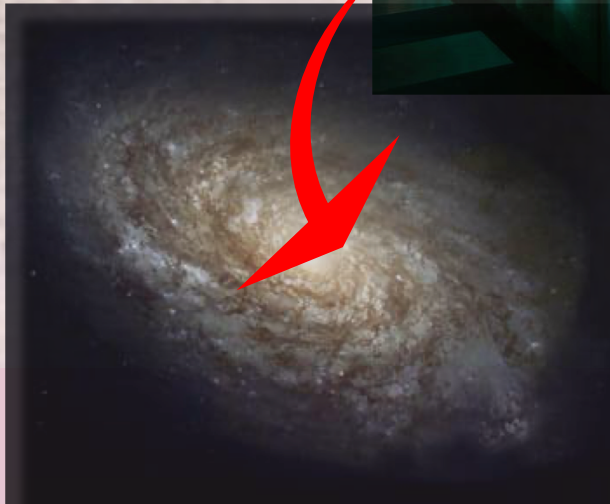
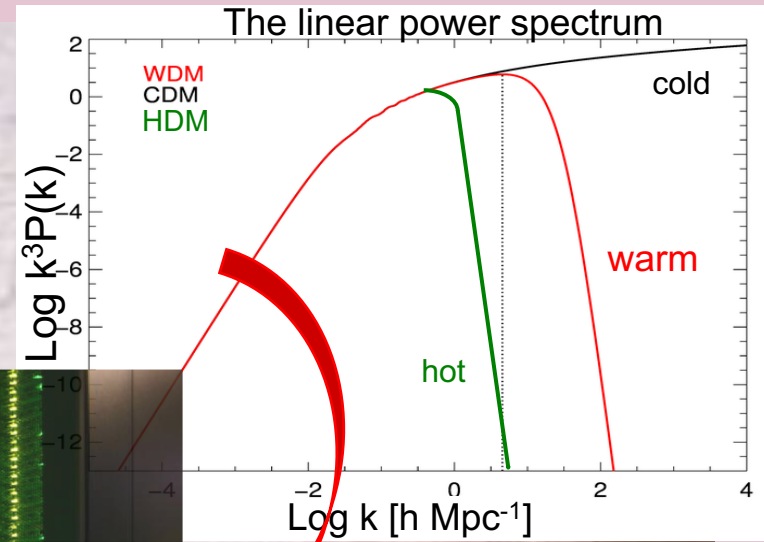
for a thermal relic



These possibilities can be tested with astrophysics



# Non-linear evolution

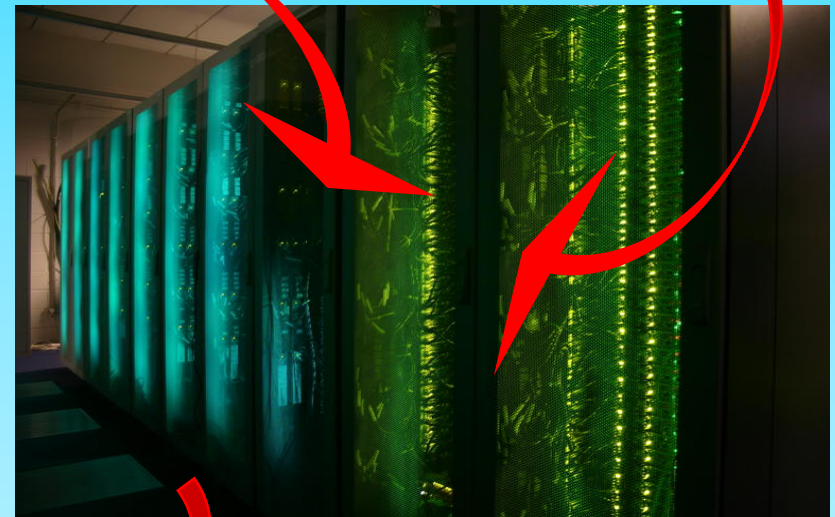


# Non-linear evolution: simulations

Assumption about content of Universe → Initial conditions

## Relevant equations:

Collisionless Boltzmann;  
Poisson; Friedmann eqns;  
Radiative hydrodynamics  
Subgrid astrophysics



How to make a virtual universe



# Hot dark matter

-7-

LUBIMOV

$$m_\nu = 30 \text{ eV} \rightarrow \Omega_m = 1$$

1981

HAS THE NEUTRINO A NON-ZERO REST MASS?  
(Tritium  $\beta$ -Spectrum Measurement)\*

V. Lubimov, E. Novikov, V. Nozik, E. Tretyakov  
Institute for Theoretical and Experimental Physics, Moscow, U.S.S.R.

V. Kosik  
Institute of Molecular Genetics, Moscow, U.S.S.R.

## ABSTRACT

The high energy part of the  $\beta$ -spectrum of tritium in the molecule was measured with high precision by a toroidal  $\beta$ -spectrometer. The results give evidence for a non-zero electron anti-neutrino mass.

Fifty years ago Pauli introduced the neutrino to explain the  $\beta$ -spectrum shape. Pauli made the first estimate of the neutrino mass ( $E_{\beta \text{ max}} \approx$  nuclei mass defect): it should be very small or maybe zero. Up to now the study of the  $\beta$ -spectrum shape is the most sensitive, direct method of neutrino mass measurement.

For allowed  $\beta$ -transitions, if  $M_\nu = 0$ , then  $S \approx (E - E_0)^2$ . The Kurie plot is then a straight line with the only kinematic parameter being  $E_k = E_0$  (total  $\beta$ -transition energy). If  $M_\nu \neq 0$ , then  $S \approx (E_0 - E) \sqrt{(E_0 - E)^2 - M_\nu^2}$ . The Kurie plot is then distorted, especially near the endpoint.

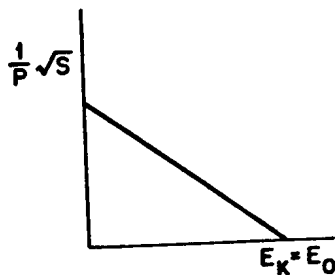


Fig. 1. Kurie plot for  $M_\nu = 0$ .

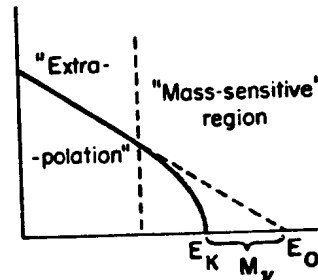
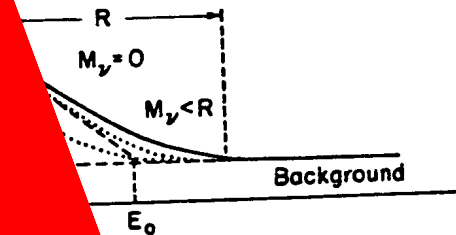


Fig. 2. Kurie plot for  $M_\nu \neq 0$ .

The method for the neutrino mass measurement is to obtain  $E_0$  from the extrapolation and obtain  $E_k$  from the spectrum intercept. Then  $M_\nu = E_0 - E_k$ . Qualitatively,  $M_\nu \neq 0$  if the  $\beta$ -spectrum near the endpoint runs below the extrapolated curve.

\* Paper presented by Oleg Egorov.

things are more complicated. The apparatus resolution strongly affects the spectrum endpoint and rather the spectrum slope.



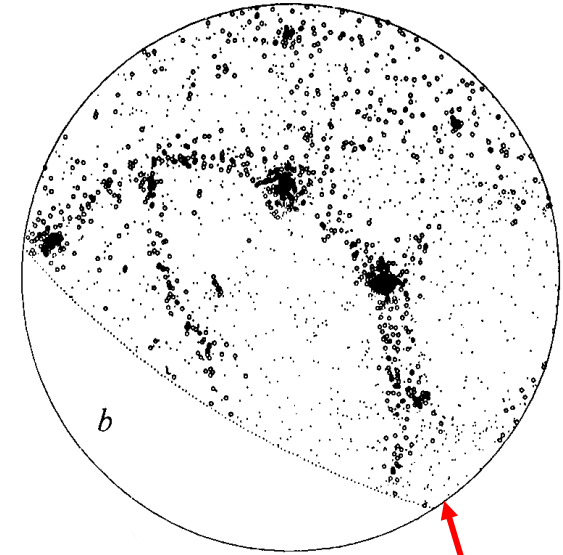
A realistic Kurie plot.

extrapolation. However, we are unable to determine  $M_\nu$ , then once again the lack of counts near the endpoint indicate that  $M_\nu \neq 0$ . If  $M_\nu \leq R$ , the changes due to  $M_\nu$  and the influence of  $R$  are indistinguishable. For  $M_\nu > R$ , the determination of the knowledge of  $R$  is compulsory. The background determines the statistical accuracy near the endpoint, i.e., in the region of the highest sensitivity to the  $\nu$  mass. So: 1)  $R$  should be  $\sim M_\nu$ , 2) the smaller  $M_\nu$  is, the smaller the background ( $\sim M_\nu^2$ ) must be and the higher the statistics ( $\sim M_\nu^{-3}$ ) must be. For example, suppose that for  $M_\nu = 100 \text{ eV}$  we need resolution  $R$ , background  $Q$ , and statistics  $N$ . If  $M_\nu = 30 \text{ eV}$ , to achieve the same  $\Delta M/M$  they should be  $R/3$ ,  $Q/10$ , and  $N \times 30$ , respectively.

The shorter the  $\beta$ -spectrum, the less it is spread due to  $R$  (as  $R \sim \Delta p/p \approx \text{const.}$ ). A classical example is  $^3\text{H}$   $\beta$ -decay, which has 1) the smallest  $E_0 \sim 18.6 \text{ keV}$ , 2) an allowed  $\beta$ -transition, simple nucleus, and simple theoretical interpretation, 3) highly reduced radioactivity. The first experiments with  $^3\text{H}$  were by S. Curran et al. (1948) and G. Hanna, B. Pontecorvo (1949). Using  $^3\text{H}$  gas in a proportional counter, they obtained  $M_\nu \leq 1 \text{ keV}$ . Further progress required magnetic spectrometer development. This allowed the resolution to be improved considerably, and L. Langer and R. Moffat (1952) obtained  $M_\nu \leq 250 \text{ eV}$ . The best value was obtained by K. Bergqvist (1972):  $R \sim 50 \text{ eV}$  and  $M_\nu \leq 55 \text{ eV}$ .

The ITEP spectrometer is of a new type: ironless, with toroidal magnetic field (E. Tretyakov, 1973). The principle of the toroidal magnetic field focusing systems was proposed by V. Vladimirov et al. (An example is a "Horn" of  $\nu$ -beams.) It turns out that a rectilinear conductor (current) has a focusing ability for particles emitted perpendicular to the rotation axis. This system has infinite periodical focusing structure. The ITEP spectrometer is based on this principle.

# Non-baryonic dark matter cosmologies



Neutrinos  
 $\Omega=1$

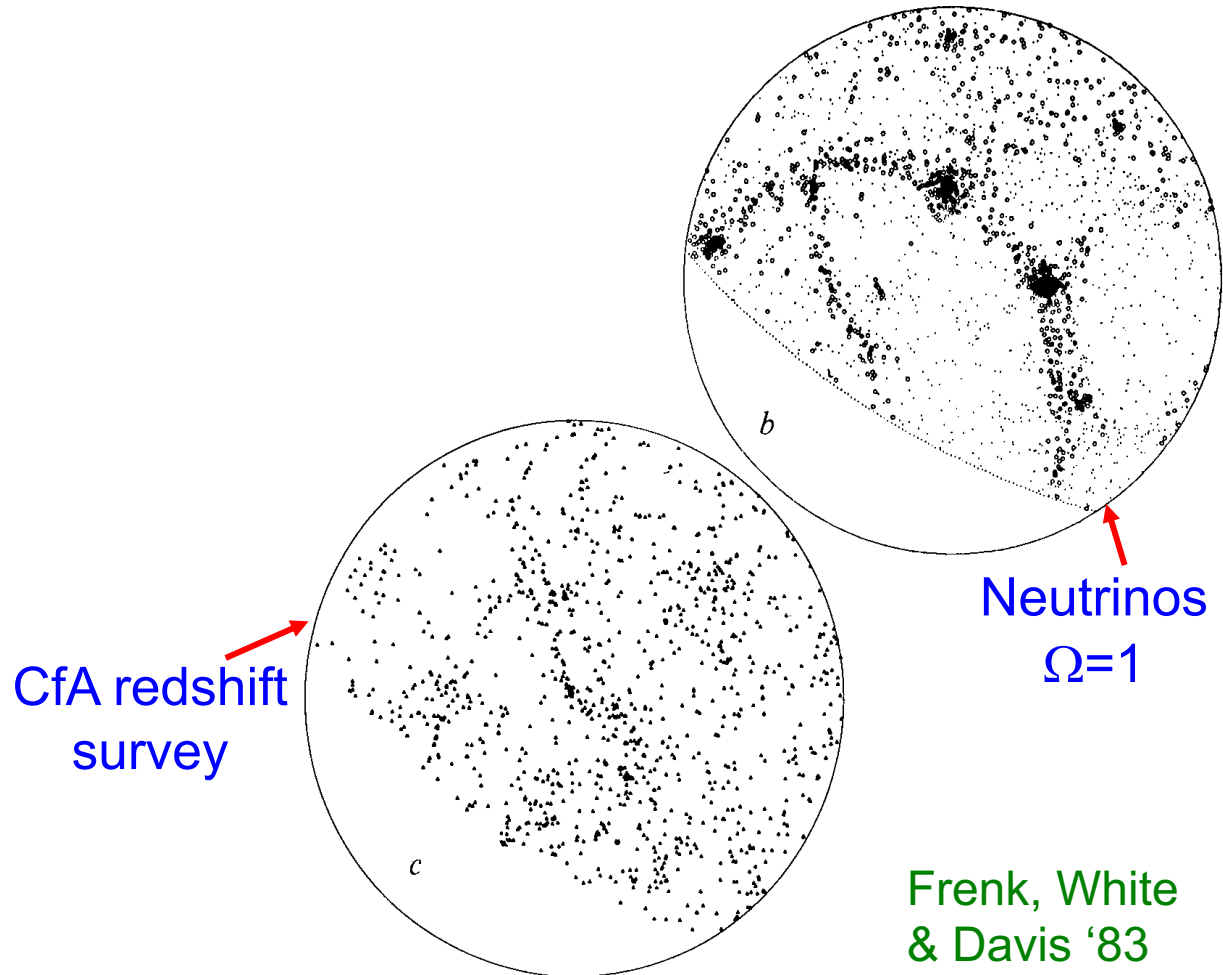
Frenk, White  
& Davis '83



# Non-baryonic dark matter cosmologies

Neutrino DM →  
wrong clustering

Neutrinos cannot  
make appreciable  
contribution to  $\Omega$   
→  $m_\nu \ll 30$  eV



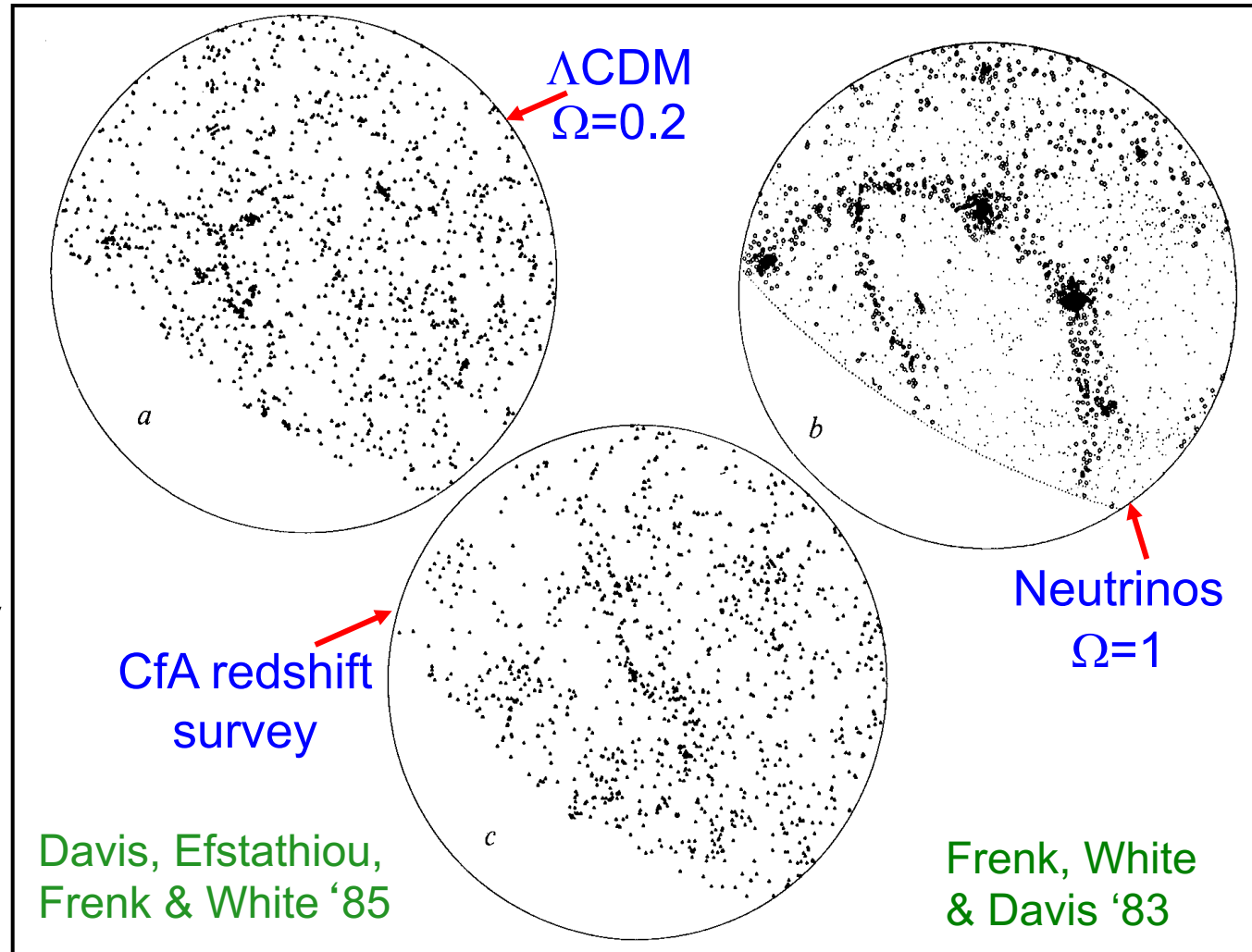
# Non-baryonic dark matter cosmologies

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→  $m_\nu \ll 30$  eV

Early CDM N-body  
simulations gave  
promising results

In CDM structure  
forms hierarchically





# The big Bang



300 tho

3 minutes

15 thousand million years

The temperature of this radiation should show small irregularities

Production of particle dark matter  
( $t \sim 10^{-10}$  s)

$10^{-43}$  seconds

$10^{32}$  degrees

$10^{27}$  degrees

$10^{15}$  degr

1 degrees

18 degrees

3 degrees K

$t = 13.7$  billion yrs

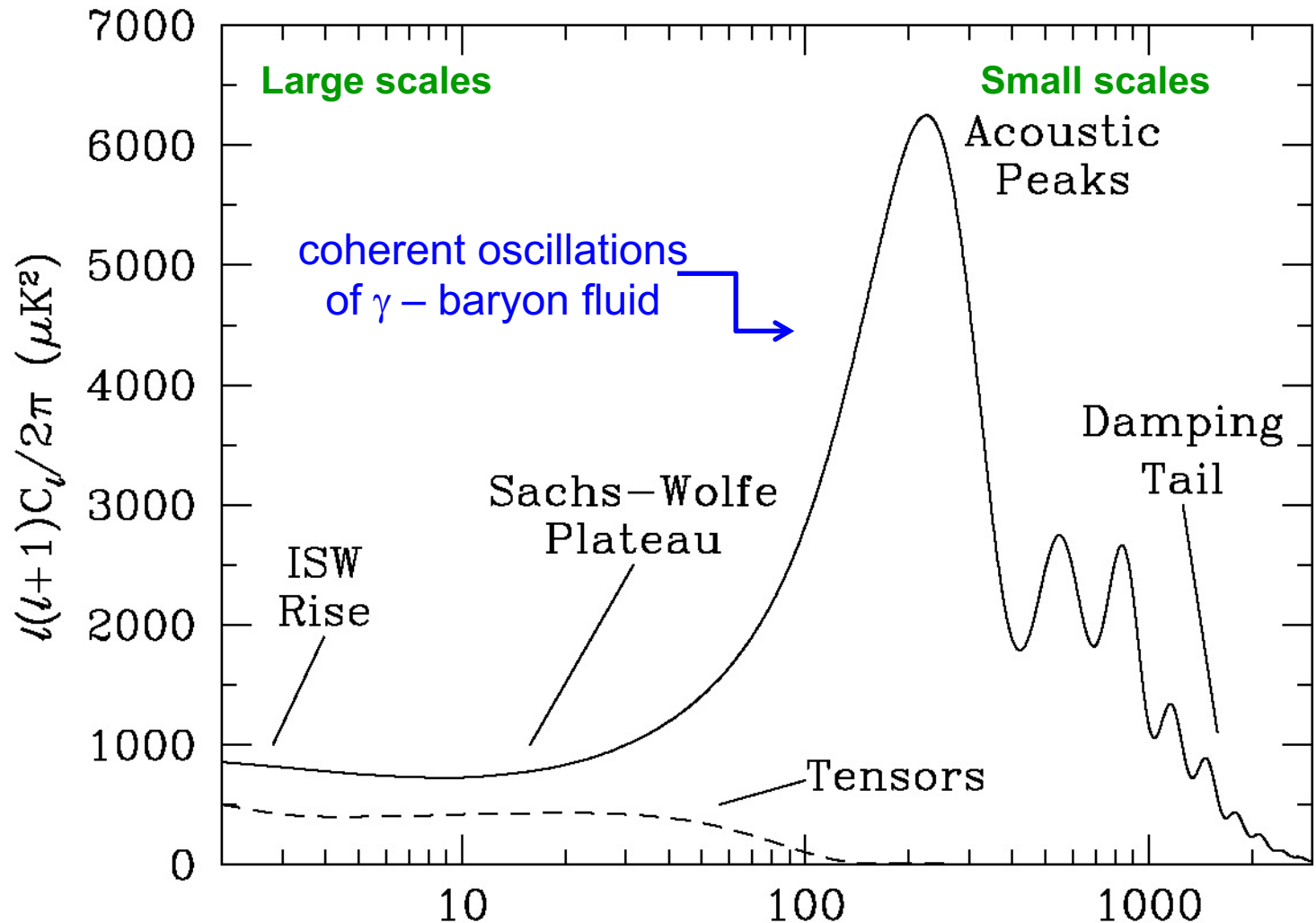
Cosmic inflation  
(initial conditions)  
( $t \sim 10^{-35}$  s)

- radiation
- particles
- $W^+$  heavy particles carrying the weak force
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- $Z$
- quark
- anti-quark
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- hydrogen
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- helium
- lithium



# Temperature anisotropies in CMB

2D power spectrum



Peebles & Yu '70 Sunyev & Zel'dovich '70

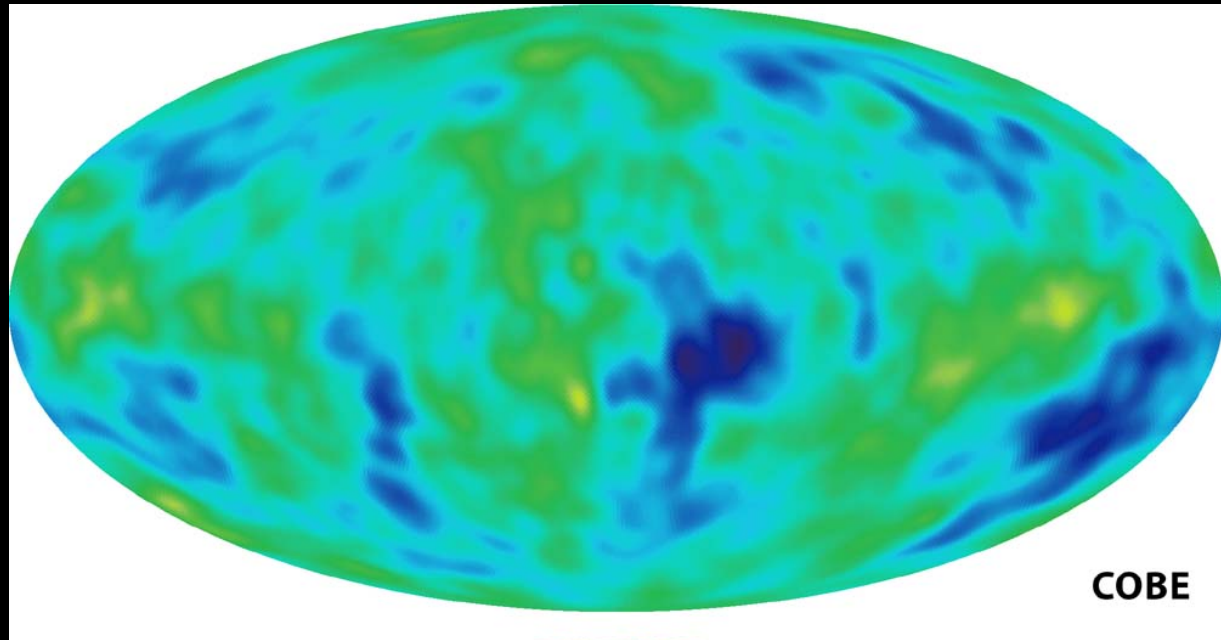
For CDM: Peebles '82; Bond & Efstathiou '84

Jim Peebles

Nobel prize 2019



1992



The cosmic microwave background radiation (CMB) provides a window to the universe at  $t \sim 3 \times 10^5$  yrs

In 1992 COBE discovered temperature fluctuations ( $\Delta T/T \sim 10^{-5}$ ) consistent with inflation predictions





# THE INDEPENDENT

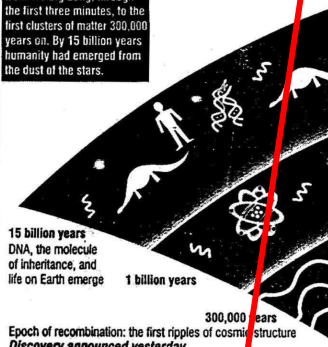
No 1,722

A Nasa spacecraft has detected the stars after the Big Bang has

## How

### BACK TO CREATION

How the universe evolved from the Big Bang, through the first three minutes, to the first clusters of matter 300,000 years on. By 15 billion years humanity had emerged from the dust of the stars.



FOURTEEN thousand million years ago the universe hiccuped. Yesterday, American scientists announced that they have heard the echo.

A Nasa spacecraft has detected ripples at the edge of the Cosmos which are the fossilised imprint of the birth of the stars and galaxies around us today.

According to Michael Rowan-Robinson, a leading British cosmologist, "What we are seeing here is the moment when the structures we are part of — the stars and galaxies of the universe — first began to form."

The ripples were spotted by the Cosmic Background Explorer (Cobe) satellite and presented to excited astronomers at a meeting of the American Physical Society in Washington yesterday. "Oh wow... you can have no idea how exciting this is," Carlos Frenk, an astronomer at Durham University, said yesterday. "All the world's cosmologists are on the telephone to each other at the moment trying to work out what these numbers mean."

Cobe has provided the answer to a question that has baffled scientists for the past three decades in their attempts to understand the structure of the Cosmos. In the 1960s two American researchers found definitive evidence that the Big Bang had started the whole thing off about 15 billion years ago. But the Big Bang would have spread matter like thin gruel evenly throughout the universe. The problem was to work out how

the lumps (stars, planets and galaxies) got into the porridge.

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3 minutes

1 second  
Stable subnuclear particles, neutrons and protons, are formed

10<sup>-10</sup> second

10<sup>-3</sup>  
The quark bare parti

able to view the young universe, Dr Smoot said.

A remnant glow from the Big Bang is still around today, in the form of microwave radiation that has bathed the universe for the billions of years since the explosion. Galaxies must have formed by growing gravitational forces bringing matter together. To produce a "lumpy" universe, radiation from the Big Bang should itself show signs of being lumpy.

Cobe, which has been orbiting 500 miles above the Earth since the end of 1989, has instruments on board that are sensitive to this extremely old radiation. The ripples Cobe has found are the first hard evidence of the long-sought lumpiness in the radiation.

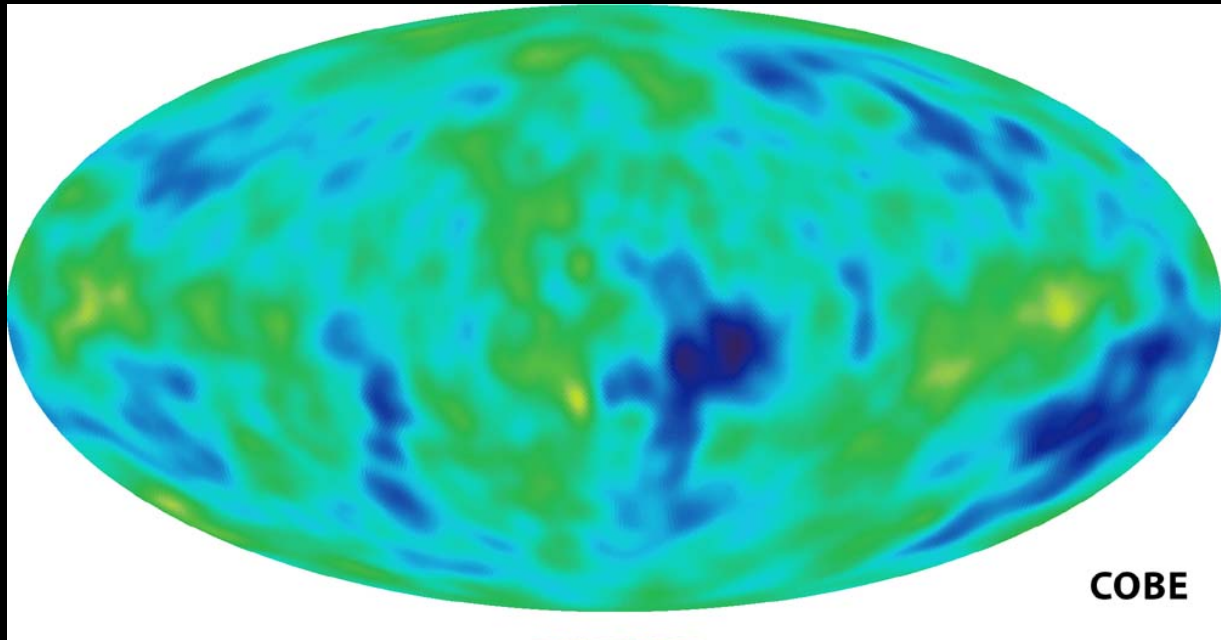
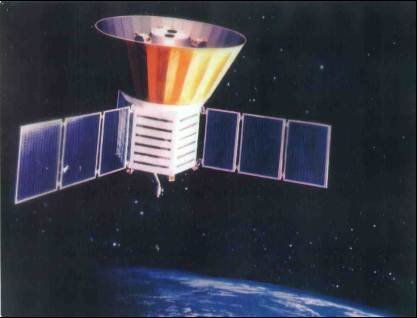
Cobe detected almost imperceptible variations in the tem-

Flammarion 1888: tete des etoiles

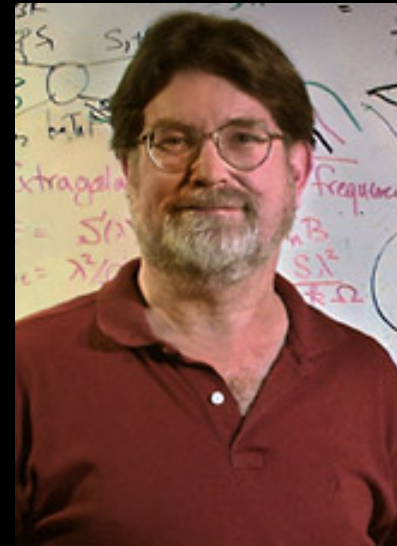


# The CMB

1992



George Smoot - Nobel Prize 2006

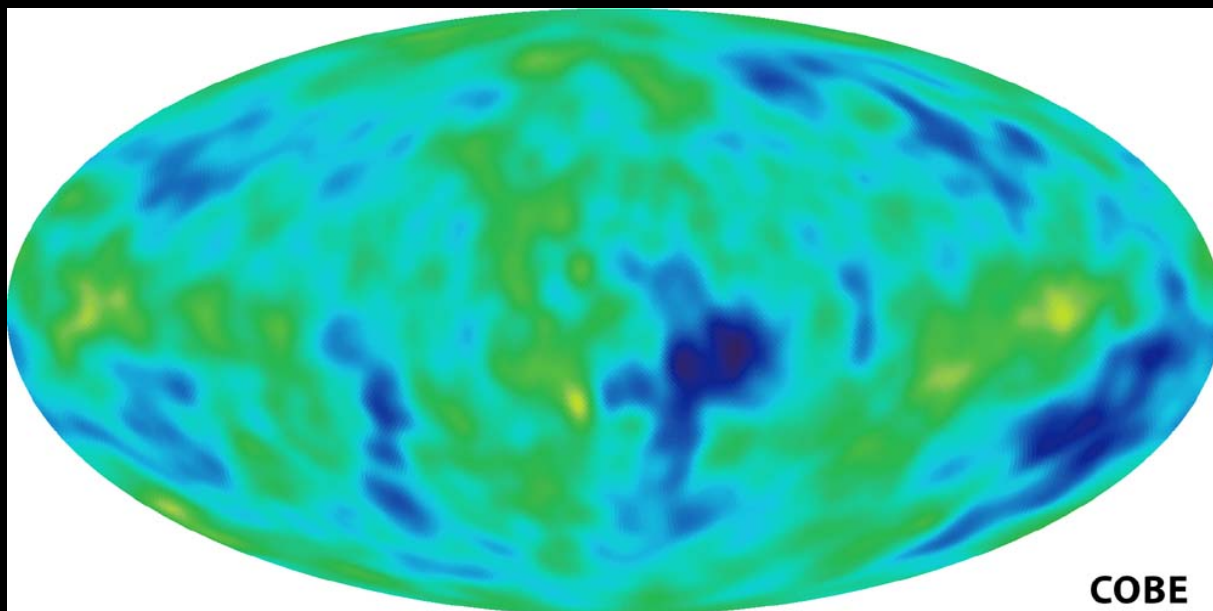






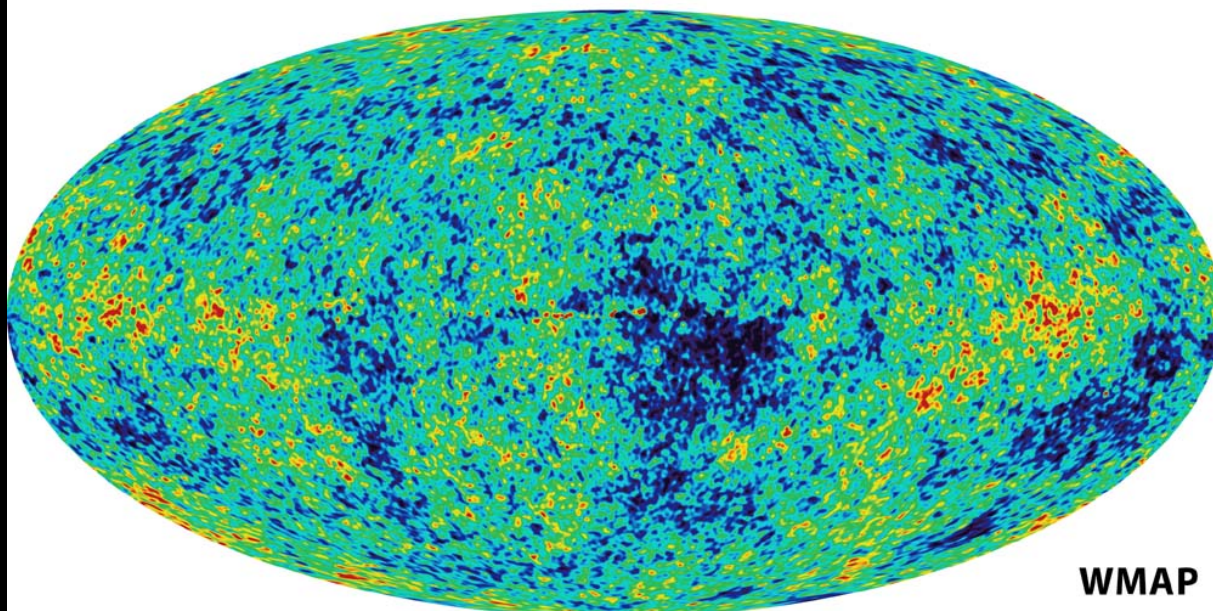
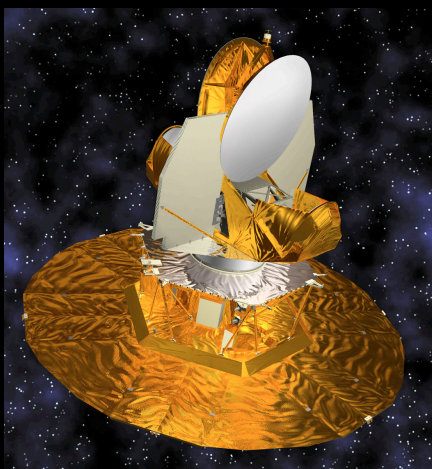
# The CMB

1992



COBE

2003



WMAP



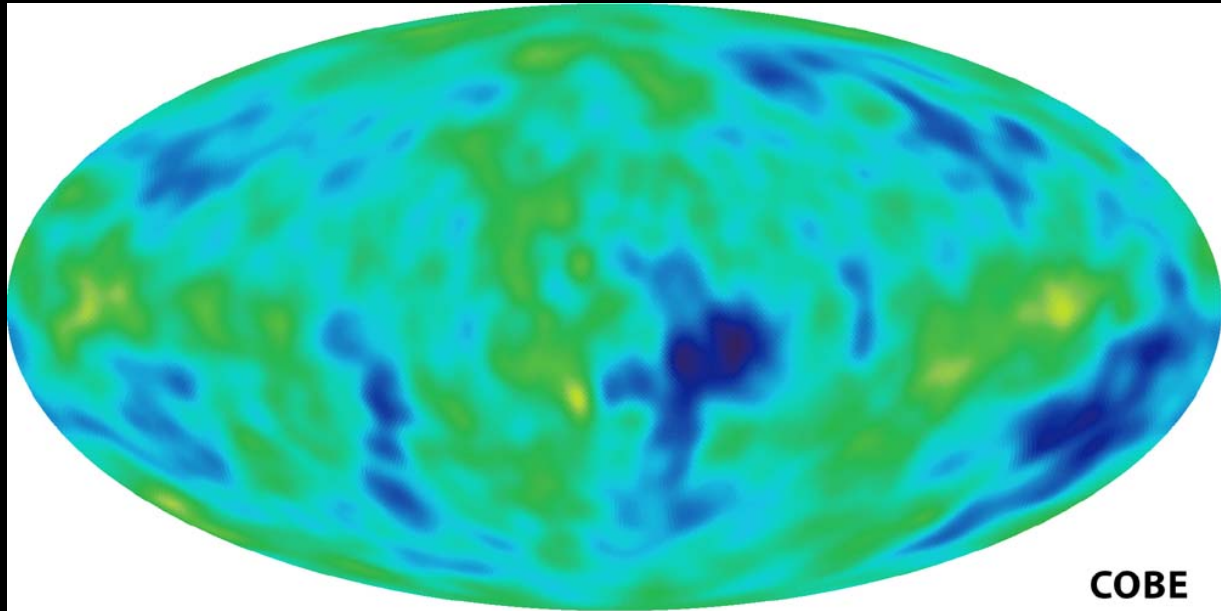
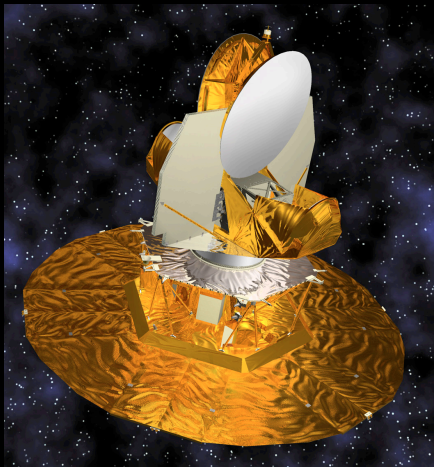
ICC

# The CMB

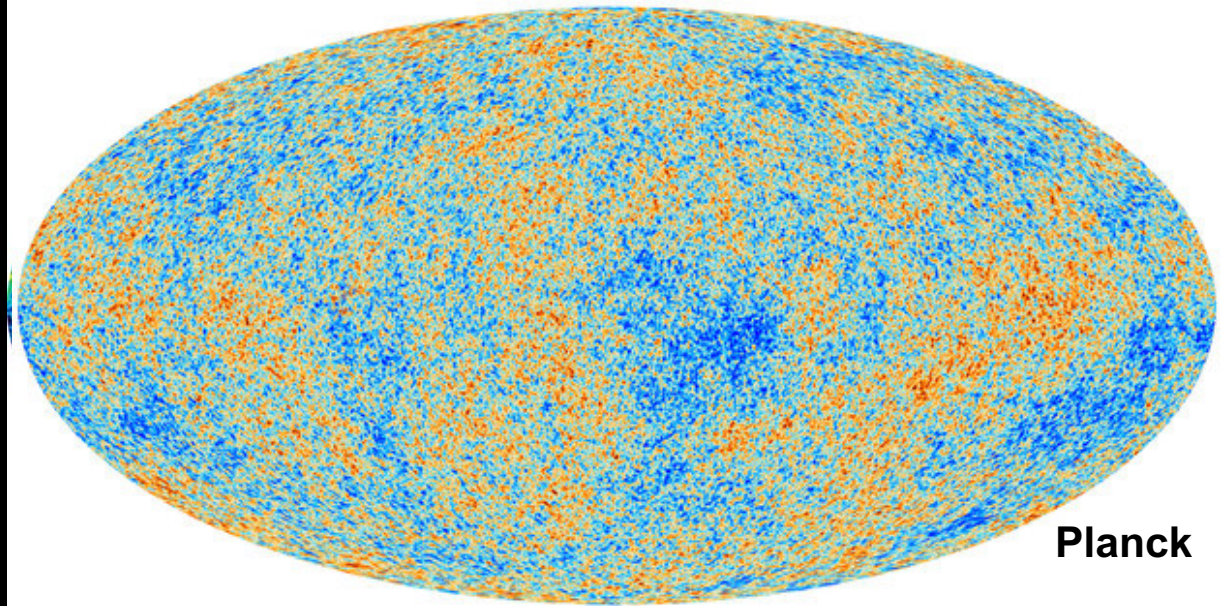
1992



2012



COBE



Planck

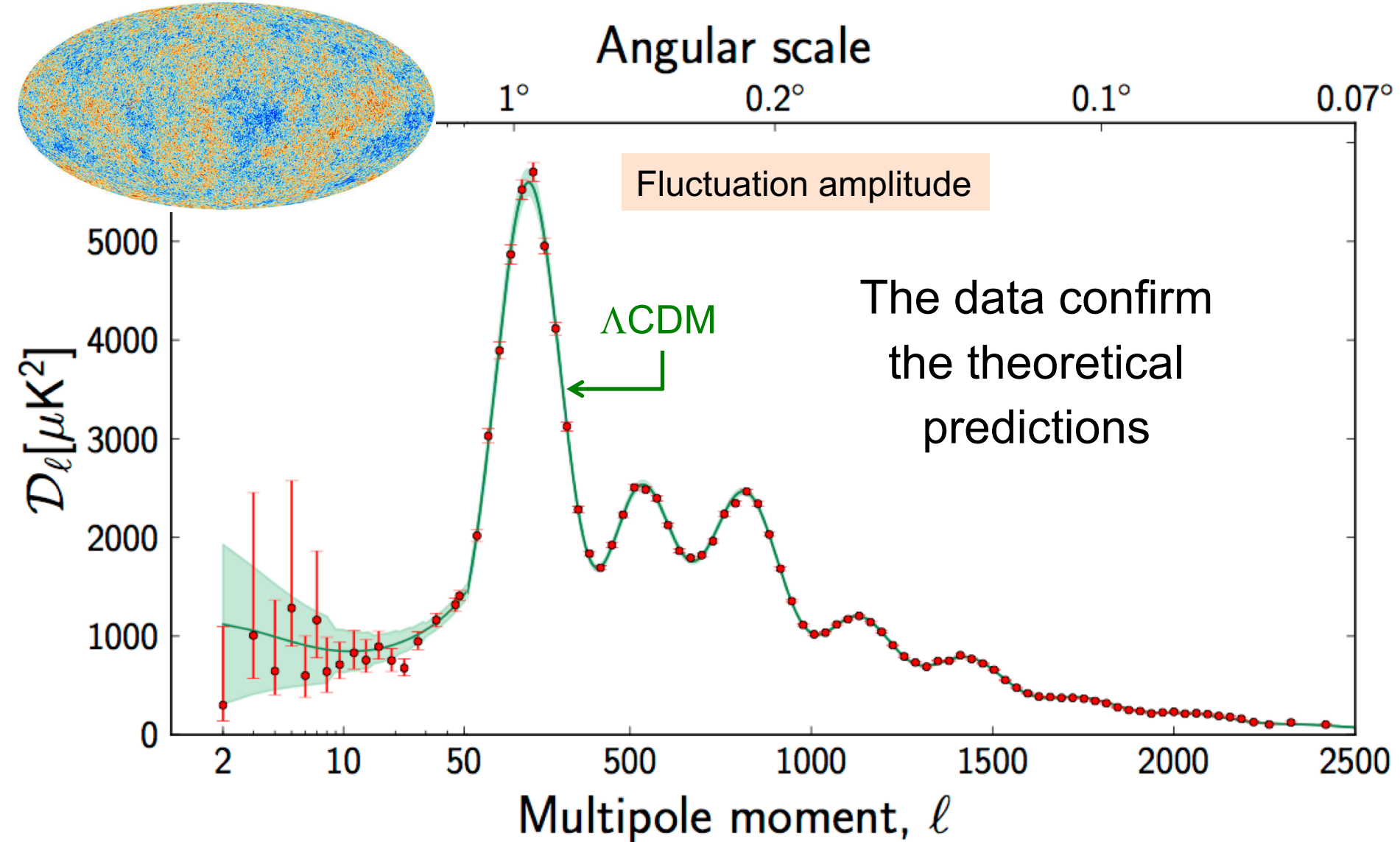


# The initial conditions for galaxy formation



Quantum fluctuations from inflation

# Planck: CMB temperature anisotropies





# The six parameters of minimal $\Lambda$ CDM model

	Parameter	<i>Planck</i> +WP	
		Best fit	68% limits
$\Omega_b h^2$ . density of baryons .		0.022032	0.02205 $\pm$ 0.00028
$\Omega_c h^2$ . density of CDM . .		0.12038	0.1199 $\pm$ 0.0027
$100\theta_{MC}$ . . . . .		1.04119	1.04131 $\pm$ 0.00063
$\tau$ . . . . .		0.0925	0.089 $^{+0.012}_{-0.014}$
$n_s$ . . . . .		0.9619	0.9603 $\pm$ 0.0073
$\ln(10^{10} A_s)$ . . . . .		3.0980	3.089 $^{+0.024}_{-0.027}$

A 40 $\sigma$  detection of non-baryonic dark matter!

# The curvature of the Universe

The Planck power spectra (temperature and polarization) (positions of acoustic peaks) → the Universe is spatially flat

Combined with LSS data, Planck →  $\Omega_k = 0.0004 \pm 0.0018$

$$\rightarrow \Omega_{\text{tot}} = \Omega_m + \Omega_\Lambda + \Omega_k = 1$$

Since  $\Omega_{\text{matter}} = 0.28 \pm 0.005$  → “dark energy”, e.g.  $\Omega_\Lambda = 0.72$

$\Lambda$  anticipated from galaxy distribution in 1991;

inferred from accelerated expansion → 2011 Nobel prize

# Observational tests of $\Lambda$ CDM

## Fundamental prediction of $\Lambda$ CDM

→ Primordial PS of density perturbations + random phases

Can test this in **two regimes**:

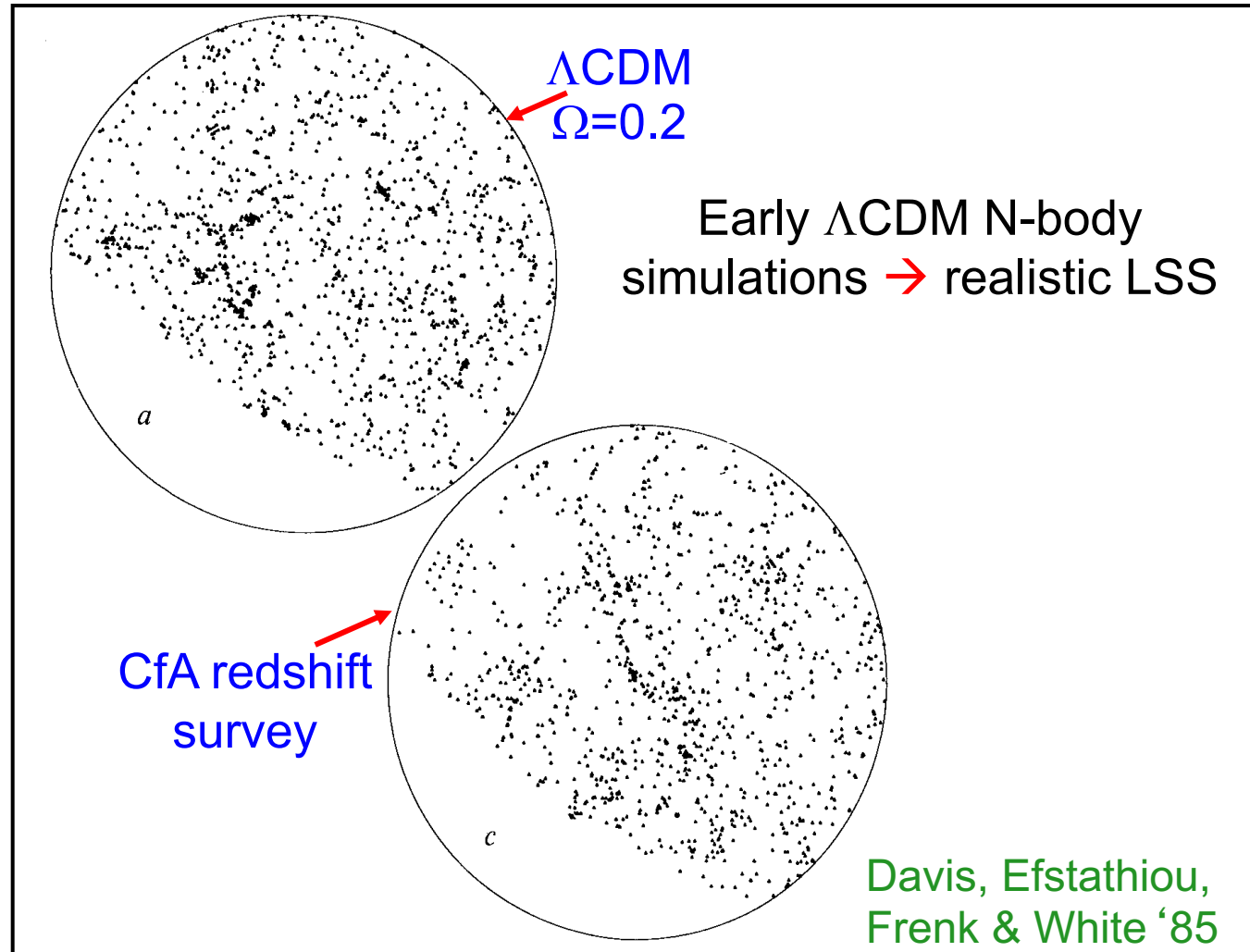
**Linear regime:** cosmic microwave background ✓  
large-scale structure

**Evolved non-linear regime:** dark matter halos →

- abundance
- structure
- clustering



# The $\Lambda$ CDM cosmology





VIRGO

# The Millennium/Aquarius/Phoenix simulation series

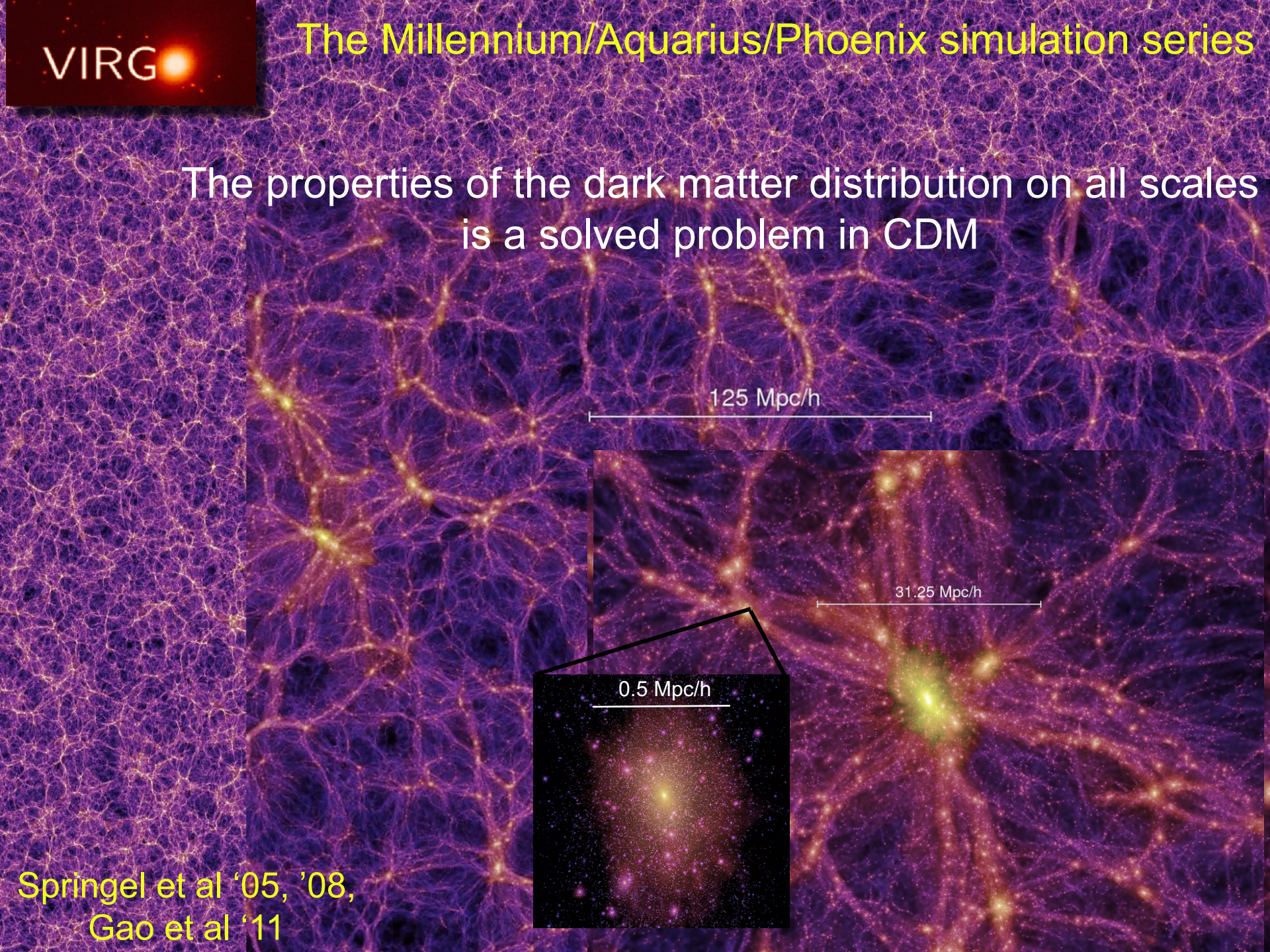
The properties of the dark matter distribution on all scales  
is a solved problem in CDM

125 Mpc/h

31.25 Mpc/h

0.5 Mpc/h

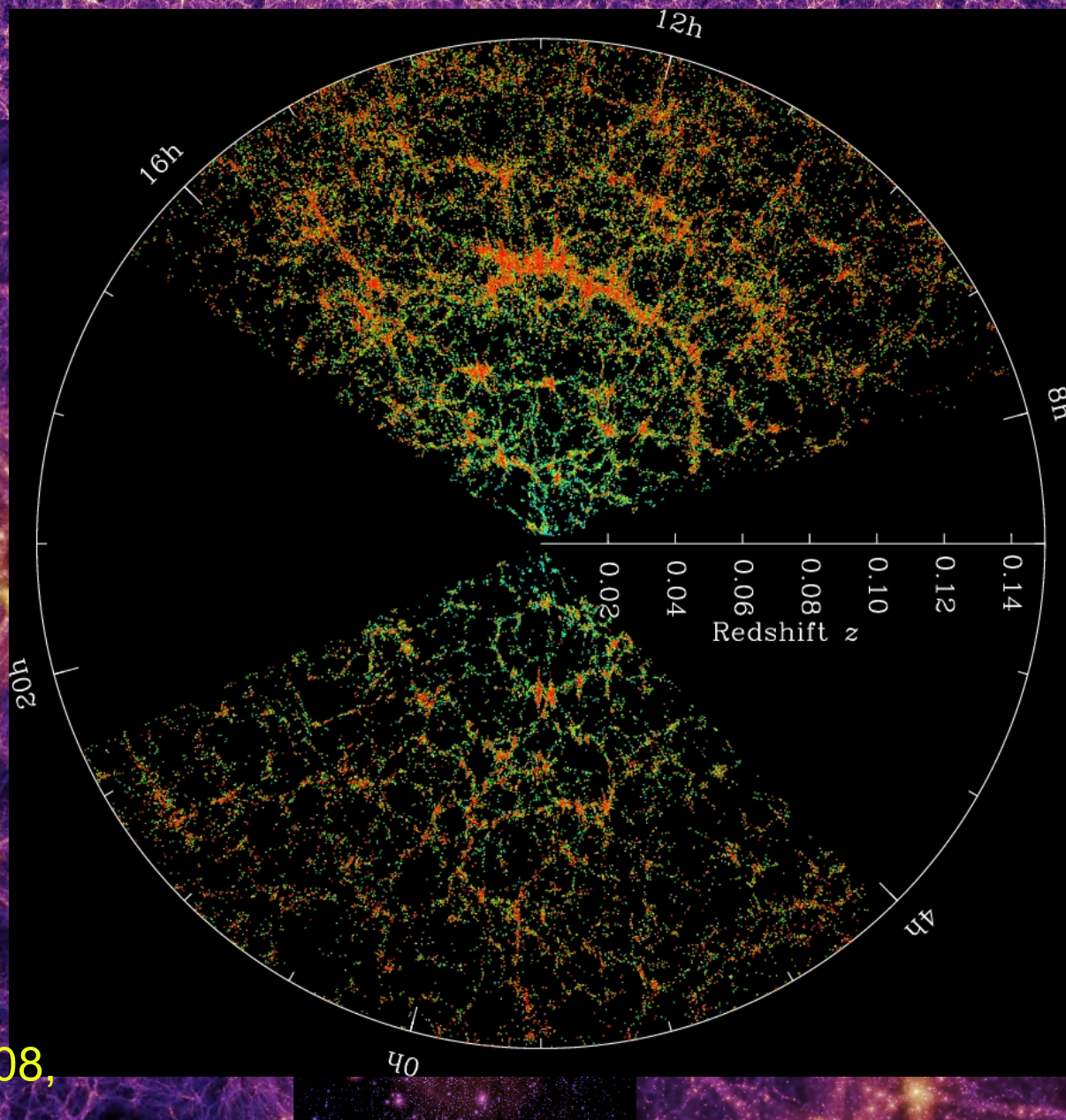
Springel et al '05, '08,  
Gao et al '11





VIRGO

# The Millennium/Aquarius/Phoenix simulation series



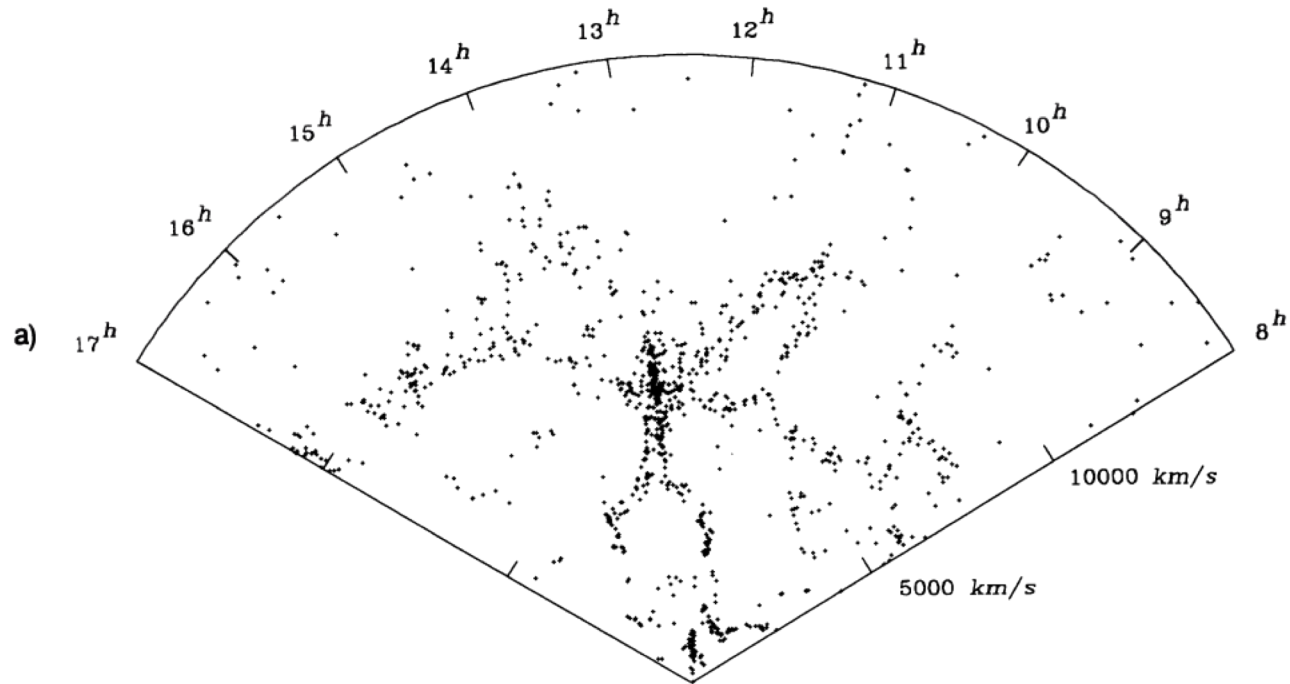
Springel et al '05, '08,  
Gao et al '11



1980s

DE LAPPARENT, GELLER, AND HUCHRA

Vol. 302



The CfA redshift survey

2020s

Galaxy distribution encodes info about dark matter and dark energy

5 billion yrs

DESI already has > 10 million spectra

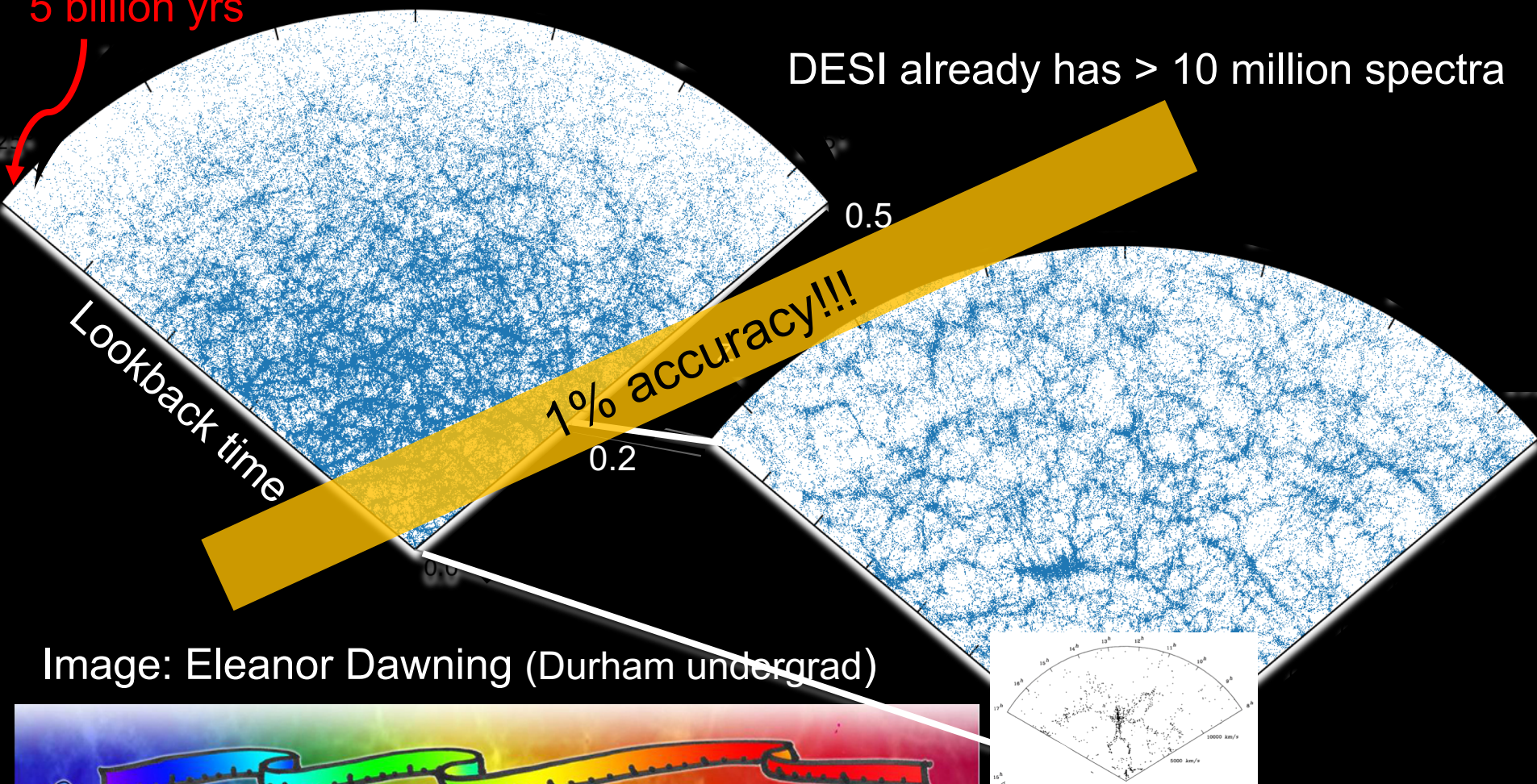


Image: Eleanor Dawning (Durham undergrad)

Dark Energy Spectroscopic Instrument



The figure displays a comparison between real and simulated galaxy distributions. The top half, labeled 'real', shows four sectors of the sky filled with blue dots representing galaxies. These sectors are labeled: 'SDSS' (top right), 'Sloan Great Wall' (top left), '2dFGRS' (bottom left), and 'CfA' (bottom right). The bottom half, labeled 'simulated', shows four corresponding sectors filled with red dots, labeled 'Millennium Simulation'. The sectors are arranged in a circular pattern around a central point. The axes for the simulated sectors are labeled: 'redshift  $z$ ' (0.05 to 0.20), 'lookback time in billion years' (0.5 to 1.5), and 'peculiar velocity  $cz$  [km/s]' (5000 to 25000). The real sectors also have axes for 'redshift  $z$ ' and 'lookback time in billion years'. The distribution of galaxies in both real and simulated data shows a clear filamentary structure, with galaxies concentrated along lines and planes, indicating a highly non-uniform distribution of matter in the universe.

simulated

Springel, Frenk & White  
Nature, April '06





STARS

NEUTRINOS

Neutrinos make  
up  $< 1\%$  of total  
dark matter

Can simulate their  
distribution with 1%  
accuracy

DESI may be able to measure the mass of the neutrino

GAS

CDM

200 Mpc

Elbers, Frenk, Jenkins, Li,  
Pascoli '23





# $\Lambda$ CDM

Basic ideas proposed in 1980s

- Cosmic structure forms from primordial **quantum fluctuations** from inflation amplified by gravity of **dark matter** (DM)
- N-body simulations compared to large-scale structure data
  - **neutrinos** are **not** bulk of DM
  - **CDM** promising
- $\delta T/T$ -fluctuations in **CMB** (→ **DM**, Flatness →  $\Lambda$ ) →  **$\Lambda$ CDM**
- Impressive **agreement**: modern **simulations** & **galaxy surveys**
- $\Lambda$  first appeared in '90s for CDM to agree **galaxy distribution**
- Era of **1% accuracy** is here: test  **$\Lambda$ CDM** + measure  $\nu$  **mass**

# Observational tests of $\Lambda$ CDM

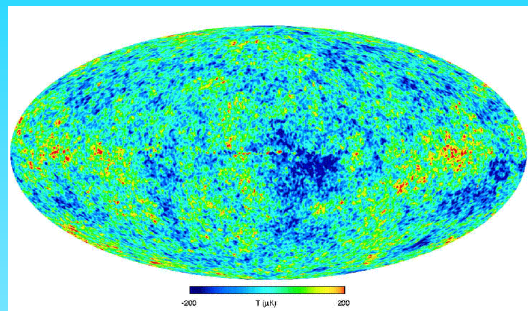
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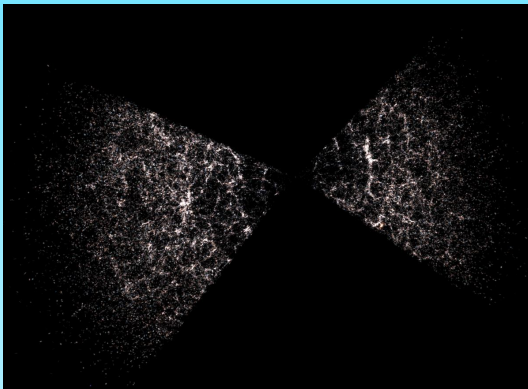
**Linear regime:** cosmic microwave background  
large-scale structure



# The cosmic power spectrum: from the CMB to the 2dFGRS



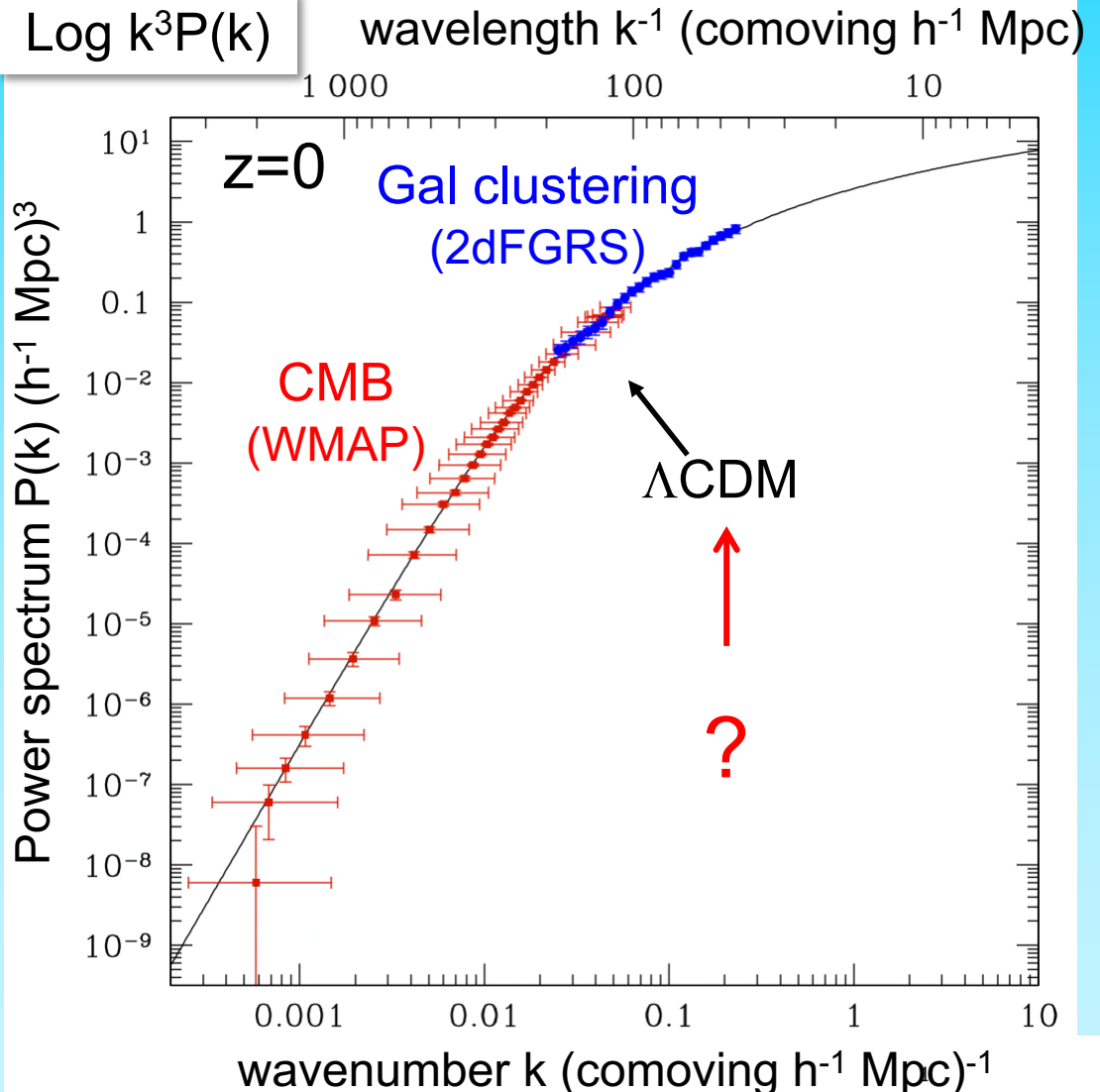
$z \sim 1000$



$z \sim 0$

⇒  $\Lambda$ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06





# The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming →

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

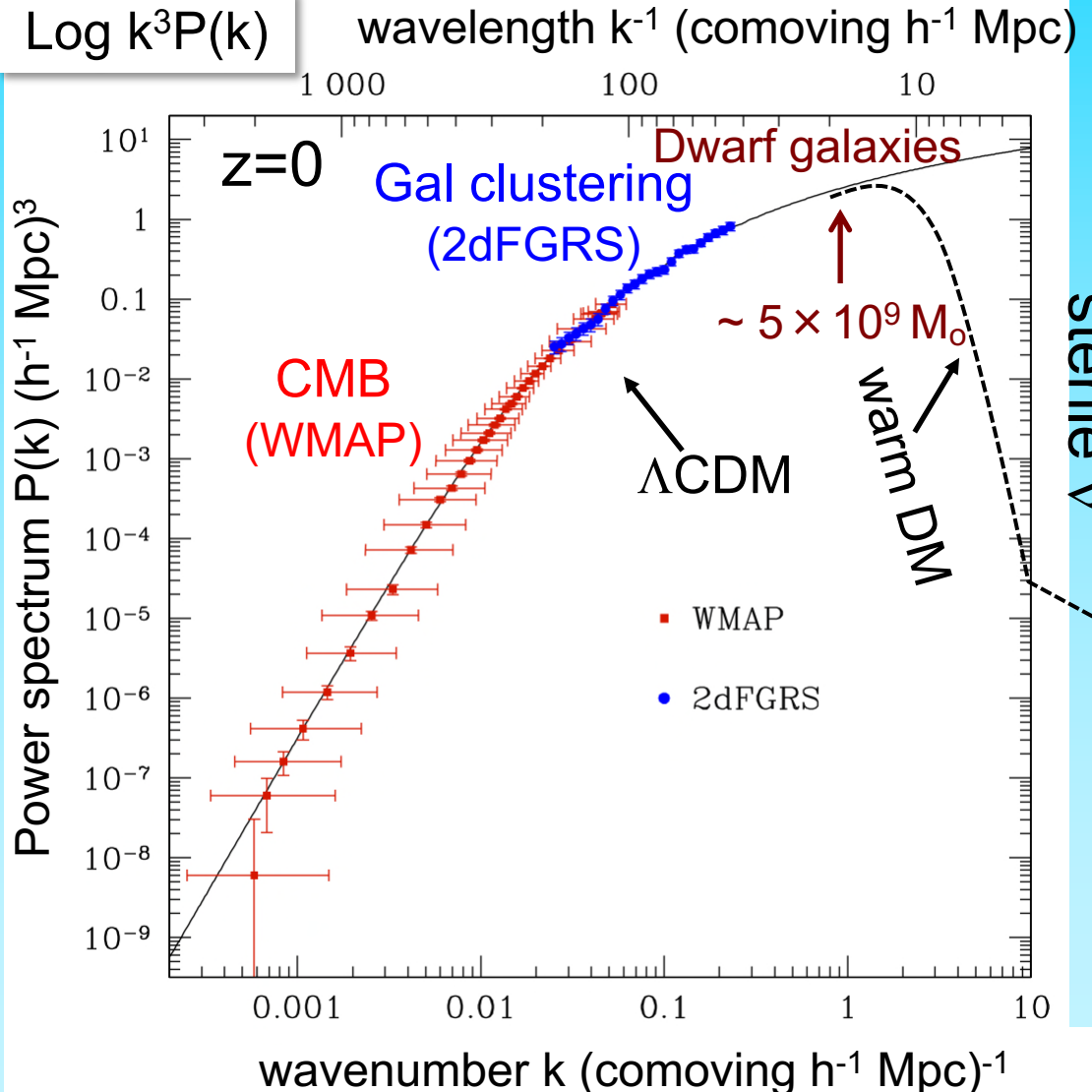
for thermal relic

$$m_{\text{CDM}} \sim 100 \text{ GeV}$$

$$\text{susy}; M_{\text{cut}} \sim 10^{-6} M_{\odot}$$

$$m_{\text{WDM}} \sim \text{few keV}$$

$$\text{sterile } \nu; M_{\text{cut}} \sim 10^9 M_{\odot}$$



## Explain:

- Neutrino oscillations and masses
- Baryogenesis
- Absence of right-handed neutrinos in standard model
- Dark matter

## Sterile neutrino minimal standard model ( $\nu$ MSM; Boyarski+ 09):

- Extension of SM w. 3 sterile neutrinos: 2 of GeV; 1 of keV mass
- If  $\Omega_N = \Omega_{DM}$ , 2 parameters: mass, lepton asymmetry/mixing angle
- GeV particles may be detected at CERN (SHiP)
- Dark matter candidate can be detected by X-ray decay

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Can test this in **two regimes**:

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large-scale structure ✓

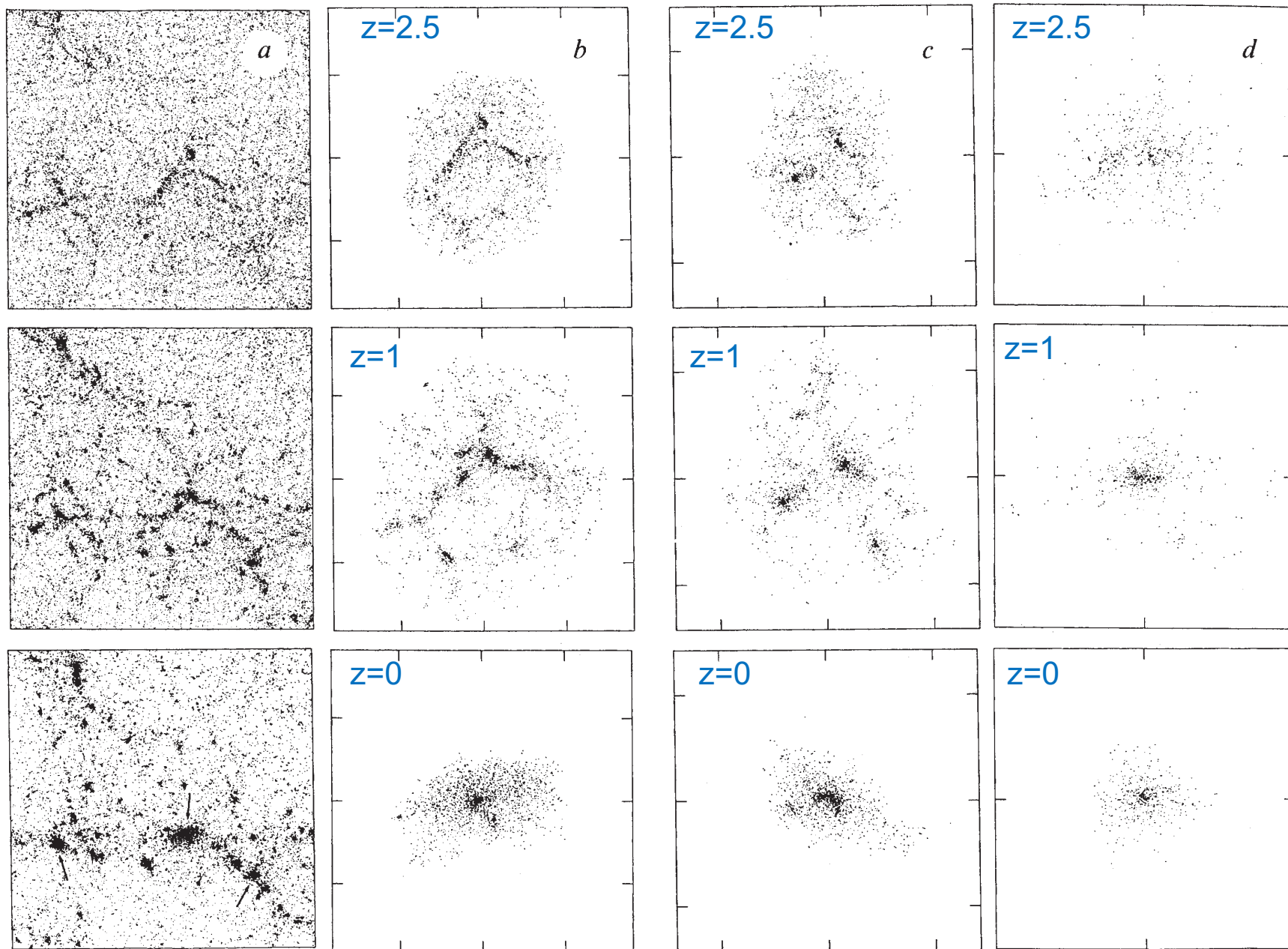
**Evolved non-linear regime:** dark matter halos →

- abundance
- structure
- clustering



Fig. 1

## Formation of CDM halos



Frenk et al 1985



We now know:

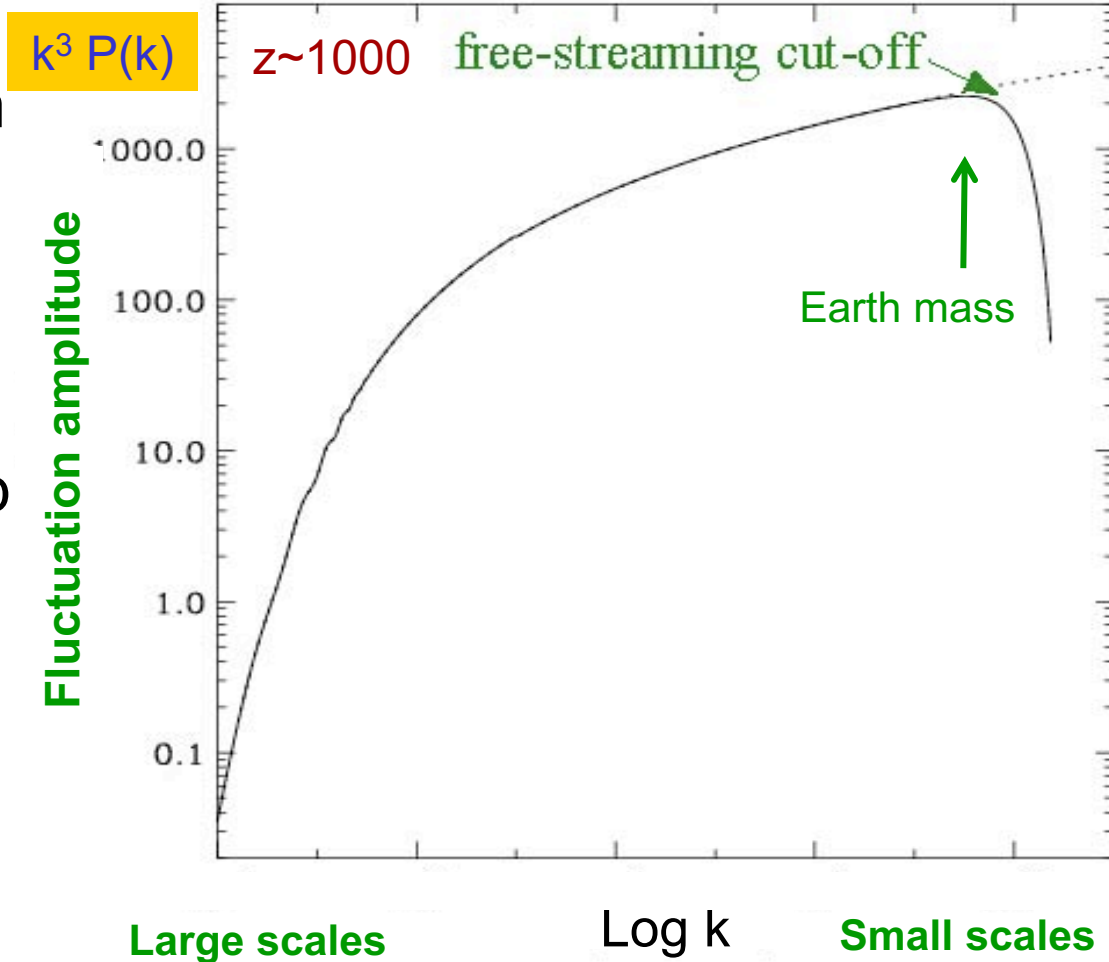
- halo mass function down to cutoff mass
- the internal structure of halos of all mass



# The cold dark matter power spectrum

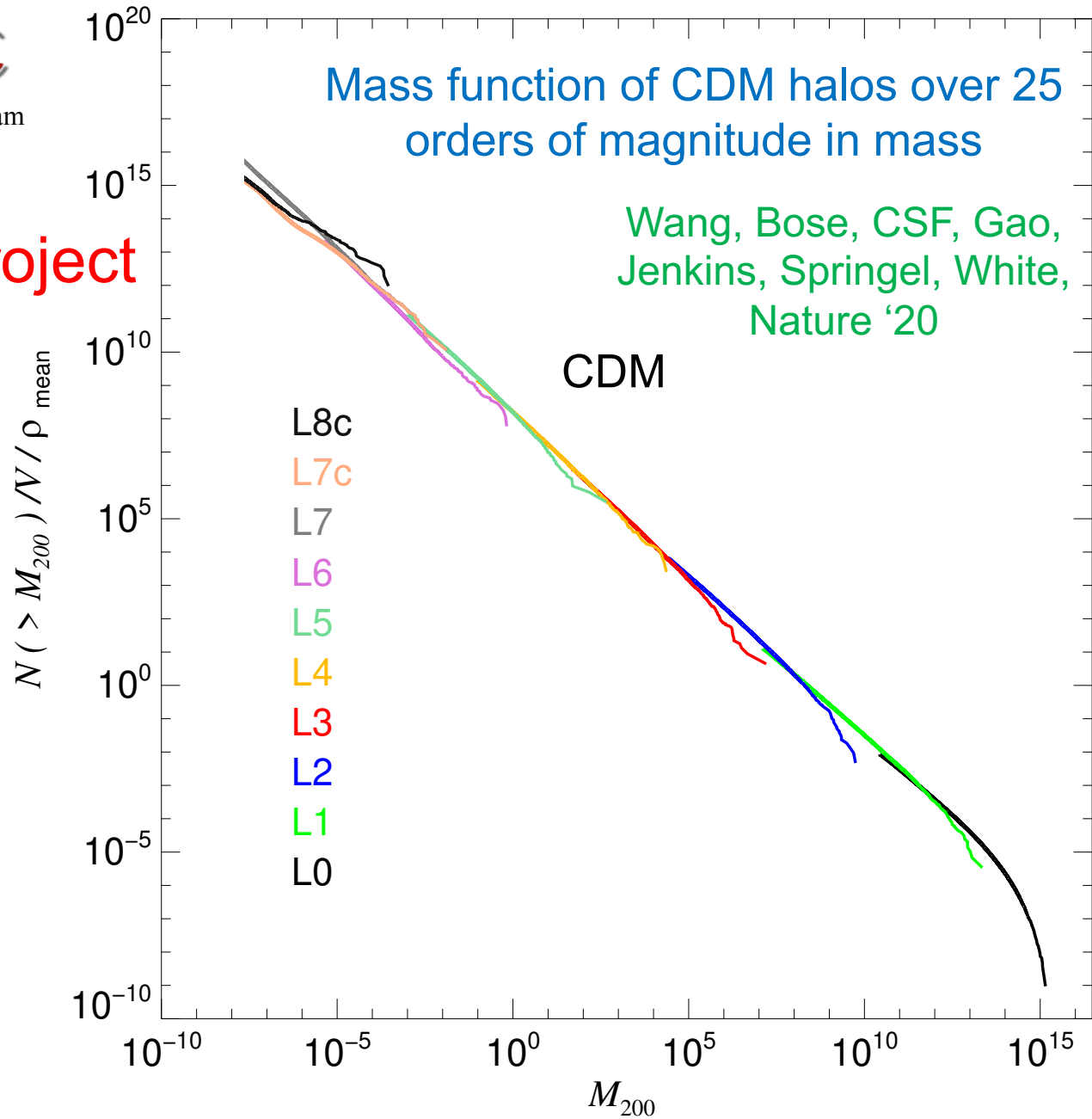
The linear power spectrum  
("power per octave")

Assumes a 100GeV wimp  
Green et al '04

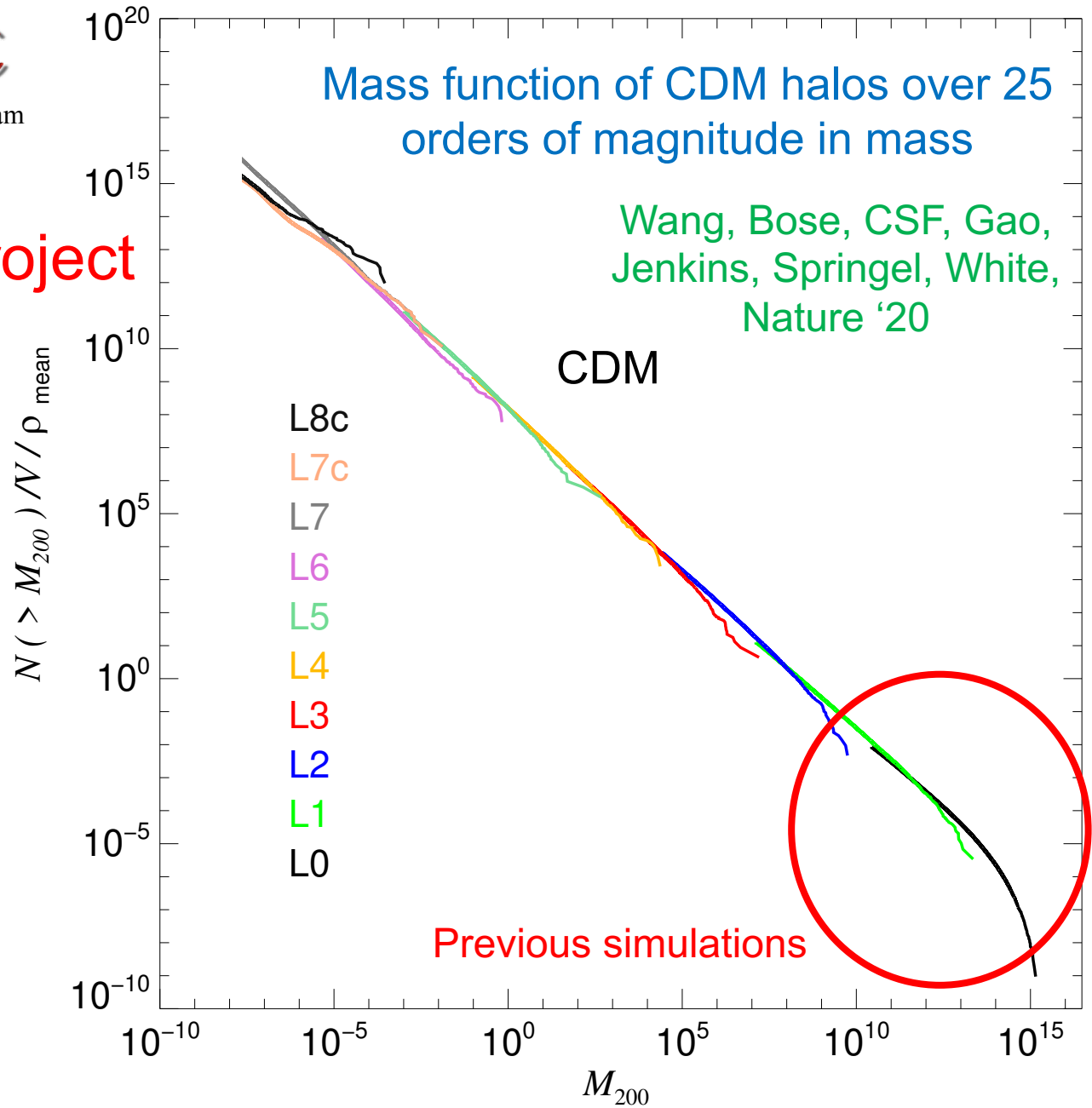




# The VVV project



# The VVV project





# The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of  
30 orders of  
magnitude in mass

$$M_{\text{char}} = 10^{14} M_{\odot}$$

**Base Level**

**L0**

**150 Mpc**



# The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of  
30 orders of  
magnitude in mass

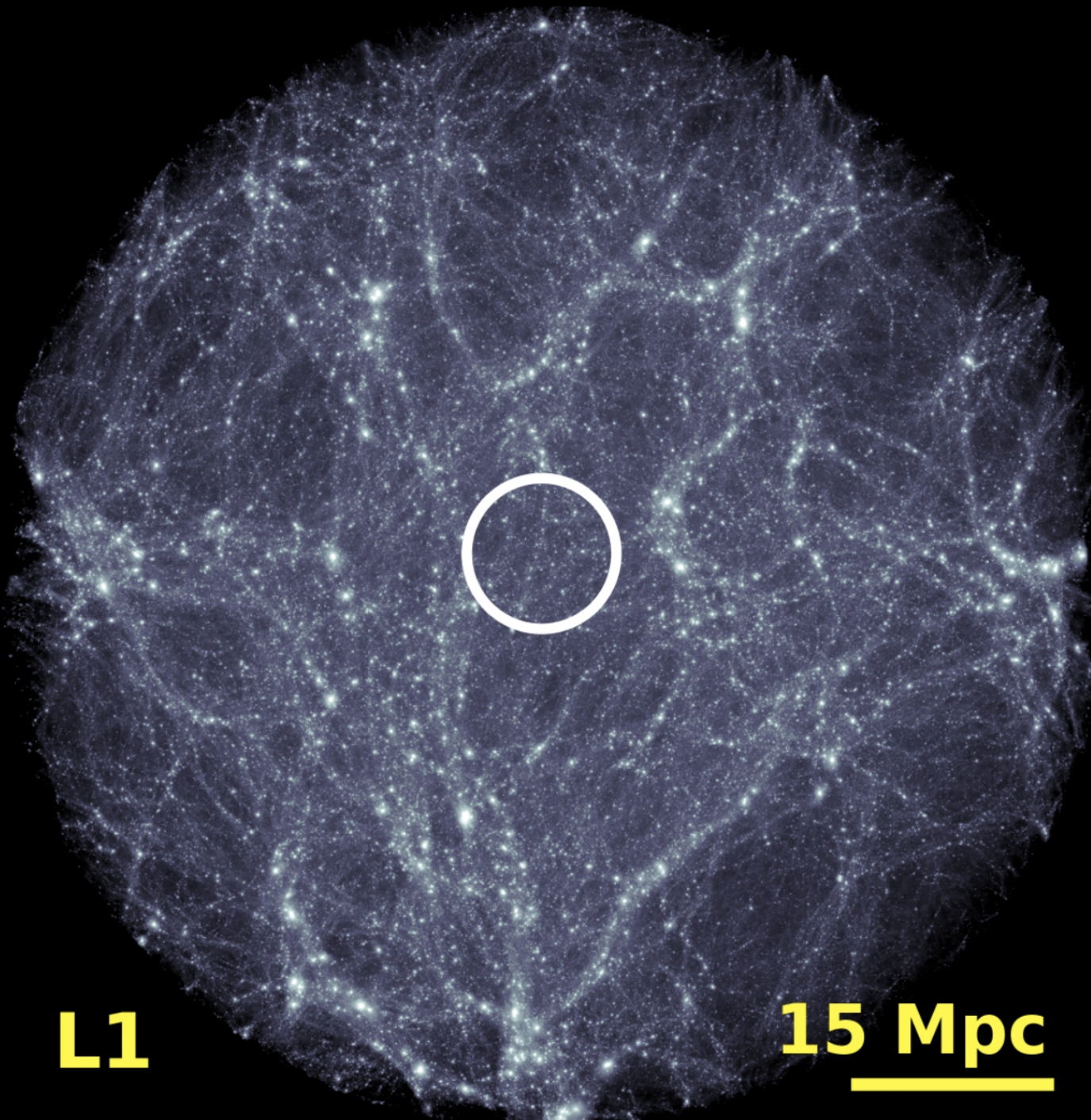
$$M_{\text{char}} = 10^{12} M_{\odot}$$

**Zoom Level 1**

**L1**

**15 Mpc**

Wang, Bose et al 2020





# The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of  
30 orders of  
magnitude in mass

$$M_{\text{char}} = 10^9 M_{\odot}$$

**Zoom Level 2**

**L2**

**1 Mpc**

Wang, Bose et al 2020



# The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of  
30 orders of  
magnitude in mass

$$M_{\text{char}} = 10^6 M_{\odot}$$

**Zoom Level 3**

**L3**

**150 kpc**

Wang, Bose et al 2020

# The VVV simulation

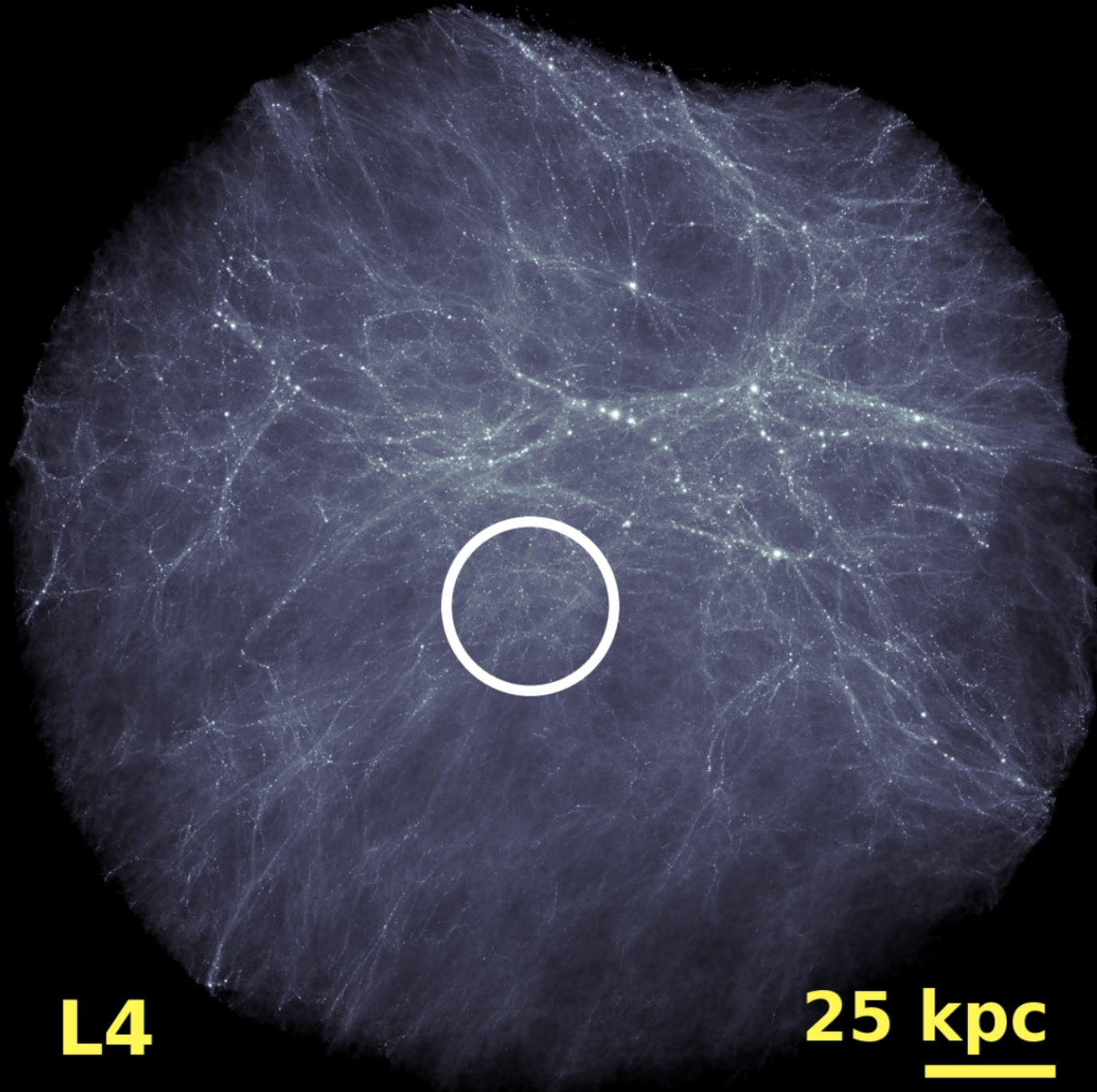
Planck cosmology

Dark matter only

Dynamic range of  
30 orders of  
magnitude in mass

$$M_{\text{char}} = 10^3 M_{\odot}$$

**Zoom Level 4**



**L4**

**25 kpc**

Wang, Bose et al 2020



# The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of  
30 orders of  
magnitude in mass

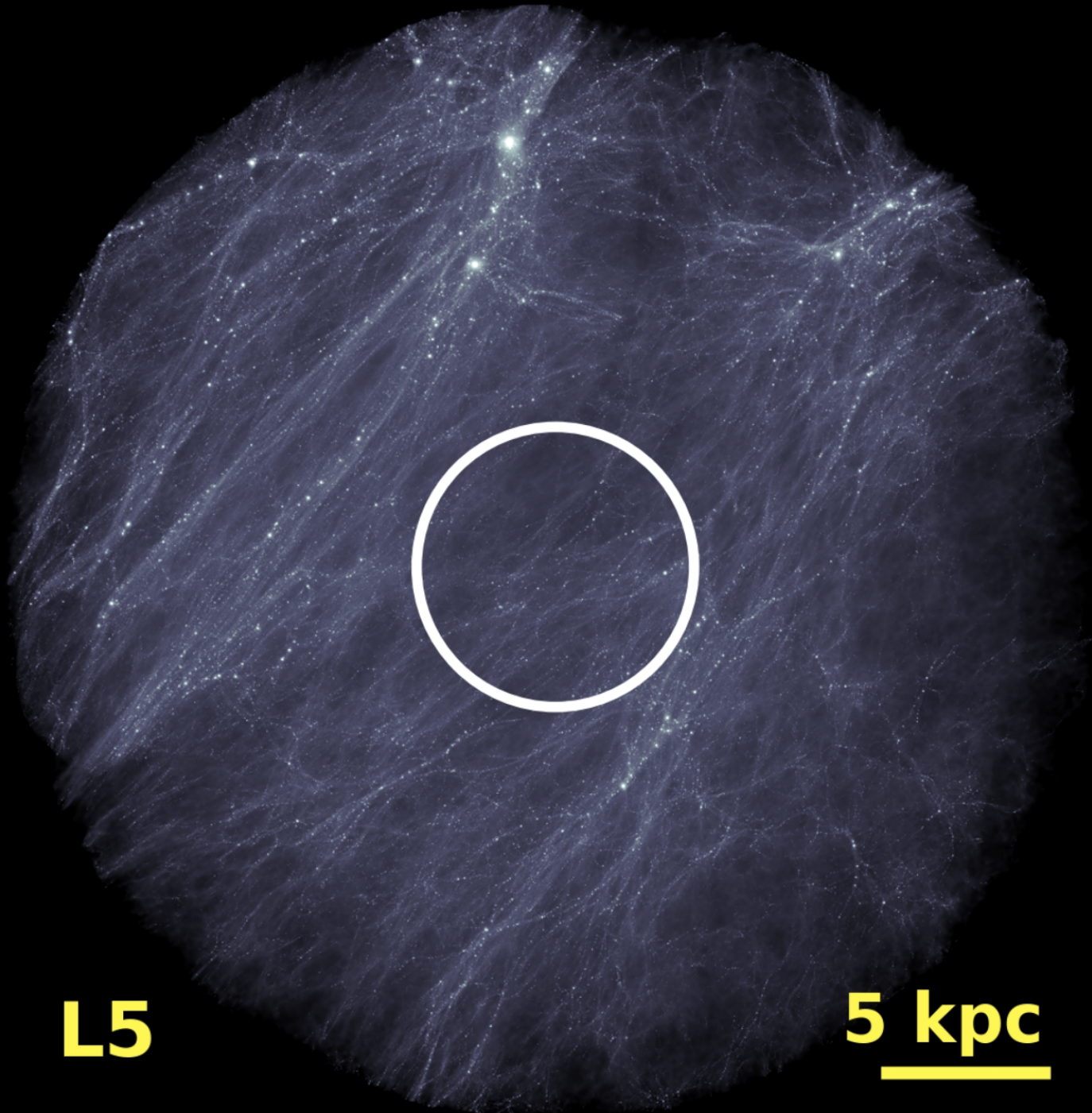
$$M_{\text{char}} = 10 M_{\odot}$$

**Zoom Level 5**

**L5**

**5 kpc**

Wang, Bose et al 2020



# The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of  
30 orders of  
magnitude in mass

$$M_{\text{char}} = 10^{-1} M_{\odot}$$

**Zoom Level 6**

**L6**

**1 kpc**

Wang, Bose et al 2020



# The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of  
30 orders of  
magnitude in mass

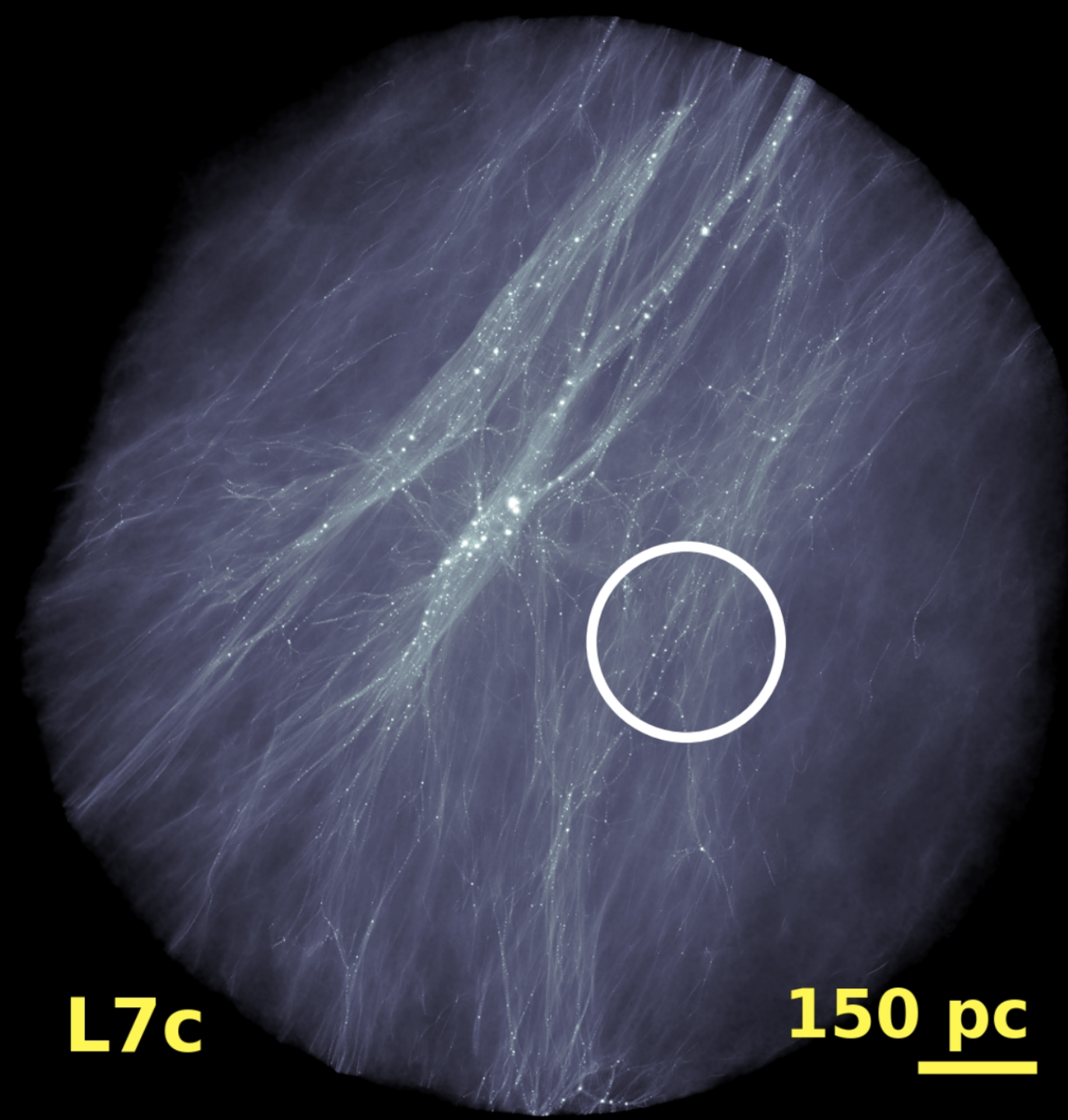
$$M_{\text{char}} = 10^{-4} M_{\odot}$$

**Zoom Level 7**

**L7c**

**150 pc**

Wang, Bose et al 2020



# The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of  
30 orders of  
magnitude in mass

$$M_{\text{char}} = 10^{-6} M_{\odot}$$

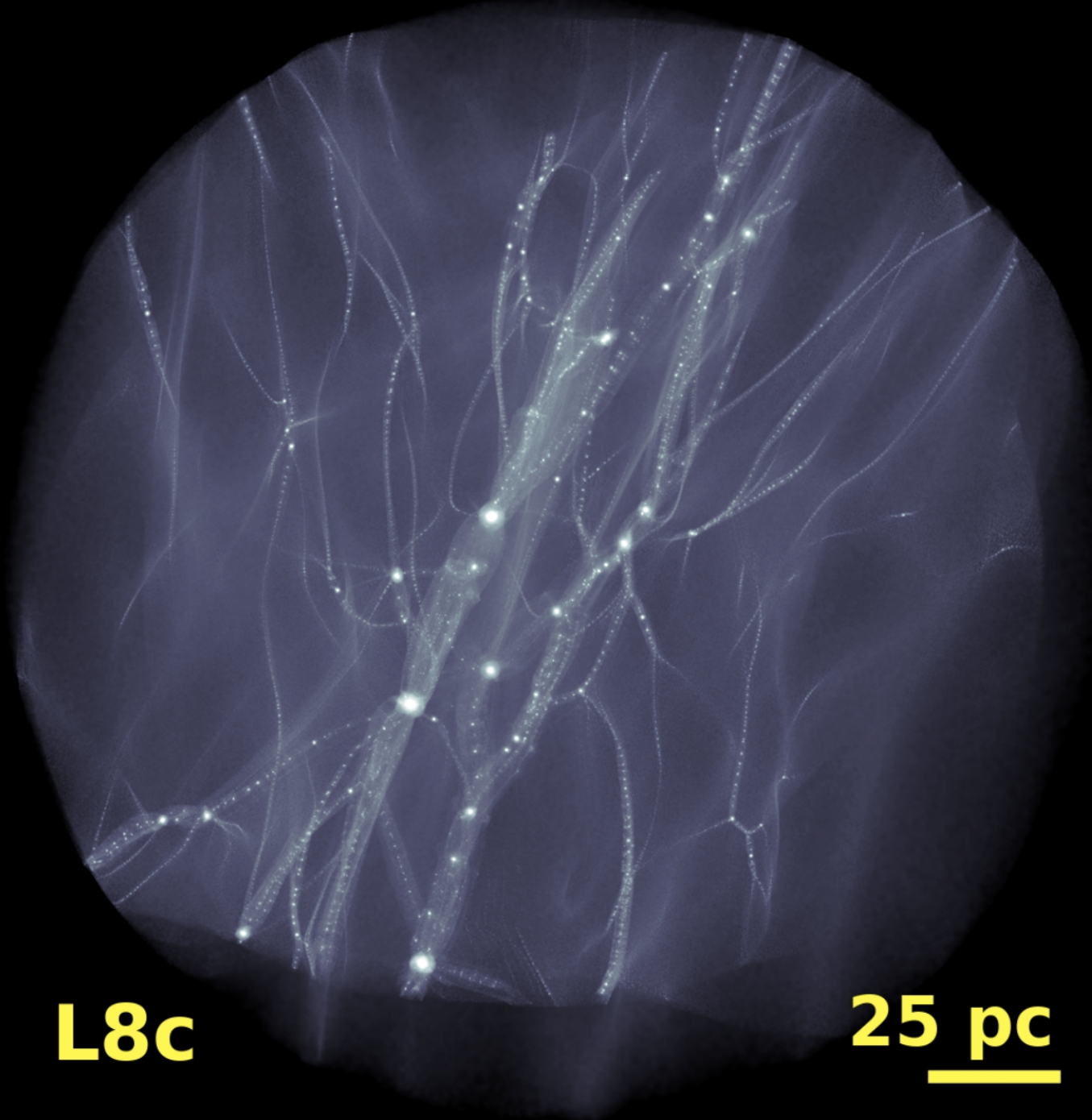
**Zoom Level 8**

The density of  
this region is  
only  $\sim 3\%$  of the  
cosmic mean

Wang, Bose et al 2020

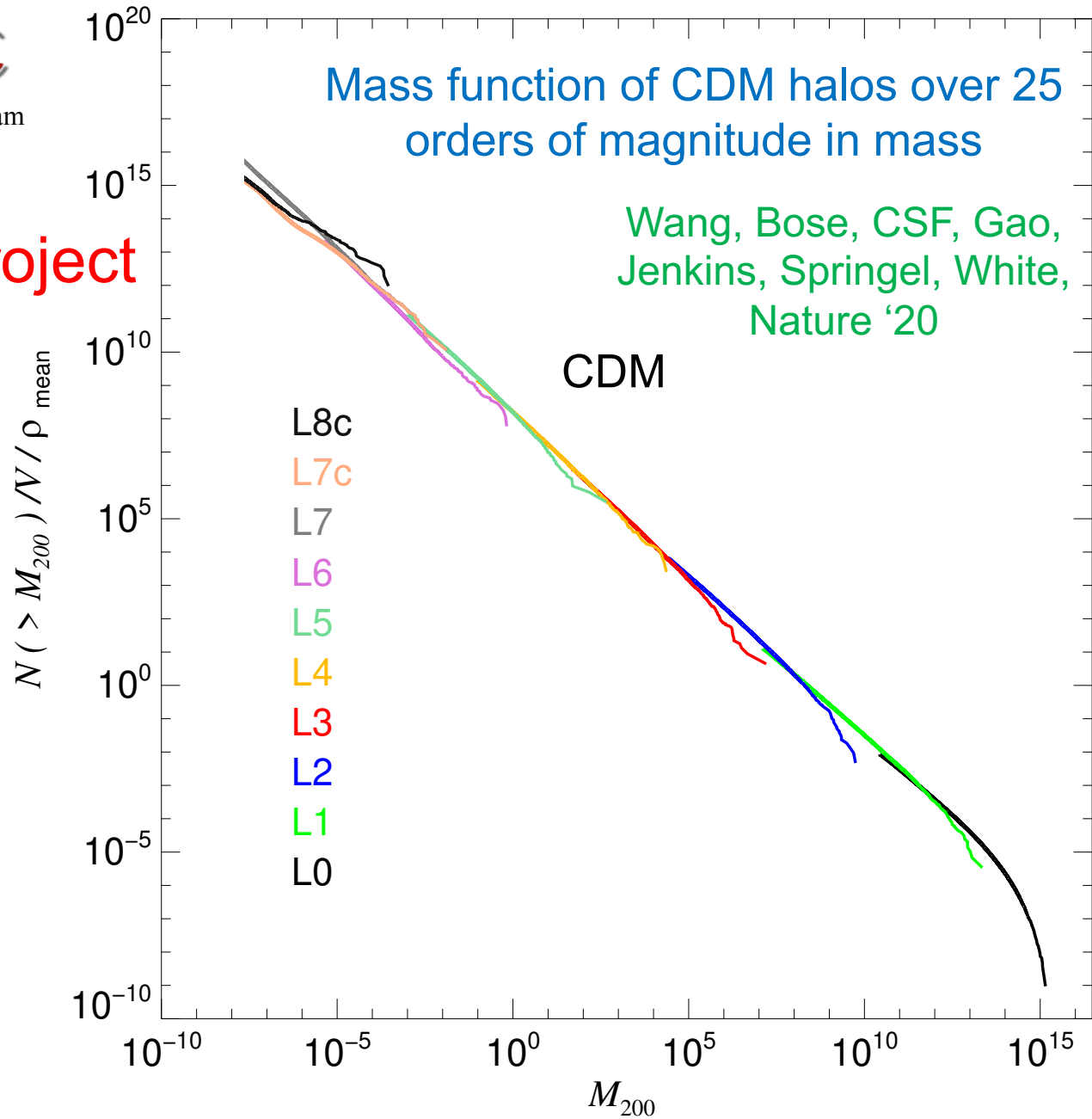
**L8c**

**25 pc**

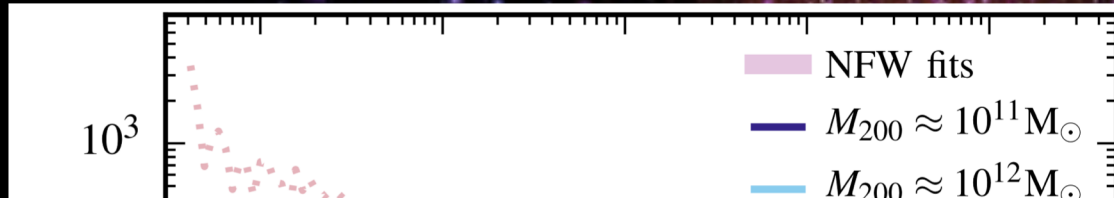




# The VVV project



# The density profile of cold dark matter halos



Shape of halo profiles  
~independent of halo mass & parameters

are “cuspy” -  
high density at the centre

formula:

$$\frac{\delta_c}{(1 + r/r_s)^2}$$

(White '97)

halos and  
earlier have  
higher densities (bigger  $\delta$ )



# Universal halo density profiles

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

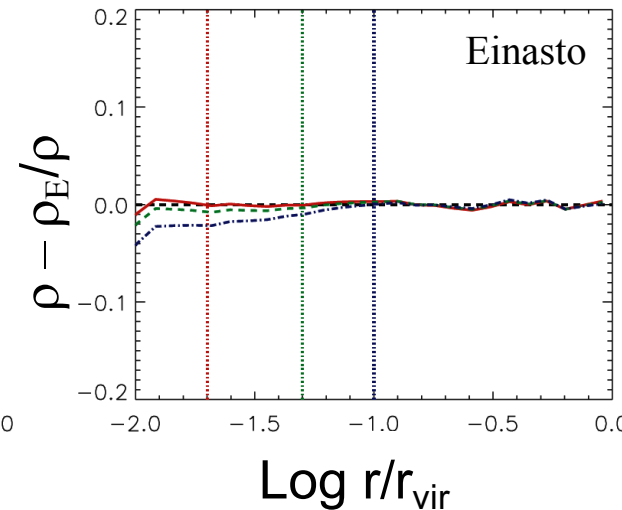
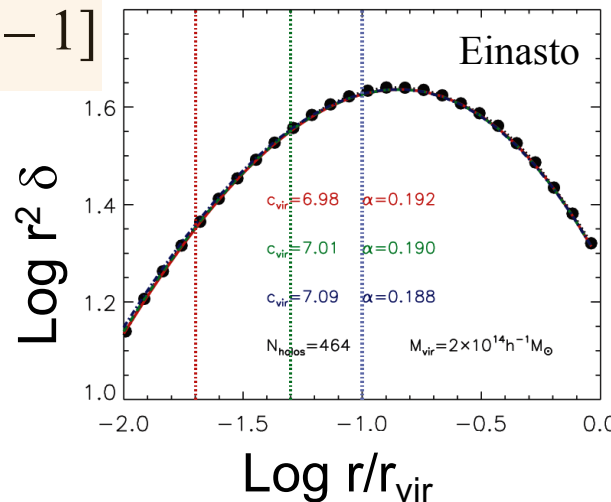
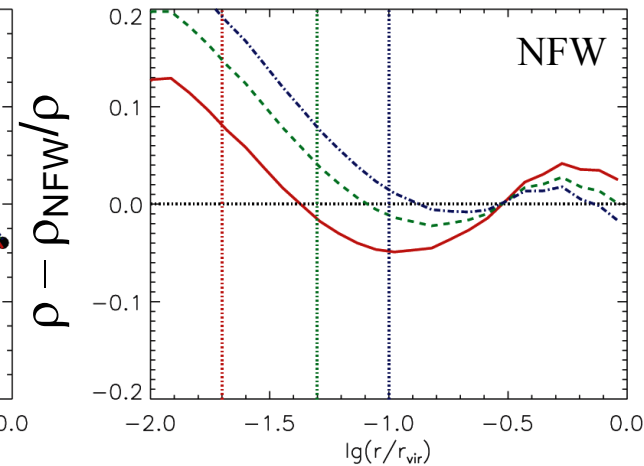
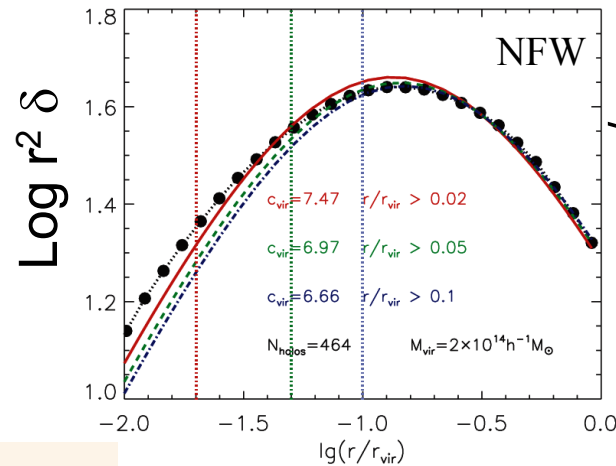
The “Einasto” formula

$$\ln(\rho(r)/\rho_{-2}) = (-2/\alpha) [(r/r_{-2})^\alpha - 1]$$

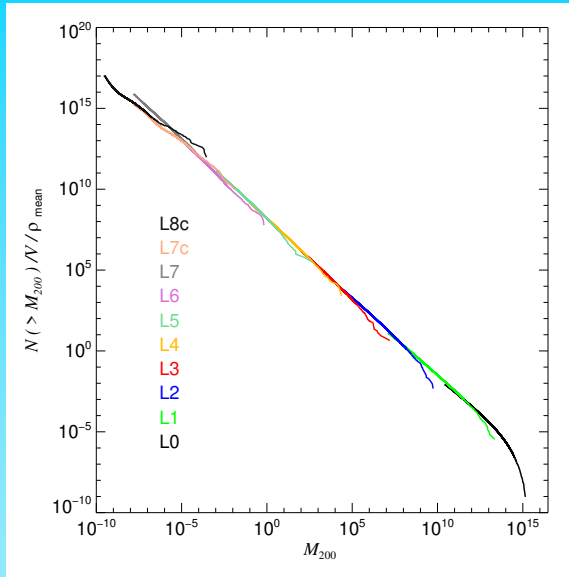
Fits mean profiles  
even better

Gao, N, F, W + 2008

Averaged cluster mass halos fit with NFW and Einasto

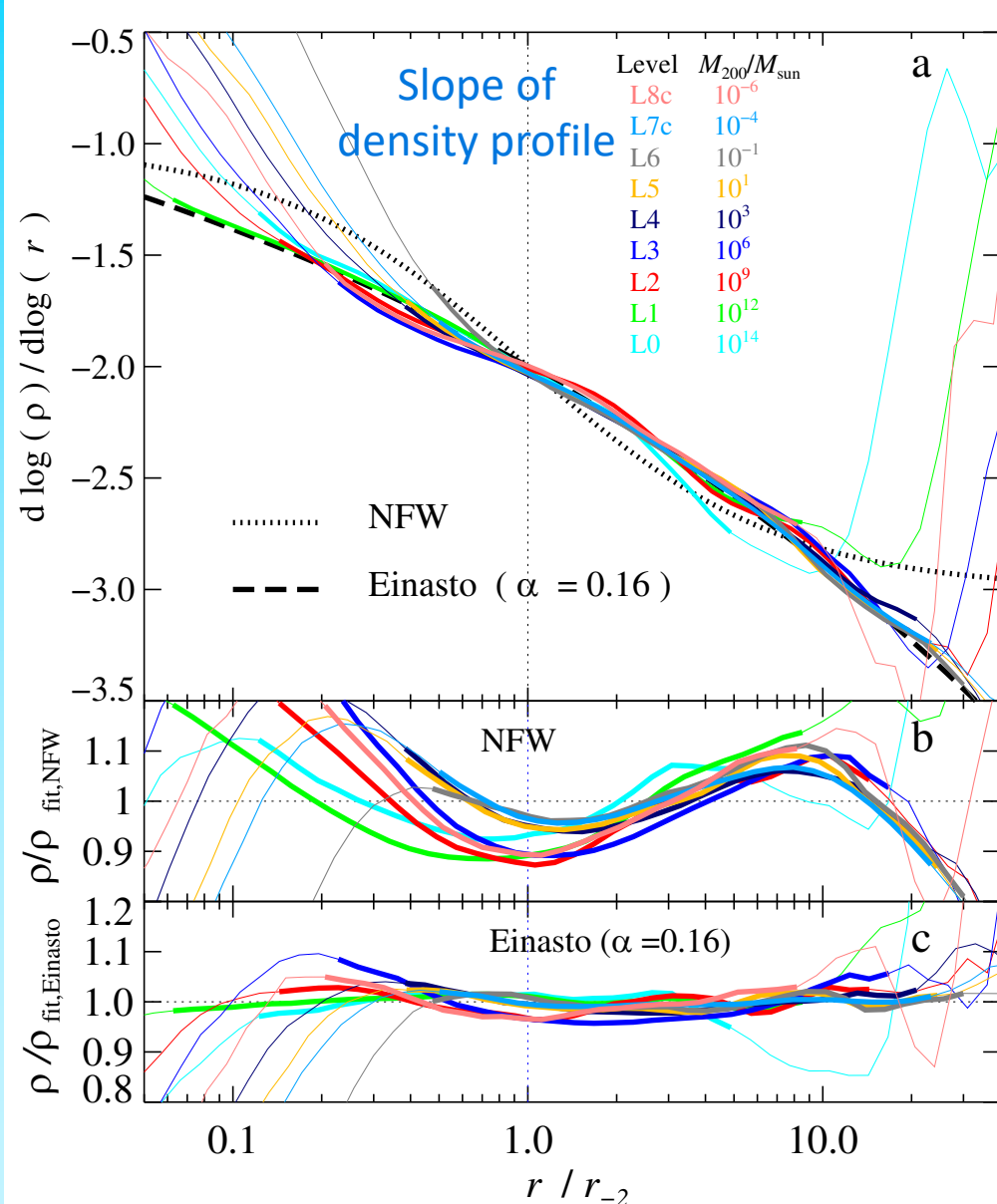


# Density profiles of ALL halos



Over **20 orders** of magnitude in halo **mass** and 4 orders of magnitude in density, the mean density **profiles** of halos are **fit** by **NFW** to within **20%** and by **Einasto** ( $\alpha = 0.16$ ) to within **7%**

Wang, Bose, CSF + '20





# Observational tests of $\Lambda$ CDM

## Fundamental prediction of $\Lambda$ CDM

→ Primordial PS of density perturbations + random phases

Can test this in **two regimes**:

**Linear regime:** cosmic microwave background  
large-scale structure

**Evolved non-linear regime:** dark matter halos →

- abundance
- structure
- clustering

# A galaxy formation primer

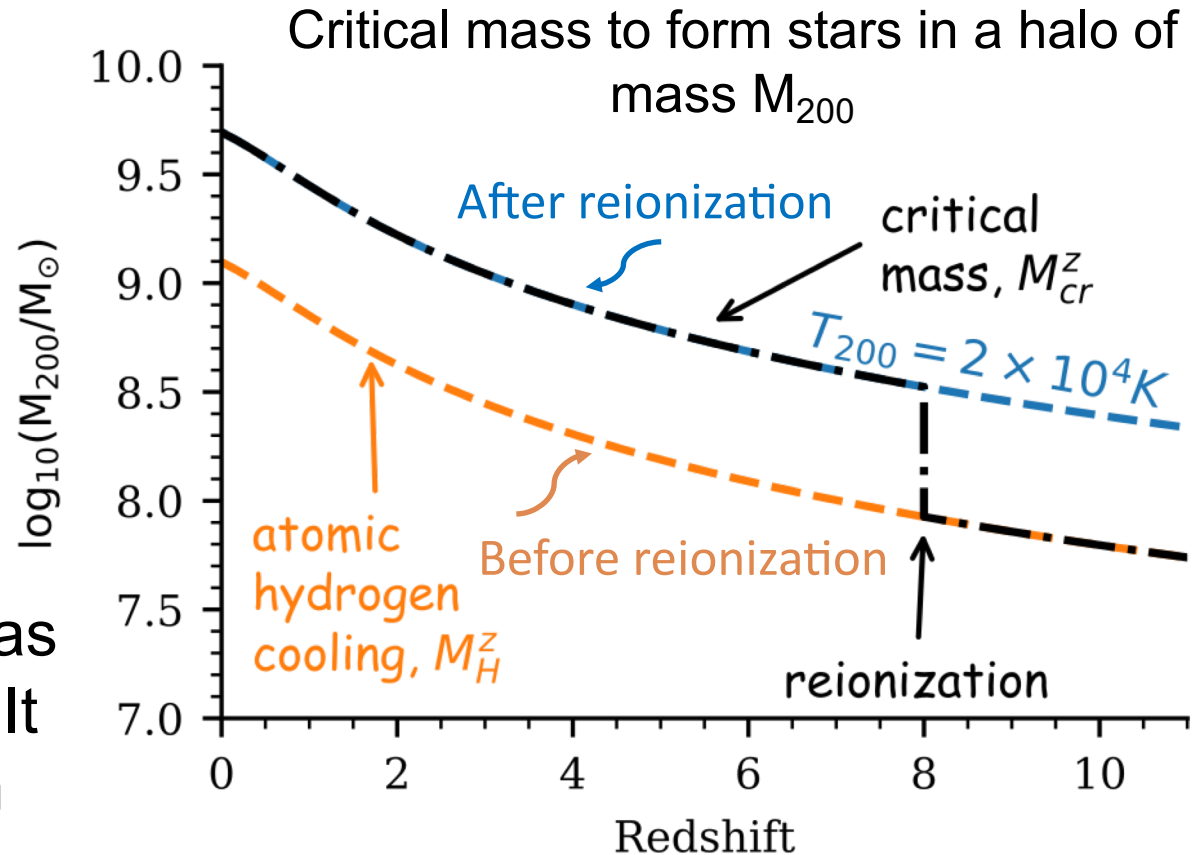
In which halos do galaxy form?

1. Before reionization, stars can only form if atomic H cooling is effective:  $\rightarrow T > 7000 \text{ K}$

$$M_H^z \sim (4 \times 10^7 M_\odot) \left( \frac{1+z}{11} \right)^{-3/2}$$

2. After H reionization, gas is heated to  $T = 2 \times 10^4 \text{ K}$ . It can only cool and form stars in halos with:

$$T_{\text{vir}} > T_{\text{IGM}} = 2 \times 10^4 \text{ K}$$



Benitez-Llambay & CSF '20



# A galaxy formation primer

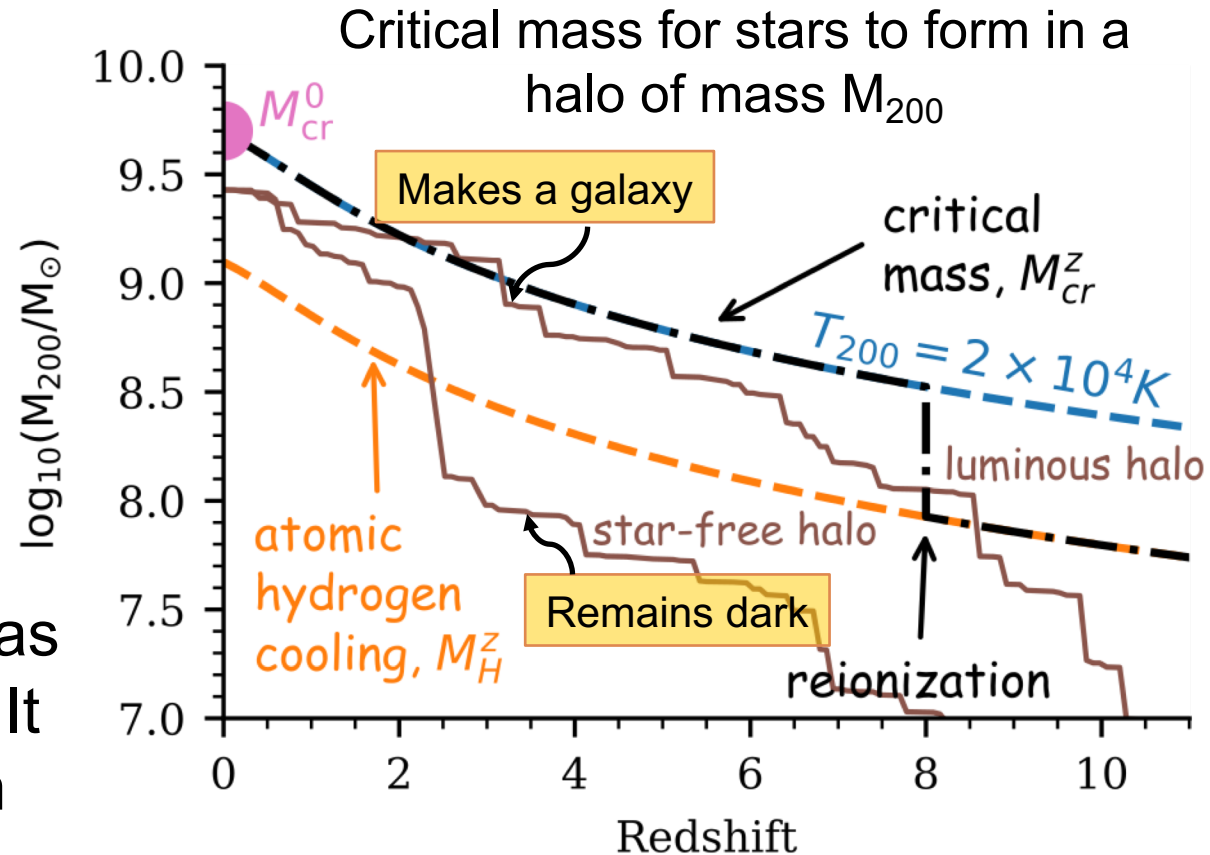
1. Before reionization, stars can only form if gas can cool for which

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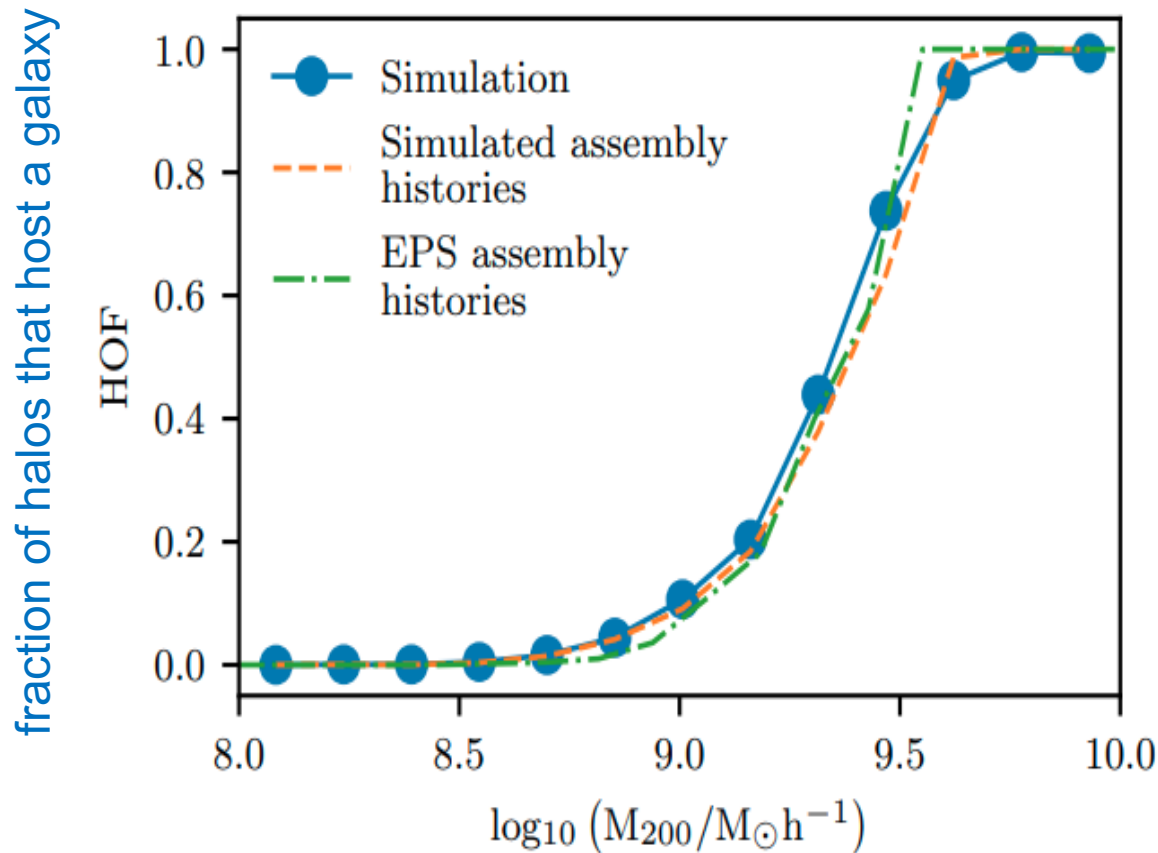
$$T_{\text{vir}} > T_{\text{IGM}} = 2 \times 10^4 \text{ K}$$



Benitez-Llambay & CSF '20

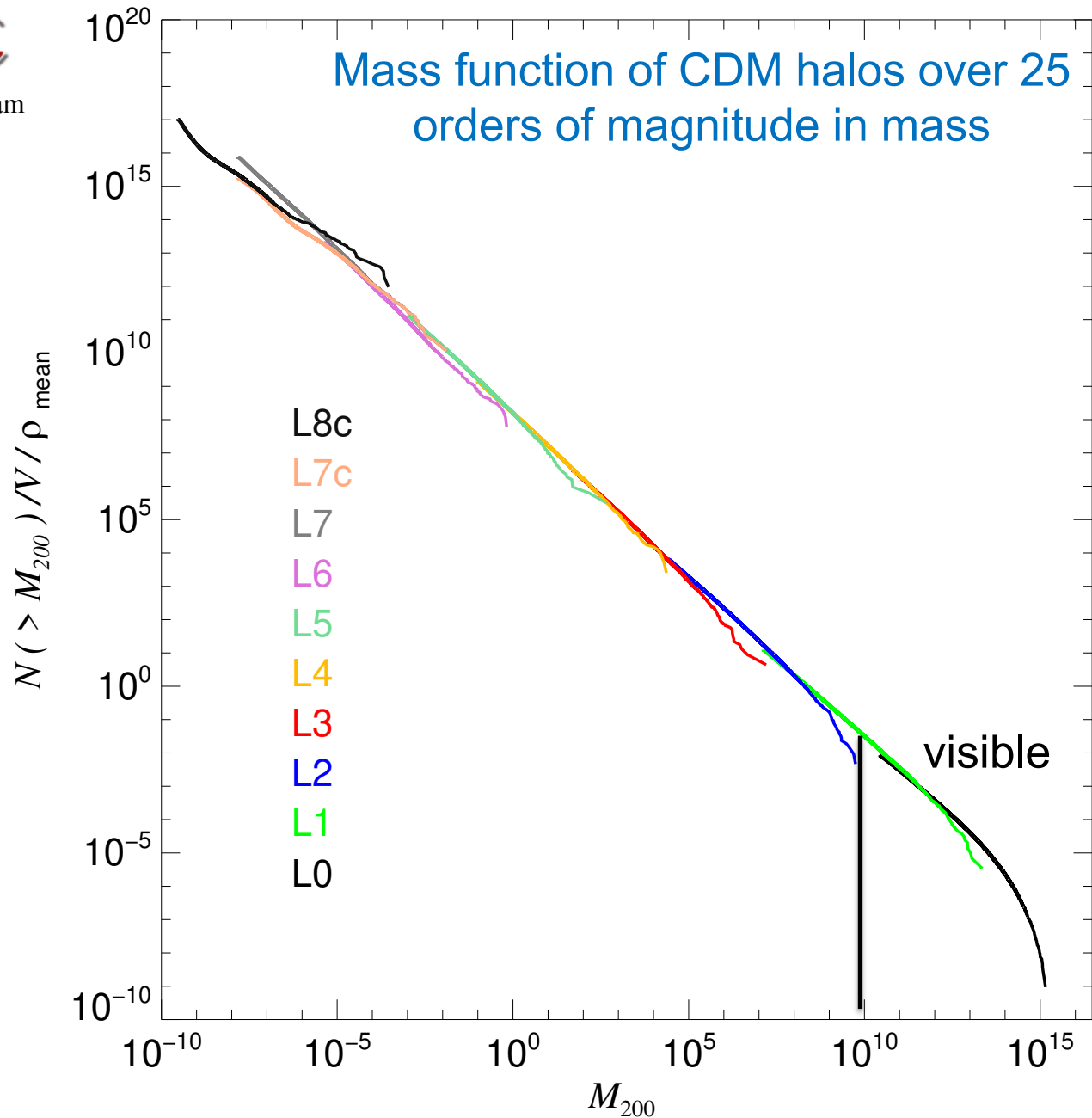
# A galaxy formation primer

Halo Occupation Fraction (HOF): fraction of halos of a given mass today that host a galaxy



$M < 3 \times 10^8 M_{\odot}$   
→ dark

$M > 3 \times 10^9 M_{\odot}$   
→ visible





# The small-scale “crisis”: four problems

“Solved” in:

- |                          |      |   |                |
|--------------------------|------|---|----------------|
| 1. “Missing satellites”  | 2002 | } | Baryon effects |
| 2. “Too-big-to-fail”     | 2015 |   |                |
| 3. “Core-cusp”           | 1996 |   |                |
| 4. “Plane of satellites” | 2023 |   |                |



# CDM

DM-only CDM simulations predict many more subhalos in the Milky Way than there are observed satellites

“Missing satellites” problem

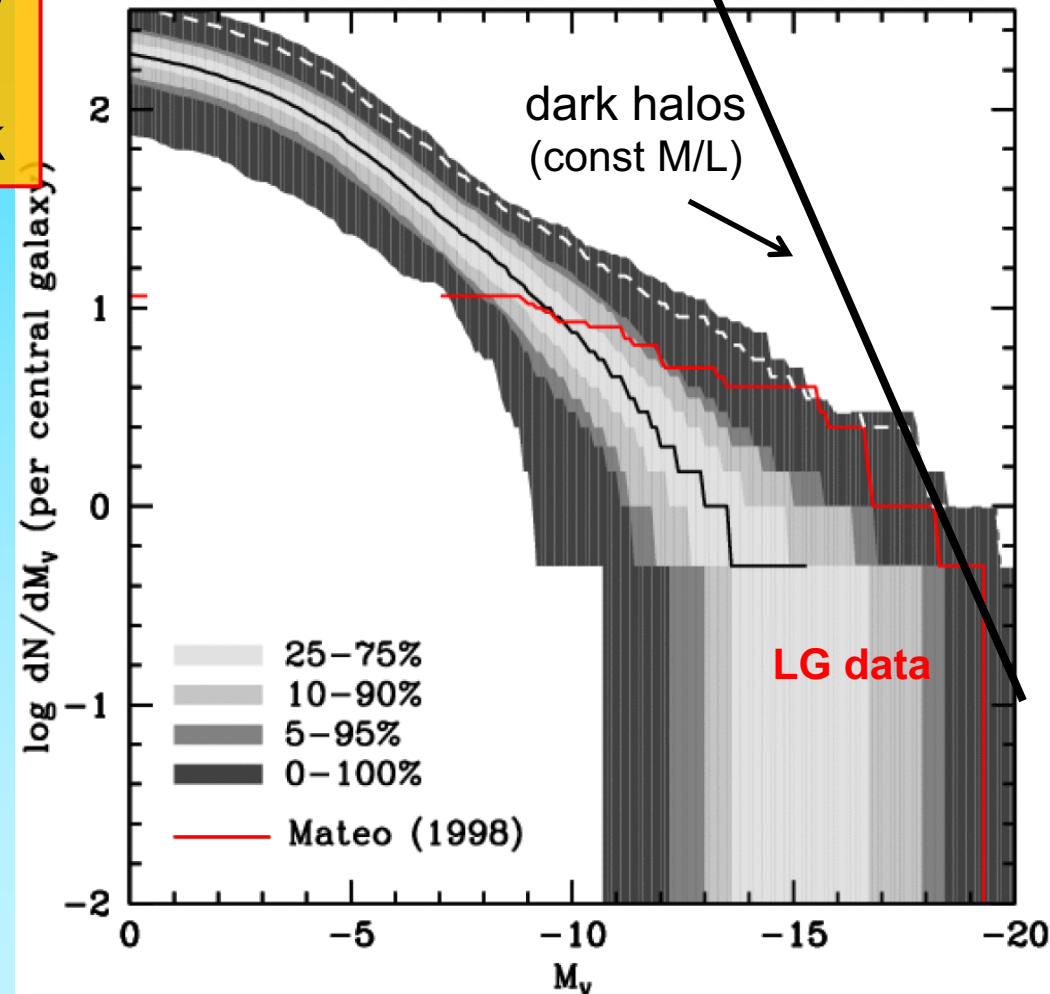
Most subhalos never make a galaxy!



# Luminosity Function of Local Group Satellites

Semi-analytic model of galaxy formation including effects of reionization and SN feedback

- Median model → correct abundance of sats brighter than  $M_V = -9$  ( $V_{\text{cir}} > 12$  km/s)
- Model predicts many, as yet undiscovered, faint satellites

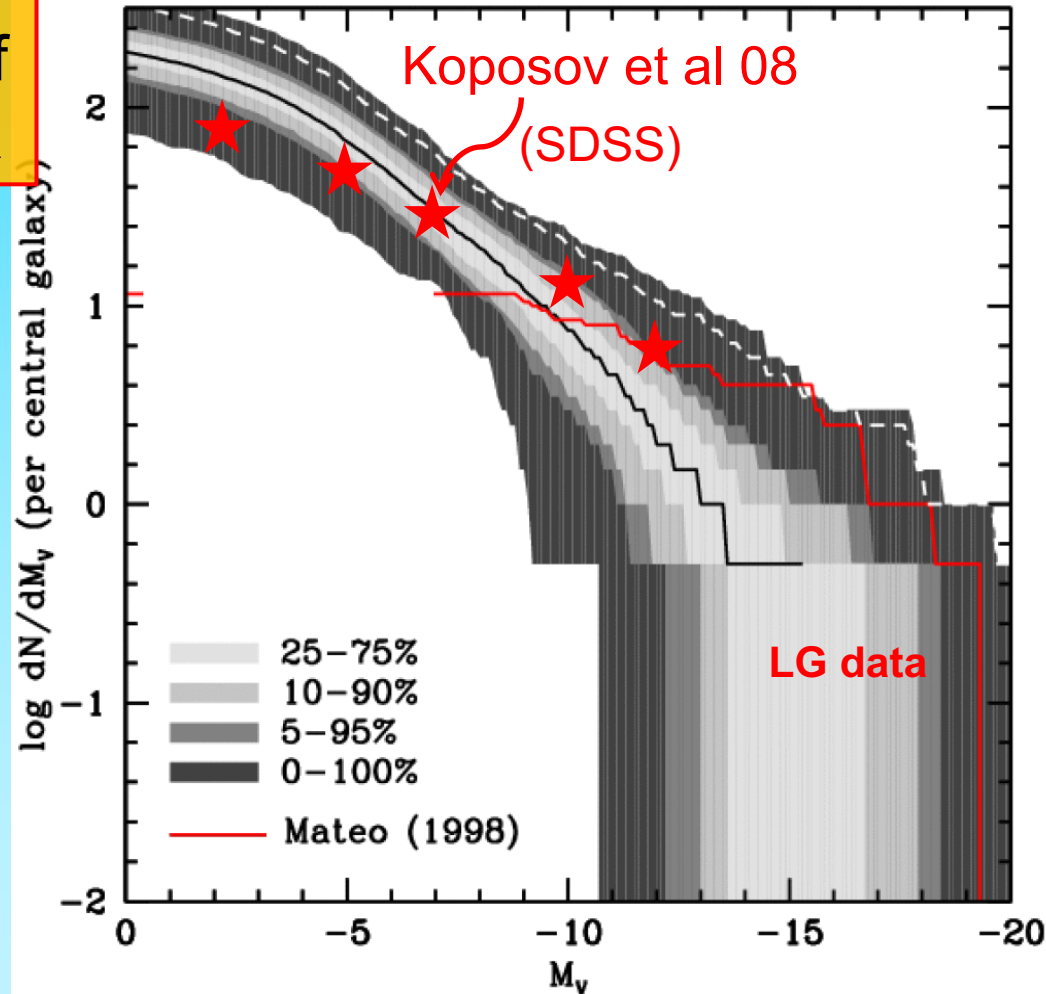




# Luminosity Function of Local Group Satellites

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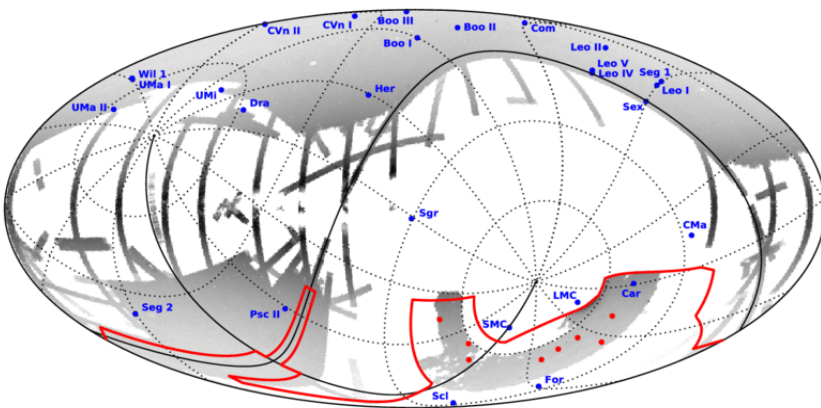


Benson, Frenk, Lacey, Baugh & Cole '02  
(see also Kauffman+ '93, Bullock+ '00, Somerville '02)

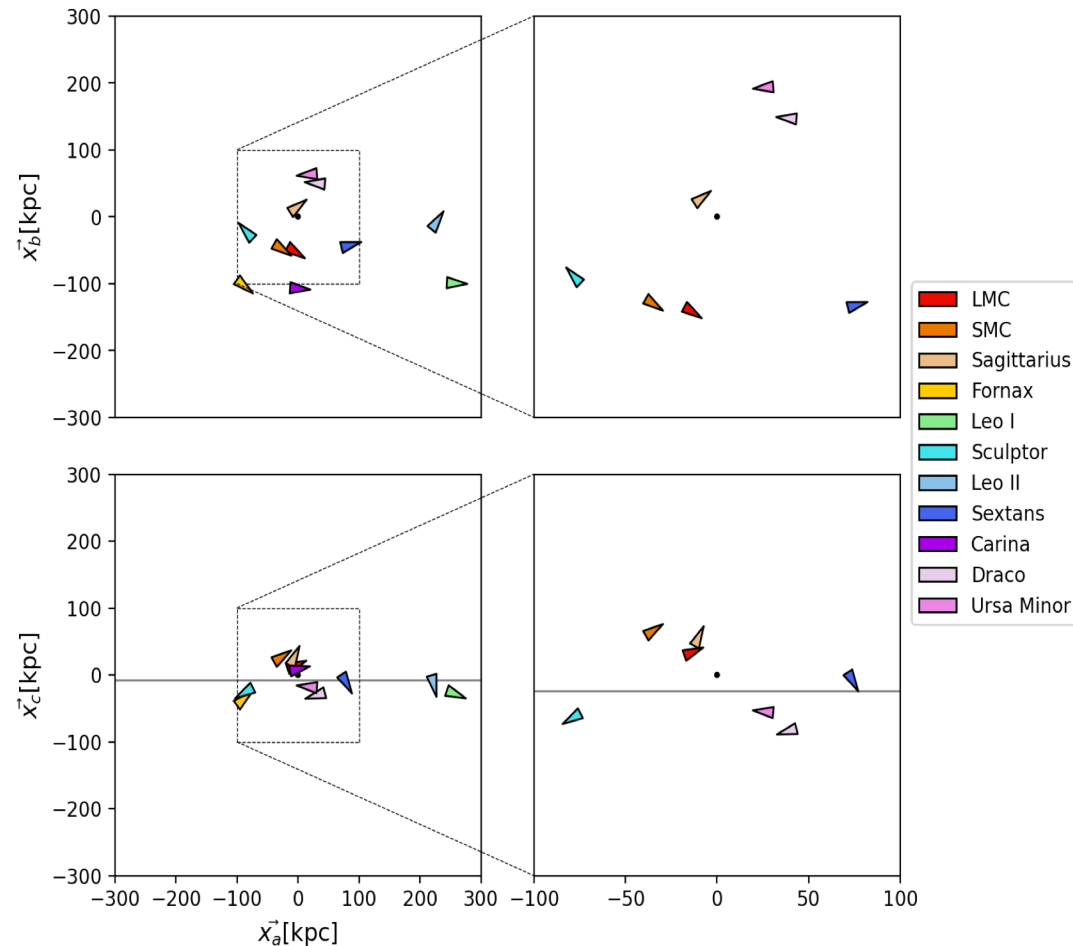
# The plane of satellites in the MW

# The plane of satellites in the MW

**Problem:** the 11 “classical” Milky Way satellites are in a thin, possibly rotating plane (Lynden-Bell 1976)



Bechtol+ 2015



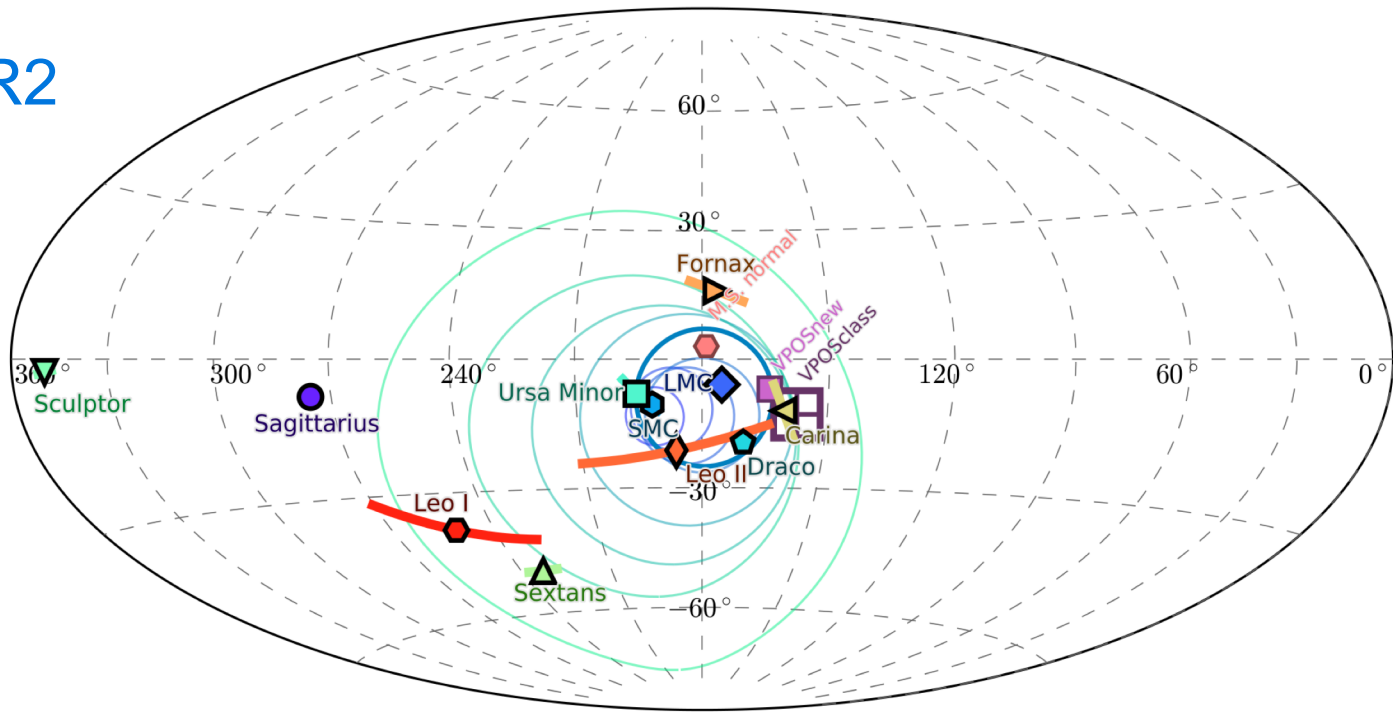


# The plane of satellites in the MW

The plane could be a spinning disk

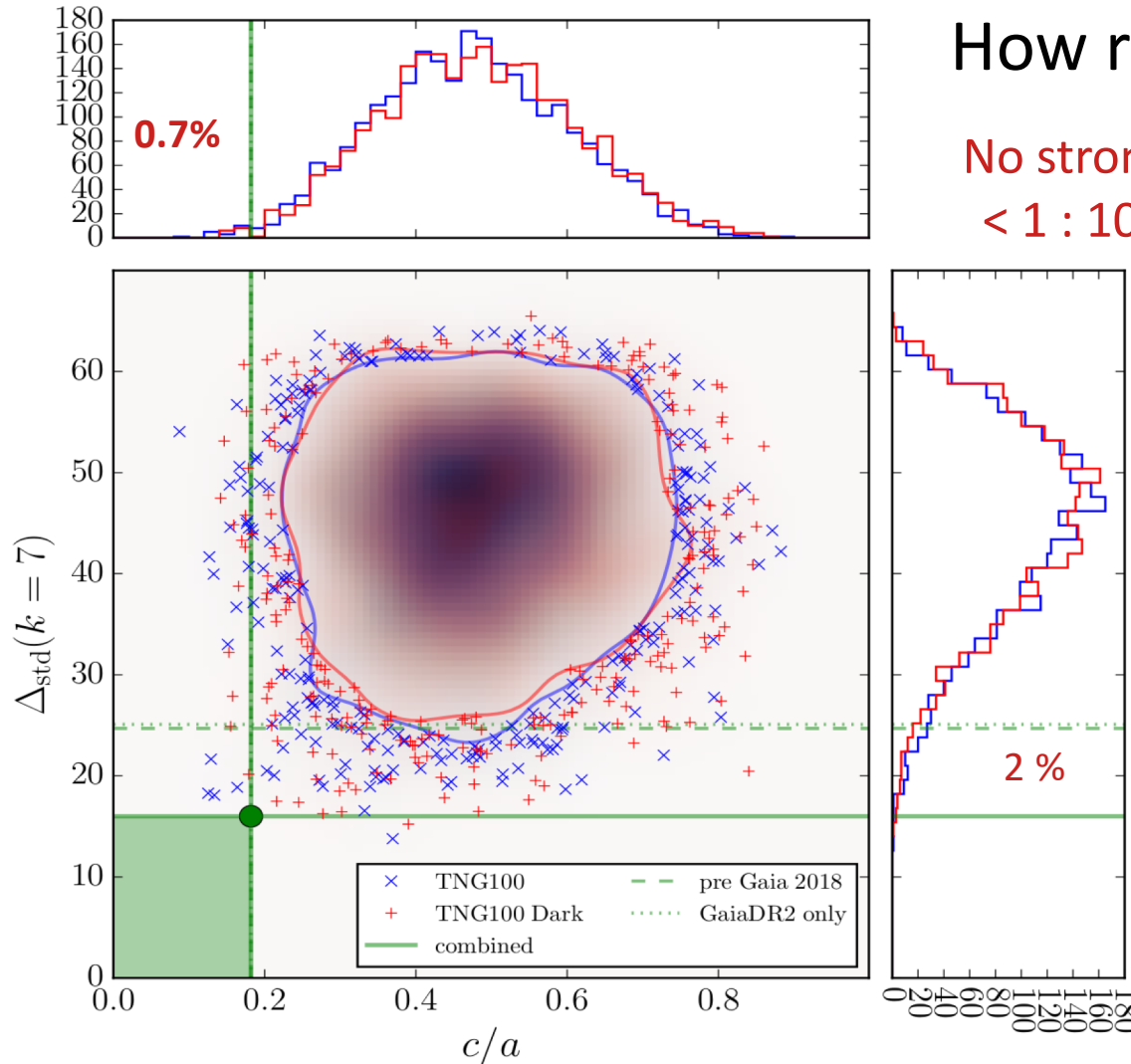
The orbital poles of 7 of the 11 satellites are clustered

GAIA DR2



Pawlowski & Kroupa (2020)

# The plane of satellites in the MW



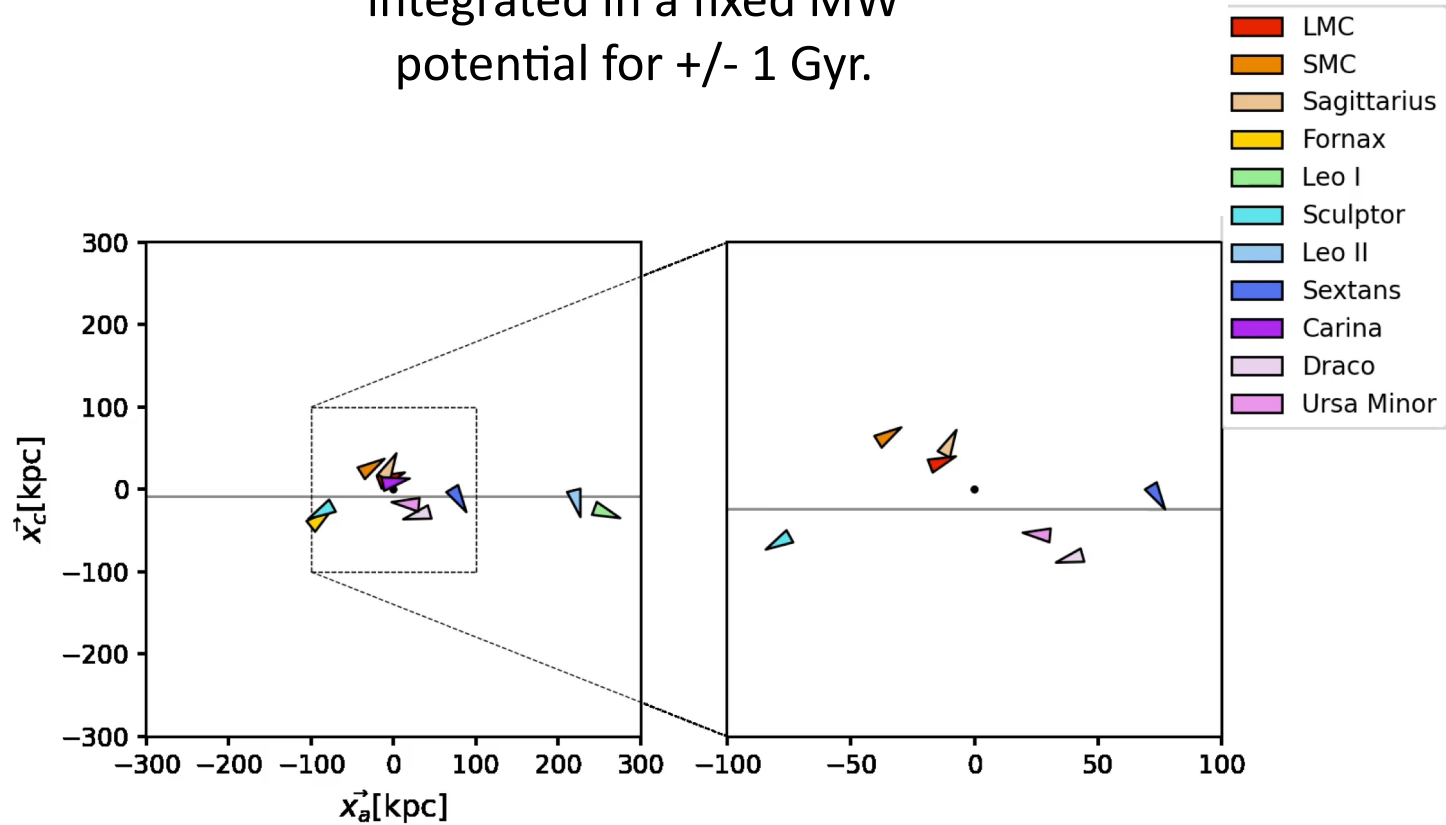
How rare is it?

No strong correlation –  
 $< 1 : 100,000$  chance?

Eigenvalues  
 of inertia  
 tensor  
 $a > b > c$

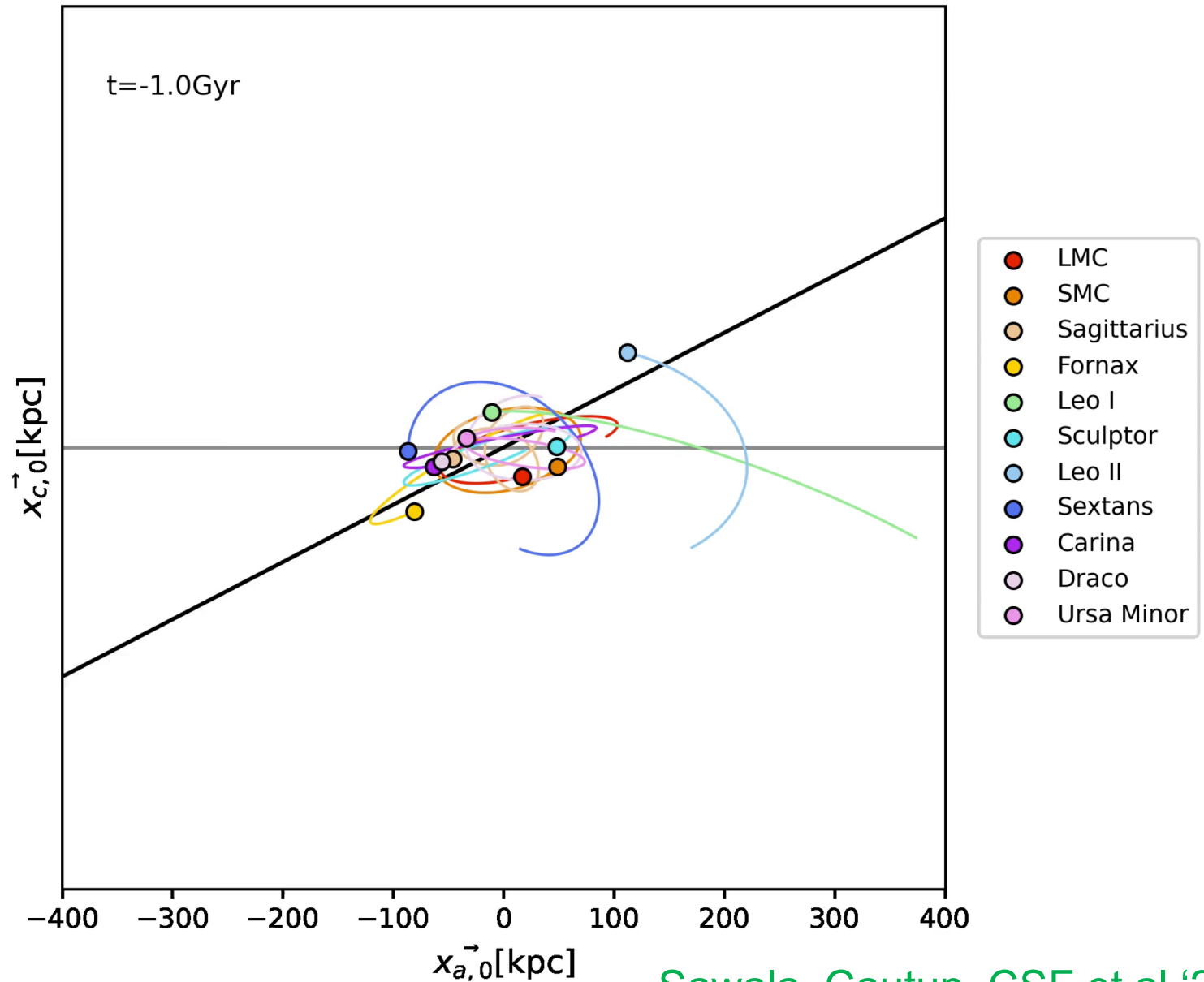
Pawlowski & Kroupa (2020)

Gaia EDR3 proper motions,  
integrated in a fixed MW  
potential for +/- 1 Gyr.





# The MW plane of satellites is transient



Sawala, Cautun, CSF et al '23

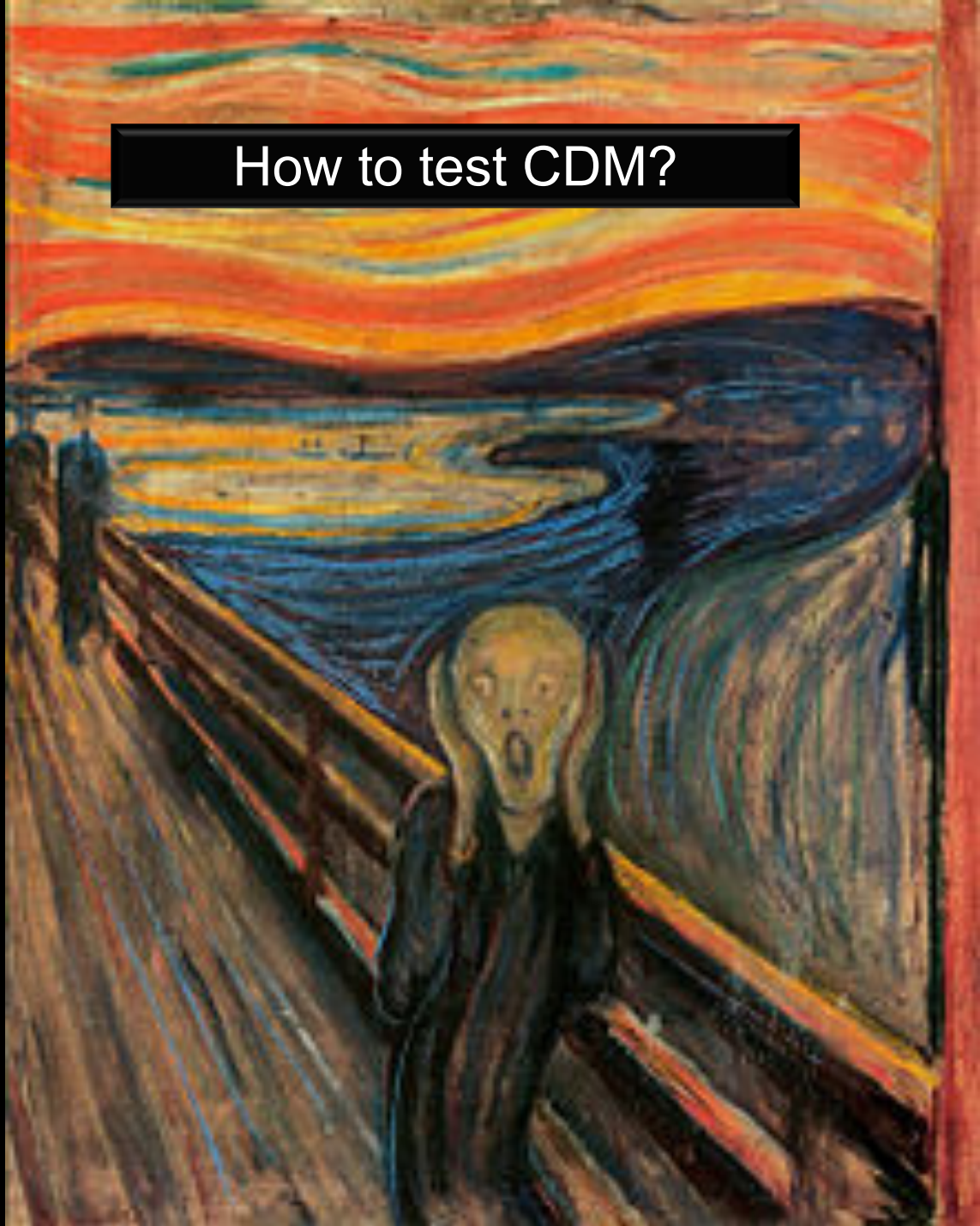
# The rotating plane of satellites

200  $\Lambda$ CDM N-body  
simulations of Local Group  
analogues:  $m_p = 1 \times 10^6 M_\odot$

We have 5/200 (2.5%) more clustered than the MW (compared to 0.04%)  
Still rare, but *not astronomically unlikely*

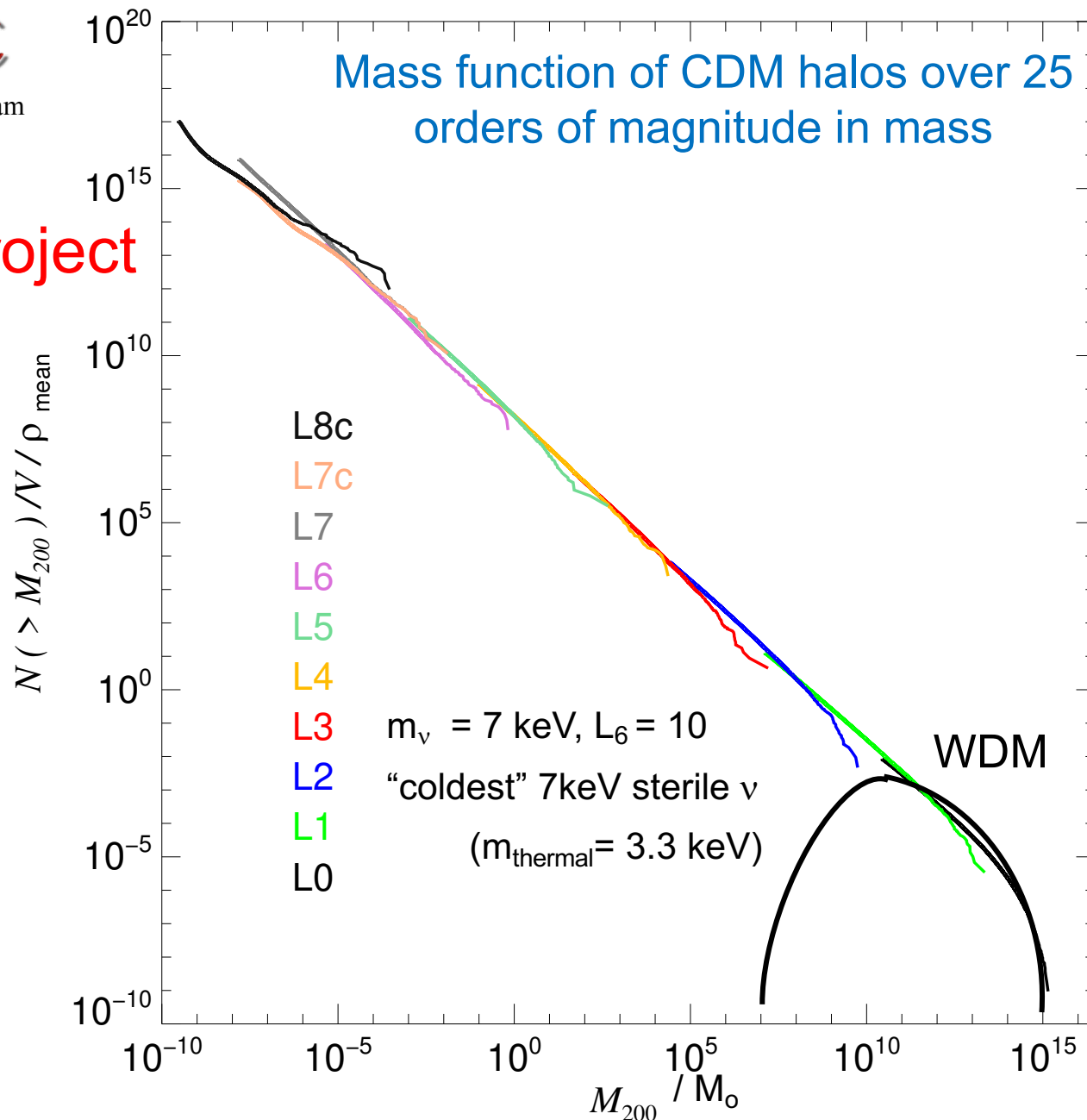


How to test CDM?





# The VVV project



cold dark matter

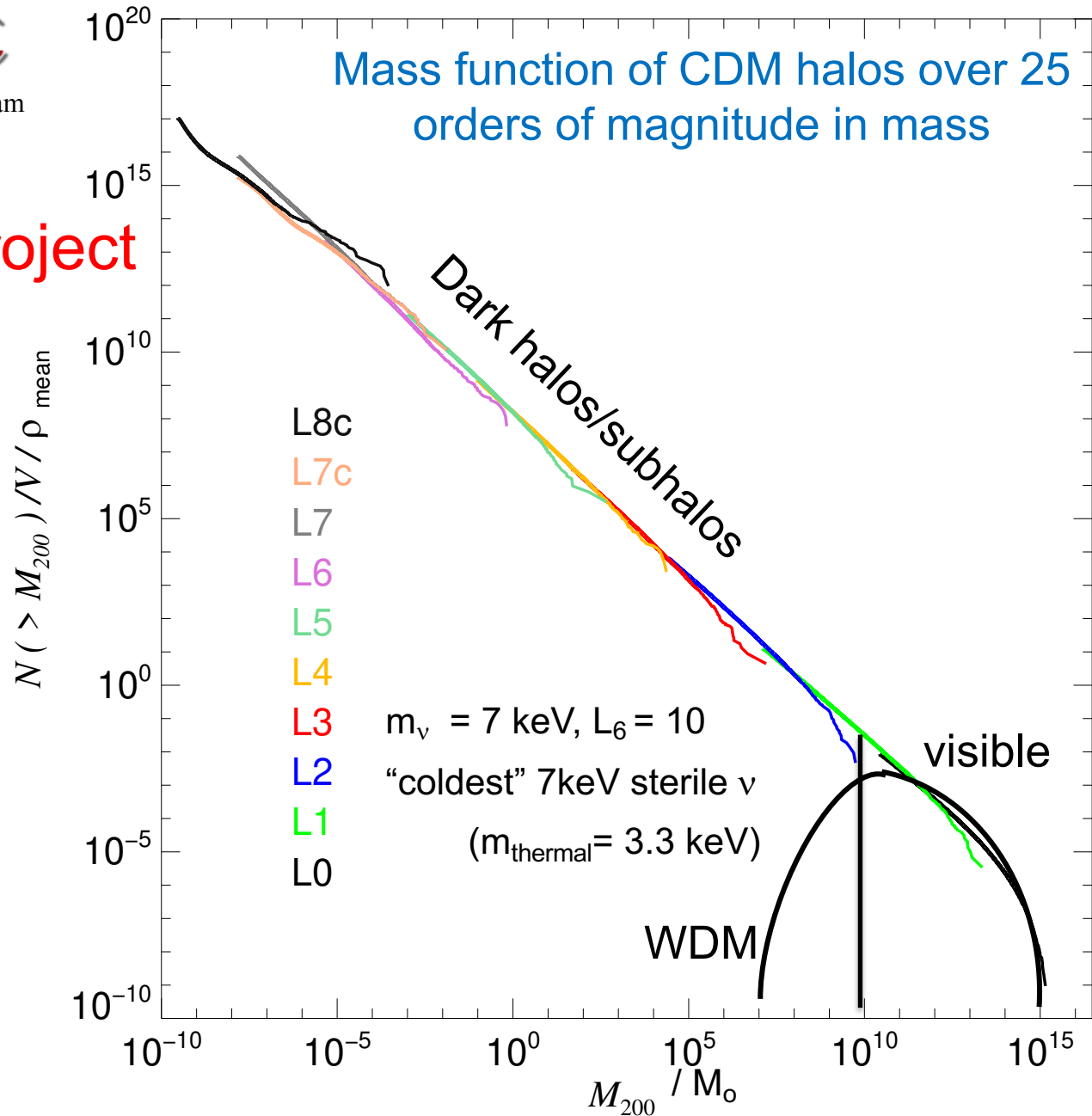


warm dark matter



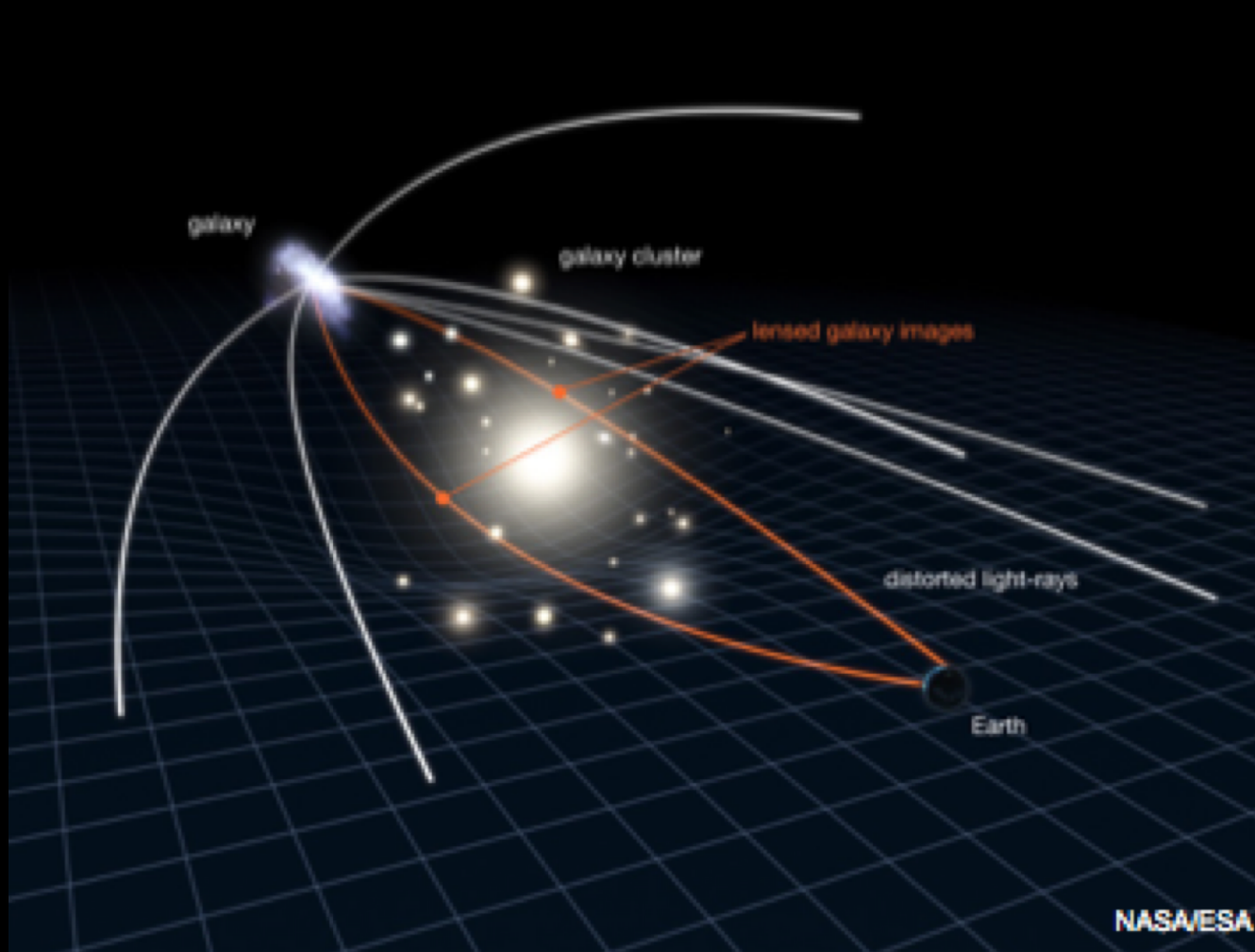
Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
Boyarski & Ruchayskiy '12

# The VVV project





# Gravitational lensing: Einstein rings

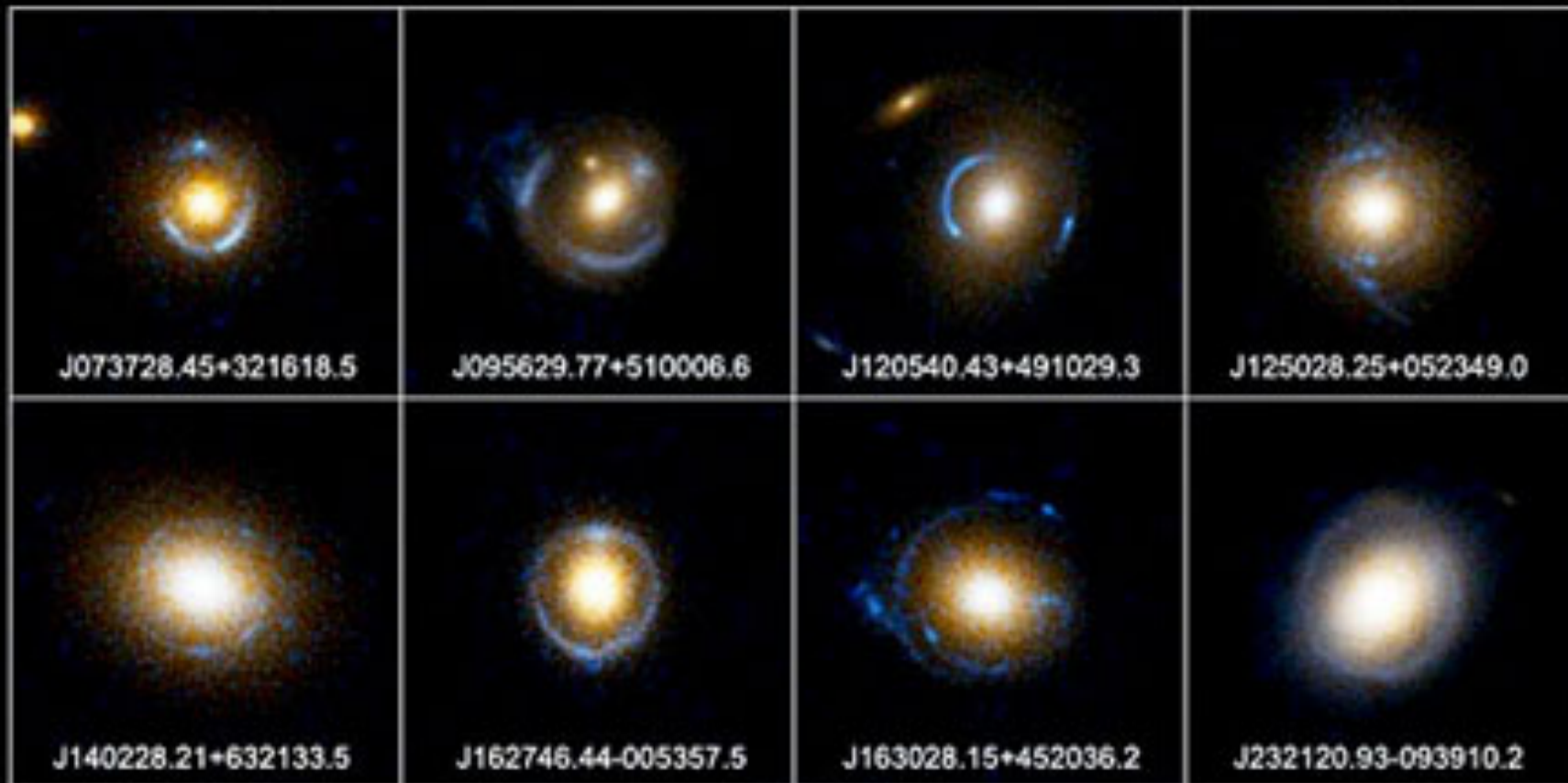


When the source and the lens are well aligned → strong arc or an Einstein ring

# SLAC sample of strong lenses

## Einstein Ring Gravitational Lenses

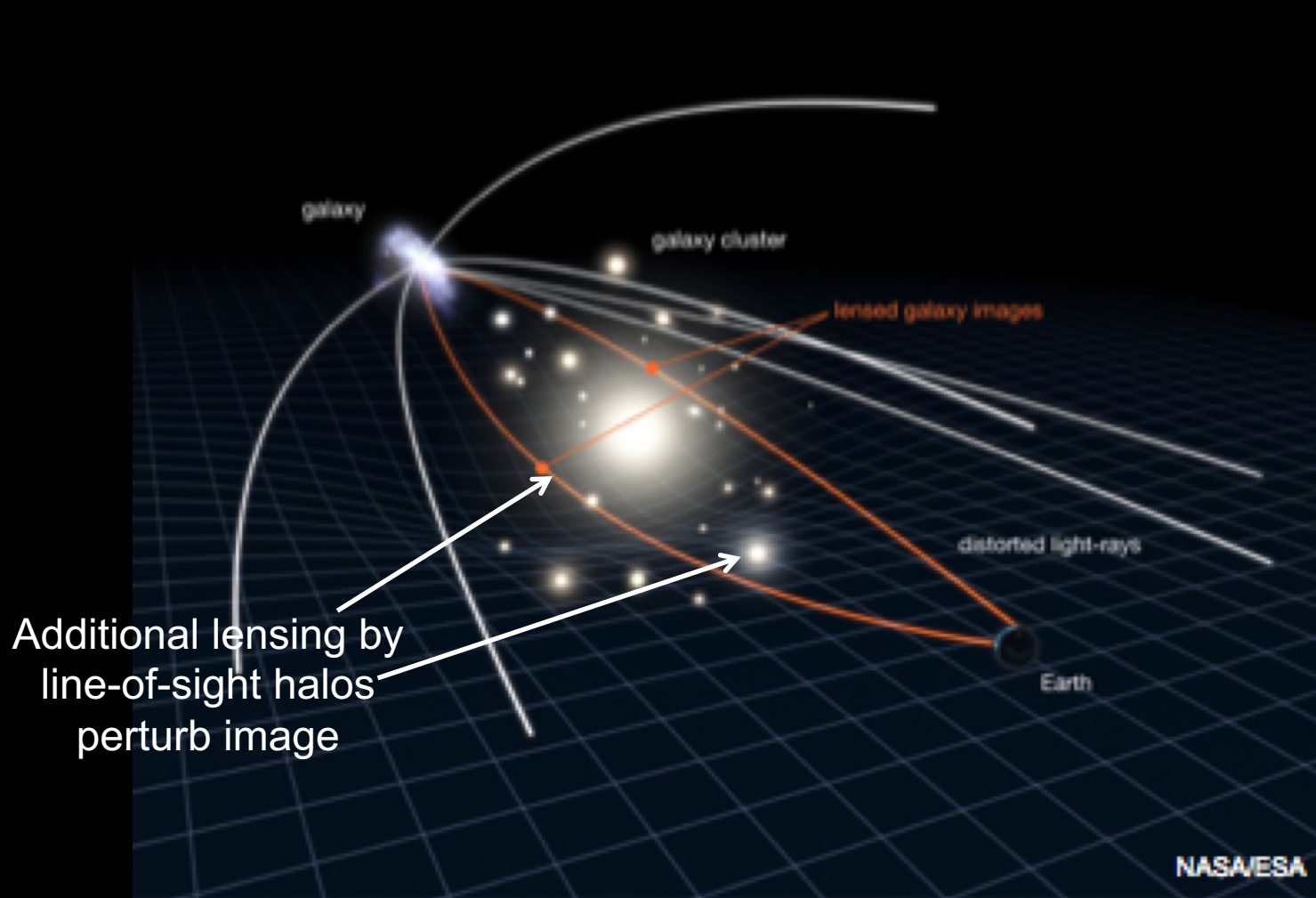
*Hubble Space Telescope • ACS*



NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

STScI-PRC05-32

# Gravitational lensing: Einstein rings

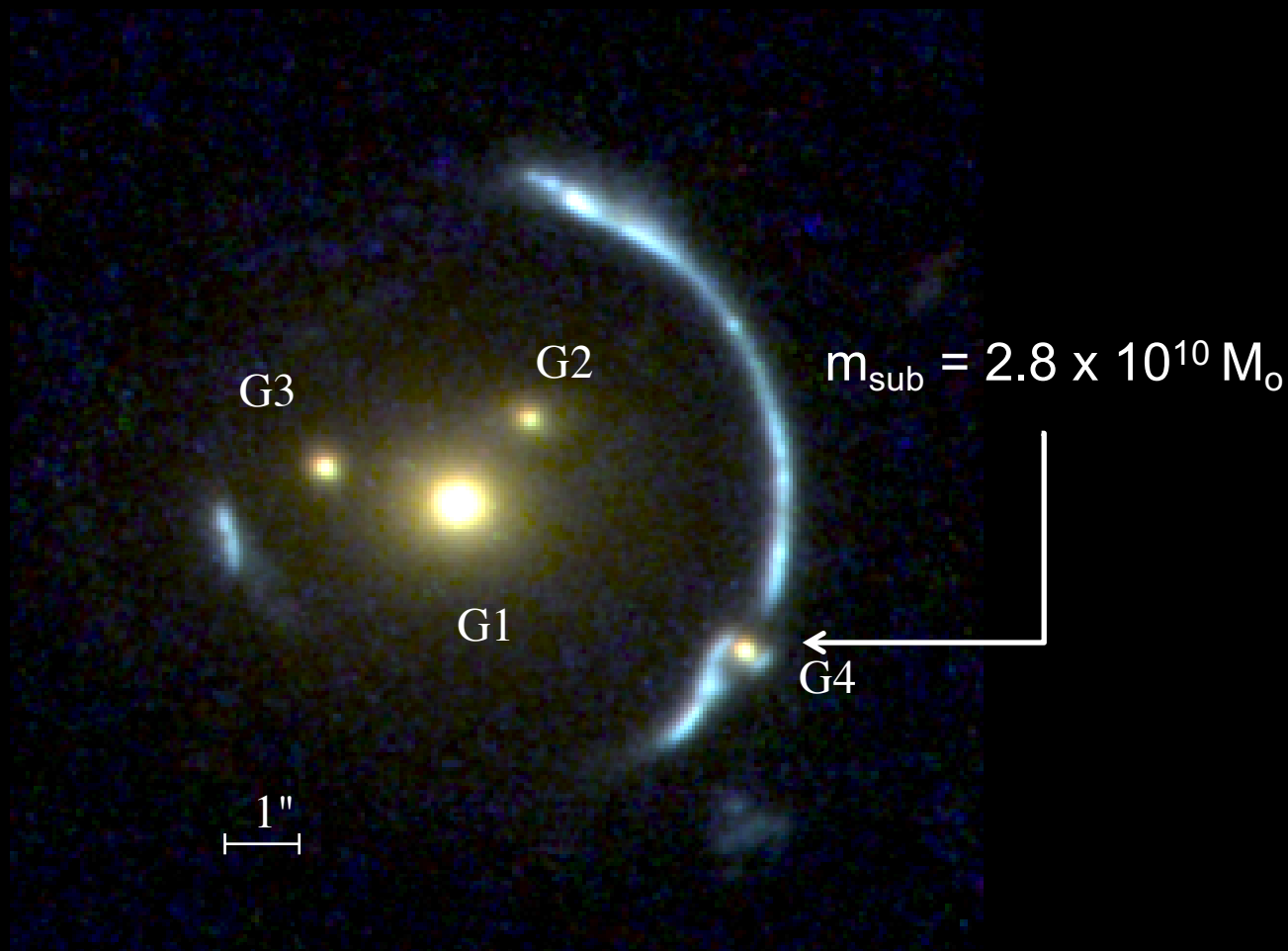


When the source and the lens are well aligned → strong arc or an Einstein ring



# Gravitational lensing: Einstein rings

Halos projected onto an Einstein ring distort the image



Vegetti et al '10

Searched for substructure in 55 lenses with good HST imaging

→ 2 detections:  G3

SLACS0946+1006 →  $\text{Log } M_{\text{sub}} = 11.59^{+0.18}_{-0.34}$

BELLS1226+5457 →  $\text{Log } M_{\text{sub}} = 11.80^{+0.16}_{-0.30}$

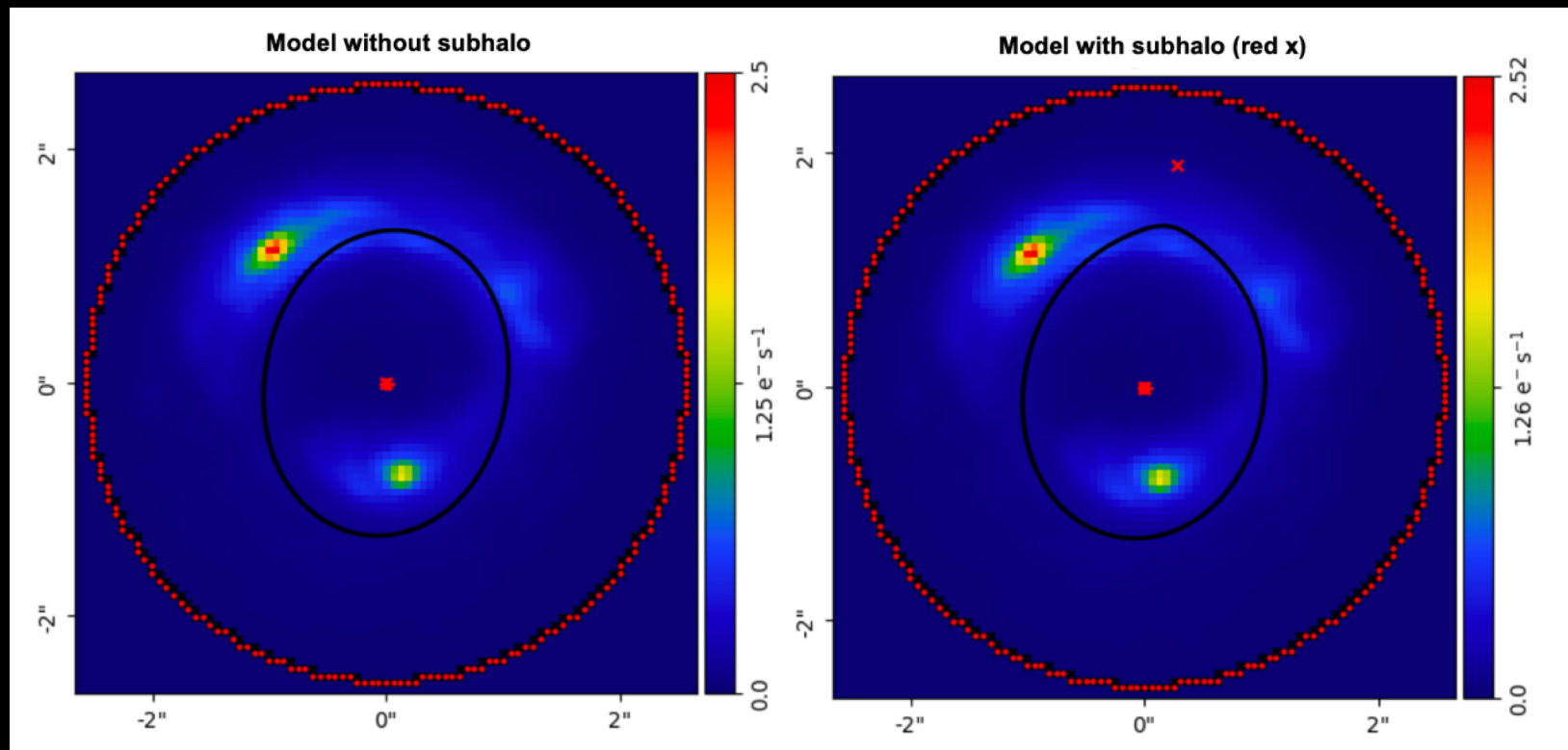
G1

Nightingale + '22

G4

1"  
|-----|

JWST



And another one in JWST data:

$$\rightarrow \text{Log } M_{\text{sub}} = 11.59^{+0.18}_{-0.34}$$

Lange, Nightingale, CSF+ '23

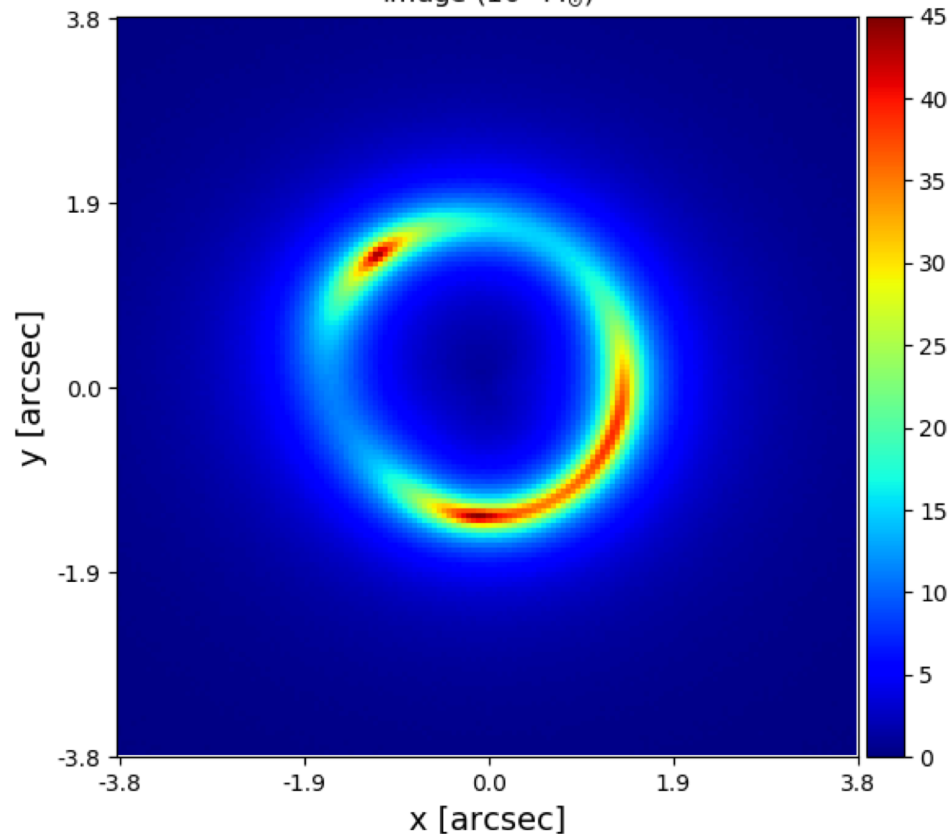


# Strong lensing: detecting small halos

HST “data”:  $z_{\text{source}}=1$ ;  $z_{\text{lens}}=0.2$   $10^7 M_{\odot}$  halo – **NOT** so easy to spot

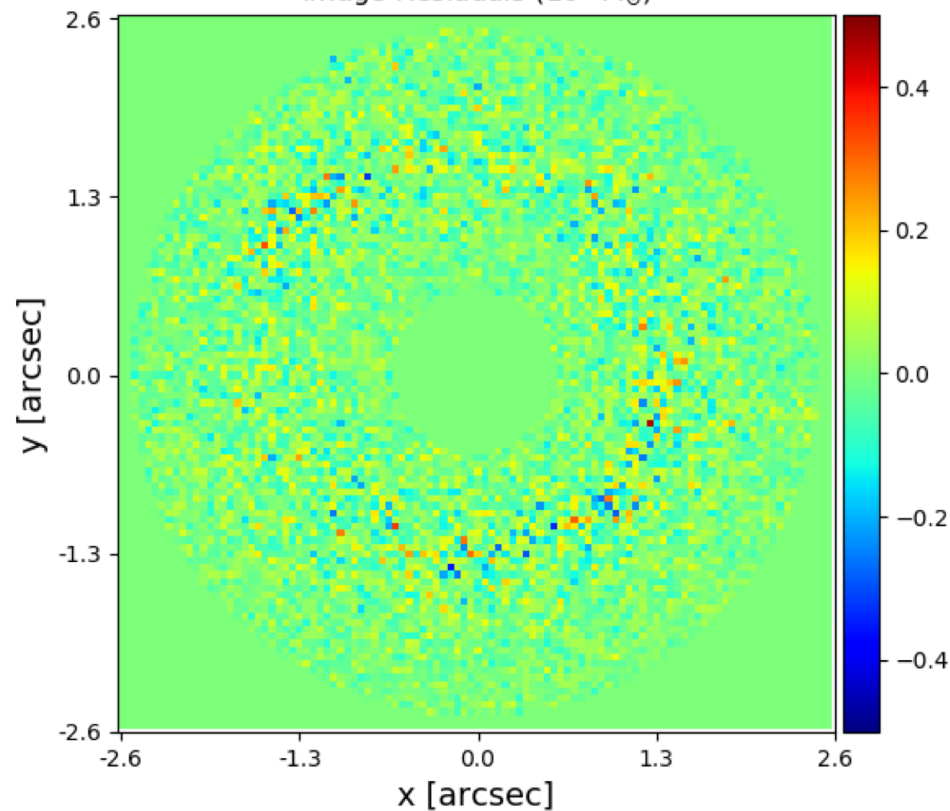
Image

Image ( $10^7 M_{\odot}$ )



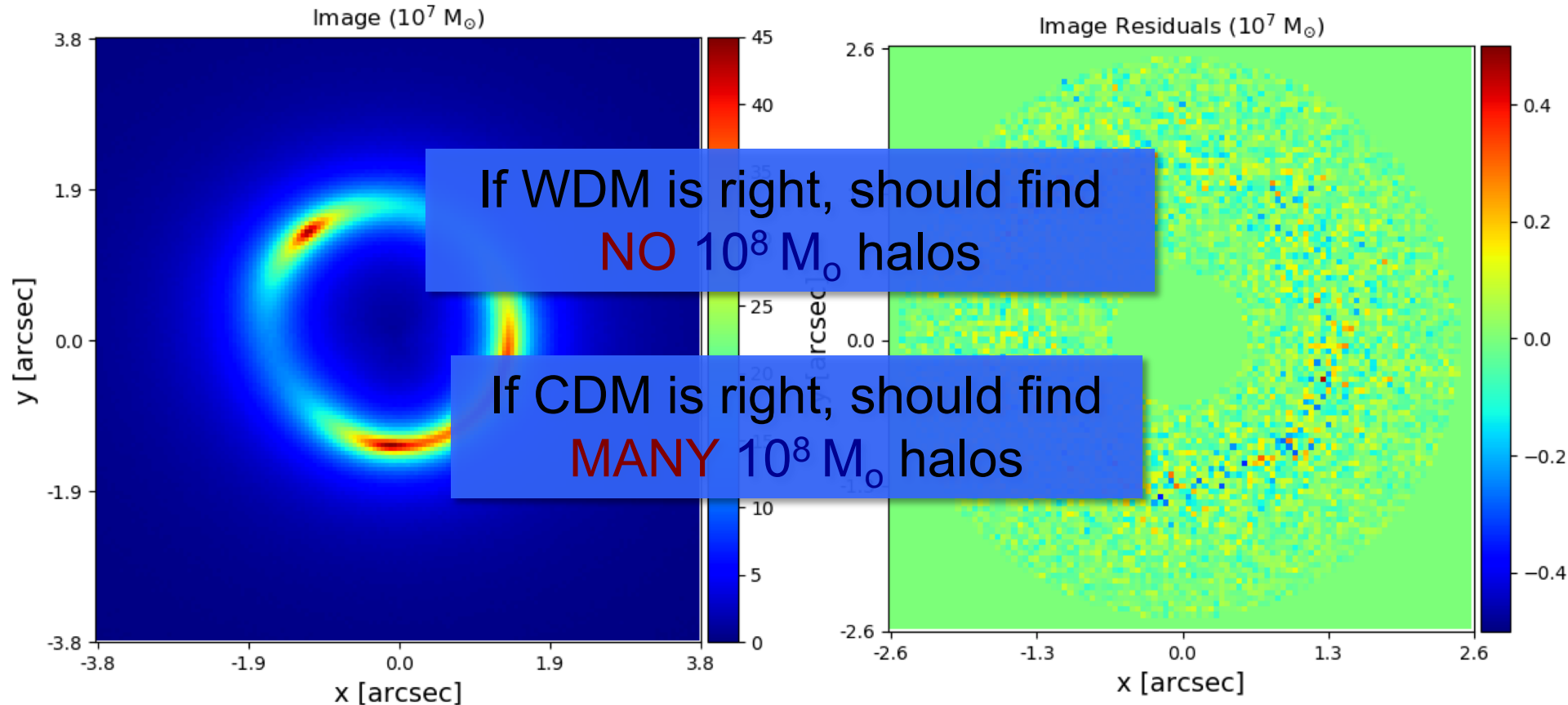
Residuals (image – smooth model)

Image Residuals ( $10^7 M_{\odot}$ )



# Detecting halos w. strong lensing

Can detect halos as small as  $10^7 M_\odot$





# Conclusions

- $\Lambda$ CDM: great **success** on scales  $> 1\text{Mpc}$ : CMB, LSS, gal evolution
- But on these scales  $\Lambda$ CDM cannot be distinguished from **WDM**
- Need to test  $\Lambda$ CDM on **non-linear scales**
- Non-linear **DM** problem **solved**: halo abundance, structure, distr.
- Halos of  $M < 5 \cdot 10^8 M_0$  are dark; halos of  $> 5 \cdot 10^9 M_0$  have a galaxy
- Satellite, TBTF, core/cusp “**problems**” in CDM  $\rightarrow$  baryon effects
- Distortions of **strong** gravitational **lenses**  $\rightarrow$  detect **small haloes**  
 $\rightarrow$  offer a **clean test** of CDM vs WDM  
 $\rightarrow$  can potentially **rule out** CDM!